



University of Colorado  
Boulder



# Finite Temperature Study of a $4+6$ Mass-Split System

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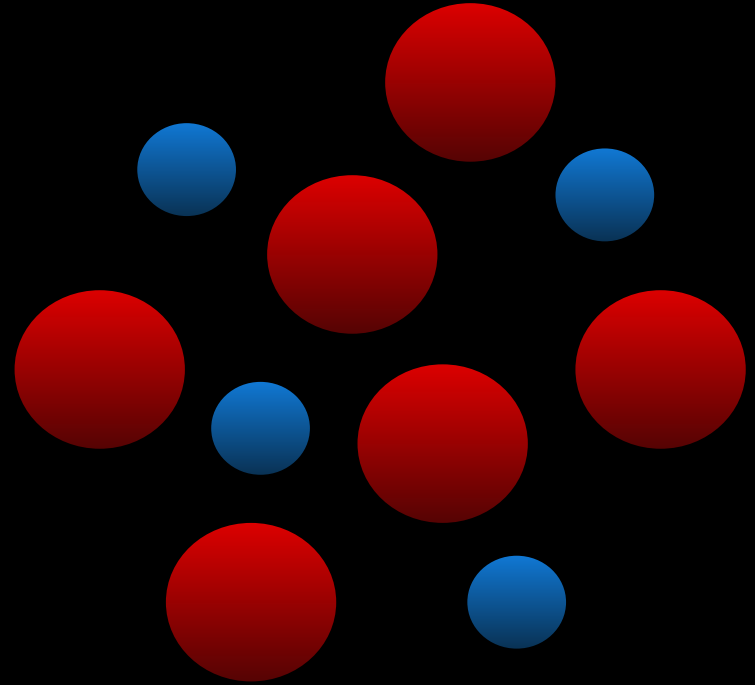
Curtis Peterson

In collaboration with Anna Hasenfratz and Oliver Witzel

Composite Higgs assumes the Higgs boson to be **bound state** of a new, **strongly-interacting sector**.

This new strong sector **has** to be **chirally broken** and hence **should** experience a **finite-temperature phase transition**.

The observation of a **first-order finite-temperature** transition would have **implications for the early universe**, such as the production of **primordial gravitational waves**.



# 4+6 Mass-Split System

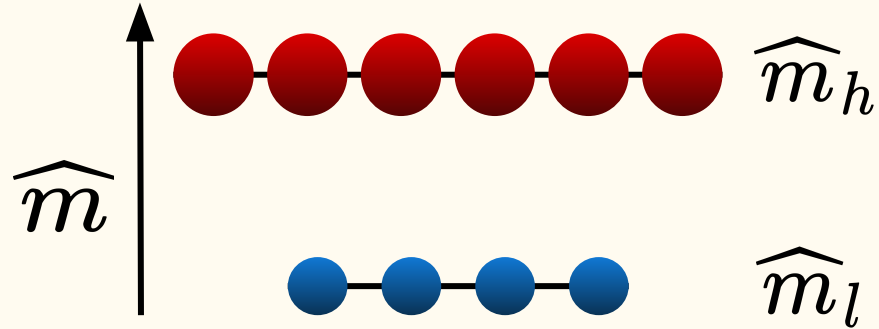
The 4+6 mass-split system provides a framework to explore the composite Higgs scenario.

The system is an SU(3) gauge theory composed of  $N_l = 4$  light flavors and  $N_h = 6$  heavy flavors of fermions with masses  $\widehat{m}_l$ ,  $\widehat{m}_h$ , respectively.

$N_l$  is chosen so that the light system is chirally broken.

$N_h$  is chosen so that the mass-degenerate limit is conformal.

In this system, the gauge coupling is irrelevant and the scale is set by heavy mass  $\widehat{m}_h$ .



The continuum limit is tuned to

$$\widehat{m}_h \rightarrow 0 \text{ with } \widehat{m}_l/\widehat{m}_h \text{ fixed.}$$

The chiral limit is tuned to

$$\widehat{m}_l/\widehat{m}_h \rightarrow 0.$$

The gauge coupling is held fixed.

