

Disentangling polarization of the ϕ meson through hadronic and electronic decay channel

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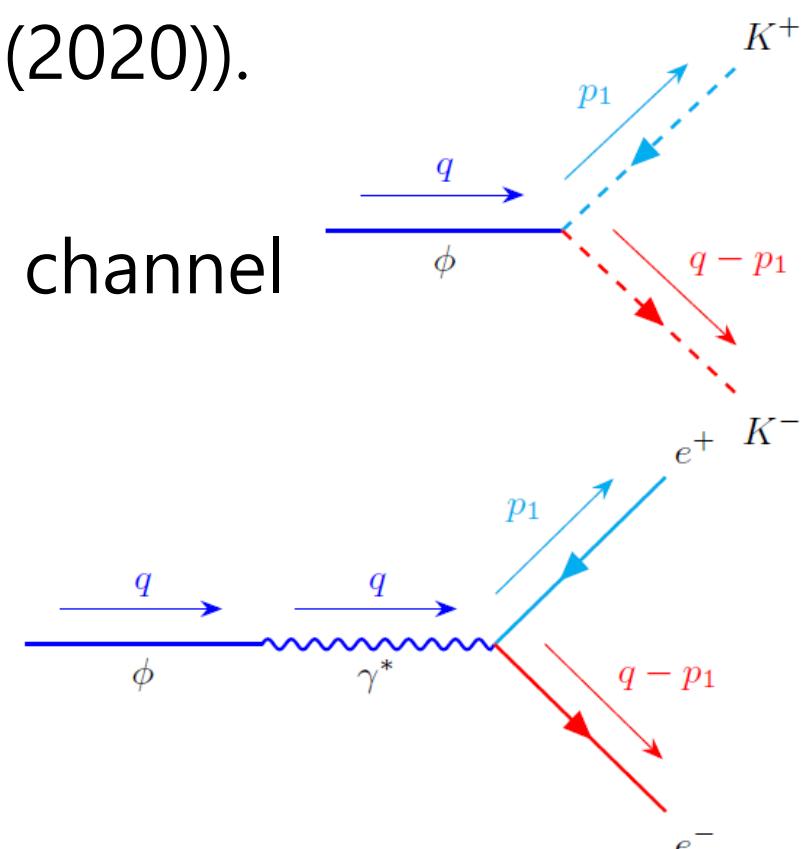
J-PARC

KEK
加速器だから見える世界。
Insight through Accelerators.
is in vacuum & matter"

