

Observability of the Higgs boson decay to a photon and a dark photon

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General context I

The dark photon A' is an hypothetical Abelian gauge boson that can mix with the photon and has been the subject of extensive theoretical and experimental studies.

A potential discovery channel that has received considerable attention is the decay

$$h \rightarrow AA',$$

where A' is assumed to be (effectively) massless and invisible.

General context II

An extensive phenomenological literature on the subject

- ▶ Gabrielli '14 [Phys.Rev.D 90 no. 5, (2014) 055032]
- ▶ Biswas '15 [JHEP 06 (2015) 102]
- ▶ Biswas '16 [Phys.Rev.D 93 no. 9, (2016) 093011]
- ▶ Biswas '17 [Phys.Rev.D 96 no. 5, (2017) 055012]
- ▶ ...

which predicted an upper limit $\text{BR}(h \rightarrow AA') < 5\%$.

Motivations:

- ▶ Predicted by certain BSM models (flavour)
- ▶ Potentially observable
- ▶ Interesting experimental channel

General context III

This motivated four experimental searches

- ▶ CMS '19 [JHEP 10 (2019) 139]
Z-associated channel
- ▶ CMS '20 [JHEP 03 (2021) 011]
VBF channel
- ▶ ATLAS '21 [Eur.Phys.J.C 82 no. 2, (2022) 105]
VBF channel
- ▶ ATLAS '22 [2212.09649]
Z-associated channel

The strongest limit obtained is $\text{BR}(h \rightarrow AA') < 1.8\%$ at 95% CL by ATLAS '21.

Overview

Goal:

Investigate experimental and theoretical constraints on $h \rightarrow AA'$

Improvements:

- ▶ Additional constraints
- ▶ More rigorous treatment
- ▶ More recent data

Constraints:

- ▶ Higgs signal strengths
- ▶ Oblique parameters
- ▶ Electric dipole moment (EDM) of the electron
- ▶ Unitarity

General form of the amplitude and what it tells us

Gauge invariance imposes

$$M^{h \rightarrow AA'} = \left[S^{h \rightarrow AA'} (p_1 \cdot p_2 g_{\mu\nu} - p_{1\mu} p_{2\nu}) + i \tilde{S}^{h \rightarrow AA'} \epsilon_{\mu\nu\alpha\beta} p_1^\alpha p_2^\beta \right] \epsilon_{p_1}^\nu \epsilon_{p_2}^\mu.$$

This amplitude cannot be generated at tree-level with a renormalizable Lagrangian.

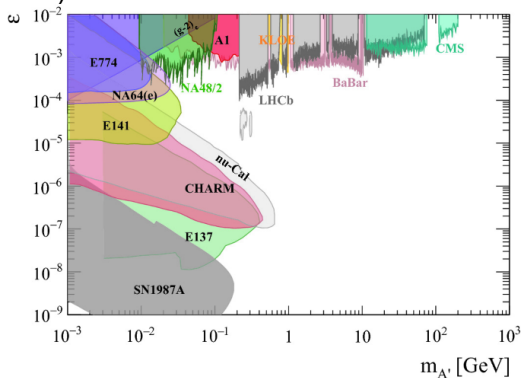
The process must take place at loop-level.

SM particles in the loop?

- ▶ There could be kinetic mixing between A and A'

$$\epsilon F^{\mu\nu} F'_{\mu\nu}$$

- ▶ SM particles in the loop could then contribute to $h \rightarrow AA'$.
- ▶ However, ϵ is constrained to be very small for a light A' .
- ▶ $\text{BR}(h \rightarrow AA')$ would be too small for the LHC.



Fabbrichesi '20

Mediators I

Solution:

New mediators that:

- ▶ Interact with the Higgs
- ▶ Are charged under EM
- ▶ Are charged under a new $U(1)'$

Comments:

- ▶ It's not possible to be completely model independent.
- ▶ We will consider a very large set of mediators and explain why the bounds would be difficult to avoid.
- ▶ The constraints on these mediators are what gives the constraints on $BR(h \rightarrow AA')$.

Mediators II

We will consider models that:

1. Have a renormalizable Lagrangian that preserves all gauge symmetries
2. Lead to the $h \rightarrow AA'$ decay at one loop
3. Contain no mediators charged under QCD
4. Contain only mediators that are complex scalars or vector-like fermions
5. Contain no more than two new fields
6. Contain no mediators that mix with SM fields or have a non-zero expectation value

Mediators III

All models must include an interaction term between the Higgs boson and the mediators.

These terms fall into a finite number of categories:

$$\text{Fermion: } \bar{\psi}_1(A_L P_L + A_R P_R)\psi_2 H + \text{h.c.},$$

$$\text{Scalar: I: } \mu\phi_1^\dagger\phi_2 H + \text{h.c.}, \quad \text{II: } \lambda H^\dagger H\phi^\dagger\phi,$$

$$\text{III: } \lambda H^\dagger H\phi_1^\dagger\phi_2 + \text{h.c.}, \quad \text{IV: } \lambda H H\phi_1^\dagger\phi_2 + \text{h.c.}$$

Each possible form corresponds to a category of models.

