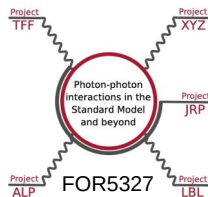


# Experimental input from for the HLbL contribution

7<sup>th</sup> Plenary Workshop of the Muon  $g-2$  Theory Initiative

2024-09-13 | Christoph Florian Redmer



JOHANNES GUTENBERG  
UNIVERSITÄT MAINZ



# “Wish List” from 2020 WP

**Table 14**

Priorities for new experimental input and cross-checks.

issue	experimental input [I] or cross-checks [C]
axials, tensors, higher pseudoscalars missing states	$\gamma^{(*)}\gamma^* \rightarrow 3\pi, 4\pi, K\bar{K}\pi, \eta\pi\pi, \eta'\pi\pi$ [I] inclusive $\gamma^{(*)}\gamma^* \rightarrow$ hadrons at 1–3 GeV [I]
dispersive analysis of $\eta^{(\prime)}$ TFFs	$e^+e^- \rightarrow \eta\pi^+\pi^-$ [I] $\eta' \rightarrow \pi^+\pi^-\pi^+\pi^-$ [I] $\eta' \rightarrow \pi^+\pi^-e^+e^-$ [I] $\gamma\pi^- \rightarrow \pi^-\eta$ [C]
dispersive analysis of $\pi^0$ TFF	$\gamma\pi \rightarrow \pi\pi$ [I] high accuracy Dalitz plot $\omega \rightarrow \pi^+\pi^-\pi^0$ [C] $e^+e^- \rightarrow \pi^+\pi^-\pi^0$ [C] $\omega, \phi \rightarrow \pi^0l^+l^-$ [C]
pseudoscalar TFF pion, kaon, $\pi\eta$ loops (including scalars and tensors)	$\gamma^{(*)}\gamma^* \rightarrow \pi^0, \eta, \eta'$ at arbitrary virtualities [I,C] $\gamma^{(*)}\gamma^* \rightarrow \pi\pi, K\bar{K}, \pi\eta$ at arbitrary virtualities, partial waves [I,C]

Phys.Rept. 887 (2020) 1 – 166

# “Wish List” from 2020 WP

**Table 14**

Priorities for new experimental input and cross-checks.

issue	experimental input [I] or cross-checks [C]
axials, tensors, higher pseudoscalars	$\gamma^{(*)}\gamma^* \rightarrow 3\pi, 4\pi, K\bar{K}\pi, \eta\pi\pi, \eta'\pi\pi$ [I]
missing states	inclusive $\gamma^{(*)}\gamma^* \rightarrow$ hadrons at 1–3 GeV [I]
dispersive analysis of $\eta^{(\prime)}$ TFFs	$e^+e^- \rightarrow \eta\pi^+\pi^-$ [I]
	$\eta' \rightarrow \pi^+\pi^-\pi^+\pi^-$ [I]
	$\eta' \rightarrow \pi^+\pi^-e^+e^-$ [I]
	$\gamma\pi^- \rightarrow \pi^-\eta$ [C]
dispersive analysis of $\pi^0$ TFF	$\gamma\pi \rightarrow \pi\pi$ [I]
	high accuracy Dalitz plot $\omega \rightarrow \pi^+\pi^-\pi^0$ [C]
	$e^+e^- \rightarrow \pi^+\pi^-\pi^0$ [C]
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pseudoscalar TFF	$\gamma^{(*)}\gamma^* \rightarrow \pi^0, \eta, \eta'$ at arbitrary virtualities [I,C]
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Hadronic cross sections

Meson decays

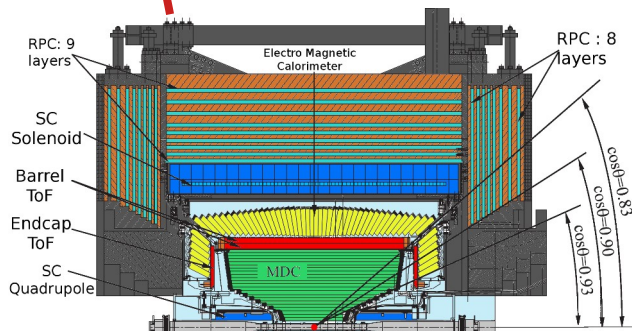
Two-photon reactions

Phys.Rept. 887 (2020) 1 – 166

# BESIII at BEPCII



- Center-of-mass energies from 2 – 5 GeV
- Design luminosity exceeded:  $1.1 \times 10^{33} \text{ cm}^{-2} \text{ s}^{-1}$  at 3.77 GeV