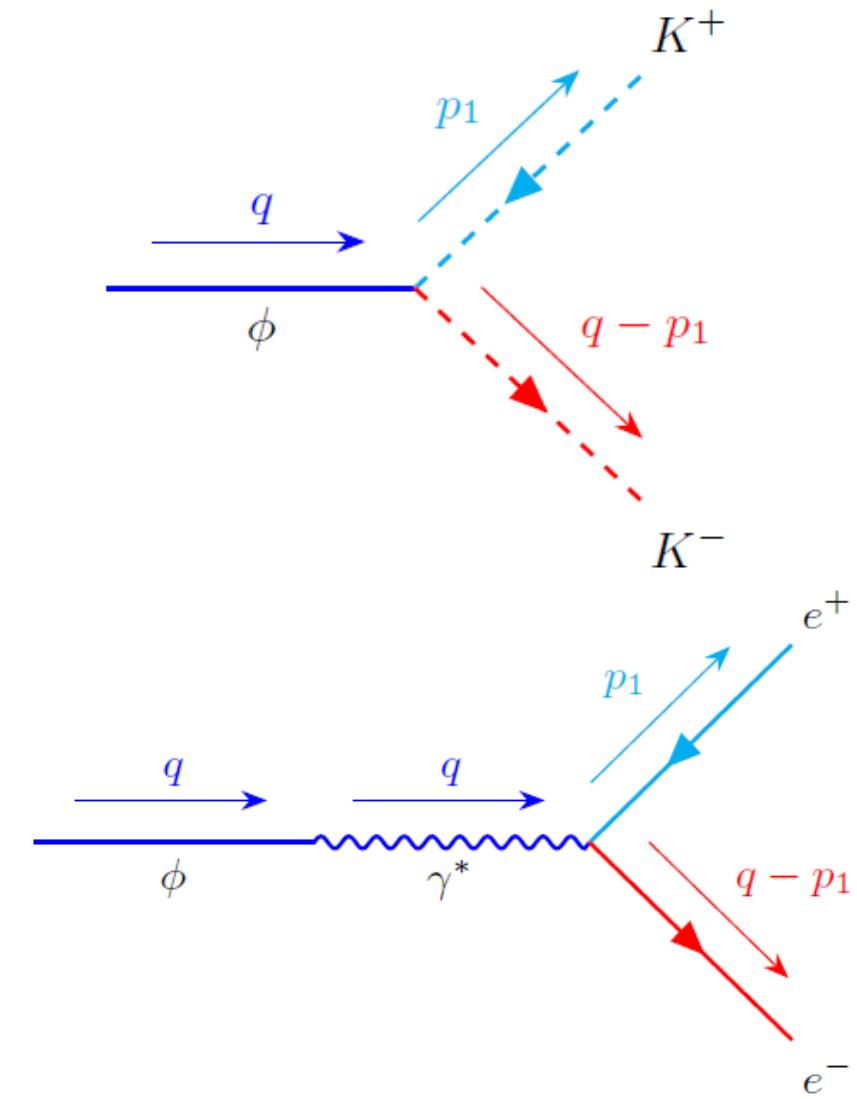
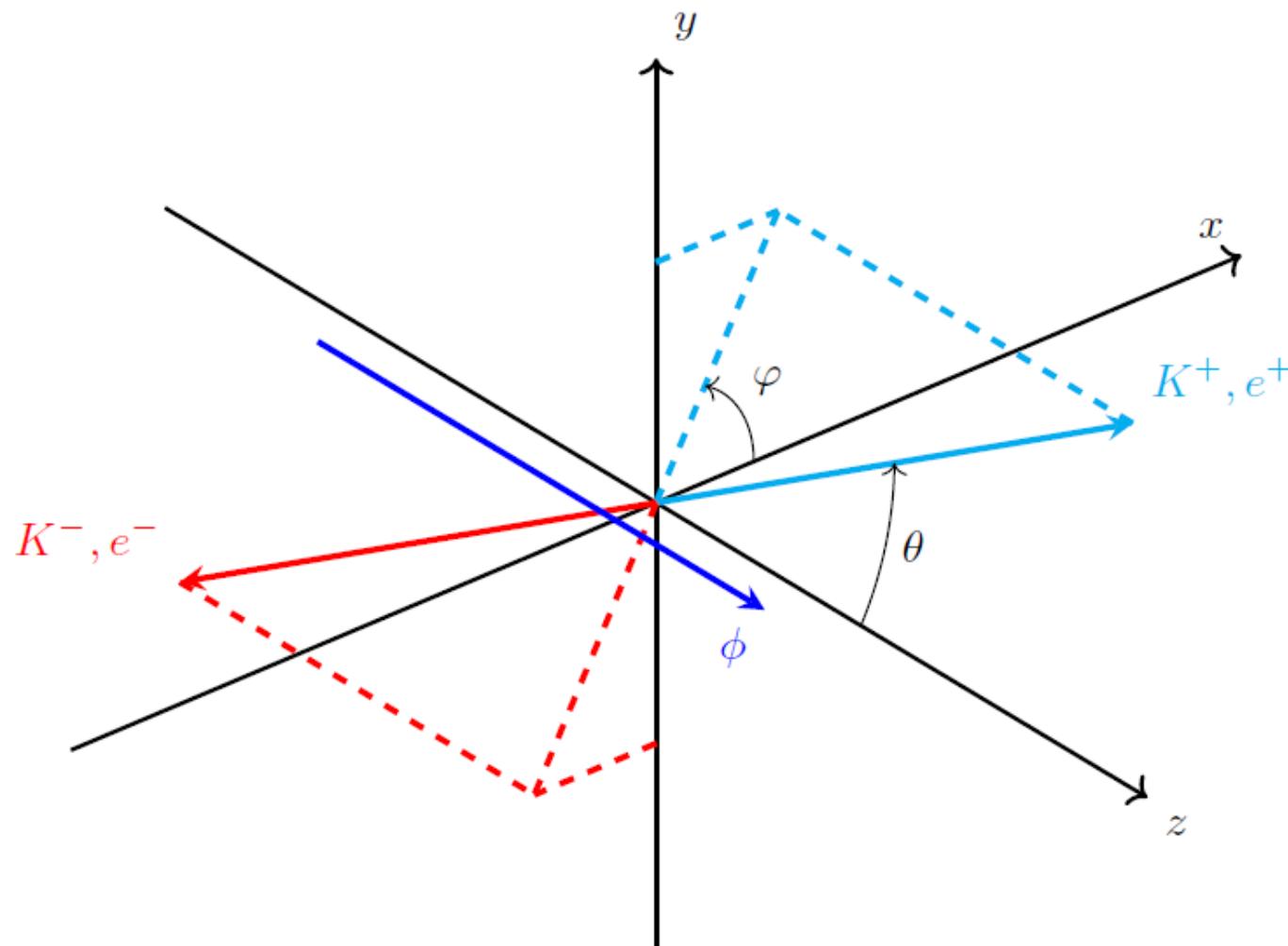
RIKEN

Why calculate angular distribution of each polarization

- Mass shift in nuclear matter depends on momentum and polarization mode when three momentum is not zero.
- Current on-going experiment, ϕ meson invariant mass in the nucleus is studied through dilepton channel(ex: J-PARC E16(2020)).
- Recently proposed experiment J-PARC E88: Kaon channel
- $\phi \rightarrow K^+ + K^-$ has a larger branching ratio
- Kaon channel can complement dilepton channel