Example: Fermion mediators

Consider the Lagrangian

$$\mathcal{L}_m = - \left[\sum_{a,b,c} \hat{d}_{abc}^{pn} \bar{\psi}_1^a (A_L P_L + A_R P_R) \psi_2^b H^c + \text{h.c.} \right] - m_1 \bar{\psi}_1 \psi_1 - m_2 \bar{\psi}_2 \psi_2.$$

where a , b and c are $SU(2)_L$ indices and are summed from 1 to the size of the corresponding multiplet and with

$$\hat{d}_{abc}^{pn} = C_{j_1 m_1 j_2 m_2}^{JM} = \langle j_1 j_2 m_1 m_2 | JM \rangle,$$

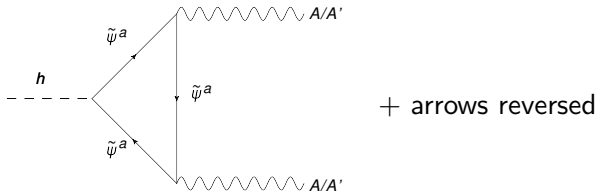
where

$$J = \frac{p-1}{2}, \quad j_1 = \frac{n-1}{2}, \quad j_2 = \frac{1}{2},$$

$$M = \frac{p+1-2a}{2}, \quad m_1 = \frac{n+1-2b}{2}, \quad m_2 = \frac{3-2c}{2}.$$

There is a phase that cannot be reabsorbed.

Higgs decay I



The amplitudes are

$$\begin{aligned}
 M^{h \rightarrow AA} &= \left[S^{h \rightarrow AA} (p_1 \cdot p_2 g_{\mu\nu} - p_{1\mu} p_{2\nu}) + i \tilde{S}^{h \rightarrow AA} \epsilon_{\mu\nu\alpha\beta} p_1^\alpha p_2^\beta \right] \epsilon_{p_1}^\nu \epsilon_{p_2}^\mu, \\
 M^{h \rightarrow AA'} &= \left[S^{h \rightarrow AA'} (p_1 \cdot p_2 g_{\mu\nu} - p_{1\mu} p_{2\nu}) + i \tilde{S}^{h \rightarrow AA'} \epsilon_{\mu\nu\alpha\beta} p_1^\alpha p_2^\beta \right] \epsilon_{p_1}^\nu \epsilon_{p_2}^\mu, \\
 M^{h \rightarrow A'A'} &= \left[S^{h \rightarrow A'A'} (p_1 \cdot p_2 g_{\mu\nu} - p_{1\mu} p_{2\nu}) + i \tilde{S}^{h \rightarrow A'A'} \epsilon_{\mu\nu\alpha\beta} p_1^\alpha p_2^\beta \right] \epsilon_{p_1}^\nu \epsilon_{p_2}^\mu,
 \end{aligned}$$

Higgs decay II

With

$$\begin{aligned}
 S^{h \rightarrow AA} &= e^2 \sum_a \operatorname{Re}(\Omega_{aa}) \tilde{Q}_{aa}^2 S_a + S_{\text{SM}}^{h \rightarrow AA}, & \tilde{S}^{h \rightarrow AA} &= e^2 \sum_a \operatorname{Im}(\Omega_{aa}) \tilde{Q}_{aa}^2 \tilde{S}_a + \tilde{S}_{\text{SM}}^{h \rightarrow AA}, \\
 S^{h \rightarrow AA'} &= ee' \sum_a \operatorname{Re}(\Omega_{aa}) \tilde{Q}_{aa} Q' S_a, & \tilde{S}^{h \rightarrow AA'} &= ee' \sum_a \operatorname{Im}(\Omega_{aa}) \tilde{Q}_{aa} Q' \tilde{S}_a, \\
 S^{h \rightarrow A'A'} &= e'^2 \sum_a \operatorname{Re}(\Omega_{aa}) Q'^2 S_a, & \tilde{S}^{h \rightarrow A'A'} &= e'^2 \sum_a \operatorname{Im}(\Omega_{aa}) Q'^2 \tilde{S}_a,
 \end{aligned}$$

where in the example of the fermion case

$$S_a = -\frac{m_a}{2\pi^2 m_h^2} \left(2 + (4m_a^2 - m_H^2) C_0(0, 0, m_H^2; m_a, m_a, m_a) \right),$$

$$\tilde{S}_a = -i \frac{m_a}{2\pi^2} C_0(0, 0, m_H^2; m_a, m_a, m_a),$$

and

$$\begin{aligned}
 \Gamma^{h \rightarrow AA} &= \frac{|S^{h \rightarrow AA}|^2 + |\tilde{S}^{h \rightarrow AA}|^2}{64\pi} m_h^3, & \Gamma^{h \rightarrow AA'} &= \frac{|S^{h \rightarrow AA'}|^2 + |\tilde{S}^{h \rightarrow AA'}|^2}{32\pi} m_h^3, \\
 \Gamma^{h \rightarrow A'A'} &= \frac{|S^{h \rightarrow A'A'}|^2 + |\tilde{S}^{h \rightarrow A'A'}|^2}{64\pi} m_h^3.
 \end{aligned}$$

Higgs decay III

Comments:

- ▶ The presence of the Levi-Civita symbols comes from γ^5 in the Higgs/fermion vertex.
- ▶ The amplitudes are correlated. The constraints on $h \rightarrow AA$ and $h \rightarrow A'A'$ will constrain $h \rightarrow AA'$.
- ▶ The Higgs signal strengths have two potential blind spots:
 - ▶ Purely imaginary contribution to $S^{h \rightarrow AA}$
 - ▶ LEP forces $S^{h \rightarrow AA}$ to be purely real.
 - ▶ Contribution only to $\tilde{S}^{h \rightarrow AA}$
 - ▶ Will be constrained by the electron EDM

Higgs signal strengths

κ formalism

$$\kappa_i^2 = \frac{\sigma_i}{\sigma_i^{\text{SM}}} \quad \text{or} \quad \kappa_i^2 = \frac{\Gamma_i}{\Gamma_i^{\text{SM}}},$$

