

Foundation of Collider (1)

Circular Collider
Linear Collider
Energy Recovery Collider
Gamma-Gamma Collider
Muon Collider
Plasma Collider

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4th International School on Beam Dynamics
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Limitation of Target Experiments

➤ By using synchrotrons/linacs we can accelerate particles (proton/electron, etc) up to some tens of GeV, even some 100's of GeV

➤ However, the center-of-mass energy of a 1000GeV proton and a proton at rest is only some 40GeV (next page)

$$\sqrt{2Mc^2E} = \sqrt{2 \times 1000 \times 0.938} = 43 \text{ GeV}$$

➤ High energy physics demands higher and higher energies

➤ How can we reach such energies?

Collider

➤ Consider a collision of two beams

- ✓ Either scheme is equivalent if the collision energy is the same



- ✓ Energy of the projectile beam is lower in the right-hand scheme
- ✓ When the particle energy is so high ($E \gg mc^2$), the right-hand-side scheme is by far better

$$E_{CM} \approx \sqrt{2mE} \quad \text{target experiment}$$

$$E_{CM} = 2E \quad \text{colliding beam}$$

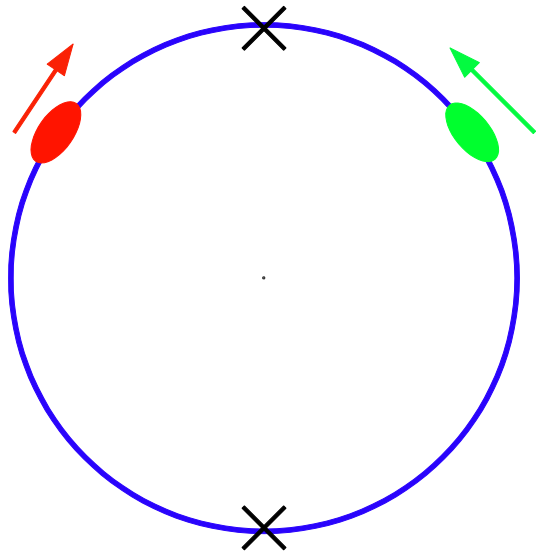
note: here mc^2 is simplified to m

$$\begin{aligned} \text{Derivation: } \sqrt{s} &= \sqrt{(p_1 + p_2)^2} = \sqrt{p_1^2 + p_2^2 + 2p_1 p_2} = \sqrt{2m^2 + 2(E_1 E_2 - \mathbf{p}_1 \cdot \mathbf{p}_2)} \\ &= \begin{cases} \sqrt{2mE} & (E_1 = E, E_2 = m, \mathbf{p}_2 = 0, m \ll E) \\ 2E & (E_1 = E_2 = E, \mathbf{p}_2 = -\mathbf{p}_1, m \ll E) \end{cases} \end{aligned}$$

- For example, a collision of two 0.5GeV electrons is equivalent to collision of 1TeV electron with an electron at rest

How to make particles collide?

- Beams of same energy and opposite charge
- Can use a single ring
- You need (electro-static) separators to avoid unnecessary collisions



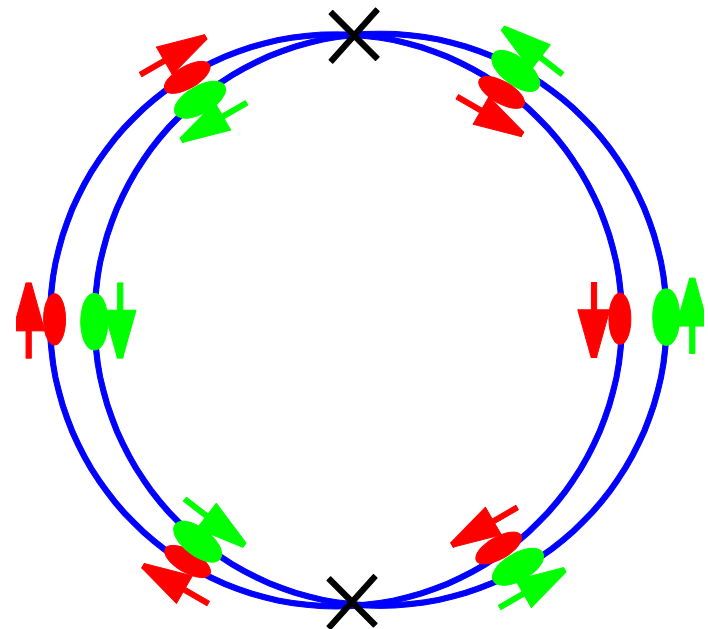
.... PETRA, TRISTAN, LEP,

..... SppS, Tevatron

2022/11/23 ISBA22

Yokoya

- Much more freedom by using two rings



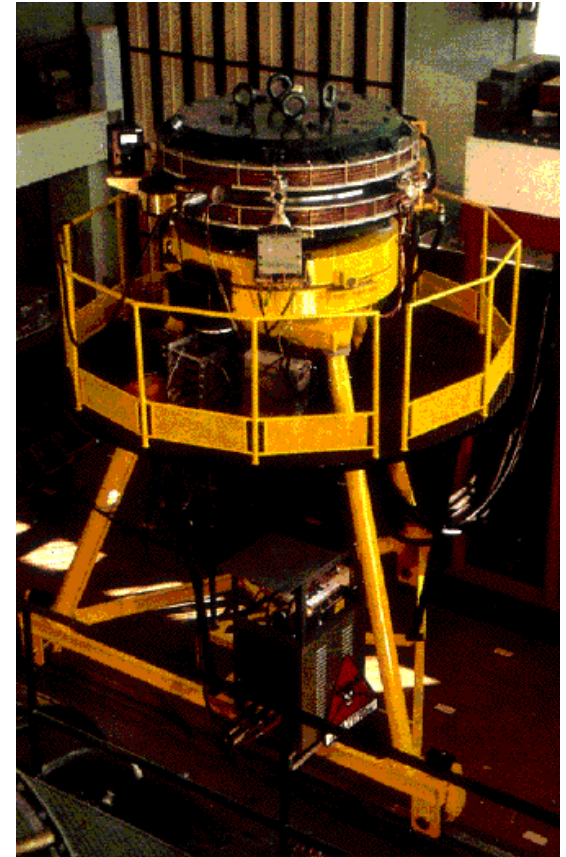
PEP-II, KEKB, LHC,

First Electron-Positron Collider: AdA

- First beam in Italy in 1961
- Moved to Orsay (France) and the first collision in 1964
- Orbit radius 65cm, collision energy 0.5GeV