Basic kinematics of $1 \rightarrow 2$ decay in the CM frame

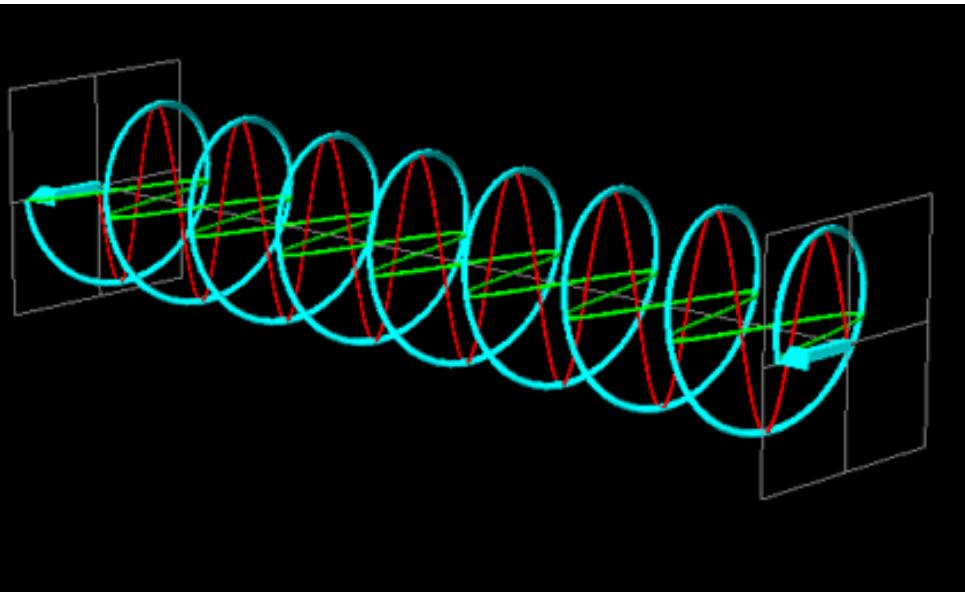


Polarization vector

- Four momentum, circularly polarized basis vectors of the ϕ meson in its rest frame

$$q^\mu = (m_\phi, \vec{0}), \varepsilon_{+1}^\mu = \left(0, -\frac{1}{\sqrt{2}}, -\frac{i}{\sqrt{2}}, 0\right), \varepsilon_{-1}^\mu = \left(0, \frac{1}{\sqrt{2}}, -\frac{i}{\sqrt{2}}, 0\right), \varepsilon_0^\mu = (0, 0, 0, 1)$$

- Satisfy a constraint $q^\mu \varepsilon_{\lambda\mu} = 0 (\lambda = \pm 1, 0)$



From Applied PhotoPhysics

Effective Lagrangian & Decay width of each process

$$\mathcal{L}_{\phi \rightarrow K^+ K^-} = g_K \phi_\mu (K^+ \partial^\mu K^- - K^- \partial^\mu K^+)$$

$$\mathcal{L}_{\phi \rightarrow e^+ e^-} = -\frac{e}{2g_J} F^{\mu\nu} \phi_{\mu\nu} \& - e \bar{\psi} \gamma^\mu A_\mu \psi$$