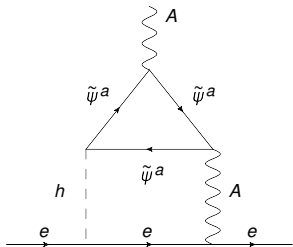
and

$$\kappa_{AA}^2 = \frac{|S^{h \rightarrow AA}|^2 + |\tilde{S}^{h \rightarrow AA}|^2}{|S_{\text{SM}}^{h \rightarrow AA}|^2 + |\tilde{S}_{\text{SM}}^{h \rightarrow AA}|^2}, \quad \kappa_{ZA}^2 = \frac{|S^{h \rightarrow ZA}|^2 + |\tilde{S}^{h \rightarrow ZA}|^2}{|S_{\text{SM}}^{h \rightarrow ZA}|^2 + |\tilde{S}_{\text{SM}}^{h \rightarrow ZA}|^2}.$$

Do χ^2 fit using results from

- ▶ CMS-PAS-HIG-19-005
- ▶ ATLAS-CONF-2021-053

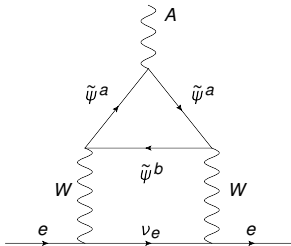
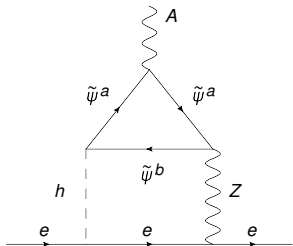
EDM



hA diagrams are dominant near limits

hA contribution $\propto \text{Im}(\Omega_{aa})$

Effectively forces Ω_{aa} to be purely real or tiny



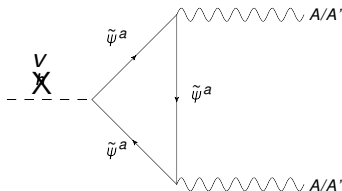
Oblique parameters

The Peskin-Takeuchi parameters are defined as

$$\alpha S = 4s_W^2 c_W^2 \left[\Pi'_{ZZ}(0) - \frac{c_W^2 - s_W^2}{s_W c_W} \Pi'_{ZA}(0) - \Pi'_{AA}(0) \right]$$

$$\alpha T = \frac{\Pi_{WW}(0)}{m_W^2} - \frac{\Pi_{ZZ}(0)}{m_Z^2}.$$

Unsurprising constraint



Unitarity

An amplitude can be expanded as

$$\mathcal{M} = 16\pi \sum_l (2l+1) a_l P_l(\cos\theta), \quad \max \left(\left| \operatorname{Re} \left(a_0^{\text{eig}} \right) \right| \right) < \frac{1}{2}.$$

Different cases:

$$\text{Fermion: } |A_R|^2 + |A_L|^2 < \frac{32\pi}{p}$$

$$\text{Scalar II: } \frac{1}{16\sqrt{2}\pi} \left[\sum_{i,j} \left| \sum_r \lambda^r \hat{d}_{22ij}^{nr} \right|^2 \right]^{\frac{1}{2}} < \frac{1}{2},$$

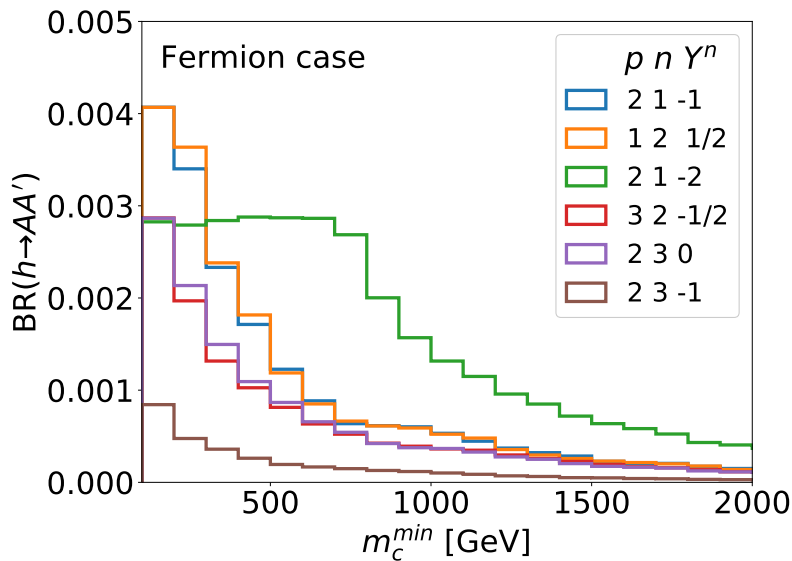
$$\text{Scalar III: } \frac{1}{16\sqrt{2}\pi} \left[\sum_{i,j} \left| \sum_r \lambda^r \hat{d}_{22ij}^{pnr} \right|^2 \right]^{\frac{1}{2}} < \frac{1}{2},$$

$$\text{Scalar IV: } \frac{|\lambda|}{16\sqrt{2}\pi} \left[\sum_{i,j} \left| \hat{d}_{22ij}^{pn} \right|^2 \right]^{\frac{1}{2}} < \frac{1}{2}.$$

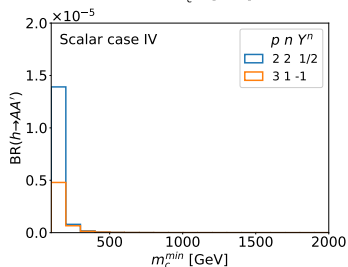
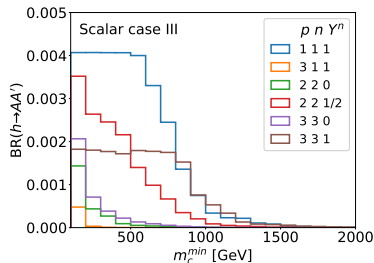
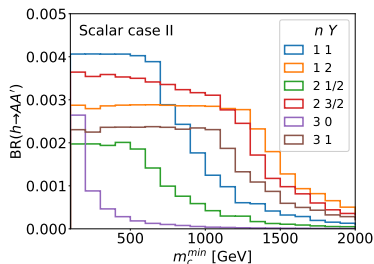
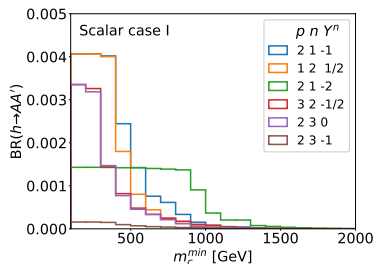
Assembling everything

- ▶ Consider multiple benchmark models for each category
- ▶ Scan entire parameter space with Markov chain using Metropolis-Hasting algorithm
- ▶ Impose $|Q'e'| < \sqrt{4\pi}$ for fermions or $|Q'e'| < \frac{\sqrt{4\pi}}{q^{1/4}}$ for scalars.