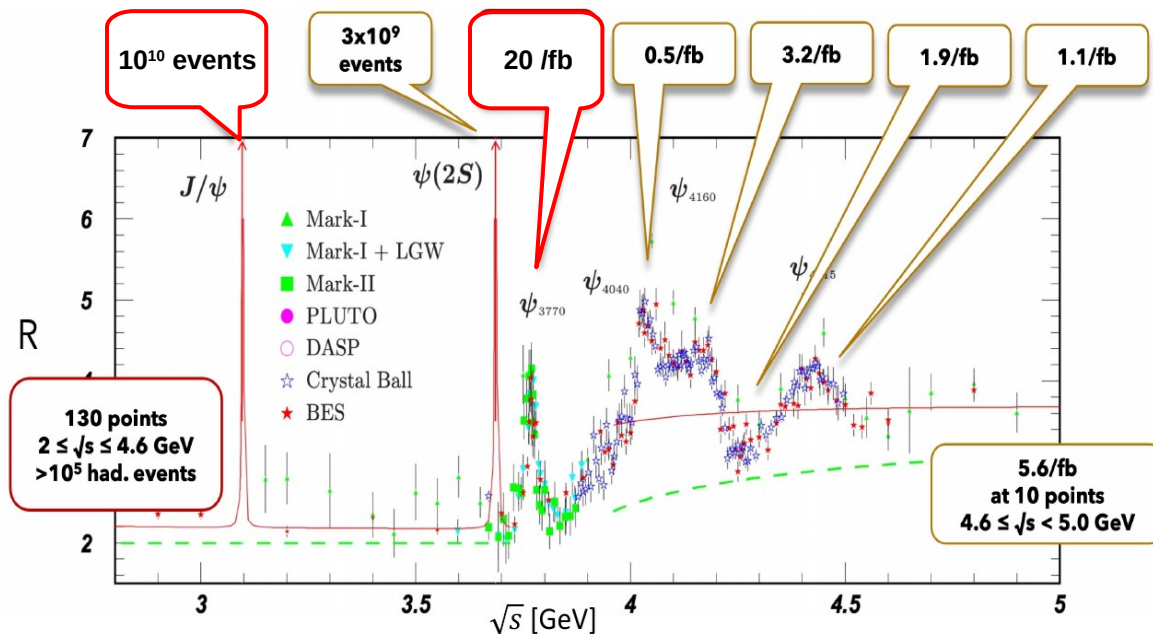
Time of Flight

EM Calorimeter

Muon Counter

Drift Chamber

Solenoid

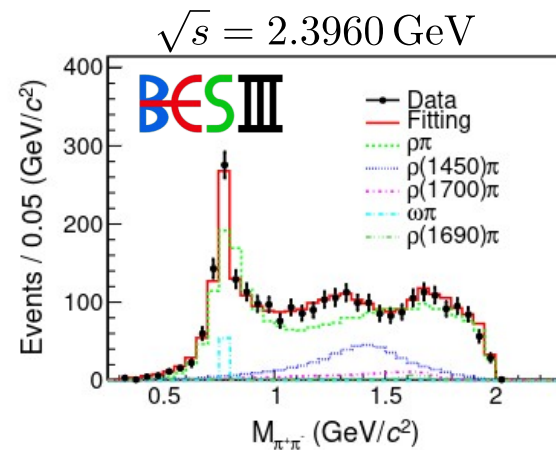
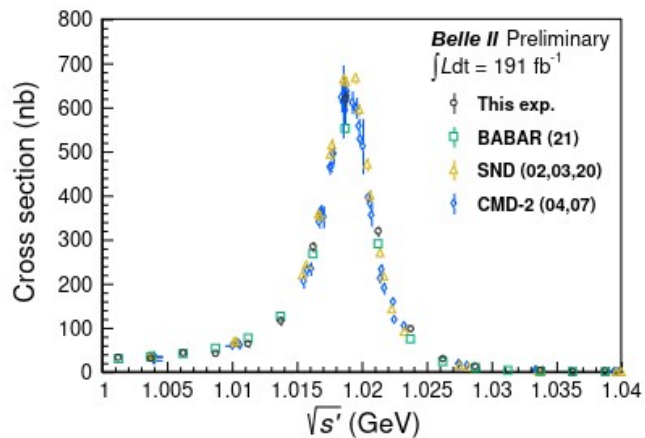
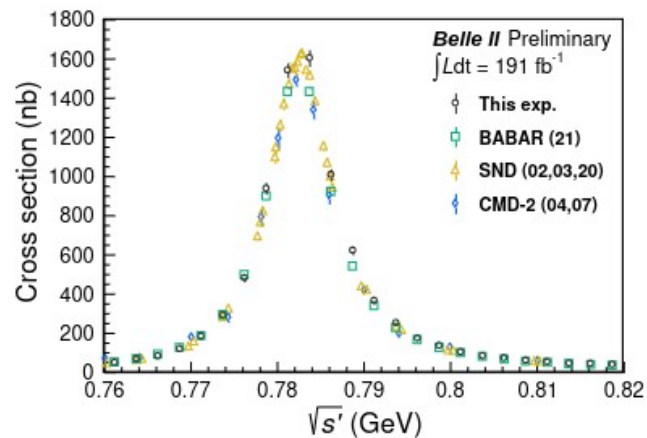


Worlds largest  $\tau$ -charm data sets in  $e^+e^-$  collisions

# Hadronic cross sections

$$e^+e^- \rightarrow \pi^+\pi^-\pi^0$$

BaBar	ISR	total cross section	Phys. Rev. D104 (2021) 11203
BESIII	scan	PWA at three energies	Phys. Rev. D110 (2024) 032005
Belle II	ISR	total cross section	arXiv:2404.04915



# Hadronic cross sections

$$e^+e^- \rightarrow \pi^+\pi^-\eta$$

PWA at three energies

Phys.Rev. D108 (2023) 111101

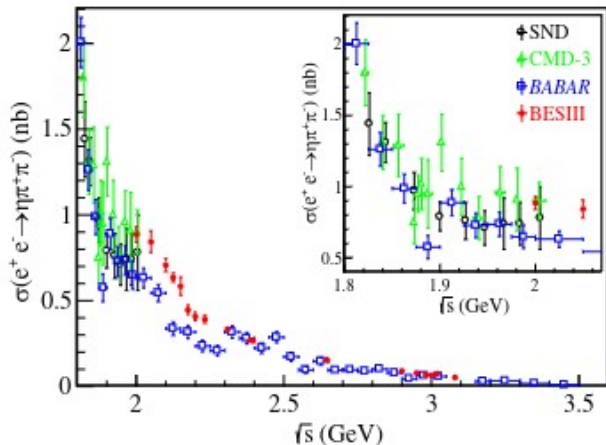


TABLE I. Statistical significances and fit fractions of possible intermediate processes at  $\sqrt{s} = 2.125, 2.396,$  and  $2.900$  GeV.