F. Klingl, N. Kaiser and W. Weise, Z. Phys. A 356,
193-206 (1996)

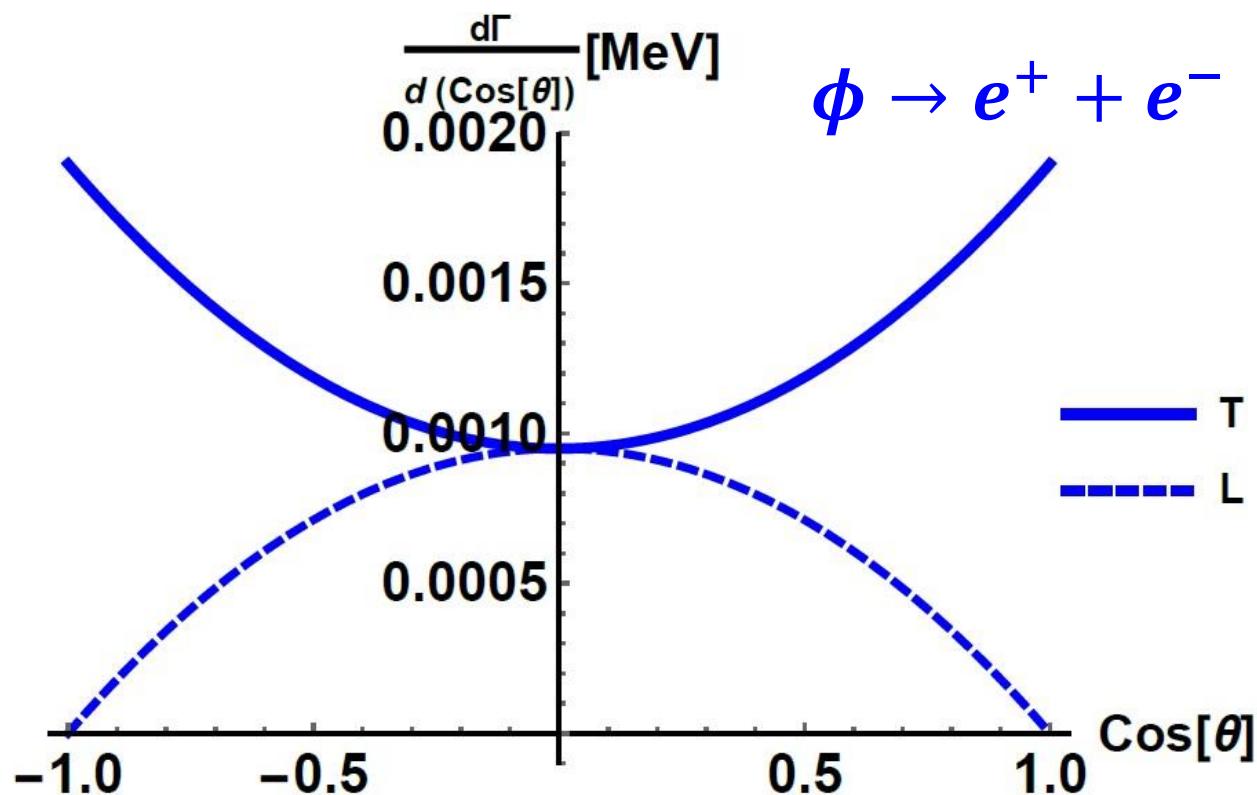
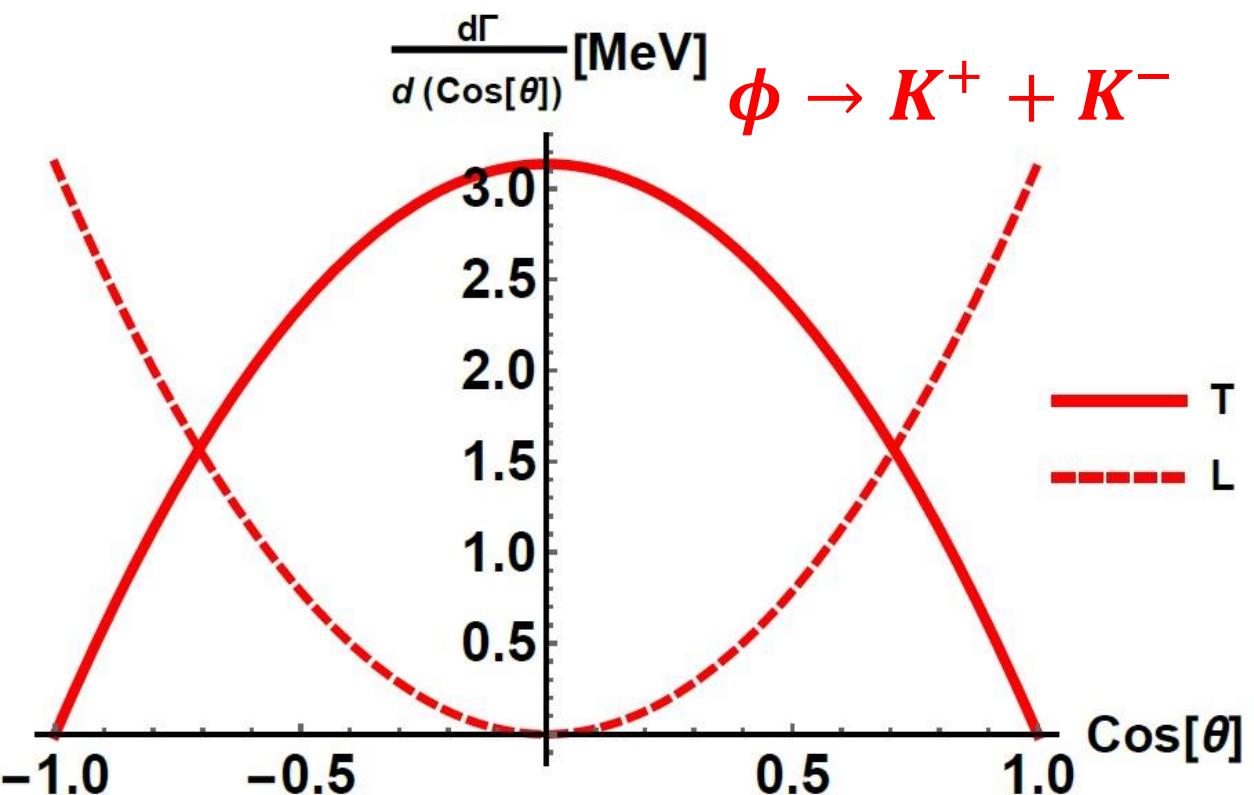
$$\Gamma = \begin{cases} 4.249 \times 0.492 \text{ MeV} (\phi \rightarrow K^+ + K^-) \\ 4.249 \times (2.974 \times 10^{-4}) \text{ MeV} (\phi \rightarrow e^+ + e^-) \end{cases}$$