Constraints: Fermion mediators



Constraints: Scalar mediators



Caveats

Three caveats:

- ▶ There should be a lower limit on the mass of the charged mediators, but there does not exist sufficiently general searches. The limits would probably be stronger.
- ▶ It could have been possible that $S_{\text{BSM}}^{h \rightarrow AA} \approx -2S_{\text{SM}}^{h \rightarrow AA}$. That would avoid most of the Higgs signal strength constraints, but it does not happen for the fermion cases considered. It can technically happen for some scalar cases, but only for rare cases and extreme fine-tuning.
- ▶ The bounds are model dependent.

Conclusion

Goal:

Investigate experimental and theoretical constraints on $h \rightarrow AA'$

Conclusions:

- ▶ $\text{BR}(h \rightarrow AA') \lesssim 0.4\%$ at best*
- ▶ Difficult to even get this large
- ▶ Far stronger constraints than previous phenomenology papers (5%) and experimental searches (1.8%)
- ▶ Seems like it would be very challenging to find something in this channel at the LHC

Thanks!

Higgs decay IV

- ▶ If the loops are dominated by one particle, $S^{h \rightarrow AA}$ is purely real and $\tilde{S}^{h \rightarrow AA} = 0$, we have

$$\text{BR}(h \rightarrow AA') \approx \sqrt{\text{BR}(h \rightarrow A'A')\text{BR}(h \rightarrow AA)} \left| \frac{\Delta\text{BR}(h \rightarrow AA)}{\text{BR}(h \rightarrow AA)} \right|,$$

where $\text{BR}(h \rightarrow AA) = \text{BR}(h \rightarrow AA)_{\text{SM}} + \Delta\text{BR}(h \rightarrow AA)$.

Considering

$$\begin{aligned} \text{BR}(h \rightarrow AA) &\sim 0.23\%, \quad \left| \frac{\Delta\text{BR}(h \rightarrow AA)}{\text{BR}(h \rightarrow AA)} \right| \lesssim 25\%, \\ \text{BR}(h \rightarrow A'A') &\lesssim 10\%. \end{aligned}$$

we get a rough estimate of $\text{BR}(h \rightarrow AA') \lesssim 0.4\%$.

EDM I

$$\frac{d_e^{Ah}}{e} = - \sum_a \frac{\alpha \tilde{Q}_{aa}^2 m_a m_e}{16\pi^3 m_h^2 v} \text{Im}(\Omega_{aa}) \int_0^1 dx \frac{1}{x(1-x)} j \left(0, \frac{m_a^2}{x(1-x)m_h^2} \right),$$

where

$$j(r, s) = \frac{1}{r-s} \left(\frac{r \ln r}{r-1} - \frac{s \ln s}{s-1} \right).$$

EDM II

$$\frac{d_e^{Zh}}{e} = \sum_{a,b} \frac{\tilde{Q}_{bb}}{32\pi^4 m_h^2} g_{ee}^V g_{ee}^S \left(m_a C_{ab}^1 f_1(m_a, m_b) + m_b C_{ab}^2 f_2(m_a, m_b) \right),$$

where

$$C_{ab}^1 = \text{Re} \left(i g_{ba}^S g_{ab}^{A*} - g_{ba}^P g_{ab}^{V*} \right), \quad C_{ab}^2 = -\text{Re} \left(i g_{ba}^S g_{ab}^{A*} + g_{ba}^P g_{ab}^{V*} \right),$$

with

$$\begin{aligned} g_{ee}^S &= -\frac{m_e}{v}, & g_{ee}^V &= -\frac{\sqrt{g^2 + g'^2}}{2} \left(-\frac{1}{2} + 2s_W^2 \right), \\ g_{ab}^S &= -\frac{(\Omega_{ba} + \Omega_{ab}^*)}{2}, & g_{ab}^P &= -i \frac{(\Omega_{ba} - \Omega_{ab}^*)}{2}, \\ g_{ab}^V &= -\frac{\sqrt{g^2 + g'^2}}{2} (B_{Rba} + B_{Lba}), & g_{ab}^A &= -\frac{\sqrt{g^2 + g'^2}}{2} (B_{Rba} - B_{Lba}), \end{aligned}$$

and

$$f_1(m_a, m_b) = \int_0^1 dx j \left(\frac{m_Z^2}{m_h^2}, \frac{\tilde{\Delta}_{ab}}{m_h^2} \right), \quad f_2(m_a, m_b) = \int_0^1 dx j \left(\frac{m_Z^2}{m_h^2}, \frac{\tilde{\Delta}_{ab}}{m_h^2} \right) \frac{(1-x)}{x},$$