$\sqrt{s} = 2.125$ GeV			$\sqrt{s} = 2.396$ GeV			$\sqrt{s} = 2.900$ GeV		
Process	Significance ( $\sigma$ )	Fraction (%)	Process	Significance ( $\sigma$ )	Fraction (%)	Process	Significance ( $\sigma$ )	Fraction (%)
$\rho(770)\eta$	>20	$58.0 \pm 1.0$	$\rho(770)\eta$	>20	$69.5 \pm 2.5$	$\rho(770)\eta$	>20	$66.8 \pm 2.2$
$a_2(1320)\pi$	>20	$24.1 \pm 0.8$	$a_2(1320)\pi$	>20	$13.0 \pm 1.1$	$a_2(1320)\pi$	>10	$21.7 \pm 2.1$
$\rho(1450)\eta$	>10	$1.8 \pm 0.3$	$\rho(1450)\eta$	5.1	$1.0 \pm 0.4$	$\rho(1450)\eta$	>10	$16.5 \pm 0.4$
$a_2(1700)\pi$	>10	$2.0 \pm 0.3$	$\rho_3(1690)\eta$	9.7	$2.5 \pm 0.5$	$\rho(1700)\eta$	6.5	$2.1 \pm 0.1$
...	...	...	$a_2(1700)\pi$	6.8	$2.7 \pm 0.4$	...	...	...
...	...	...	$\rho(1700)\eta$	5.8	$1.9 \pm 0.9$	...	...	...

Related studies at BESIII:

$$e^+e^- \rightarrow \omega\pi^0/\eta \quad \text{Phys.Lett. B813 (2021) 136059}$$

$$e^+e^- \rightarrow \pi^+\pi^-\eta' \quad \text{Phys.Rev. D103 (2021) 072007}$$

$$e^+e^- \rightarrow \omega\eta' \quad \text{JHEP 07 (2024) 093}$$

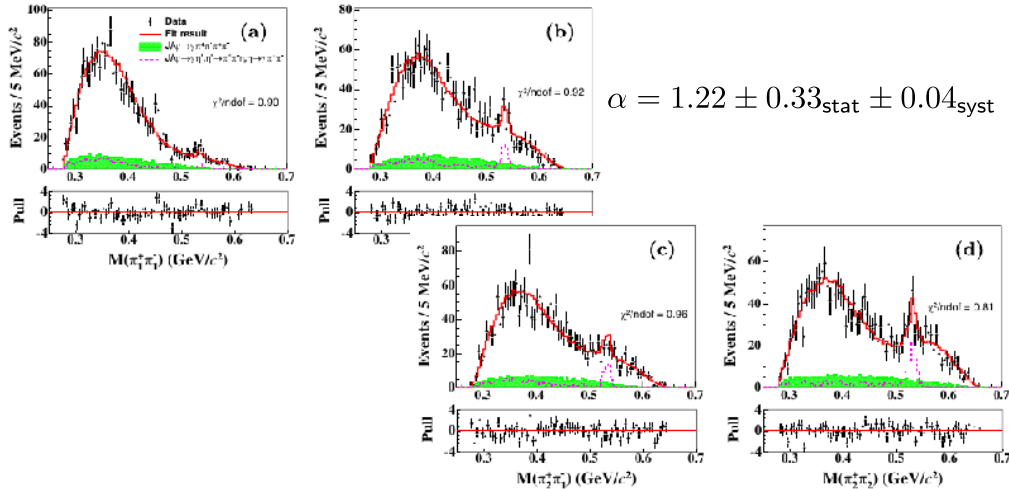
# Meson decays

$$\eta' \rightarrow \pi\pi\pi\pi$$

Phys. Rev. D109 (2024) 032006

Mode	$N$	$\varepsilon$ (%)	$B(\eta' \rightarrow X)$
$\eta' \rightarrow \pi^+\pi^-\pi^+\pi^-$	$1650 \pm 48$	36.4	$(8.56 \pm 0.25(\text{stat.}) \pm 0.23(\text{syst.})) \times 10^{-5}$
$\eta' \rightarrow \pi^+\pi^-\pi^0\pi^0$	$865 \pm 49$	7.8	$(2.12 \pm 0.12(\text{stat.}) \pm 0.10(\text{syst.})) \times 10^{-4}$
$\eta' \rightarrow \pi^0\pi^0\pi^0\pi^0$	$< 10$	1.6	$< 1.24 \times 10^{-5}$

- Access to doubly virtual time-like isovector transition form factor
- Amplitude analysis following Guo, Kubis, Wirzba [PRD 85 (2012) 014014] suggests coupling constants  $c_1 - c_2 \approx c_3$



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$$\eta' \rightarrow \pi^+\pi^-\ell^+\ell^-$$

Phys.Rev. D103 (2021) 072006

Phys.Rev. D103 (2021) 092005

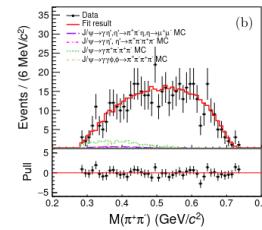
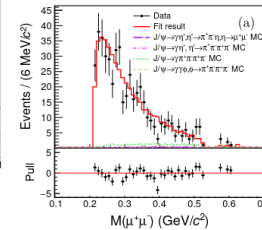
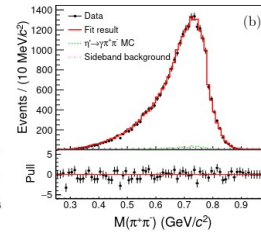
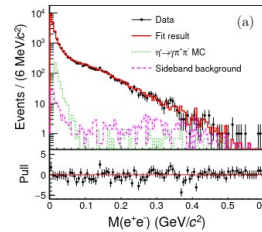
JHEP 07 (2024) 135

$$\mathcal{B}(\eta' \rightarrow \pi^+\pi^-e^+e^-) = (2.45 \pm 0.02(\text{stat.}) \pm 0.08(\text{syst.})) \times 10^{-3}$$

$$\mathcal{B}(\eta' \rightarrow \pi^+\pi^-\mu^+\mu^-) = (2.16 \pm 0.12(\text{stat.}) \pm 0.06(\text{syst.})) \times 10^{-5}$$

