

From QCD string breaking to quarkonium spectrum

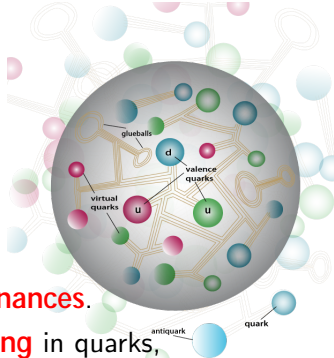
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August 6th, APLAT Symposium 2020



Motivation



Interest in **quarkonium states** and **resonances**.

Study the phenomenon of **string breaking** in quarks, analyzing its implication in the study of the spectrum.

Looking for **exotic states**: tetraquarks, pentaquarks, ...

Exploring new techniques in Lattice QCD for **improving signal to noise ratio**.

String breaking

String breaking occurs when distance between two quarks ($Q\bar{Q}$) increases.

In this case it is more convenient for the system to produce **couple meson-meson** ($B\bar{B}$).

The potential describing the system before string breaking occur is (**Cornell potential**)

$$V(r) = A + \frac{B}{r} + r$$

E. Eichten et al. (1975)

E. Eichten et al. (1978)

C. Bernard et al. (2001)

String breaking

At the end, we have 2 mesons
 $B = Q\bar{q}$, $\bar{B} = \bar{Q}q$ with mass E_B .

Condition for string breaking:

$$V(r) - 2E_B > 0.$$

Just **Wilson loops** are **not enough**
to get string breaking:
quarkonium and meson-meson
operators are needed.

*Alternatively, see F. Gliozzi, A.
Rago (2005)*

An interested approach is to study
the matrix correlator:

Bali et al. (2005)

J. Bulava et al. (2019)
V. Koch et al. (2019)

$$C(t) = \begin{pmatrix} C_{QQ}(t) & C_{QB}(t) \\ C_{BQ}(t) & C_{BB}(t) \end{pmatrix}$$

Computation

Matrix of correlators:

$$C(t) = \begin{pmatrix} C_{QQ}(t) & C_{QB}(t) \\ C_{BQ}(t) & C_{BB}(t) \end{pmatrix}$$

$$= e^{-2m_Q t} \begin{pmatrix} B_{p, \bar{n}_f} & 1 \\ A_{p, \bar{n}_f} & C_{n_f} \end{pmatrix} + \dots$$

We concentrate on the first element and get the potential:

$$C_{QQ}(t) = e^{-2m_Q t}$$

$$V_{QQ}(r) = \lim_{t \rightarrow \infty} \frac{1}{a} \log \frac{C_{QQ}(t)}{C_{QQ}(t+a)}$$

Lattice setup

79 configurations generated with $n_f = 2$ O(a) improved Wilson fermion action (**CLS ensembles**).

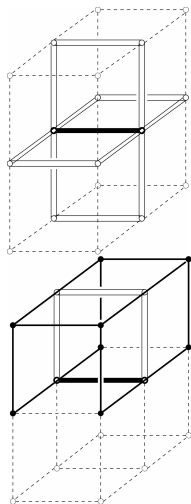
Lattice volume:
64x32x32x32.

$m = 330$ MeV.

Lattice spacing:
 $a = 0.0755(11)$ fm.

On smearing techniques

The improving of the signal pass through the use of the right gauge configurations. We explore different methods:



APE smearing (**smoothing over nearest gauge links**). It depends on 1 parameter : $\omega = 0.5$ or 0.7
M. Albanese et al. (1987)

HYP smearing (**smoothing on hypercubes**). It depends on 3 parameters $\alpha = (\alpha_1; \alpha_2; \alpha_3)$.
 $\alpha = (0.75; 0.6; 0.3)$
A. Hasenfratz et al. (2002)

\hat{O} HYP2) improved choice of parameters.
 $\alpha = (1.0; 1.0; 0.5)$
M. Donnellan et al. (2011)

On smearing techniques

$$W(r; t)_{lm} = \text{tr} \left[V_t^y(r; 0) U_r(t; 0)^{(l)} V_0(r; 0) U_0^y(t; 0)^{(m)} \right]$$

where

$$U_r(t; 0)^{(l)} = (\mathcal{S}_{sm})^{\eta_l} U_r(t; 0)$$

sHYP) HYP smearing in the spatial direction of the links.

$$\eta_2 = 0.6; \quad \eta_3 = 0.3$$

Solving the GEVP problem.)

The matrix given by different smearing levels is used to get the generalized eigenvalues.

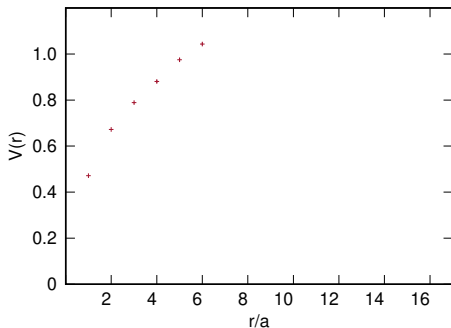
M. Donnellan et al. (2011)

M. Della Morte et al. (2004)

$$V(r) = \lim_{t \rightarrow \infty} \frac{1}{t} \log \frac{\langle \hat{W}(r; t) \mathbf{v} \rangle}{\langle \hat{W}(r; t+a) \mathbf{v} \rangle}$$