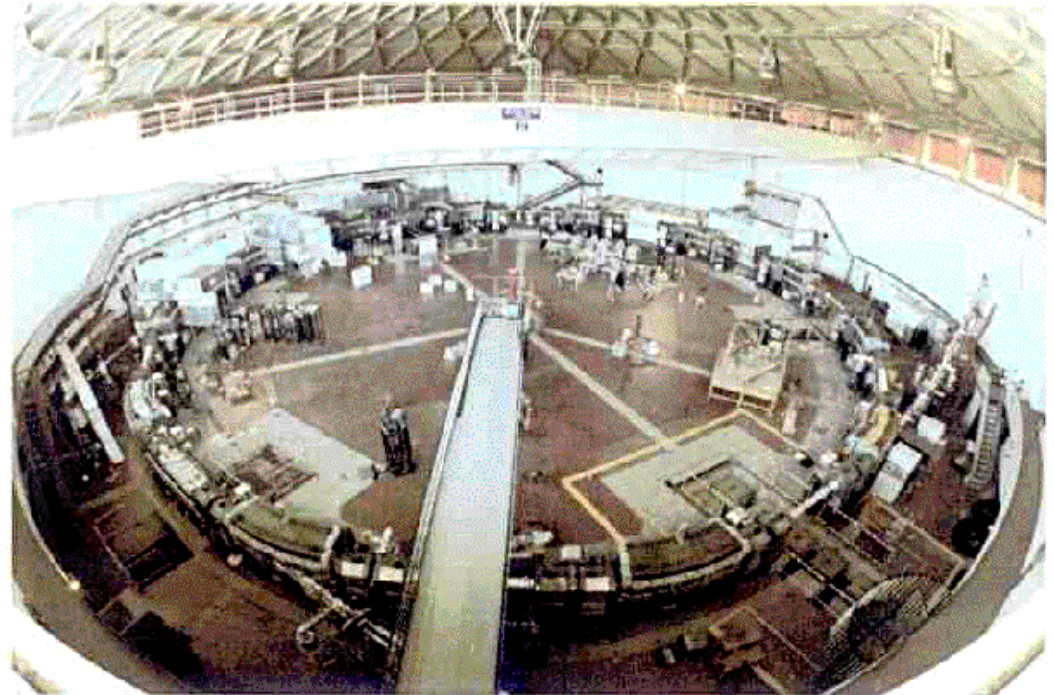


Now exhibited in a garden in Frascati, Italy



The second : Adone

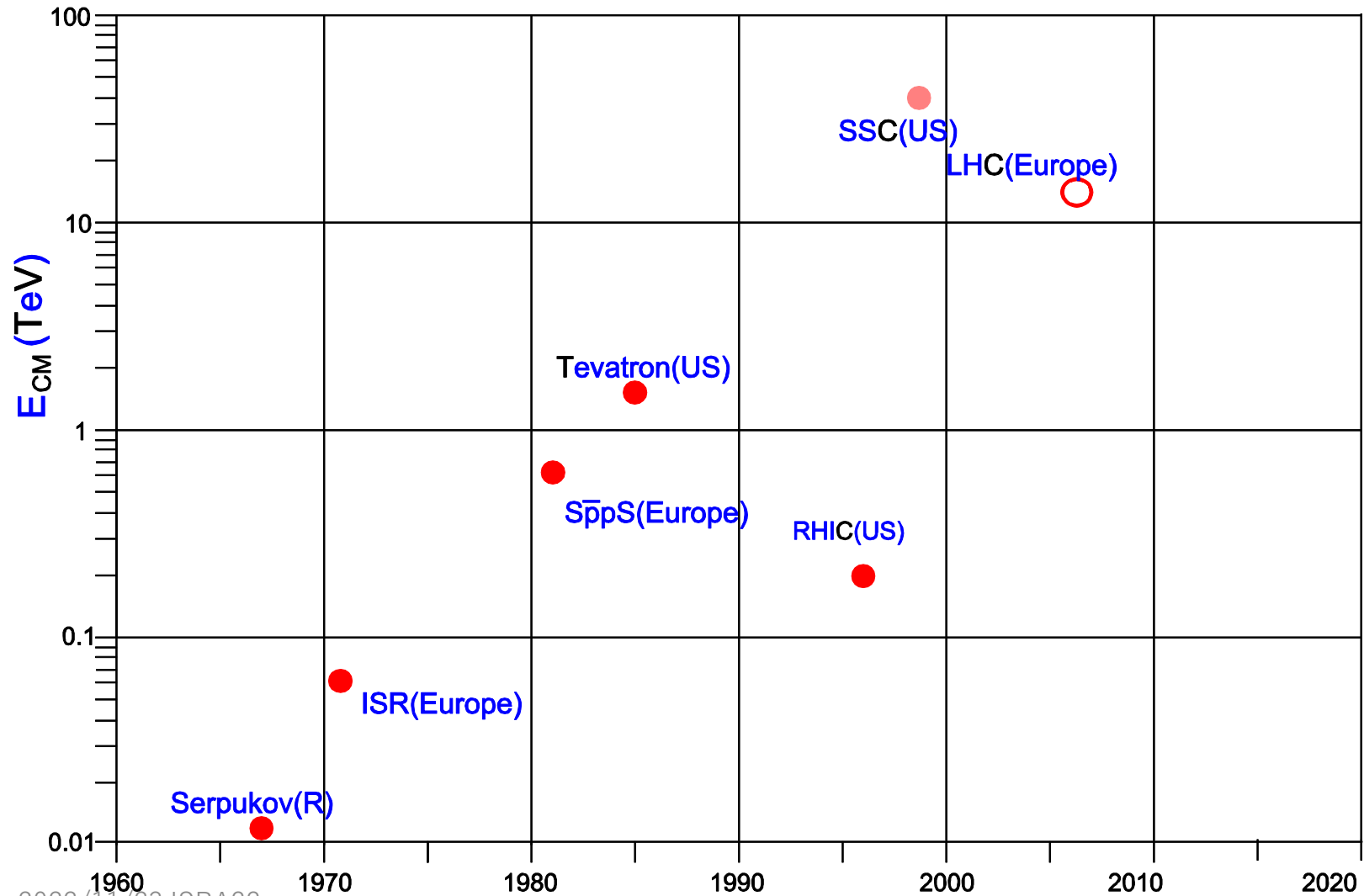
- The first beam in 1967
- Circumference 105m
- Collision energy $< 3\text{GeV}$
(Did not reach J/ψ at 3.1GeV)
- Luminosity $3 \times 10^{29} / \text{cm}^2 / \text{s}$