TFF studied for different VMD models

$$b_{\eta'} = 1.30 \pm 0.19(\text{GeV}/c^2)^2$$

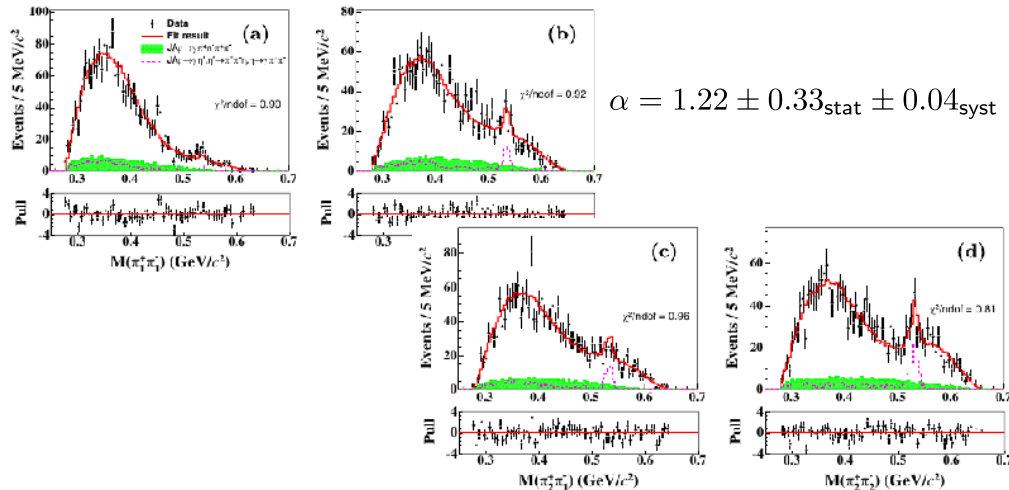


$$\alpha = 1.22 \pm 0.33_{\text{stat}} \pm 0.04_{\text{syst}}$$

Asymmetry parameter measured

$$\mathcal{A}_{CP}(\eta' \rightarrow \pi^+\pi^-e^+e^-) = (0.21 \pm 0.73(\text{stat.}) \pm 0.01(\text{syst.}))\%$$

$$\mathcal{A}_{CP}(\eta' \rightarrow \pi^+\pi^-\mu^+\mu^-) = (0.62 \pm 4.71(\text{stat.}) \pm 0.02(\text{syst.}))\%$$





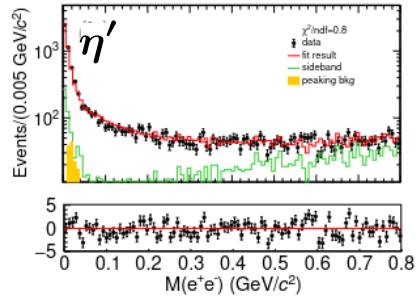
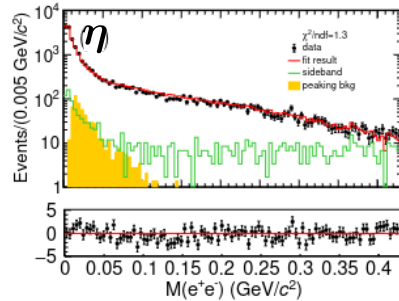
# Meson decays

$$\eta/\eta' \rightarrow \gamma e^+ e^-$$

Phys.Rev. D109 (2024) 072001

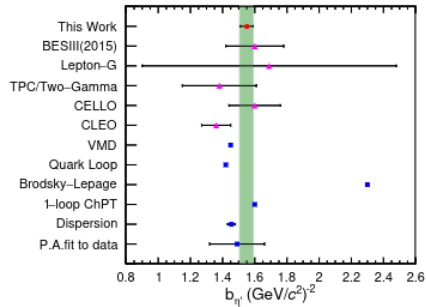
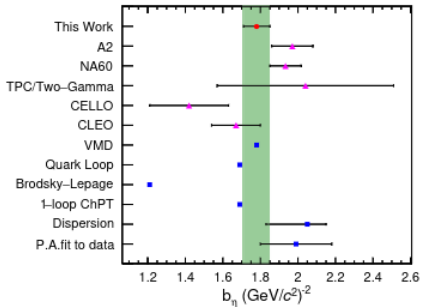
$$\mathcal{B}(\eta \rightarrow \gamma e^+ e^-) = (7.07 \pm 0.05(\text{stat.}) \pm 0.23(\text{syst.})) \times 10^{-3}$$

$$\mathcal{B}(\eta' \rightarrow \gamma e^+ e^-) = (4.83 \pm 0.07(\text{stat.}) \pm 0.14(\text{syst.})) \times 10^{-4}$$



$$\Lambda_\eta = (0.749 \pm 0.027 \pm 0.008) \text{ GeV}/c^2 \quad \Lambda_{\eta'} = (0.802 \pm 0.007 \pm 0.008) \text{ GeV}/c^2$$

$$\gamma_{\eta'} = (0.113 \pm 0.010 \pm 0.002) \text{ GeV}/c^2$$



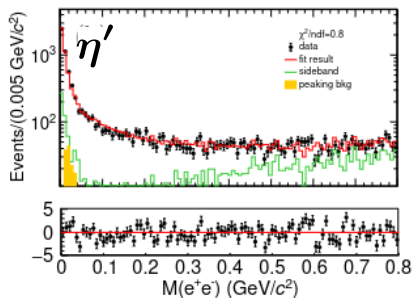
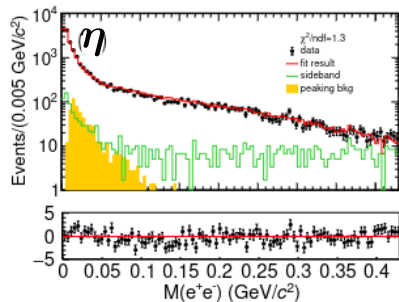
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Phys.Rev. D109 (2024) 072001