LSD, arXiv:2007.01810

# First-Order Transitions and Gravitational Waves

A **first-order phase transition** occurs when **multiple local minima** of the free energy exist for a **finite range of temperatures**.

Caprini et al., arXiv:1512.06239  
LSD, arXiv:2006.16429

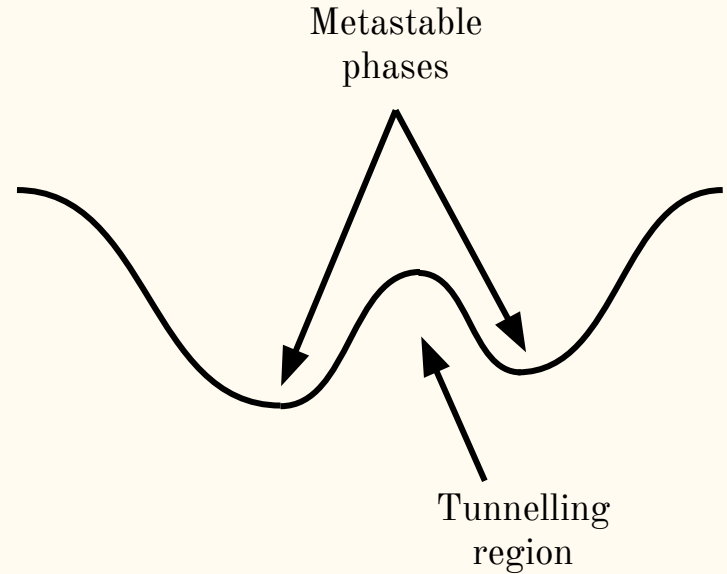
Scalar fields are allowed to **tunnel** or **thermally fluctuate** **between the local minima**.

“**Bubbles**” of **metastable states** that grow as one approaches either side of the phase boundary.

The first source of **gravitational waves (GW)** is the **collision** of the bubble walls of the emerging phase.

The second source of GW's are produced **after bubble wall collisions**.

**Spectrum** calculated from **latent heat**, the **phase transition duration**, and **bubble wall velocity**.



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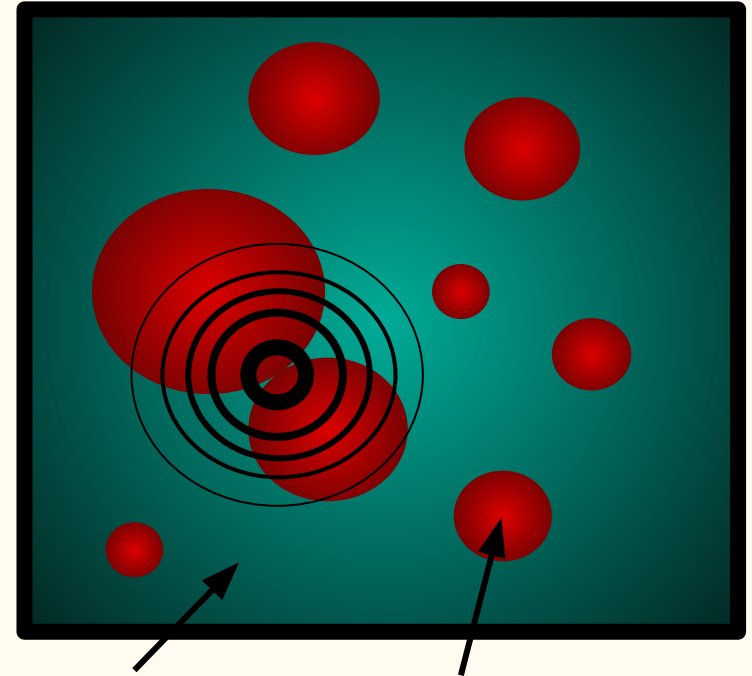
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Dominant phase

Emerging phase

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# Simulation Details

In our system, **finite-temperature phase transition** separates a confined phase from a deconfined phase.