EDM III

$$\frac{d_e^{WW}}{e} = -\frac{\alpha^2 m_e}{8\pi^2 s_W^4 m_W^2} \sum_{a,b} \frac{m_a m_b}{m_W^2} \text{Im} \left(\hat{A}_{Lba} \hat{A}_{Rba}^* \right) \left[\tilde{Q}_{bb} \mathcal{G}(r_a, r_b, 0) + \tilde{Q}_{aa} \mathcal{G}(r_b, r_a, 0) \right],$$

where $r_a = m_a^2/m_W^2$, $r_b = m_b^2/m_W^2$ and

$$\mathcal{G}(r_a, r_b, r_c) = \int_0^1 \frac{d\gamma}{\gamma} \int_0^1 dy y \left[\frac{(R - 3K_{ab})R + 2(K_{ab} + R)y}{4R(K_{ab} - R)^2} + \frac{K_{ab}(K_{ab} - 2y)}{2(K_{ab} - R)^3} \ln \frac{K_{ab}}{R} \right],$$

where

$$R = y + (1 - y)r_c \quad K_{ab} = \frac{r_a}{1 - \gamma} + \frac{r_b}{\gamma}.$$

Oblique parameters fermions

$$\begin{aligned}
 S &= \frac{1}{2\pi} \sum_{a,b} \left\{ \left(|\hat{A}_{Lab}|^2 + |\hat{A}_{Rab}|^2 \right) \psi_+(y_a, y_b) + 2\text{Re} \left(\hat{A}_{Lab} \hat{A}_{Rab}^* \right) \psi_-(y_a, y_b) \right. \\
 &\quad \left. - \frac{1}{2} \left[\left(|X_{ab}|^2 + |X_{Rab}|^2 \right) \chi_+(y_a, y_b) + 2\text{Re} \left(X_{Lab} X_{Rab}^* \right) \chi_-(y_a, y_b) \right] \right\}, \\
 T &= \frac{1}{16\pi s_W^2 c_W^2} \sum_{a,b} \left\{ \left(|\hat{A}_{Lab}|^2 + |\hat{A}_{Rab}|^2 \right) \theta_+(y_a, y_b) + 2\text{Re} \left(\hat{A}_{Lab} \hat{A}_{Rab}^* \right) \theta_-(y_a, y_b) \right. \\
 &\quad \left. - \frac{1}{2} \left[\left(|X_{Lab}|^2 + |X_{Rab}|^2 \right) \theta_+(y_a, y_b) + 2\text{Re} \left(X_{Lab} X_{Rab}^* \right) \theta_-(y_a, y_b) \right] \right\},
 \end{aligned}$$

with $y_a = m_a^2/m_Z^2$, $X_{L/R} = -2B_{L/R} + 2\tilde{Q}s_W^2$ and

$$\begin{aligned}
 \psi_+(y_1, y_2) &= \frac{1}{3} - \frac{1}{9} \ln \frac{y_1}{y_2}, \\
 \psi_-(y_1, y_2) &= -\frac{y_1 + y_2}{6\sqrt{y_1 y_2}}, \\
 \chi_+(y_1, y_2) &= \frac{5(y_1^2 + y_2^2) - 22y_1 y_2}{9(y_1 - y_2)^2} + \frac{3y_1 y_2 (y_1 + y_2) - y_1^3 - y_2^3}{3(y_1 - y_2)^3} \ln \frac{y_1}{y_2}, \\
 \chi_-(y_1, y_2) &= -\sqrt{y_1 y_2} \left[\frac{y_1 + y_2}{6y_1 y_2} - \frac{y_1 + y_2}{(y_1 - y_2)^2} + \frac{2y_1 y_2}{(y_1 - y_2)^3} \ln \frac{y_1}{y_2} \right], \\
 \theta_+(y_1, y_2) &= y_1 + y_2 - \frac{2y_1 y_2}{y_1 - y_2} \ln \frac{y_1}{y_2}, \\
 \theta_-(y_1, y_2) &= 2\sqrt{y_1 y_2} \left[\frac{y_1 + y_2}{y_1 - y_2} \ln \frac{y_1}{y_2} - 2 \right].
 \end{aligned}$$

Oblique parameters scalars

$$S = \frac{1}{2\pi} \sum_{a,b} \left[|B_{ab}|^2 - (c_W^2 - s_W^2) B_{ab} \tilde{Q}_{ab} - c_W^2 s_W^2 \tilde{Q}_{ab}^2 \right] F_1(y_a, y_b),$$

$$T = \frac{1}{16\pi c_W^2 s_W^2} \left[\sum_{a,b} |\hat{A}_{ab}|^2 F_2(y_a, y_b) - \sum_a \left[\hat{A} \hat{A}^\dagger + \hat{A}^\dagger \hat{A} \right]_{aa} F_3(y_a) \right. \\ \left. - 2 \sum_{a,b} |B_{ab}|^2 F_2(y_a, y_b) + 4 \sum_a \left[B^2 \right]_{aa} F_3(y_a) \right],$$

where $y_a = m_a^2/m_Z^2$ and

$$F_1(y_1, y_2) = -\frac{5y_1^2 - 22y_1y_2 + 5y_2^2}{9(y_1 - y_2)^2} + \frac{2(y_1^2(y_1 - 3y_2) \ln y_1 - y_2^2(y_2 - 3y_1) \ln y_2)}{3(y_1 - y_2)^3},$$

$$F_2(y_1, y_2) = 3(y_1 + y_2) - \frac{2(y_1^2 \ln y_1 - y_2^2 \ln y_2)}{y_1 - y_2},$$

$$F_3(y_1) = 2y_1 - 2y_1 \ln y_1.$$

Example: Fermion mediators II

Once the Higgs is replaced by its expectation value

$$\mathcal{L}_m \supset - \sum_{a,b} \frac{A_{LV}}{\sqrt{2}} \hat{d}_{ab2}^{pn} \bar{\psi}_1^a P_L \psi_2^b - \sum_{a,b} \frac{A_{RV}^*}{\sqrt{2}} \hat{d}_{ba2}^{pn} \bar{\psi}_2^a P_L \psi_1^b - m_1 \bar{\psi}_1 P_L \psi_1 - m_2 \bar{\psi}_2 P_L \psi_2 + \text{h.c.}$$

