



# First QCD+QED simulations with $C^*$ boundary conditions

Jens Lücke

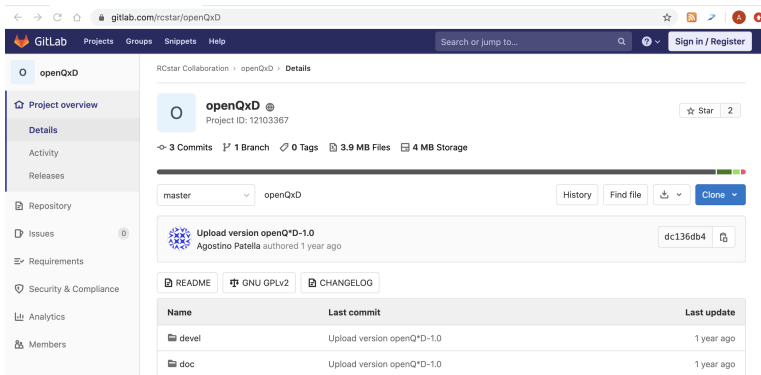


A. Bussone, I. Campos, M. Dale, P. Fritzsche,  
M. Hansen, M. K. Marinkovic, A. Patella, N. Tantalo

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# Technical setup

- First serious simulations with the openQ\*D code<sup>a</sup>



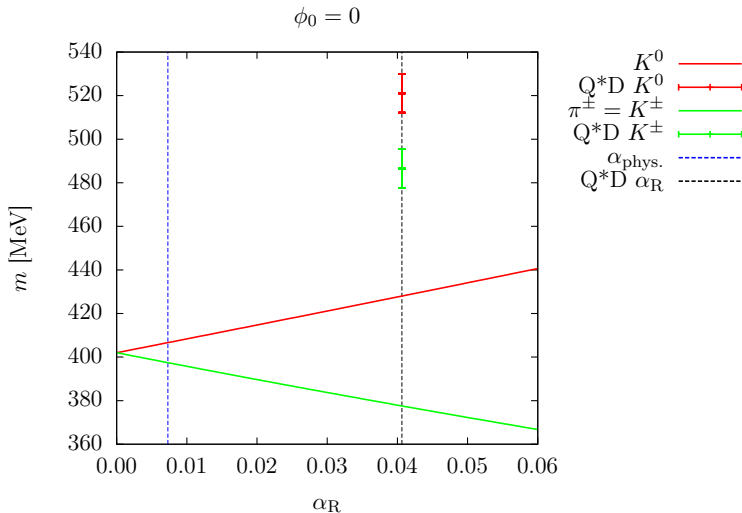
The screenshot shows the GitLab interface for the project 'openQxD'. The page includes a navigation sidebar on the left with options like 'Project overview', 'Details', 'Activity', 'Releases', 'Repository', 'Issues', 'Requirements', 'Security & Compliance', 'Analytics', and 'Members'. The main content area displays the project name 'openQxD' with its ID '12103367', a star count of 2, and statistics for 3 commits, 1 branch, 0 tags, 3.9 MB files, and 4 MB storage. A commit history table is visible below the project details.

Name	Last commit	Last update
devel	Upload version openQ*D-1.0	1 year ago
doc	Upload version openQ*D-1.0	1 year ago

Available at <https://gitlab.com/rcstar/openQxD>

<sup>a</sup>Campos et al., 'openQ\*D code: a versatile tool for QCD+QED simulations'.

# Overview



$$\phi_0 = 8t_0 (m_{K^\pm}^2 - m_{\pi^\pm}^2)$$

$$\phi_1 = 8t_0 (m_{K^0}^2 + m_{K^\pm}^2 + m_{\pi^\pm}^2) \simeq \phi_1^{\text{phys.}}$$

$$\phi_2 = \frac{8t_0}{\alpha_R} (m_{K^0}^2 - m_{K^\pm}^2) \simeq \phi_2^{\text{phys.}}$$

$$\phi_3 = \sqrt{8t_0} (m_{D_s^\pm} + m_{D^\pm} + m_{D^0}) \simeq \phi_3^{\text{phys.}}$$

## Setup

- C\* boundary conditions in all three spatial dimensions<sup>b</sup>
- All ensembles at  $\beta = 3.24^c$
- Lattice spacing is determined using  $N_f = 2 + 1$  value of  $\sqrt{8t_0^*} = 0.413(5)(2) \text{ fm}^d$