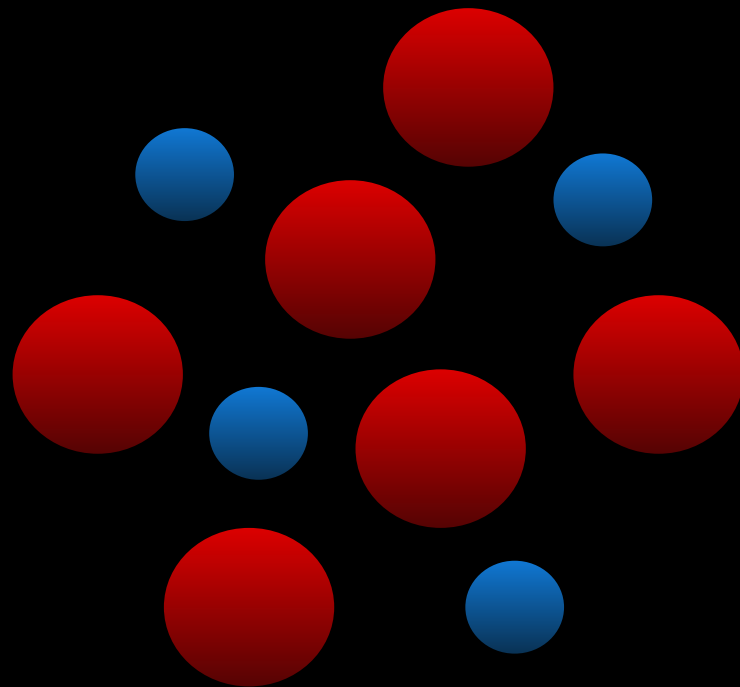
The average **plaquette** and **gradient-flowed Polyakov loop**, though **not true order parameters**, indicate a finite-temperature phase transition.

We scan in  $\widehat{m}_h$  for various **fixed** values of  $\widehat{m}_l/\widehat{m}_h$  to obtain the full finite-temperature phase diagram.

Our simulations use **dynamical stout-smear**ed Mobius domain wall fermions with Symanzik gauge action.

The results that follow are obtained on  $8^4$  and  $16^3 \times 8$  lattices. We take  $L = 2N_T$ .

Our results are **preliminary**.



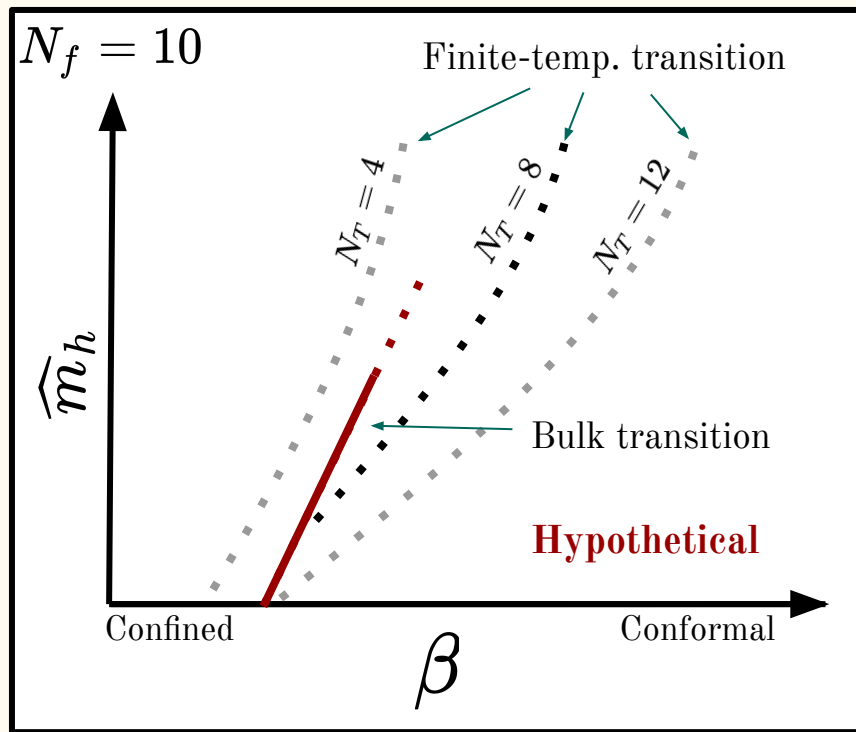
# Finite-Temperature Study of the $N_f = 10$ Mass-Degenerate System

To start off, we simulate the  $N_f = 10$  **mass-degenerate** system.