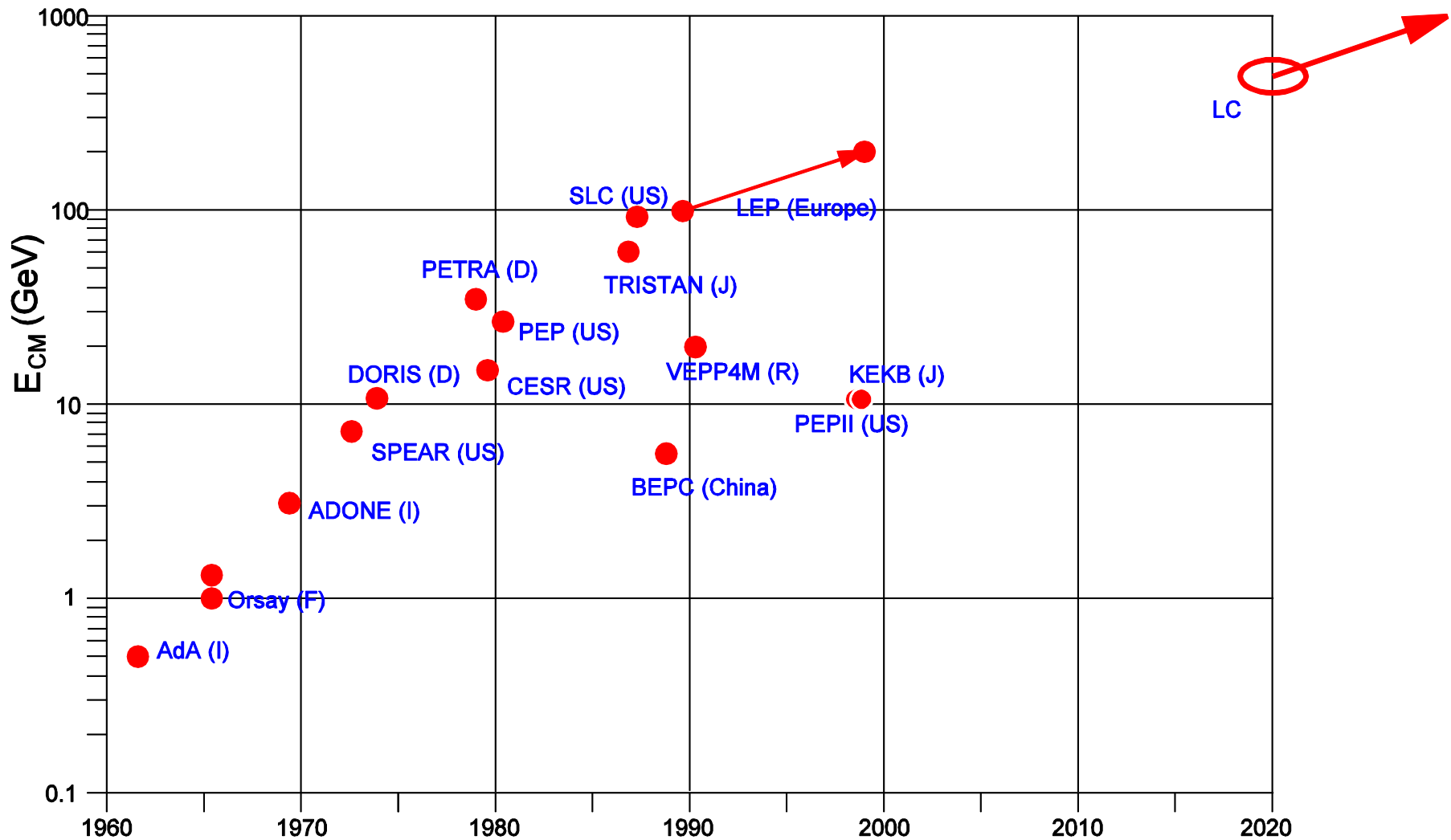
Many Colliders Built Since Then

- e^+e^-
- pp
- ppbar
- ions
- ep

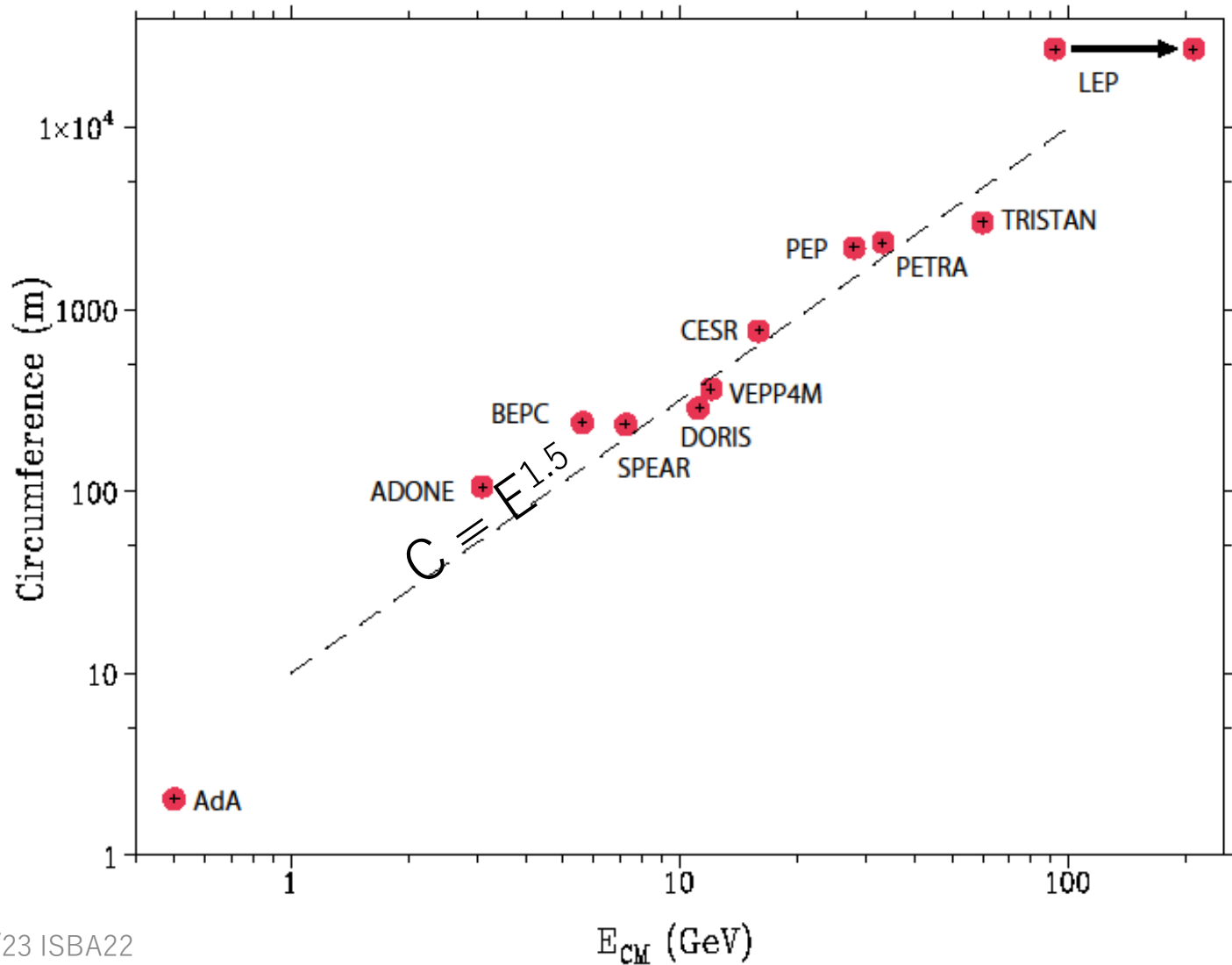
History of Proton/Antiproton Colliders



History of Electron-Positron Colliders



Energy vs. Ring Radius



Difficulty of Colliders

➤ Number of events per second

✓ Fixed target

$$F \times n \times d \times \sigma$$

- F : particle flux (number of particles per second)
- n : density of target (atoms / m³) , not the density of projectile
- d : target thickness
- σ : event cross-section

✓ Collider

$$L \times \sigma, \quad L = f_{col} \times \frac{N^2}{S} = \frac{FN}{S}$$

- L : Luminosity
- f_{col} : bunch collision frequency ($F = f_{col}N$)
- N : number of particles per bunch
- S : transverse cross-section of the bunch

➤ Essential difference: $n \times d \rightarrow N / S$ i.e., target density vs. beam density

➤ Need to pack many particles in a small area (firstly, the transverse area)

ABC of Circular Collider Dynamics

- Beam dynamics in a circular collider is basically similar to that of storage rings except for the conditions coming from the collision point
- Luminosity

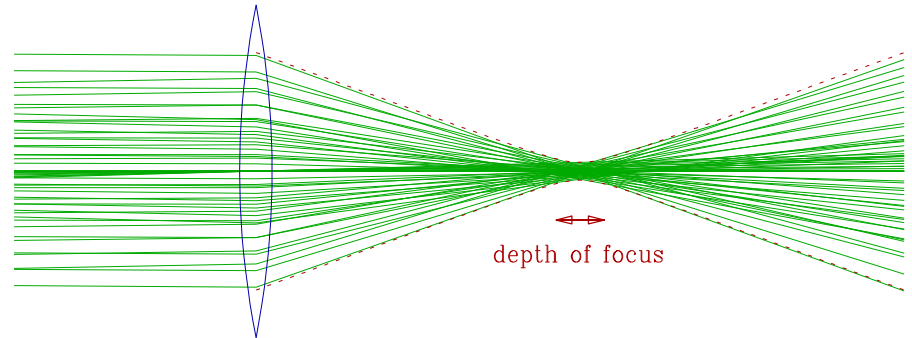
$$\mathcal{L} = \frac{f_{col} N^2}{4\pi\sigma_x\sigma_y}, \quad \sigma_x^* = \sqrt{\epsilon_x\beta_x^*}, \quad \sigma_y^* = \sqrt{\epsilon_y\beta_y^*}$$

The asterisk * indicates a quantity at the exact collision point

- Hour-glass Effect

$$\beta_y^* > \approx \sigma_z$$

$$\beta(s) = \beta^* \sqrt{1 + \frac{s^2}{\beta^{*2}}}$$



Beam-beam tune-shift

- The beam is focused (assume oppositely charged beams like e+e-) by the on-coming bunch
- This causes a shift of betatron frequency **as well as its spread**
- Their magnitude can be characterized by the parameter ξ_x, ξ_y . In the simple case of head-on collision of equal size Gaussian bunches

$$\xi_{x(y)} = \frac{r_e}{2\pi} \frac{N \beta_{x(y)}^*}{\gamma} \frac{1}{\sigma_{x(y)}^* (\sigma_x^* + \sigma_y^*)}$$

- There has been a limit of $\xi_{x,y}$ empirically to be around 0.06, but these days we can predict it by computer simulations
- It is larger when the radiation damping is strong (so, it is small for proton collider)
- For e+e- collider it is often assumed $\xi_{x,y} \sim 0.1$ these days.