Introduce the convenient notation

$$\hat{\psi} = \begin{pmatrix} \psi_1 \\ \psi_2 \end{pmatrix}$$

and

$$d_{ab}^{pn} = \begin{cases} \hat{d}_{a(b-p)2}^{pn}, & \text{if } a \in [1, p] \text{ and } b \in [p+1, n+p], \\ 0, & \text{otherwise.} \end{cases}$$

Fermion mediators: Higgs interactions and mass IV

The mass Lagrangian can be written as

$$\mathcal{L}_m \supset - \sum_{a,b} M_{ab} \tilde{\psi}^a P_L \hat{\psi}^b + \text{h.c.},$$

where the mass matrix is

$$M = m_1 \begin{pmatrix} \mathbb{I}_{p \times p} & 0_{p \times n} \\ 0_{n \times p} & 0_{n \times n} \end{pmatrix} + m_2 \begin{pmatrix} 0_{p \times p} & 0_{p \times n} \\ 0_{n \times p} & \mathbb{I}_{n \times n} \end{pmatrix} + \frac{A_L v}{\sqrt{2}} d^{pn} + \frac{A_R^* v}{\sqrt{2}} d^{pnT}.$$

The mass matrix can then be diagonalized by introducing $\tilde{\psi}^a$

$$P_L \hat{\psi} = R_L P_L \tilde{\psi}, \quad P_R \hat{\psi} = R_R P_R \tilde{\psi},$$

where R_L and R_R are unitary matrices that diagonalize $M^\dagger M$ and MM^\dagger respectively.

Fermion mediators: Higgs interactions and mass V

The interactions of the Higgs with the mass eigenstates are

$$\mathcal{L}_m \supset - \sum_{a,b} \Omega_{ab} h \bar{\psi}^a P_L \psi^b + \text{h.c.},$$

where Ω is

$$\Omega = \frac{A_L}{\sqrt{2}} R_R^\dagger d^{pn} R_L + \frac{A_R^*}{\sqrt{2}} R_R^\dagger d^{pnT} R_L.$$

Fermion mediators: Gauge interactions I

The interactions of the A/A' with $\tilde{\psi}^a$ are

$$\mathcal{L}_g \supset -eA_\mu \tilde{\psi} \gamma^\mu \tilde{Q} \tilde{\psi} - Q' e' A'_\mu \tilde{\psi} \gamma^\mu \tilde{\psi},$$

where e' is the $U(1)'$ gauge coupling and

$$\tilde{Q} = R_L^\dagger \hat{Q} R_L = R_R^\dagger \hat{Q} R_R,$$

where

$$\hat{Q} = \begin{pmatrix} Y^p + T_3^p & 0_{p \times n} \\ 0_{n \times p} & Y^n + T_3^n \end{pmatrix},$$

where $(T_3^p)_{ab} = (p+1-2a)\delta_{ab}/2$ and similarly for T_3^n .

Fermion mediators: Gauge interactions II

The interactions between the Z boson and $\tilde{\psi}^a$ are

$$\mathcal{L}_g \supset -\sqrt{g^2 + g'^2} Z_\mu \bar{\tilde{\psi}} \gamma^\mu (B_L P_L + B_R P_R) \tilde{\psi},$$

where B_L and B_R are

$$B_L = R_L^\dagger \begin{pmatrix} -s_W^2 Y^P + c_W^2 T_3^P & 0_{p \times n} \\ 0_{n \times p} & -s_W^2 Y^n + c_W^2 T_3^n \end{pmatrix} R_L,$$

$$B_R = R_R^\dagger \begin{pmatrix} -s_W^2 Y^P + c_W^2 T_3^P & 0_{p \times n} \\ 0_{n \times p} & -s_W^2 Y^n + c_W^2 T_3^n \end{pmatrix} R_R.$$

Fermion mediators: Gauge interactions III

The interactions between the W boson and $\tilde{\psi}^a$ are

$$\mathcal{L}_g \supset -\frac{g}{\sqrt{2}} \bar{\tilde{\psi}} \gamma^\mu \left(\hat{A}_L P_L W_\mu^+ + \hat{A}_R P_R W_\mu^+ \right) \tilde{\psi} + \text{h.c.},$$

where

$$\hat{A}_L = R_L^\dagger \begin{pmatrix} T_+^p & 0_{p \times n} \\ 0_{n \times p} & T_+^n \end{pmatrix} R_L, \quad \hat{A}_R = R_R^\dagger \begin{pmatrix} T_+^p & 0_{p \times n} \\ 0_{n \times p} & T_+^n \end{pmatrix} R_R,$$

with $(T_+^p)_{ab} = \sqrt{a(p-a)} \delta_{a,b-1}$ and similarly for T_+^n .

Fermion mediators: Unitarity I

The top loop has a mass of ~ 173 GeV, $y_t \sim 1$ and $N_c = 3$, yet gives a tiny contribution to $h \rightarrow AA$.

Mediators must have either large Yukawa couplings or dark electric charge.