R. L. Workman et al. [Particle Data Group], PTEP 2022,
083C01 (2022)

Hadronic tensor & Leptonic tensor

- Kaonic decay
 - $g_K = 4.476$
 - $\mathcal{M}_{Hadronic}^{\mu\nu} = g_K^2 (p_1 - p_2)^\mu (p_1 - p_2)^\nu$
- Electronic decay
 - $g_J = 13.4$
 - $\mathcal{M}_{Leptonic}^{\mu\nu} = \frac{64\pi^2\alpha^2}{g_J^2} \left(p_1^\mu p_2^\nu + p_1^\nu p_2^\mu - \frac{1}{2} m_\phi^2 g^{\mu\nu} \right)$
- Polarization tensor to separate transverse and longitudinal
 - $P_{\mu\nu} = P_{\mu\nu}^T + P_{\mu\nu}^L = \varepsilon_\mu^T \varepsilon_\nu^{T*} + \varepsilon_\mu^L \varepsilon_\nu^{L*}$

$\frac{d\Gamma}{d \cos \theta}$ for each polarization using polarization tensor



T: Transverse, L: Longitudinal

$$|\mathcal{M}|_T^2 = 4g_K^2 p_f'^2 \sin^2 \theta$$

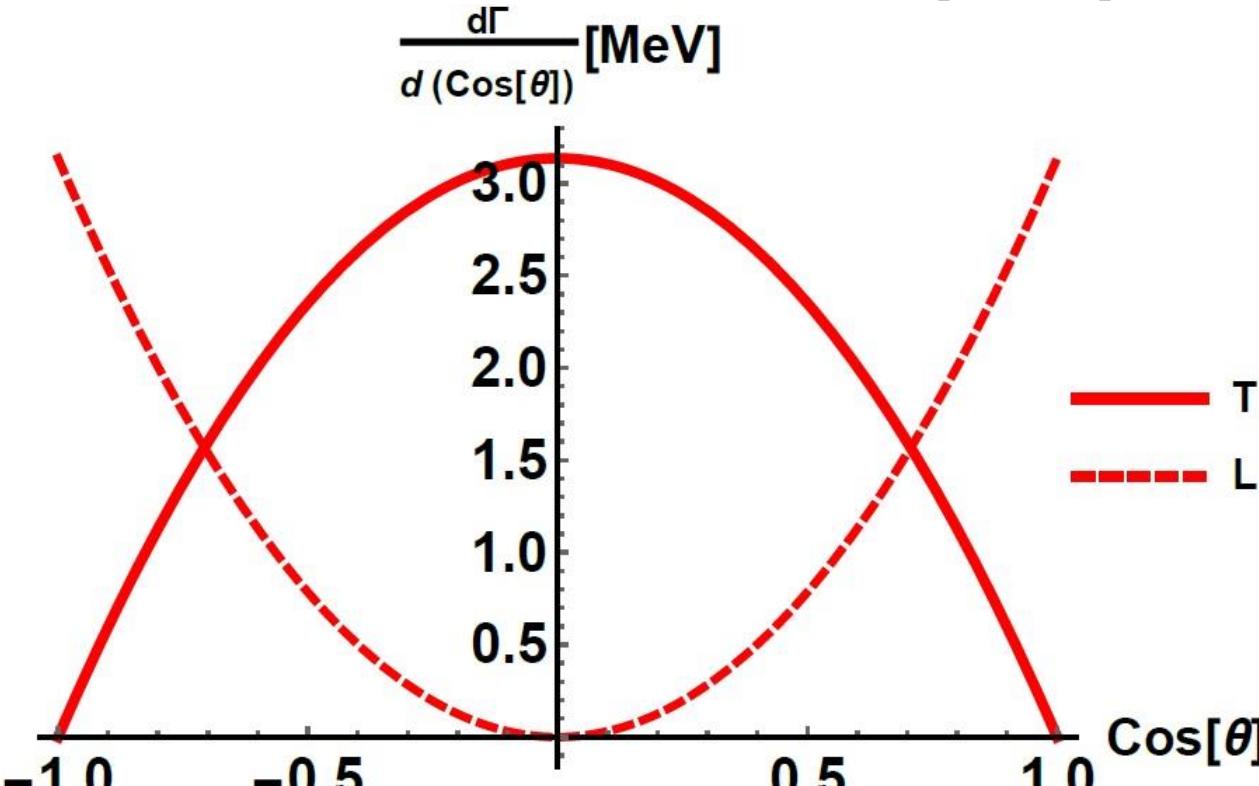
$$|\mathcal{M}|_L^2 = 4g_K^2 p_f'^2 \cos^2 \theta$$

$$|\mathcal{M}|_T^2 = \frac{64\pi^2 \alpha^2}{g_J^2} (m_\phi^2 - 2p_f'^2 \sin^2 \theta)$$

$$|\mathcal{M}|_L^2 = \frac{64\pi^2 \alpha^2}{g_J^2} \left(\frac{1}{2} m_\phi^2 - 2p_f'^2 \cos^2 \theta \right)$$

What happens at $\theta = 0, \pi$ & $\theta = \frac{\pi}{2}$?