Potentials

No smearing



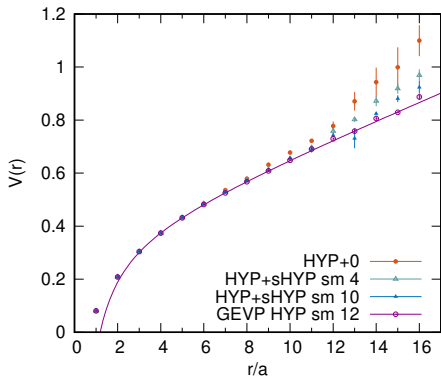
Only at small r the potential can be obtained and at large t the data gets noisy.

$$V_{QQ}(r) = \lim_{t \rightarrow \infty} \frac{1}{a} \log \frac{C_{QQ}(t)}{C_{QQ}(t+a)} = 2m_Q + \frac{1}{a} V(r)$$

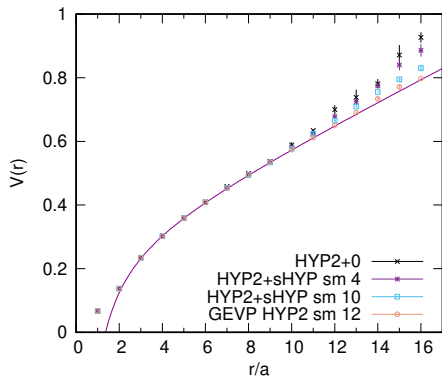
Potentials: different smearing levels

The more sHYP is applied, the more the signal gets in agreement with the theoretical expectation for large $r=a$.

HYP



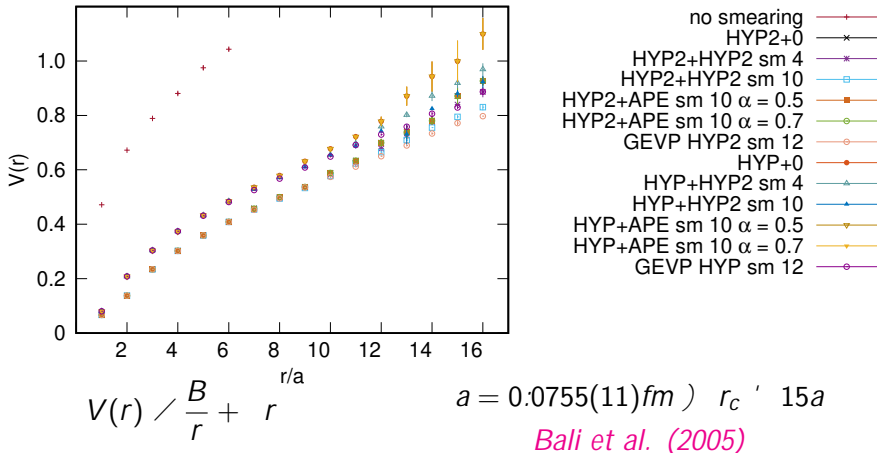
HYP2



GEVP procedure seems to give better results.

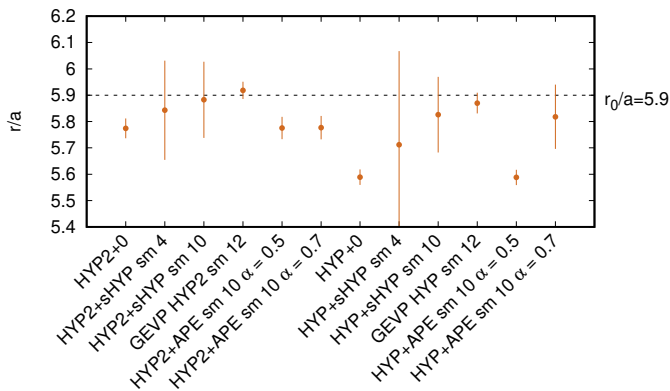
Different smearing choices

Smearing shifts the potential by a constant factor. Low- r region not well described with our parametrization and smearing choices. The potential with HYP2 is below the potential with HYP smearing.



Sommer parameter

The more smearing is applied in the spatial direction, the more the Sommer parameter approaches to $r_0=a=5.9$ (reference value taken from *P. Fritsch et al. (2012)*).



$$F(r) = V^0(r)$$

$$r_0^2 F(r_0) = 1.65$$

R. Sommer
(1994)

Summary

Different smearing techniques of gauge links are studied, APE, HYP, HYP2 and GEVP.

Smearing improves the signal for large distances but it is not good for short distances.

The GEVP procedure gives the best signal to noise ratio and agreement with the theory.

For more info, look here *M.Catillo, M. Marinkovic, P. Bicudo, N. Cardoso, arXiv:2005.05723v2 (2020)*.

Going further...

The potential that one gets from the heavy quark-antiquark system can be plugged in the Schrödinger equation (**Born-Oppenheimer approximation**):

$$\frac{1}{2} \nabla^2 \psi + \frac{2}{r} \frac{\partial \psi}{\partial r} - \frac{L^2}{2r^2} \psi + V(\mathbf{r}) \psi - E \psi = 0$$

and one can determine e.g. for bottomonium bound states and resonances (*P. Bicudo et al. (2020)*), including potential tetraquark resonances.

) See also **L. Mueller and M. Wagner talks** for similar studies.

Outlook

Obtain **remaining elements of the correlator matrix** (renormalize the potential, include mixing effects) to get the info on the string breaking.

Use the **Born-Oppenheimer approximation approach**

- to get the spectrum with increased precision (cross-check), and **look for exotic bound states**.
- Repeat calculation for different gauge ensembles (continuum limit for string breaking with dynamical quarks still missing in the literature).

Systematical study of the **noise-reduction techniques** (different stochastic methods, distillation and so on).

Exploring the static potentials with **C boundary conditions**.

Thank you!