Era of Huge Circular Colliders: Tevatron

- Fermi National Lab
- Proton - antiproton
- Circumference 6.3km
- 1TeV
- Completed in 1983
- Superconducting magnet 4.2Tesla
- 1995 Top Quark
- 2009 shutdown



Tevatron behind and Main Injector front

Era of Huge Circular Colliders: LEP

➤ LEP (Large Electron-Positron Collider)

✓ CERN

✓ Construction started in 1983

✓ Operation started in 1989

✓ Circumference 27km

✓ Ultimate beam energy
about 100GeV

✓ Closed in 2000

- LEP revealed
Generation of
elementary
particles = 3

$$n = 2.9841 \pm 0.0083$$



SPS: Super Proton Synchrotron

- Large proton synchrotron at CERN
- Operation started in 1976
- Achieved 500GeV in 1978
- Then, converted to the first proton-antiproton collider

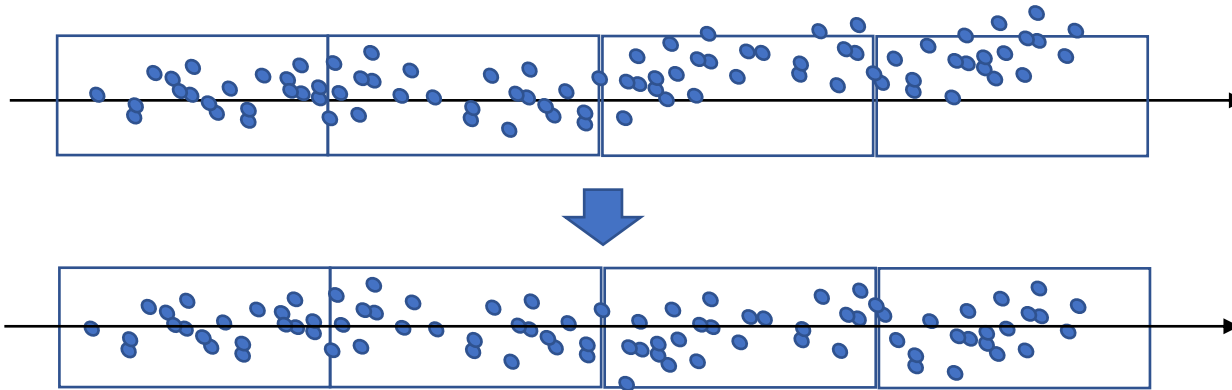
Stochastic Cooling

- Is a collider of proton and antiproton possible?
- Antiproton does not naturally exist
- Must be created by accelerator
- Anti-protons can be produced by accelerators \gg GeV, but the anti-proton beam is too big (low density)
- “Cooling” is needed for using it in colliders
- Cooling method (stochastic cooling) invented in 1968 by Simon van der Meer
- At CERN
 - ✓ Antiproton beam was cooled and accumulated in AA (Antiproton Accumulator) and transferred to SPS
 - ✓ SPS \rightarrow $S p p^{\text{bar}}$ S
 - ✓ The first $p p^{\text{bar}}$ collision in 1981
 - ✓ Discovery of W^{+-} , Z^0 in 1983



Concept of Stochastic Cooling

- Repeat the following process
 1. Measure the average beam position of the slices
 2. Kick each slice so that the center-of-mass comes to zero
 3. Shuffle the particles (actually, synchrotron oscillation)
- Average position approaches zero
- Speed proportional to $1/N$
 - ✓ N : number of particles in a slice
 - ✓ No cooling if N =infinite

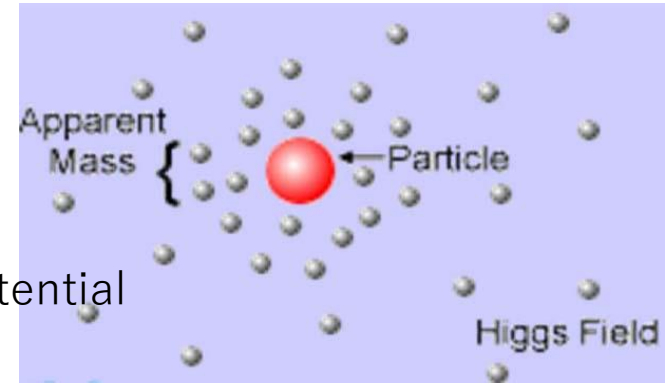


Higgs Particle

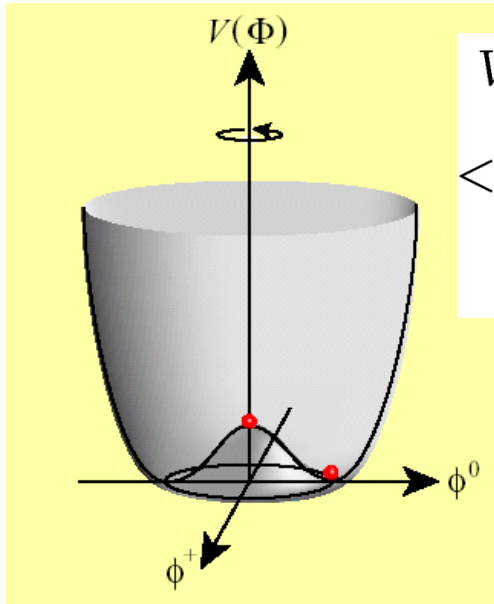
➤ Nambu-Goldstone Model

➤ Higgs mechanism

- ✓ Application of Nambu-Goldstone theory
- ✓ Start with zero-mass particles with symmetry
- ✓ Spontaneous symmetry breaking due to Higgs potential
- ✓ All particles coupled to Higgs acquire mass
- ✓ Applied to Weinberg-Salam theory



➤ Higgs particle: the only particle that had not been discovered in the Standard Model



$$V(\phi) = -\mu^2\phi^2 + \lambda\phi^4$$
$$\langle \phi \rangle = \begin{pmatrix} 0 \\ v/\sqrt{2} \end{pmatrix}$$
$$M_H = 2\lambda v^2$$



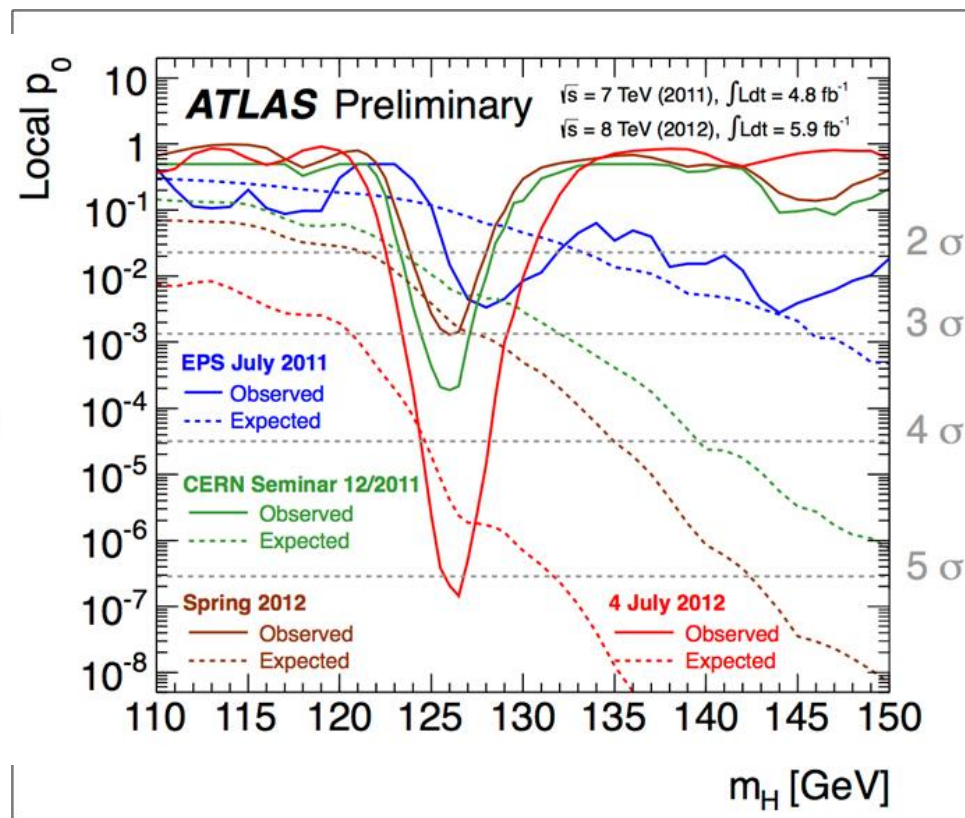
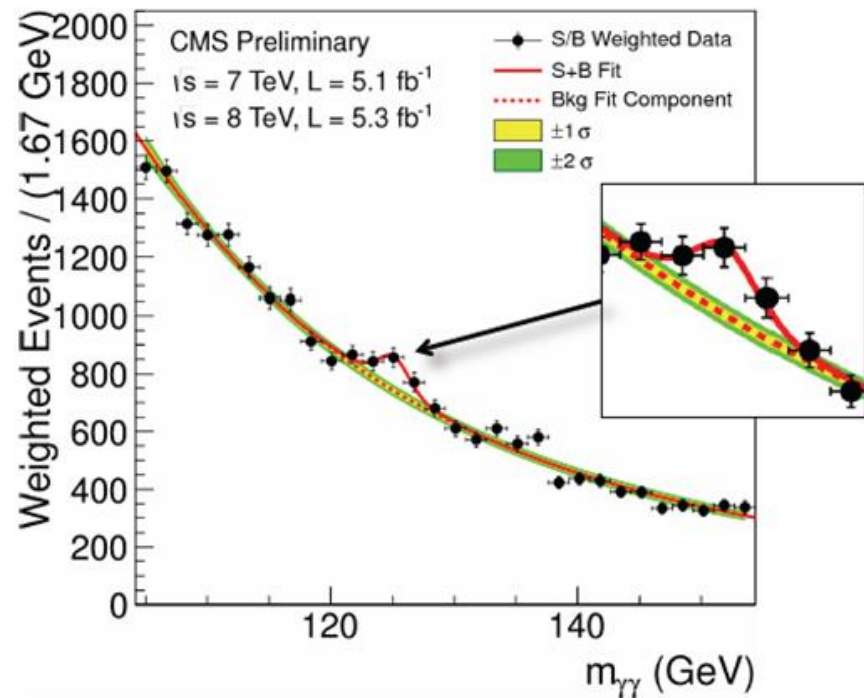
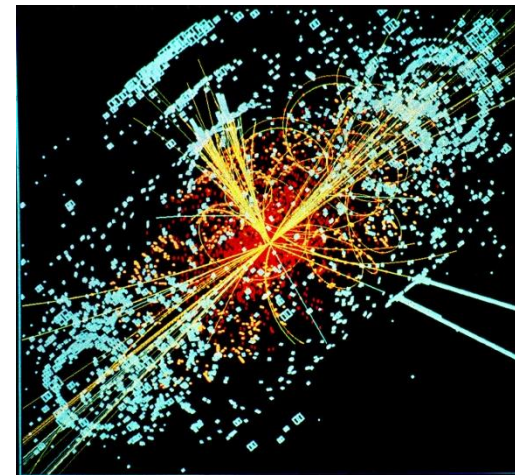
Y. Nambu