An amplitude can be expanded as

$$\mathcal{M} = 16\pi \sum_l (2l + 1) a_l P_l(\cos \theta).$$

Consider the basis of $\bar{\psi}_1^a \psi_2^b$ pairs given by

$$\bar{\psi}_1^1 \psi_2^1, \bar{\psi}_1^1 \psi_2^2, \dots, \bar{\psi}_1^1 \psi_2^n, \bar{\psi}_1^2 \psi_2^1, \bar{\psi}_1^2 \psi_2^2, \dots, \bar{\psi}_1^2 \psi_2^n, \dots, \bar{\psi}_1^P \psi_2^1, \bar{\psi}_1^P \psi_2^2, \dots, \bar{\psi}_1^P \psi_2^n.$$

Fermion mediators: Unitarity II

Then, the matrix of a_0 for the scattering $\bar{\psi}_1^a \psi_2^b \rightarrow \bar{\psi}_1^c \psi_2^d$ is

$$a_0^{\text{mat}} = \begin{pmatrix} F_{11}^{11} & F_{11}^{12} & \dots & F_{11}^{1n} & F_{11}^{21} & F_{11}^{22} & \dots & F_{11}^{2n} & \dots & F_{11}^{p1} & F_{11}^{p2} & \dots & F_{11}^{pn} \\ F_{12}^{11} & F_{12}^{12} & \dots & F_{12}^{1n} & F_{12}^{21} & F_{12}^{22} & \dots & F_{12}^{2n} & \dots & F_{12}^{p1} & F_{12}^{p2} & \dots & F_{12}^{pn} \\ \dots & \dots & \dots & \dots & \dots & \dots & \dots & \dots & \dots & \dots & \dots & \dots & \dots \\ F_{1n}^{11} & F_{1n}^{12} & \dots & F_{1n}^{1n} & F_{1n}^{21} & F_{1n}^{22} & \dots & F_{1n}^{2n} & \dots & F_{1n}^{p1} & F_{1n}^{p2} & \dots & F_{1n}^{pn} \\ F_{21}^{11} & F_{21}^{12} & \dots & F_{21}^{1n} & F_{21}^{21} & F_{21}^{22} & \dots & F_{21}^{2n} & \dots & F_{21}^{p1} & F_{21}^{p2} & \dots & F_{21}^{pn} \\ F_{22}^{11} & F_{22}^{12} & \dots & F_{22}^{1n} & F_{22}^{21} & F_{22}^{22} & \dots & F_{22}^{2n} & \dots & F_{22}^{p1} & F_{22}^{p2} & \dots & F_{22}^{pn} \\ \dots & \dots & \dots & \dots & \dots & \dots & \dots & \dots & \dots & \dots & \dots & \dots & \dots \\ F_{2n}^{11} & F_{2n}^{12} & \dots & F_{2n}^{1n} & F_{2n}^{21} & F_{2n}^{22} & \dots & F_{2n}^{2n} & \dots & F_{2n}^{p1} & F_{2n}^{p2} & \dots & F_{2n}^{pn} \\ \dots & \dots & \dots & \dots & \dots & \dots & \dots & \dots & \dots & \dots & \dots & \dots & \dots \\ F_{p1}^{11} & F_{p1}^{12} & \dots & F_{p1}^{1n} & F_{p1}^{21} & F_{p1}^{22} & \dots & F_{p1}^{2n} & \dots & F_{p1}^{p1} & F_{p1}^{p2} & \dots & F_{p1}^{pn} \\ F_{p2}^{11} & F_{p2}^{12} & \dots & F_{p2}^{1n} & F_{p2}^{21} & F_{p2}^{22} & \dots & F_{p2}^{2n} & \dots & F_{p2}^{p1} & F_{p2}^{p2} & \dots & F_{p2}^{pn} \\ \dots & \dots & \dots & \dots & \dots & \dots & \dots & \dots & \dots & \dots & \dots & \dots & \dots \\ F_{pn}^{11} & F_{pn}^{12} & \dots & F_{pn}^{1n} & F_{pn}^{21} & F_{pn}^{22} & \dots & F_{pn}^{2n} & \dots & F_{pn}^{p1} & F_{pn}^{p2} & \dots & F_{pn}^{pn} \end{pmatrix}$$

Fermion mediators: Unitarity III

Where F_{ab}^{cd} is

$$F_{ab}^{cd} = \frac{d_{ab2}^{pn} d_{cd2}^{pn}}{32\pi} \begin{pmatrix} -|A_R|^2 & A_R A_L^* \\ A_L A_R^* & -|A_L|^2 \end{pmatrix}$$

and corresponds to a_0 for different combinations of helicity in the basis $(\uparrow\uparrow, \downarrow\downarrow)$. Call a_0^{eig} the set of eigenvalues of a_0^{mat} . Unitarity requires

$$\max \left(\left| \text{Re} \left(a_0^{\text{eig}} \right) \right| \right) < \frac{1}{2}.$$

This simplifies to

$$|A_R|^2 + |A_L|^2 < \frac{32\pi}{p}.$$

Scalar mediators: Scalar case I A

Consider:

- ▶ A complex scalar ϕ_1 with the properties:
 - ▶ Representation of $SU(2)_L$ of dimension $p = n \pm 1$
 - ▶ Weak hypercharge of $Y^p = Y^n + 1/2$
 - ▶ Charge of Q' under $U(1)'$
- ▶ A complex scalar ϕ_2 with the properties:
 - ▶ Representation of $SU(2)_L$ of dimension n
 - ▶ Weak hypercharge of Y^n
 - ▶ Charge of Q' under $U(1)'$

Scalar mediators: Scalar case I B

This allows the Lagrangian

$$\mathcal{L}_m^1 = - \left[\sum_{a,b,c} \mu \hat{d}_{abc}^{pn} \phi_1^{a\dagger} \phi_2^b H^c + \text{h.c.} \right] - m_1^2 |\phi_1|^2 - m_2^2 |\phi_2|^2,$$

where

$$\hat{d}_{abc}^{pn} = C_{j_1 m_1 j_2 m_2}^{JM},$$

with

$$J = \frac{p-1}{2}, \quad j_1 = \frac{n-1}{2}, \quad j_2 = \frac{1}{2},$$

$$M = \frac{p+1-2a}{2}, \quad m_1 = \frac{n+1-2b}{2}, \quad m_2 = \frac{3-2c}{2}.$$

μ can be made real.