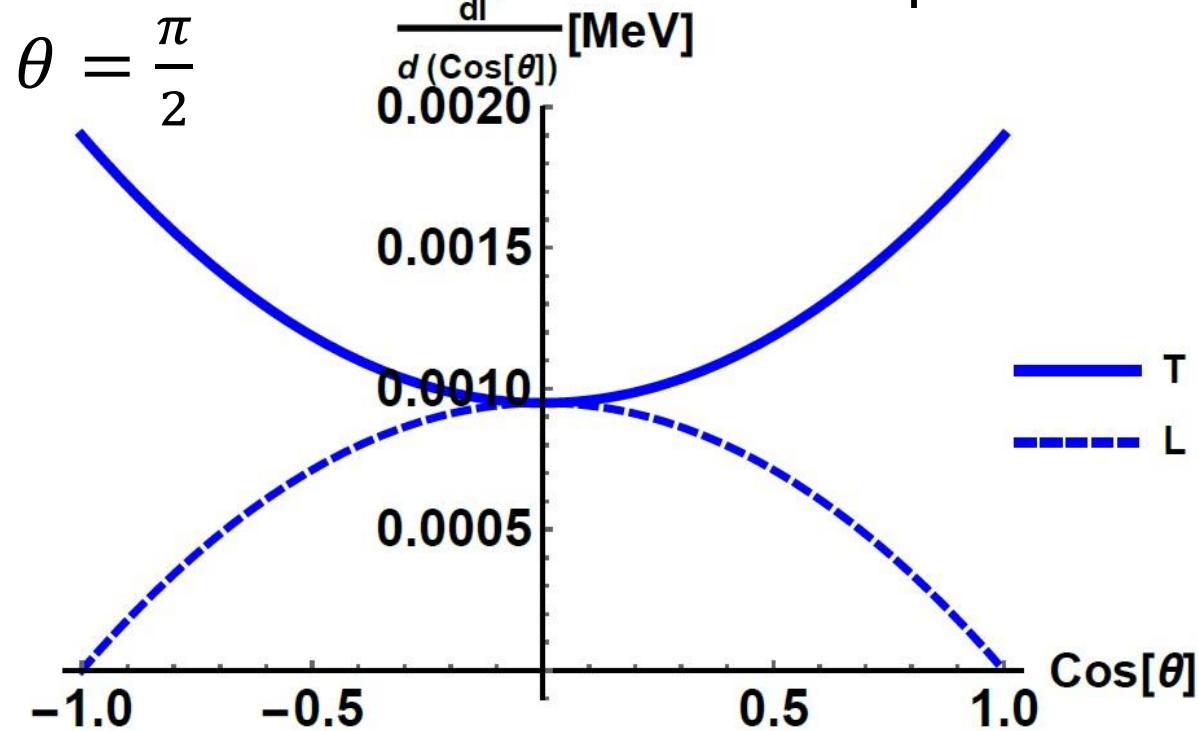
- Hadronic Decay
 - ① Forward & backward direction, $\vec{p}_1 - \vec{p}_2 \perp \vec{\varepsilon}_{\pm 1}$ (Transverse vanishes)
 - ② Transverse direction, $\vec{p}_1 - \vec{p}_2 \perp \vec{\varepsilon}_0$ (Longitudinal vanishes)



What happens at $\theta = 0, \pi$ & $\theta = \frac{\pi}{2}$?