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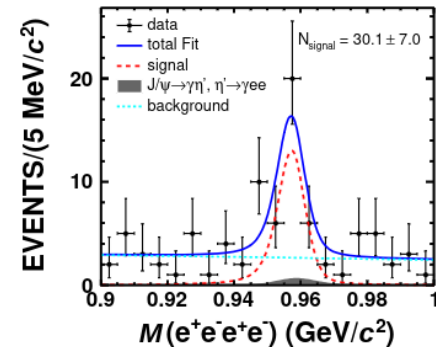
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$$\eta' \rightarrow e^+ e^- e^+ e^-$$

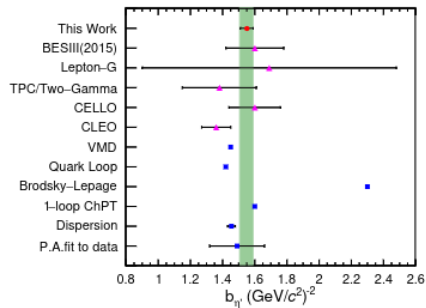
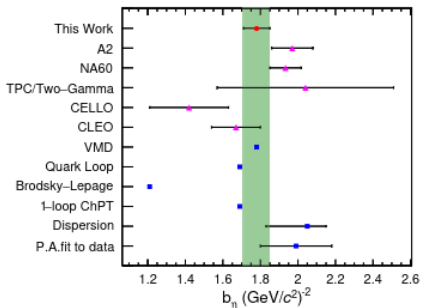
Phys.Rev. D105 (2022) 112010

$$\mathcal{B}(\eta' \rightarrow e^+ e^- e^+ e^-) = (4.5 \pm 1.0(\text{stat.}) \pm 0.5(\text{syst.})) \times 10^{-6}$$



$$\Lambda_\eta = (0.749 \pm 0.027 \pm 0.008) \text{ GeV}/c^2 \quad \Lambda_{\eta'} = (0.802 \pm 0.007 \pm 0.008) \text{ GeV}/c^2$$

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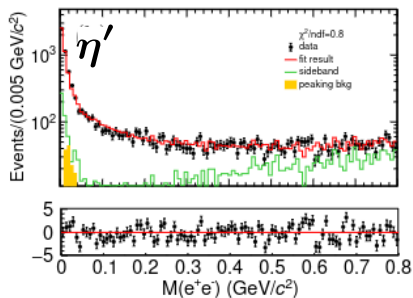
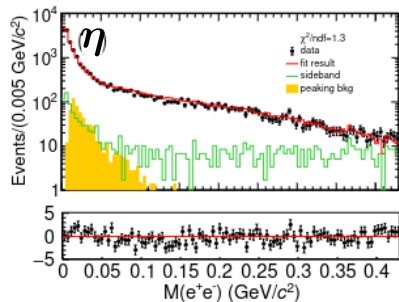
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Phys.Rev. D109 (2024) 072001

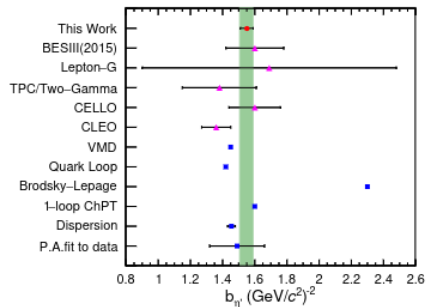
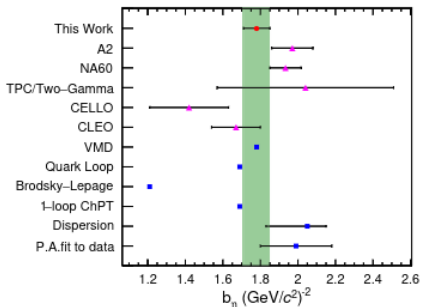
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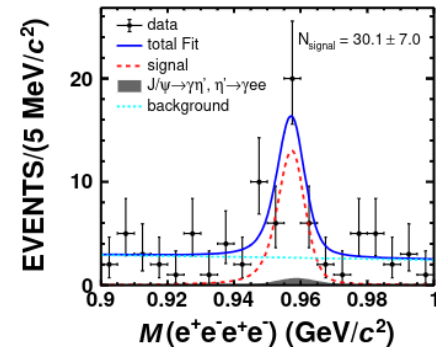
$$\gamma_{\eta'} = (0.113 \pm 0.010 \pm 0.002) \text{ GeV}/c^2$$



$$\eta' \rightarrow e^+ e^- e^+ e^-$$

Phys.Rev. D105 (2022) 112010

$$\mathcal{B}(\eta' \rightarrow e^+ e^- e^+ e^-) = (4.5 \pm 1.0(\text{stat.}) \pm 0.5(\text{syst.})) \times 10^{-6}$$



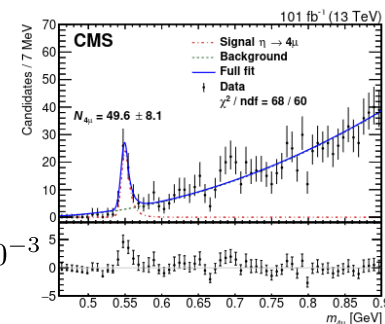
$$\eta \rightarrow \mu^+ \mu^- \mu^+ \mu^-$$