Scalar mediators: Scalar case II A

Consider:

- ▶ A complex scalar ϕ with the properties:
 - ▶ Representation of $SU(2)_L$ of dimension n
 - ▶ Weak hypercharge of Y^n
 - ▶ Charge of Q' under $U(1)'$

Scalar mediators: Scalar case II B

This allows the Lagrangian

$$\mathcal{L}_m^2 = - \sum_{r \in \{n-1, n+1\}} \sum_{a, b, c, d} \lambda^r \hat{d}_{abcd}^{nr} H^{a\dagger} H^b \phi^{c\dagger} \phi^d - m^2 |\phi|^2.$$

The $SU(2)_L$ tensor \hat{d}_{abcd}^{nr} is given by

$$\hat{d}_{abcd}^{nr} = \sum_M C_{j_1 m_1 j_2 m_2}^{JM} C_{j_3 m_3 j_4 m_4}^{JM},$$

where M is summed over $\{-J, -J+1, -J+2, \dots, +J\}$ and

$$j_1 = \frac{1}{2}, \quad j_2 = \frac{n-1}{2}, \quad j_3 = \frac{1}{2}, \quad j_4 = \frac{n-1}{2}, \quad J = \frac{r-1}{2},$$

$$m_1 = \frac{3-2a}{2}, \quad m_2 = \frac{n+1-2c}{2}, \quad m_3 = \frac{3-2b}{2}, \quad m_4 = \frac{n+1-2d}{2}.$$

Two possible coefficients if $n \neq 1$.

Scalar mediators: Scalar case III A

Consider:

- ▶ A complex scalar ϕ_1 with the properties:
 - ▶ Representation of $SU(2)_L$ of dimension $p \in \{n-2, n, n+2\}$
 - ▶ Weak hypercharge of $Y^p = Y^n$
 - ▶ Charge of Q' under $U(1)'$
- ▶ A complex scalar ϕ_2 with the properties:
 - ▶ Representation of $SU(2)_L$ of dimension n
 - ▶ Weak hypercharge of Y^n
 - ▶ Charge of Q' under $U(1)'$

Scalar mediators: Scalar case III B

This allows the Lagrangian:

$$\mathcal{L}_m^3 = - \left[\sum_{r \in \mathcal{R}} \sum_{a,b,c,d} \lambda^r \hat{d}_{abcd}^{pnr} H^{a\dagger} H^b \phi_1^{c\dagger} \phi_2^d + \text{h.c.} \right] - m_1^2 |\phi_1|^2 - m_2^2 |\phi_2|^2,$$

where $\mathcal{R} = \{n-1, n+1\} \cap \{p-1, p+1\}$ and \hat{d}_{abcd}^{pnr}

$$\hat{d}_{abcd}^{pnr} = \sum_M C_{j_1 m_1 j_2 m_2}^{JM} C_{j_3 m_3 j_4 m_4}^{JM},$$

where M is summed over $\{-J, -J+1, -J+2, \dots, +J\}$ and

$$j_1 = \frac{1}{2}, \quad j_2 = \frac{p-1}{2}, \quad j_3 = \frac{1}{2}, \quad j_4 = \frac{n-1}{2}, \quad J = \frac{r-1}{2},$$

$$m_1 = \frac{3-2a}{2}, \quad m_2 = \frac{p+1-2c}{2}, \quad m_3 = \frac{3-2b}{2}, \quad m_4 = \frac{n+1-2d}{2}.$$

If $p = n \neq 1$, there are two coefficients and 1 otherwise.

Scalar mediators: Scalar case IV A

Consider:

- ▶ A complex scalar ϕ_1 with the properties:
 - ▶ Representation of $SU(2)_L$ of dimension $p \in \{n-2, n, n+2\}$
 - ▶ Weak hypercharge of $Y^p = Y^n + 1$
 - ▶ Charge of Q' under $U(1)'$
- ▶ A complex scalar ϕ_2 with the properties:
 - ▶ Representation of $SU(2)_L$ of dimension n
 - ▶ Weak hypercharge of Y^n
 - ▶ Charge of Q' under $U(1)'$
- ▶ p and n are not both 1.

Scalar mediators: Scalar case IV B

Consider:

$$\mathcal{L}_m^4 = - \left[\lambda \hat{d}_{abcd}^{pn} H^a H^b \phi_1^{c\dagger} \phi_2^d + \text{h.c.} \right] - m_1^2 |\phi_1|^2 - m_2^2 |\phi_2|^2,$$

where

$$\hat{d}_{abcd}^{pn} = \sum_{M_1} C_{j_1 m_1 j_2 m_2}^{J_1 M_1} C_{J_1 M_1 j_3 m_3}^{J_2 M_2},$$

where M_1 is summed over $\{-1, 0, 1\}$ and

$$j_1 = \frac{1}{2}, \quad j_2 = \frac{1}{2}, \quad j_3 = \frac{n-1}{2}, \quad J_1 = 1, \quad J_2 = \frac{p-1}{2},$$

$$m_1 = \frac{3-2a}{2}, \quad m_2 = \frac{3-2b}{2}, \quad m_3 = \frac{n+1-2d}{2}, \quad M_2 = \frac{p+1-2c}{2}.$$

λ can be made real.

Scalar mediators: Constraints I

- ▶ Treatment of gauge and Higgs interactions is similar to the fermion case.
- ▶ Higgs signal strengths is similar to the fermion case.
- ▶ We computed the oblique parameters ourselves.
- ▶ EDM constraints are not needed (no γ^5).

Scalar mediators: Constraints III

For case IV, this can be simplified to:

$$|\lambda| < 8\pi \sqrt{\frac{6}{p}}.$$

Also,

$$|Q'e'| < \frac{\sqrt{4\pi}}{q^{1/4}},$$

where $q = n + p$ for cases I, III, IV and $q = n$ for case II.