Ens.	small QCD	large QCD	QCD+QED
$N_{\text{cfg}}$	2000	1082	494
Volume	$64 \times 32^3$	$80 \times 48^3$	$64 \times 32^3$
$\alpha$	0.0	0.0	0.05
$\alpha_R$	0.0	0.0	0.04
$a$ [fm]	0.0537	0.0537	0.0523
$m_{\pi^\pm}$ [MeV]	402(3)	402(2)	487(8)
$Lm_{\pi^\pm}$	3.50	5.26	4.13

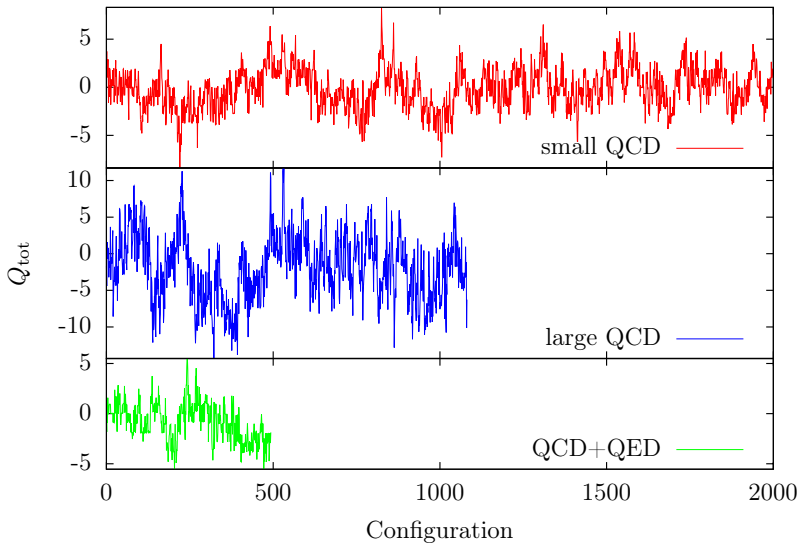
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<sup>b</sup>Lucini et al., ‘Charged hadrons in local finite-volume QED+QCD with C\* boundary conditions’.

<sup>c</sup>Höllwieser, Knechtli and Korzec, ‘Scale setting for  $N_f = 3 + 1$  QCD’.

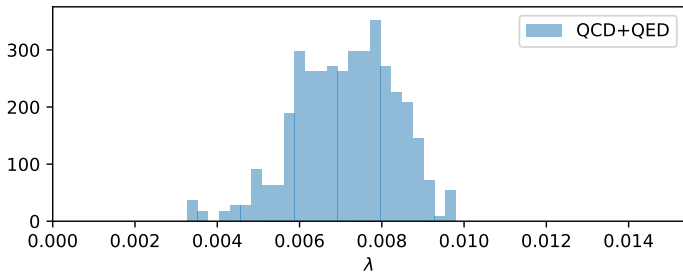
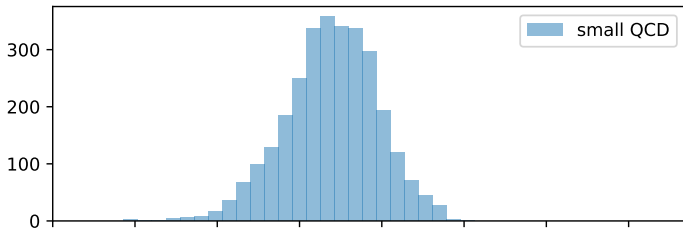
<sup>d</sup>Bruno, Korzec and Schaefer, ‘Setting the scale for the CLS 2+1 flavor ensembles’.