P. Higgs

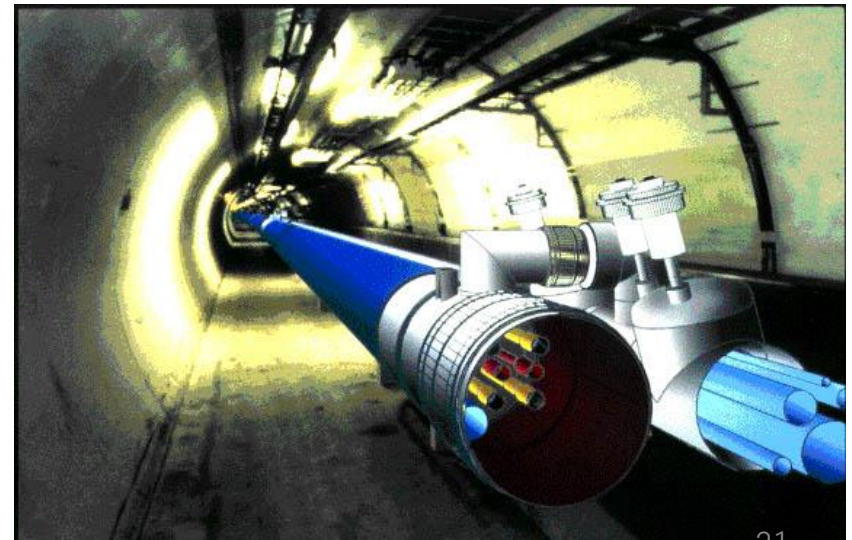
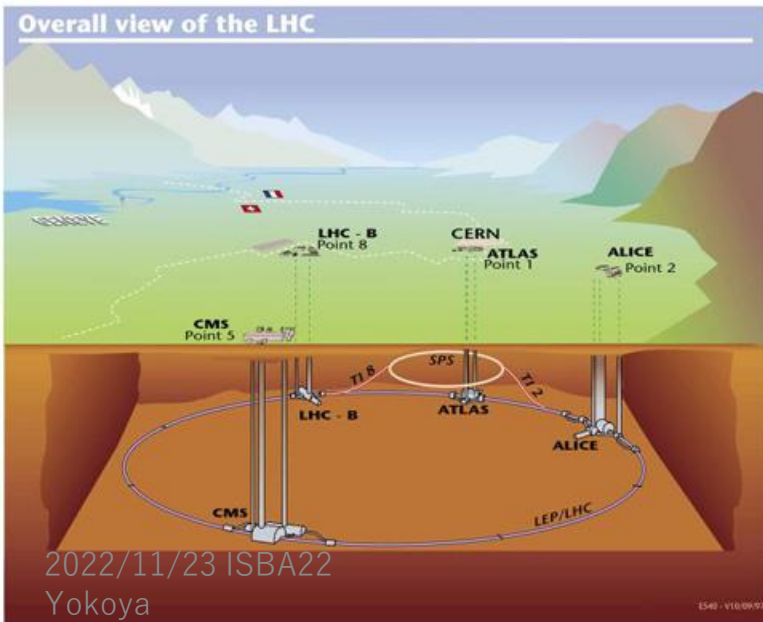
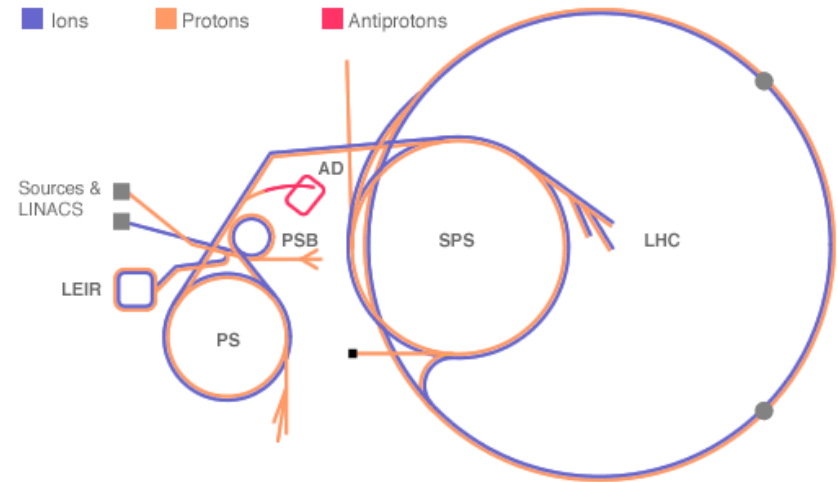
Discovery of "Higgs"