Phys.Rev.Lett. 131 (2023) 091903

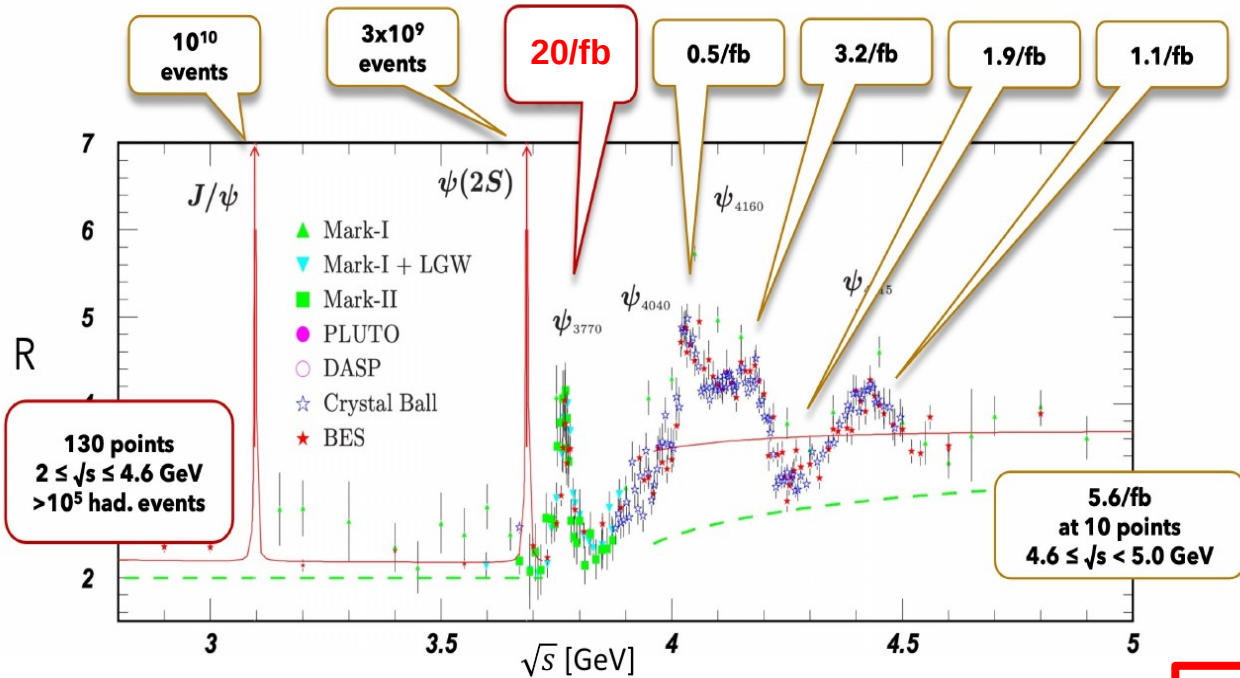


$$\text{Normalized to } \eta \rightarrow \mu^+ \mu^-$$

$$\frac{\mathcal{B}_{4\mu}}{\mathcal{B}_{2\mu}} = (0.86 \pm 0.14(\text{stat}) \pm 0.12(\text{syst})) \times 10^{-3}$$



# $\gamma^{(*)}\gamma^*$ results to be expected from BESIII



Worlds largest  $\tau$ -charm data sets in  $e^+e^-$  collisions

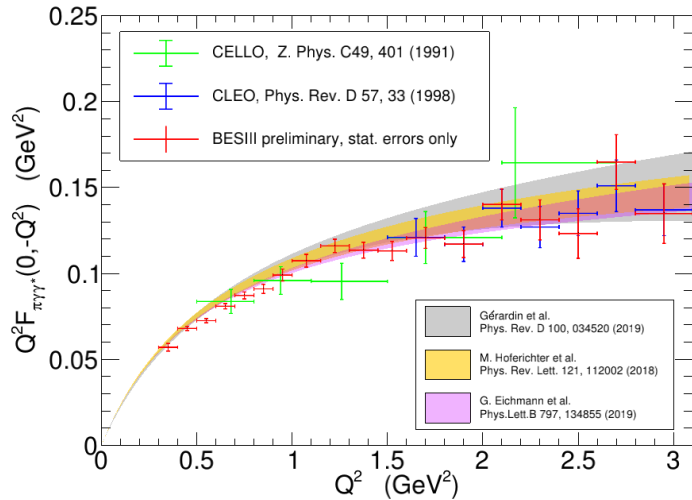
- Richest data above open charm threshold
- Access to
  - Hadronic masses up to 2 GeV
  - $0.2 \leq Q^2 [\text{GeV}^2] \leq 3$
- Access to smaller  $Q^2$  values at  $\sqrt{s} \approx 2$  GeV (limited statistics)

**New data at 3.77 GeV most relevant!**

Data taking finished June 2024

$$\gamma^{(*)}\gamma^* \rightarrow \pi^0, \eta, \eta'$$

$$\gamma\gamma^* \rightarrow \pi^0$$



**Since preliminary:**

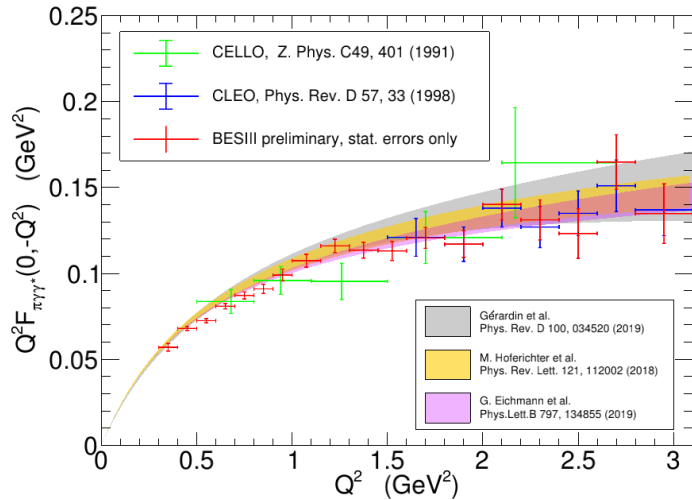
- Improved systematics
- Included radiative corrections based on Ekhar3

**Plan:**

- Publish 'old' data to be in time from WP2
- Full data set as update

$$\gamma^{(*)} \gamma^* \rightarrow \pi^0, \eta, \eta'$$

$$\gamma\gamma^* \rightarrow \pi^0$$



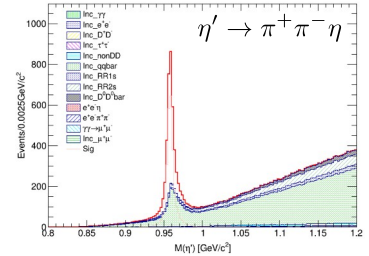
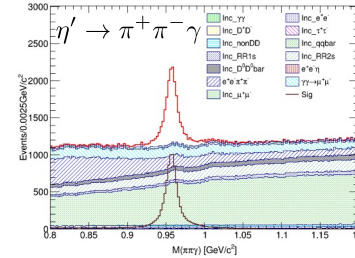
Since preliminary:

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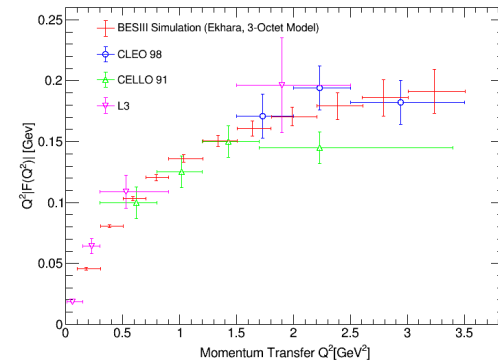
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$$\gamma\gamma^* \rightarrow \eta'$$



Simulations using full 20 fb<sup>-1</sup>

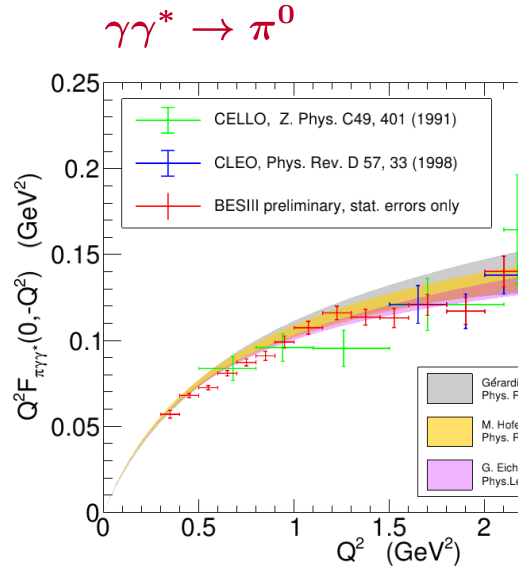


Kangshuai Zhu

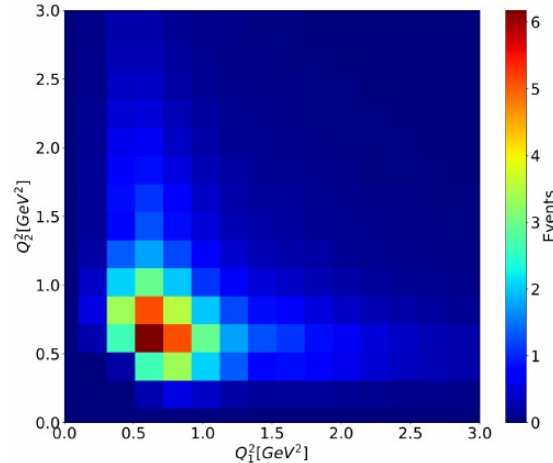
- First direct measurement at  $Q^2 < 0.3 \text{ GeV}^2$
- Unprecedented accuracy

$$\gamma^{(*)}\gamma^{*} \rightarrow \pi^0, \eta, \eta'$$

$$\gamma^{*}\gamma^{*} \rightarrow \eta, \eta'$$

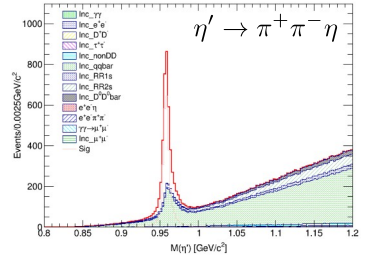


- First studies by Maurice Anderson
- Using combination of previously available data

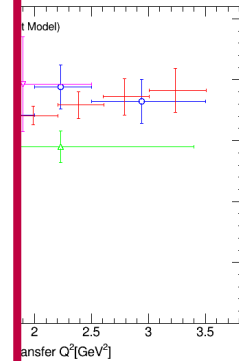


Simulation of expected yields for 13 fb<sup>-1</sup> of data at  $\sqrt{s} \geq 3.773$  GeV

- To be done on full data set



using full 20 fb<sup>-1</sup>



at  $Q^2 < 0.3$  GeV<sup>2</sup>

Kangshuai Zhu

Since preliminary:

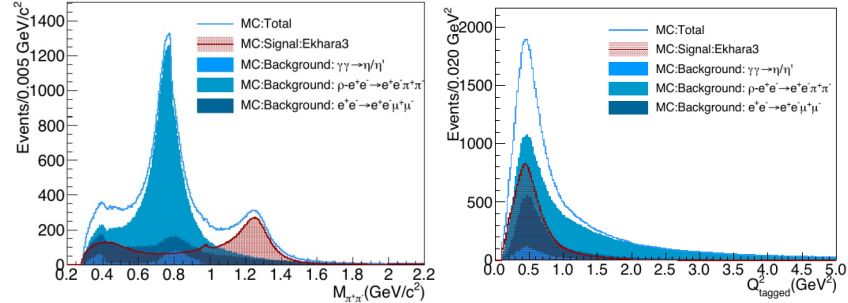
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Plan:

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- Full data set as update

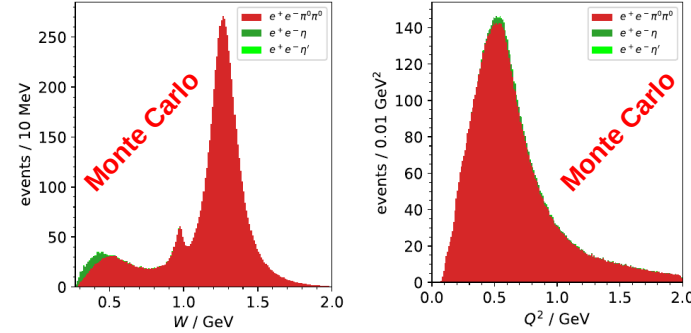
$$\gamma^{(*)} \gamma^* \rightarrow \pi \pi$$

$$\gamma \gamma^* \rightarrow \pi^+ \pi^-$$



Yuping Guo

$$\gamma \gamma^* \rightarrow \pi^0 \pi^0$$



Max Lellmann

- Combined data
- Irreducible time-like background (rad.Bhabha)
- Evaluation of efficiencies ongoing