We find that we run into a “**bulk**” phase transition for the choice of  $N_T = 8$  and  $\beta = 4.03$ .

This bulk phase transition is merely a **lattice artifact** and we move away from it as  $N_T$  increases.

This **sketch** is inspired by Schaich et al., arXiv:1207.7164.

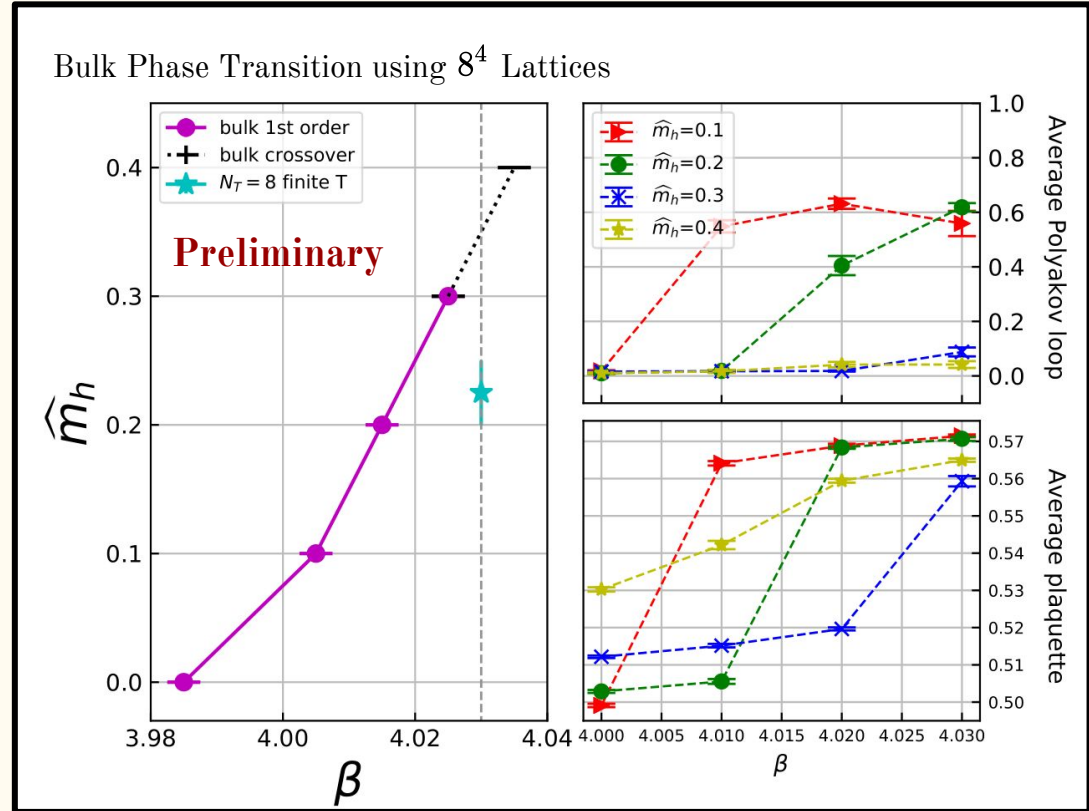


# Finite-Temperature Study of the $N_f = 10$ Mass-Degenerate System

To get a better idea of the **bulk phase transition**, we focus on  $8^4$  lattices.

Both the average **Polyakov loop** and **average plaquette** signal the existence of the bulk phase transition.

The **order** of the bulk phase transition seems to go from **first-order** to **crossover**.