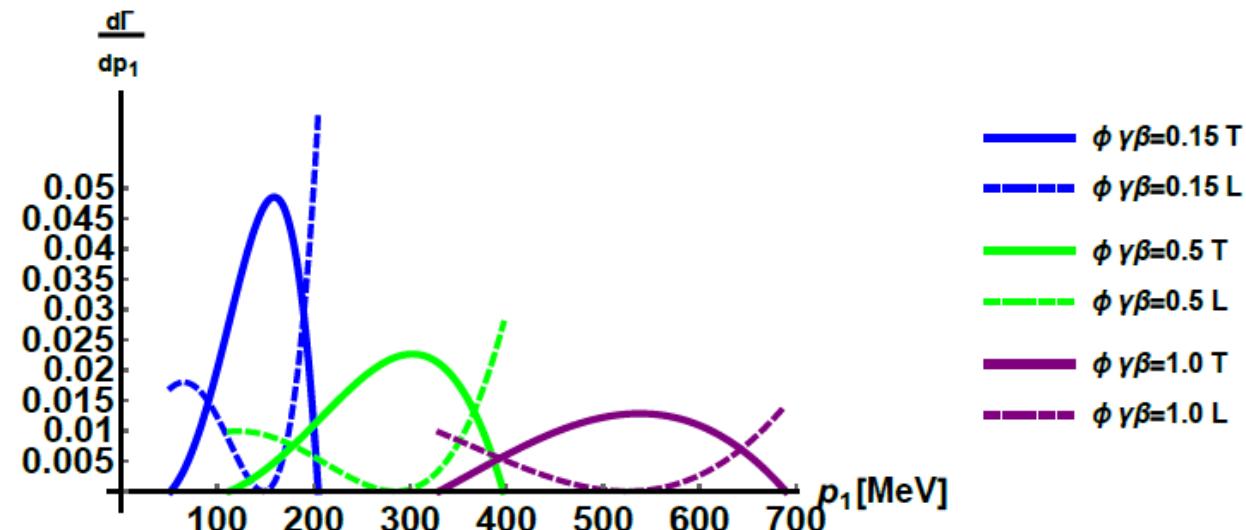
- Electronic Decay

- ① $J^\mu = \bar{u}(p_2)\gamma^\mu v(p_1)$ of opposite spin becomes 0 by helicity conservation (Combination of up & down, down & up spin)
- ② Unlike kaonic decay, vector current carries a transverse component so it has a nonvanishing value at $\theta = \frac{\pi}{2}$

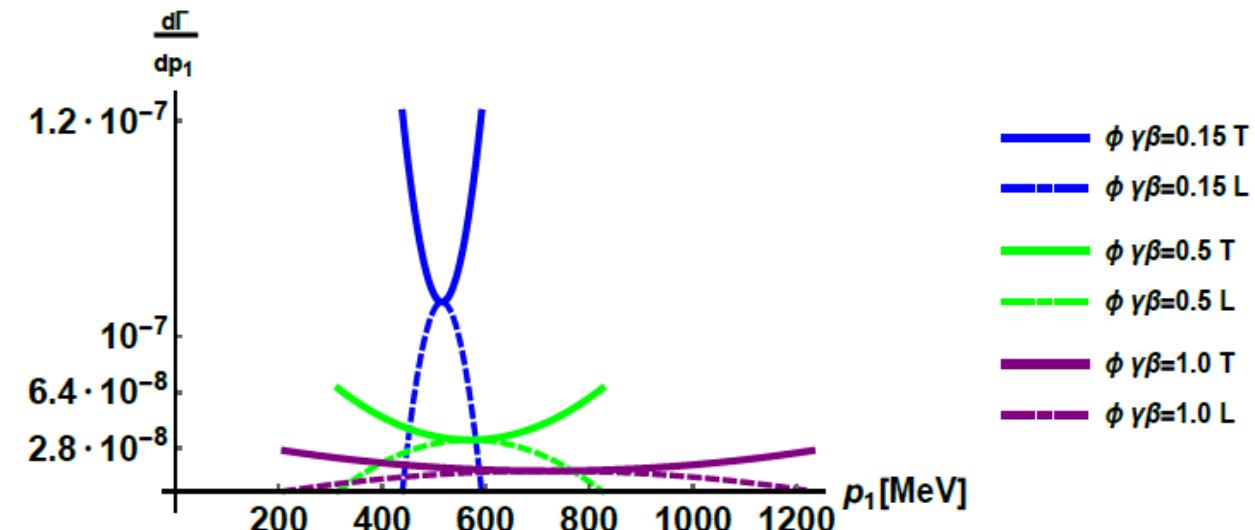


$\frac{d\Gamma}{dp_1}$ in the Lab frame

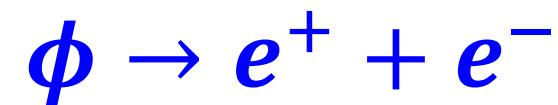
Decay width Γ decreases as $\gamma\beta$ increases due to time dilation



(a) $\frac{d\Gamma}{dp_1}$ of kaonic decay in the Lab frame



(b) $\frac{d\Gamma}{dp_1}$ of leptonic decay in the Lab frame



p_1 : Momentum of $K^+(e^+)$ in the Lab frame

Vector meson state

$$|V\rangle = \sum_{\lambda=\pm 1,0} a_\lambda |\lambda\rangle, \rho_{\lambda\lambda'} = a_\lambda a_{\lambda'}^*$$

$\rho_{\lambda\lambda'}$: Spin density matrix of massive spin 1 particle

Normalized general angular distribution in the ϕ meson rest frame

Hadronic decay

$$\frac{1}{\Gamma} \frac{d\Gamma}{d\Omega} = \frac{3}{8\pi} (\mathbf{1 - \rho_{00}} + (3\rho_{00} - 1) \cos^2 \theta - 2Re[\rho_{1-1}] \sin^2 \theta \cos 2\varphi \\ + 2Im[\rho_{1-1}] \sin^2 \theta \sin 2\varphi - \sqrt{2}Re[\rho_{10} - \rho_{-10}] \sin 2\theta \cos \varphi \\ + \sqrt{2}Im[\rho_{10} + \rho_{-10}] \sin 2\theta \sin \varphi)$$