- Announced on Jul.4, 2012
- ~125GeV



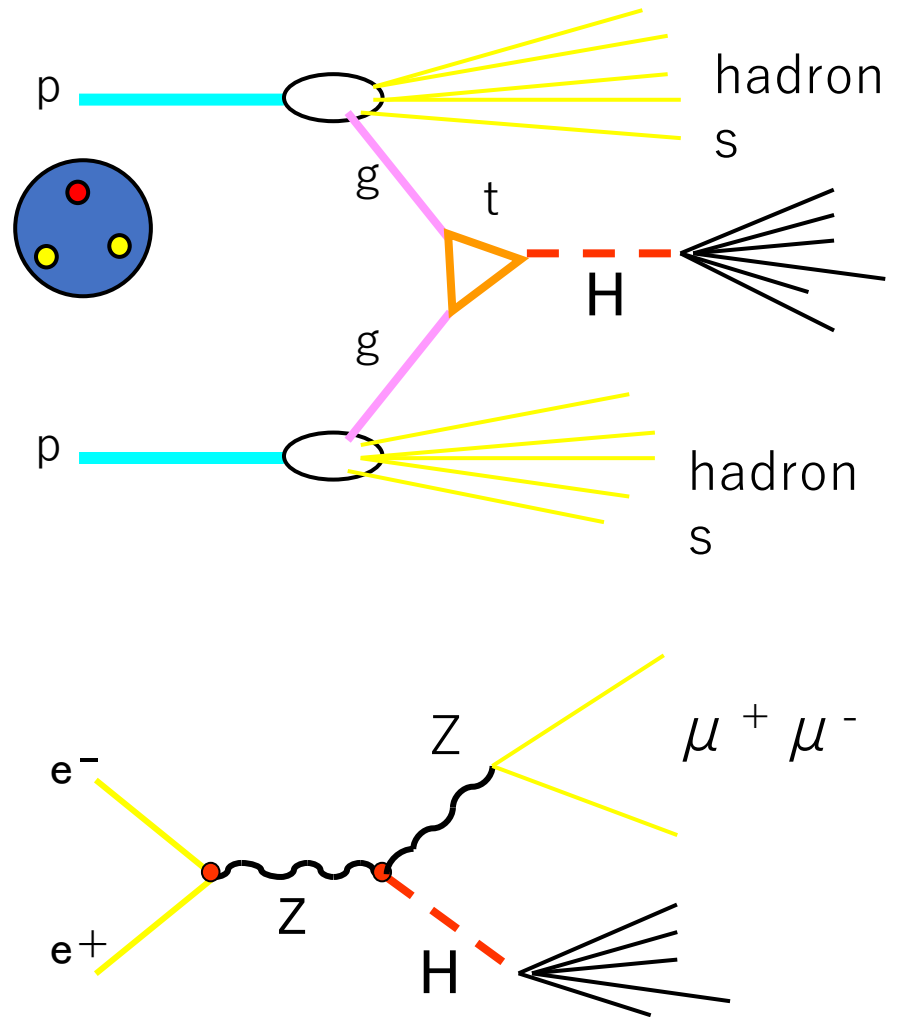
Huge Colliders Era (continued)

- LHC
- Recycle of LEP tunnel
- 14TeV proton-proton
- Discovered Higgs particle in 2012



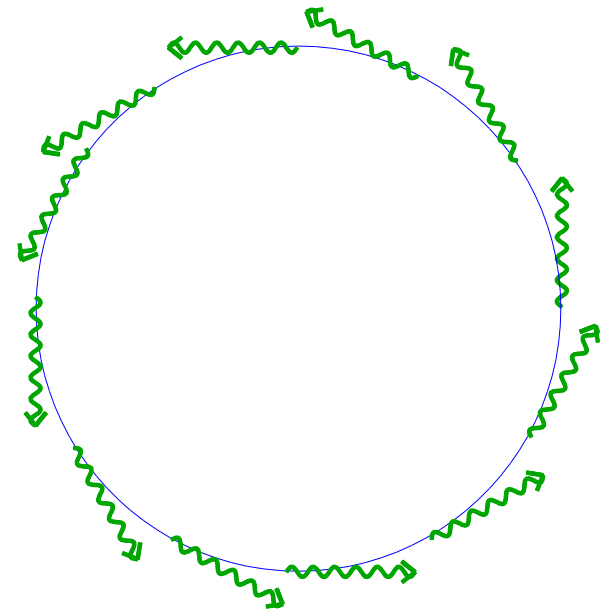
LHC is not the End

- LHC discovered Higgs
 - ✓ LHC is a proton collider
 - ✓ Protons are easier to accelerate to high energies
 - ✓ But the collision is complex due to the complexity of proton
- On the other hand, e^+e^- collider is:
 - ✓ Particle structure is simple
 - ✓ Better for probing particle properties
 - ✓ e^+e^- colliders are useful for precision measurement



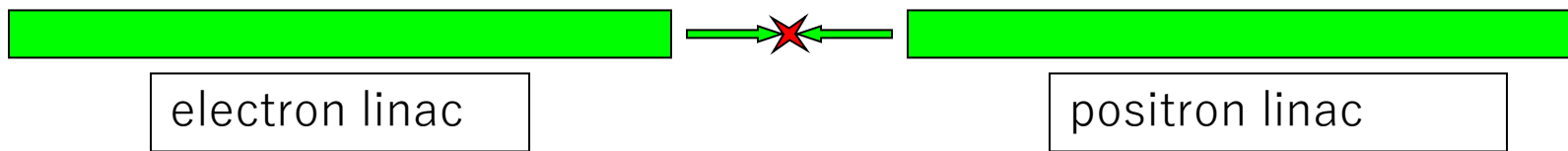
Limitation of Circular Accelerator

- High energy electron (positron) in a circular orbit emits photons (synchrotron radiation) in forward direction and loses energy
- Energy loss in one second is proportional to E^4 / ρ^2
 - This is useful for some purposes
 - Use synchrotron light for material physics
 - But is a big obstacle for getting high energy electron

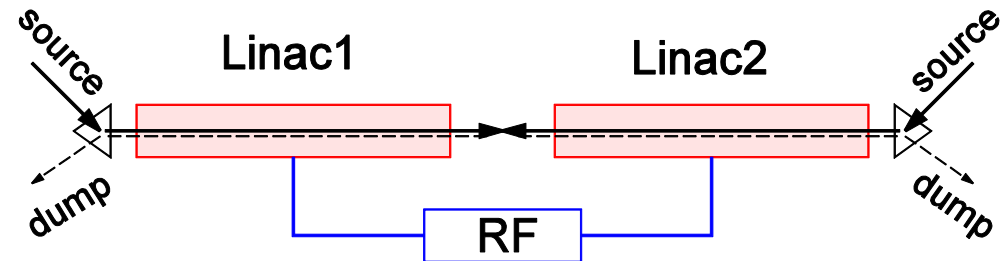


Electron-Positron Linear Collider

- To go beyond $E_{CM} = 209\text{GeV}$, linear collider is the natural choice



- Proposal in early 1960's
 - About the same time as the first circular collider AdA
 - Energy recovery was the original concern

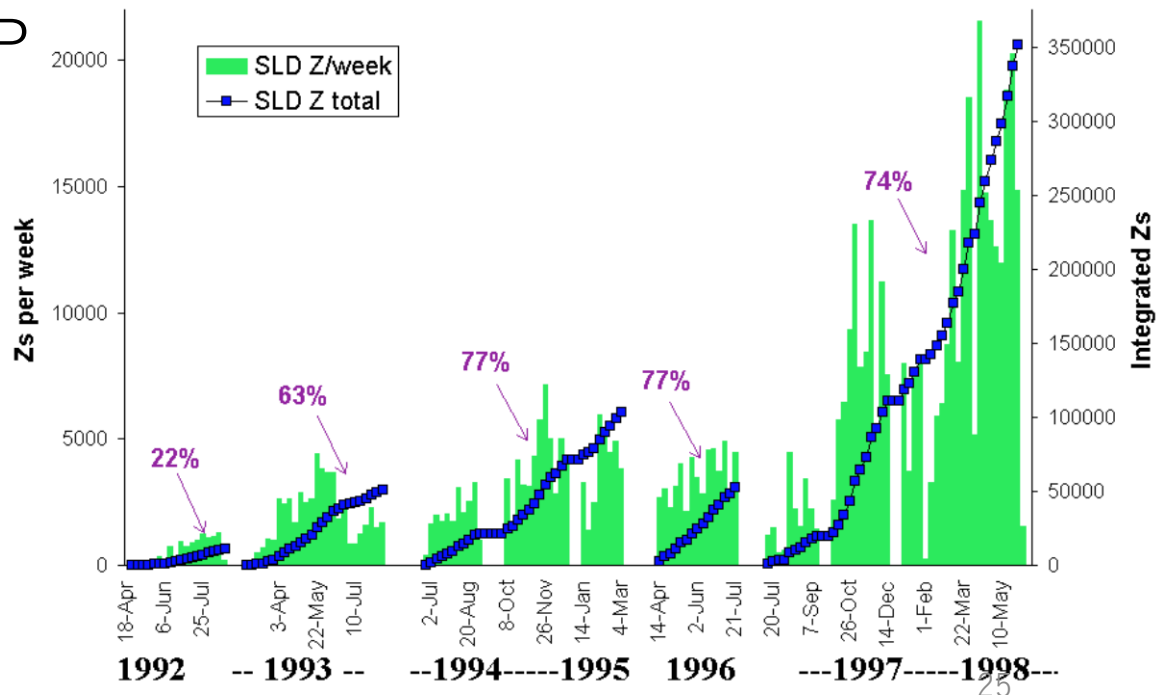
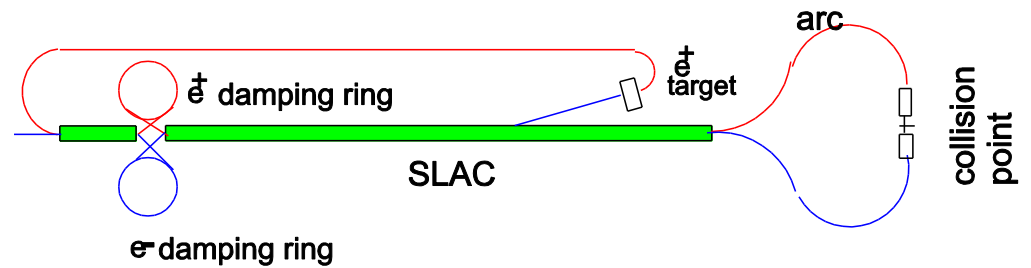