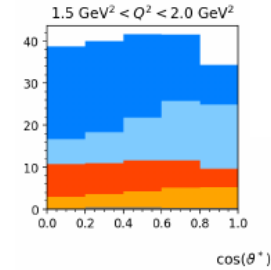
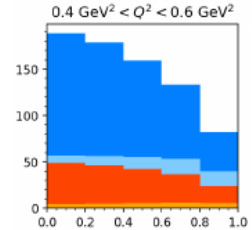
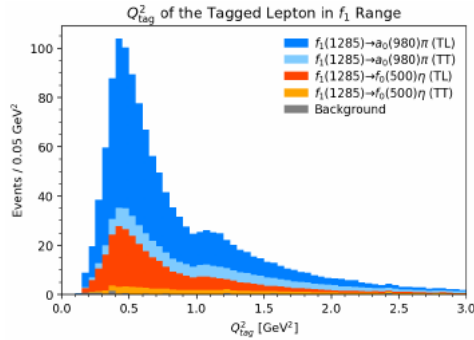
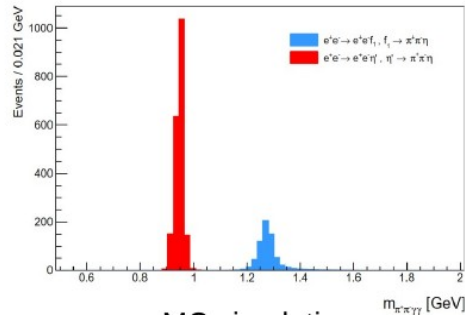
- Using only new data
- Novel strategy leads to improved  $Q^2$  resolution
  - Study dependency on 2<sup>nd</sup> virtuality
  - Study angular features of two-photon production
  - Requires different MC generator

- Invariant masses from threshold to 2 GeV
- $0.2 \leq Q^2 [\text{GeV}^2] \leq 3$
- Full coverage of helicity angle



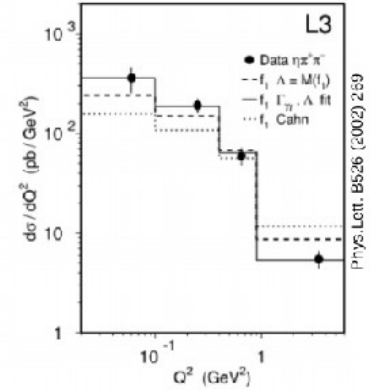
# $\gamma\gamma^* \rightarrow f_1(1285)$

- Reconstructing  $f_1(1285) \rightarrow \pi^+\pi^-\eta$
- Possibility to separate helicity states from fit to angular distributions
- PWA required due to inseparable intermediate states  $a_0^\pm(980)\pi^\mp \longleftrightarrow f_0(500)\eta$



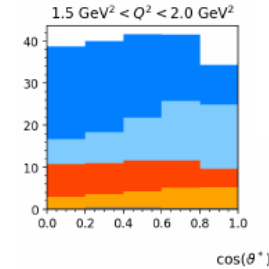
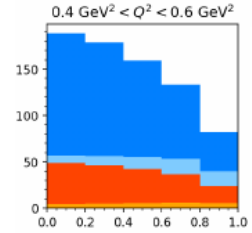
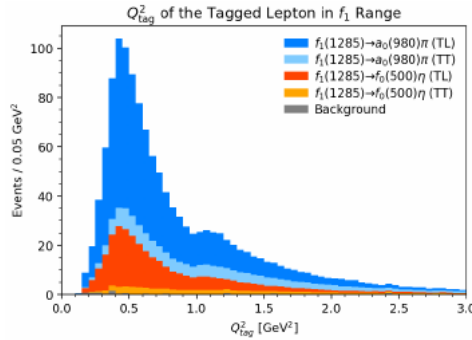
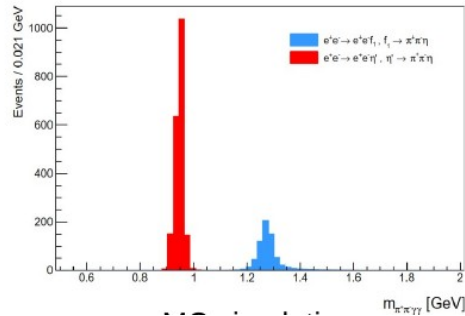
Jan Muskalla

Only available data:



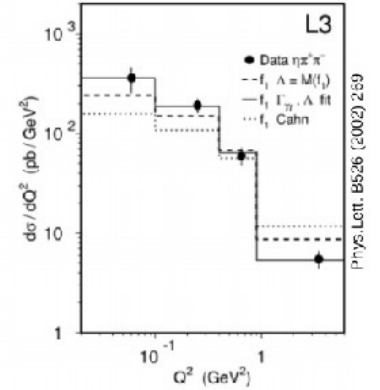
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Only available data:



## Other channels:

- Exploratory studies (B.Sc. thesis level)

$$\gamma\gamma^* \rightarrow \pi^0\eta$$

$$\gamma\gamma^* \rightarrow \pi^+\pi^-\pi^0$$

$$\gamma\gamma^* \rightarrow KK\pi$$

# Other Experimental Input

- TFF from coherent electroproduction of mesons (Primakoff contribution)
  - Plans at JLab (Hall B & D) and MAMI (A1)
  - $0.01 \leq Q^2 [\text{GeV}^2] \leq 0.1$
  - Primex- $\eta$  data taking finished
  - A1 data taking probably from next year
- TFF from meson decays
  - update from A2 on  $\pi^0$  TFF
- Radiative decays of axial vector mesons
  - Work ongoing at BESIII based on  $J/\psi$  decays
  - Contact with Martin and Bastian has been established
- .....