## Results - Diagnostic observables



## Results - Diagnostic observables

Eigenvalue of  $\sqrt{D^\dagger D}$  for up quark



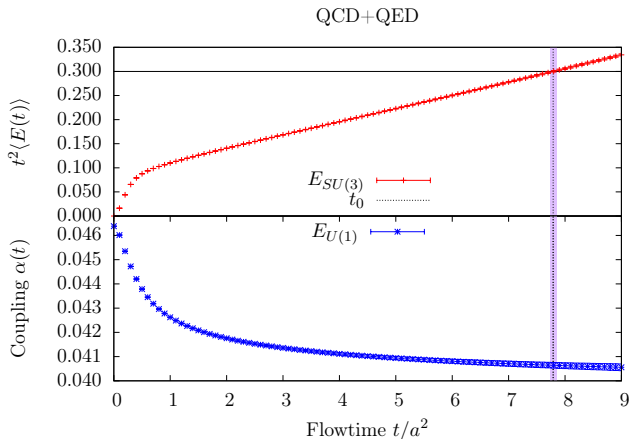
## Results - Wilson Flow

- $t_0$  is obtained by solving the equation

$$t^2 \langle E_{SU(3)}(t) \rangle \Big|_{t_0} = 0.3$$

- $\alpha_R$  is extracted via<sup>e</sup>

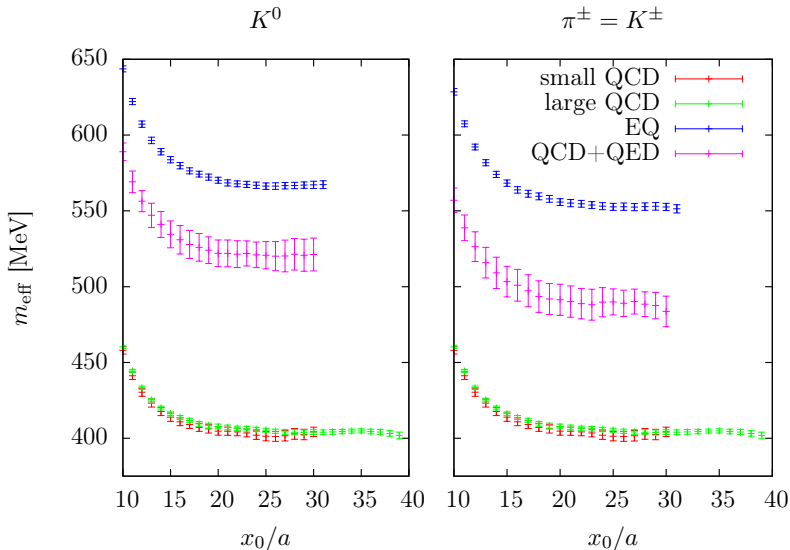
$$\alpha_R = \frac{t^2 \langle E_{U(1)}(t) \rangle \Big|_{t_0}}{4\pi\mathcal{N}}$$



<sup>e</sup>Borsanyi et al., 'Ab initio calculation of the neutron-proton mass difference'.

## Results - Masses

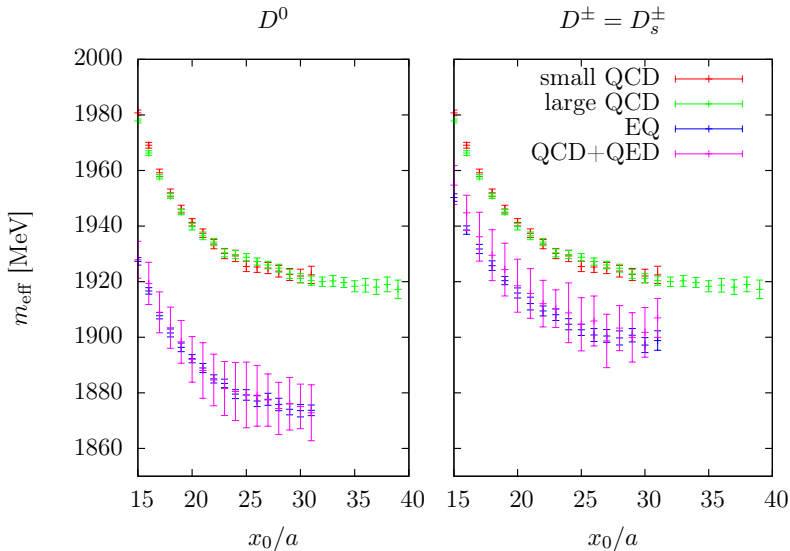
Charged masses are extracted from gauge invariant interpolating operators<sup>f</sup>



<sup>f</sup>Hansen et al., 'Gauge invariant determination of charged hadron masses'.