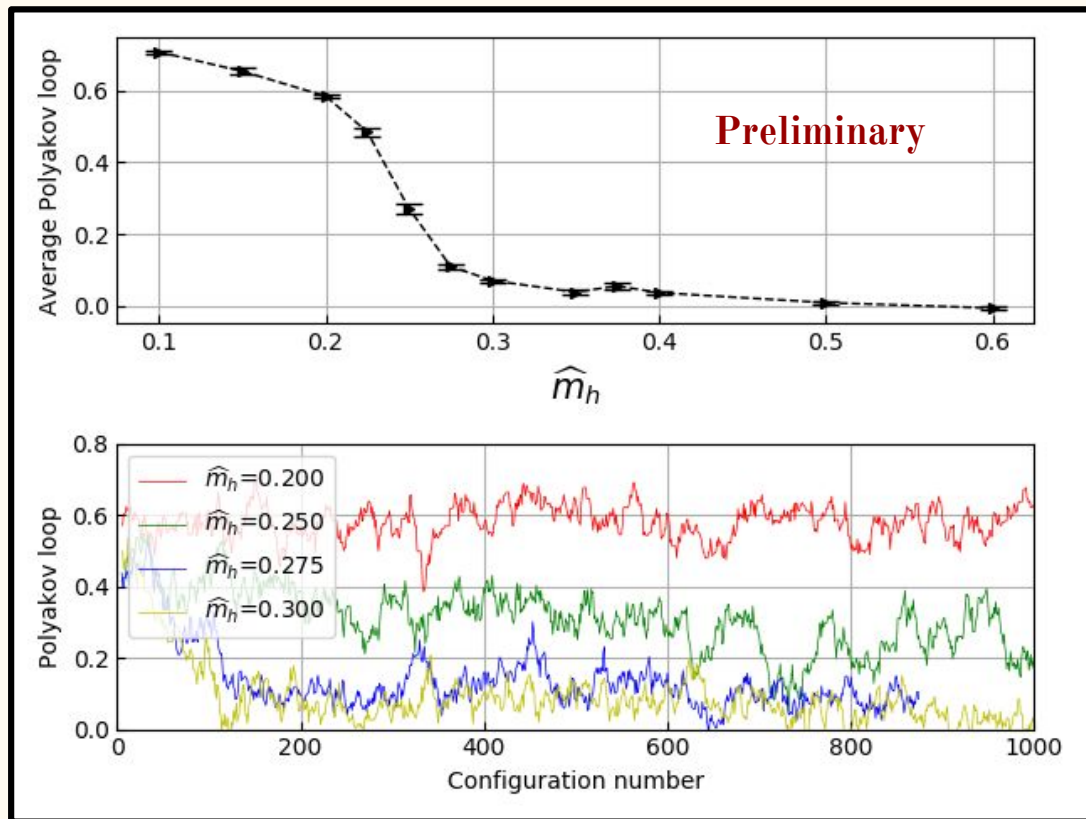


# Finite-Temperature Study of the $N_f = 10$ Mass-Degenerate System

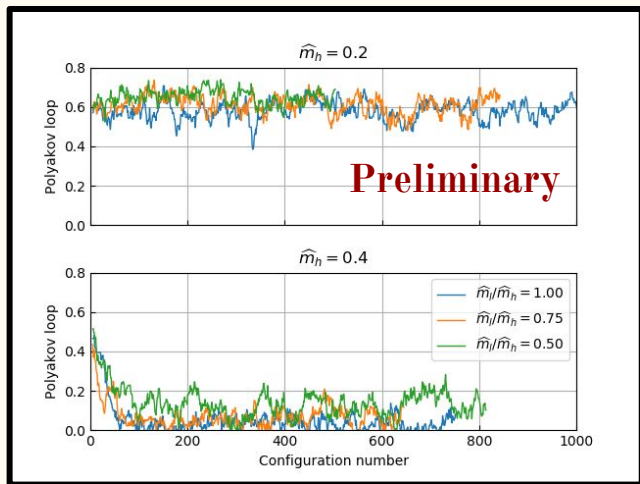
We scan in  $\widehat{m}_h$  and fix  
 $N_T = 8, L = 16, \beta = 4.03$ .