Z. T. Liang and X. N. Wang, "Spin alignment of vector mesons in non-central A+A collisions," Phys. Lett. B 629, 20-26 (2005)

Leptonic decay

$$\frac{1}{\Gamma} \frac{d\Gamma}{d\Omega} = \frac{3}{16\pi} (\mathbf{1 + \rho_{00}} + (1 - 3\rho_{00}) \cos^2 \theta + 2Re[\rho_{1-1}] \sin^2 \theta \cos 2\varphi \\ - 2Im[\rho_{1-1}] \sin^2 \theta \sin 2\varphi + \sqrt{2}Re[\rho_{10} - \rho_{-10}] \sin 2\theta \cos \varphi \\ - \sqrt{2}Im[\rho_{10} + \rho_{-10}] \sin 2\theta \sin \varphi)$$

P. Faccioli, C. Lourenco, J. Seixas and H. K. Wohri,
"Towards the experimental clarification of quarkonium polarization," Eur. Phys. J. C 69, 657-673 (2010)

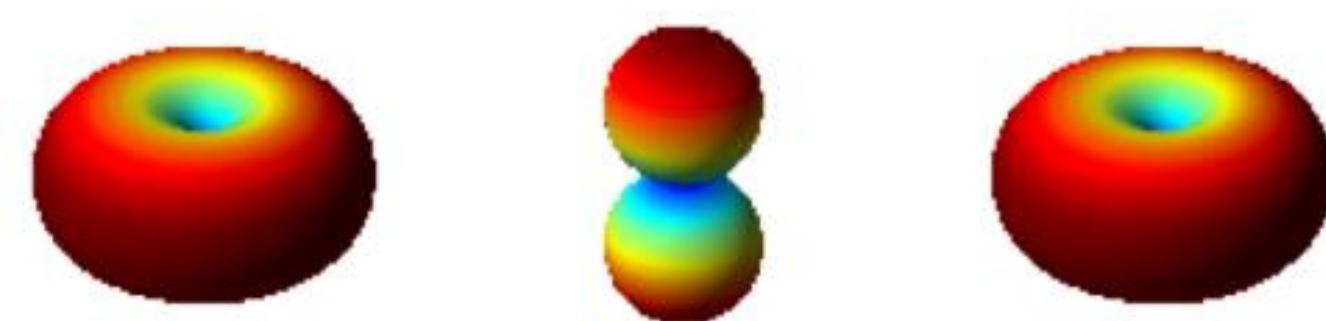
- Integrating over azimuthal angle φ , we obtain distribution of θ

- $W_{\phi \rightarrow K^+ K^-}(\theta) = \frac{3}{4}(1 - \rho_{00} + (3\rho_{00} - 1)\cos^2 \theta)$
- $W_{\phi \rightarrow e^+ e^-}(\theta) = \frac{3}{8}(1 + \rho_{00} + (1 - 3\rho_{00})\cos^2 \theta)$
- Unpolarized $\rightarrow \rho_{00} = \frac{1}{3}$
- Transversely polarized $\rightarrow \rho_{00} = 0$
- Longitudinally polarized $\rightarrow \rho_{00} = 1$

$\phi \rightarrow K^+ + K^-$ using Wigner D matrix

$$\left(\frac{1}{\Gamma} \frac{d\Gamma}{d\Omega} \right)_{K^+ K^-} \propto \sum_{m,m'=\pm 1,0} D_{0m}^{1\dagger} \rho_{mm'} D_{m'0}^1$$

- Orbital angular momentum wavefunction (Spherical Harmonics)
- $Y_1^{\pm 1}(\theta, \varphi) \propto \sin \theta e^{\pm i\varphi}$, $Y_1^0(\theta, \varphi) \propto \cos \theta$
- $K^+ K^-$: Zero spin
- Spin is transferred to relative orbital angular momentum



$\phi \rightarrow e^+ + e^-$ using Wigner D matrix

$$\left(\frac{1}{\Gamma} \frac{d\Gamma}{d\Omega} \right)_{e^+ e^-} \propto \sum_{\lambda=\pm 1} \sum_{m,m'=\pm 1,0} D_{\lambda m}^{1\dagger} \rho_{mm'} D_{m'\lambda}^1$$

- By helicity conservation, positron and electron with same spin contributes to the summation.
- Only $\lambda = \pm 1$ are permitted

Summary & Future possible work

- Polarization of the ϕ meson can be disentangled by polarization tensor $P^{\mu\nu}$.
- Though general angular distribution is anisotropic, we can make it isotropic by averaging over φ .
- Wigner D matrix can also produce the same result by rotation of axes.
- Applying the same method to $\Lambda\&\Delta$ baryon