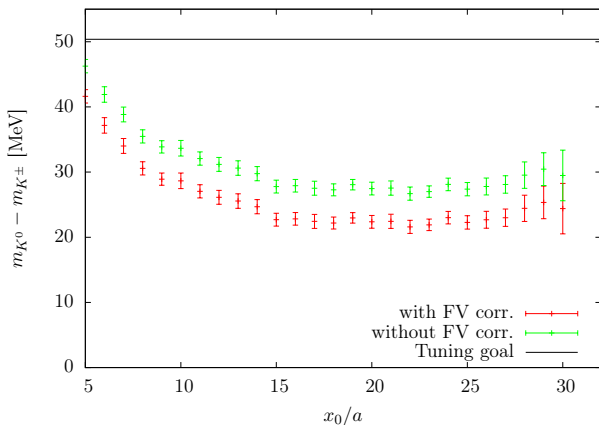
## Results - Masses



## Results - QCD+QED Kaon splitting

$$m_{K^0} = 521(11) \text{ MeV}$$

$$m_{K^\pm} = 487(8) \text{ MeV}$$



$$\text{QED FV corrections}^g : \frac{\Delta m(L)}{m} = \alpha_R \left\{ \frac{q^2 \xi(1)}{2mL} + \frac{q^2 \xi(2)}{2(mL)^2} + \mathcal{O}\left(\frac{1}{L^4}\right) \right\}$$







<sup>g</sup>Lucini et al., 'Charged hadrons in local finite-volume QED+QCD with C\* boundary conditions'.

## Summary and Outlook

- ✓ Production of  $N_f = 1 + 2 + 1$  fully dynamical QCD+QED configurations
  - Using openQ\*D with C\* boundary conditions
  - $\alpha_R \approx 0.04$
- ✓ Demonstration that the openQ\*D framework is functional and the used algorithm is stable
  - No topological freezing
  - Dirac operator has clear gap
- ✓ Measurement of charged mesons and Wilson flow observables
  - Charged meson masses were extracted in a gauge invariant setup
  - Wilson flow observables were used to fix the scale and extract  $\alpha_R$
- ✓ Extraction of the Kaon mass splitting with good precision
  - Reduction of the statistical error through taking correlation between Kaons into account
- Tuning of the parameters for the QCD+QED ensemble
  - Currently: Light mesons are too heavy
  - Goal: Light meson masses close to the  $SU(3)$  symmetric point with the correct splitting
- Reevaluation of the tuning strategy

Thank you!

## References I

-  Sz. Borsanyi et al. ‘Ab initio calculation of the neutron-proton mass difference’. In: *Science* 347 (2015), pp. 1452–1455. DOI: 10.1126/science.1257050. arXiv: 1406.4088 [hep-lat].
-  Mattia Bruno, Tomasz Korzec and Stefan Schaefer. ‘Setting the scale for the CLS 2+1 flavor ensembles’. In: *Physical Review D* 95.7 (2017). ISSN: 24700029. DOI: 10.1103/PhysRevD.95.074504. arXiv: 1608.08900.
-  Isabel Campos et al. ‘openQ\*D code: a versatile tool for QCD+QED simulations’. In: (Aug. 2019). arXiv: 1908.11673. URL: <http://arxiv.org/abs/1908.11673>.
-  Martin Hansen et al. ‘Gauge invariant determination of charged hadron masses’. In: *JHEP* 05 (2018), p. 146. DOI: 10.1007/JHEP05(2018)146. arXiv: 1802.05474 [hep-lat].
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-  Biagio Lucini et al. ‘Charged hadrons in local finite-volume QED+QCD with  $C^*$  boundary conditions’. In: 2016 (2015). DOI: 10.1007/JHEP02(2016)076. arXiv: 1509.01636.

## Backup - Setup

- Lüscher-Weisz  $SU(3)$  gauge action
- Compact  $U(1)$  with Fourier acceleration
- Non-perturbatively  $\mathcal{O}(a)$  improved Wilson fermions for the QCD ensembles
- For QCD+QED ensemble same value of  $c_{\text{SW}}$  as for the QCD ones
- Periodic boundary conditions in time
- C\* boundary conditions in all spatial directions
- RHMC with rational approximation for all quarks
- Deflation solvers for up and down/strange quarks

## Backup - Results - Stability of the Algorithm

Ens.	$N_{\text{cfg}}$	Acceptance	$\langle e^{-\Delta H} \rangle$	$\tau_{\langle E(t_0) \rangle}$	Cost per MDU [ch]
small QCD	2000	95%	0.998(5)	57(29)	228(4)
large QCD	1082	98%	0.995(2)	29(14)	1924(44)
QCD+QED	494	97%	0.998(3)	7.2(8)	826(24)