M. Tigner, Nuovo Cimento **37** (1965) 1228

- Note: Linear Collider not needed for proton

SLC : The First Linear Collider

- Single linac
 - ✓ One revolution was possible if up to 46GeV
- Completed in 1987 at SLAC
- First Z^0 event in May 1989
- Competition with LEP
- Polarized electron beam ($\sim 80\%$)
- Finished in 1998
- luminosity 3×10^{30} /cm²/s (design 6×10^{30})



Why LC was not built till 1987 ?

- Difference from Ring collider : **single pass**
 - ✓ Pass accelerating structure only once
 - ✓ Beam is thrown away after one collision
- 2 Issues come from this nature of LC
 - ✓ High gradient acceleration
 - Total length is decided by the accelerating gradient
 - ✓ Fine beam
 - Low collision rate
 - Beam must be focused to a tiny spot at the collision point

Luminosity

➤ Number of events in unit time = $\mathcal{L} \times \sigma$

- ✓ σ comes from physics
- ✓ \mathcal{L} accelerator parameter

➤ Luminosity

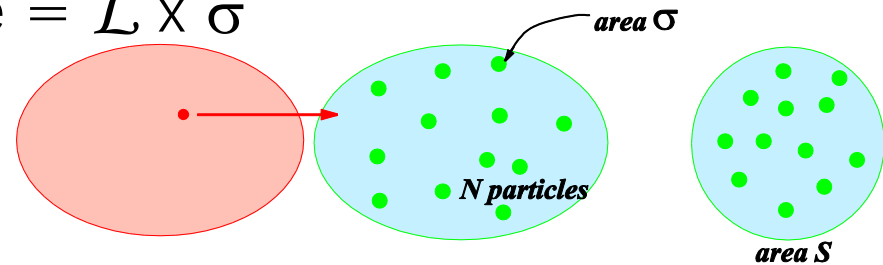
$$\mathcal{L} = \frac{f_{col} N^2}{\text{beam crosssection}}$$

➤ N: number of particles per bunch

➤ f_{col} bunch collision frequency

- ✓ Circular: number of bunches x revolution frequency
- ✓ Linear: number of bunches x pulse repetition frequency
- ✓ LC loses factor 100-10000

➤ To compensate for this difference, LC must squeeze the beam to a tiny spot at the interaction point (IP)



Development of LC Technology

- Serious R&D started in mid 1980's
 - ✓ US, Germany, Soviet Union, CERN, Japan
 - ✓ Many machine names were born
NLC, TESLA, VLEPP, CLIC, JLC
- Acceleration method
 - ✓ New advanced schemes proposed in early stages
 - Laser grating, inverse FEL, dielectric accelerator, plasma
 - ✓ Settled to the conventional **microwave method** but with improved technologies
 - ✓ SCRF, Xband NC, C-band NC, Xband single bunch, two beam
 - ✓ R&D's unified to SCRF for the next (after SLC) generation LC in 2004

Advantages of SCRF

➤ Low loss

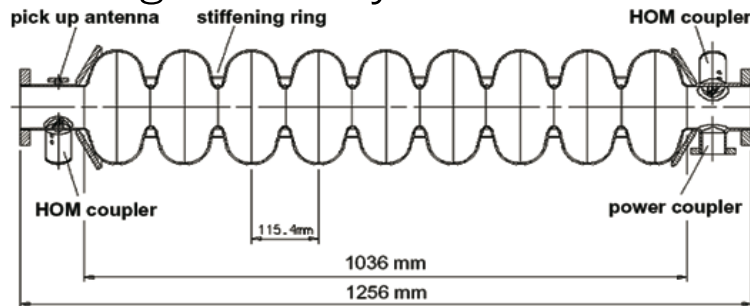
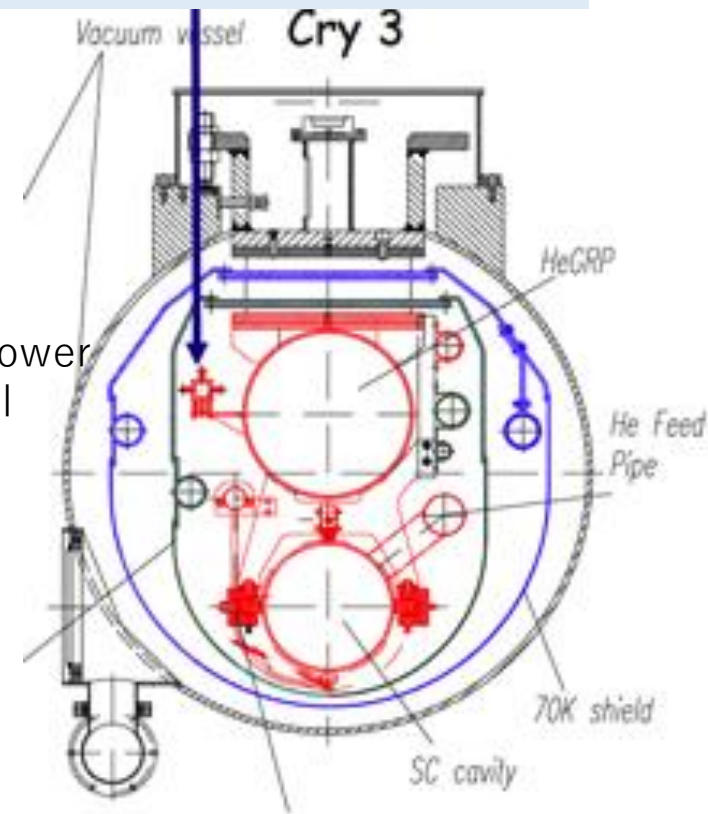
- ✓ The Ohmic energy loss per unit time proportional to $1/Q_0$
- ✓ $Q_0 \sim 10^{10}$ (SC), 10^4 (NC)
- ✓ But, keep in mind
 - Pulse length \sim ms (SC), $\sim \mu$ s (NC)
 - To remove 1W of heat, SC required 1kW AC power
 - So, the difference between SC and LC is small (see the next page)

➤ Long pulse

- ✓ Easier intra-pulse feedback
- ✓ Detector deadtime

➤ Disadvantages of SC

- ✓ Lower accelerating gradient
 - ~ 30 MV/m (ILC), ~ 100 MV/m (CLIC)
- ✓ Large refrigeration system