The **change** in the **average gradient-flowed Polyakov loop** and the **average plaquette** indicate that the mass-degenerate system experiences a **finite-temperature phase transition**.

Some ensembles may **still have long thermalization times**; hence, more time is needed to fully determine the nature of the transitions.



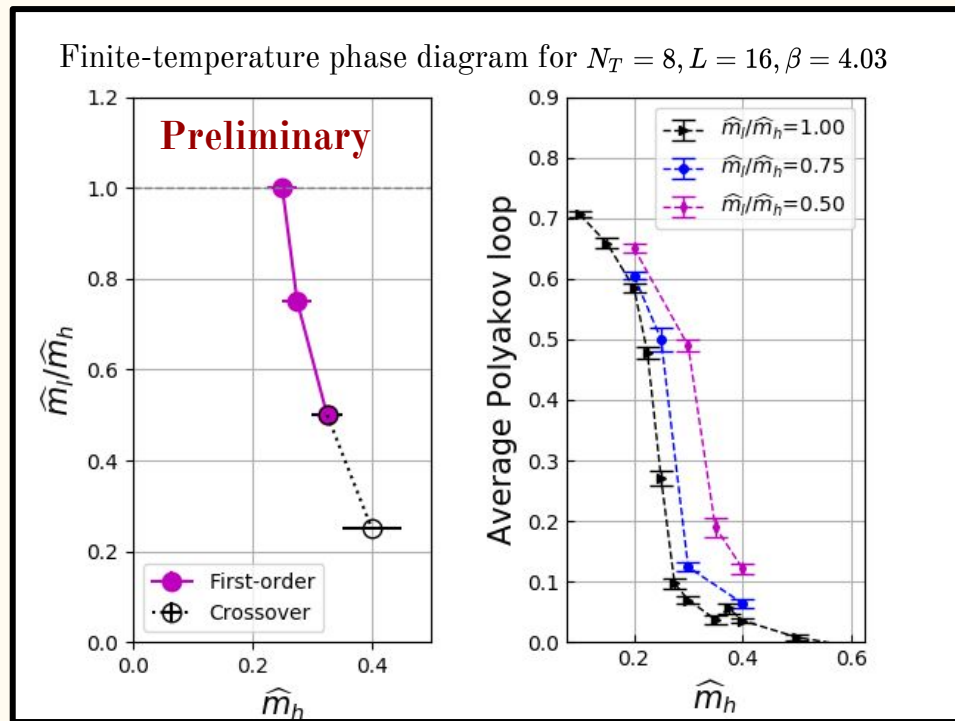
# Finite-Temperature Transition in the 4+6 Mass-Split System



We probe different  $\widehat{m}_l/\widehat{m}_h$  values for  $N_T = 8, L = 16, \beta = 4.03$ .

We suspect that  $\widehat{m}_l/\widehat{m}_h = 1.0, 0.75, 0.5$  may be **first-order** and ratios below  $\widehat{m}_l/\widehat{m}_h = .5$  may turn into a **crossover**.

We need more statistics to better understand the nature of the phase transition.



# Outlook

## Summary

We have presented **preliminary** results on a **finite-temperature** study of a **4+6 mass-split system**.  
We found that our initial choice of  $N_T = 8$  **runs into a bulk phase transition**. Our simulations indicate that there **could be a first-order phase transition** for  $N_T = 8$ .

## The Future

Accumulate **more statistics**.

Look at **different observables** (such as **susceptibilities**).

Simulate at different **gauge couplings**,  $\widehat{m}_l/\widehat{m}_h$ , **spatial volumes**, and **temperatures**.

**Establish** order of **finite-temperature** phase transition.

Understand better how to **convert lattice results** into **gravitational wave spectra**.

# Acknowledgements

CU Boulder Summit computing resources

USQCD computing resources

NSF Graduate Research Fellowship Program