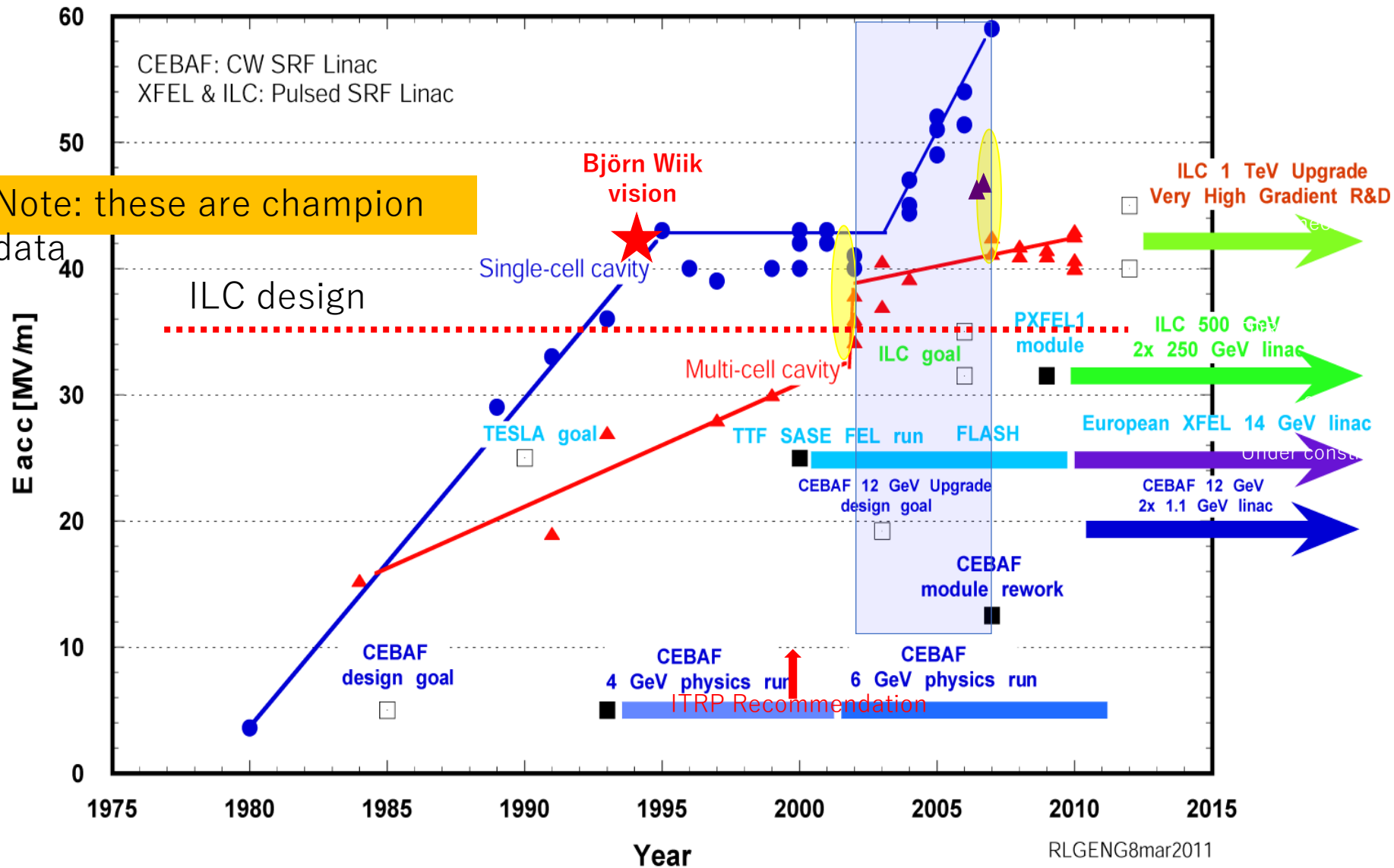
NC vs. SC --- Power Efficiency

		ILC 500GeV	CLIC 3TeV
Loaded gradient	MV/m	31.5	100
Beam power/beam	MW	5.2	14
Total power consumption	MW	163	582
Beam power/total AC power	%	6.4	4.8
Main linac power efficiency*)	%	12	6

- *) = beam power gain / AC power for main linac
- Including cryogenics (ILC), drive linac and drive beam manipulation (CLIC), linac magnets,
 - Not including AC high power line

History of Gradient of SCRF Cavities

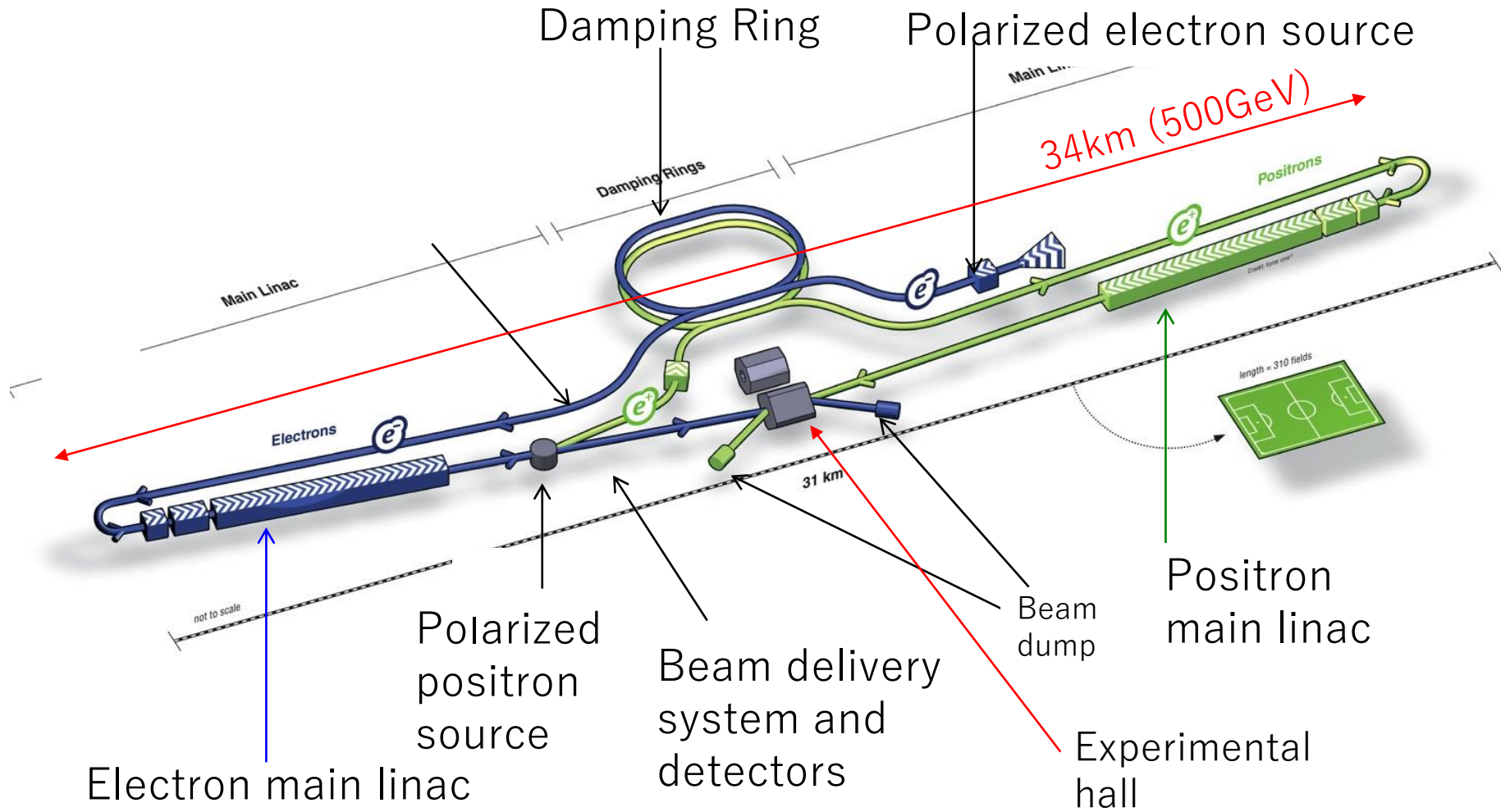
Note: these are champion data



ILC

- e+e- linear collider using superconducting acceleration technology
- Start with $E_{\text{CM}}=250\text{GeV}$, to be later upgraded to $500\text{GeV}/1\text{TeV}$
 - ✓ Site length $\sim 20\text{km}$ ($\sim 30\text{km}$ for 500GeV , $\sim 50\text{km}$ for 1TeV)
- Average accelerating gradient 31.5MV/m
 - ✓ Site length for $E_{\text{CM}}=500\text{GeV}$ is $\sim 30\text{km}$
 - ✓ Now under R&D for higher gradient
 - Even to 2-3 TeV?
- I will not describe it in detail
 - ✓ You will hear many times in this school
 - ✓ In particular, Kuriki san's lecture

ILC Layout



ILC Schema | © www.form-one.de
not to scale