

Coherence amplification using atoms (ions) for fundamental physics

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on behalf of SPAN collaboration



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For crystal projects

H. Hara, Y. Miyamoto, Junseok Han,
Y. Imai, N. Sasao, K. Yoshimura, M. Yoshimura

Introduction

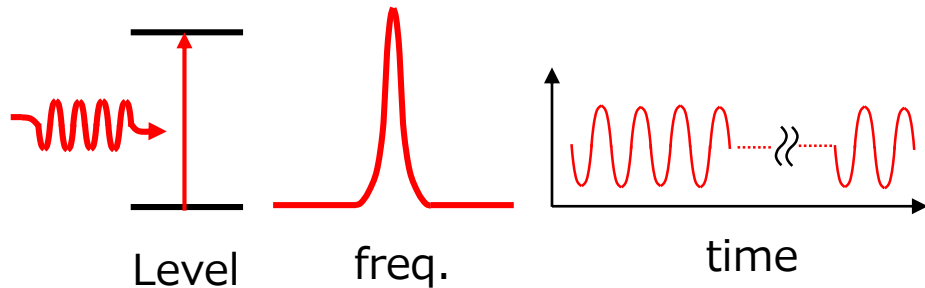
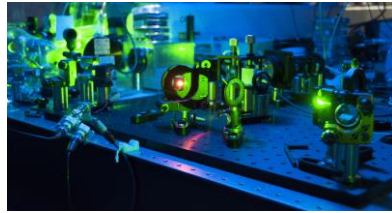
Precision measurement

Nuclear clock

Muonium spectroscopy

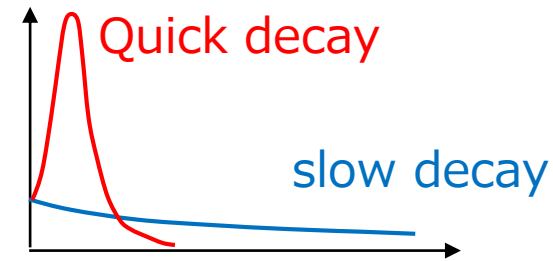
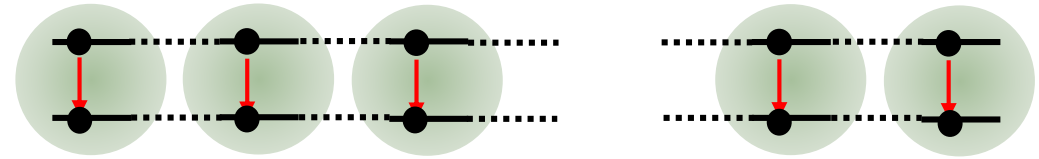
EDM

Cold molecule ...



Amplification of "weak" process

using quantum coherence



Neutrino mass spectroscopy

Dark matter (Axion, DP, ..) search

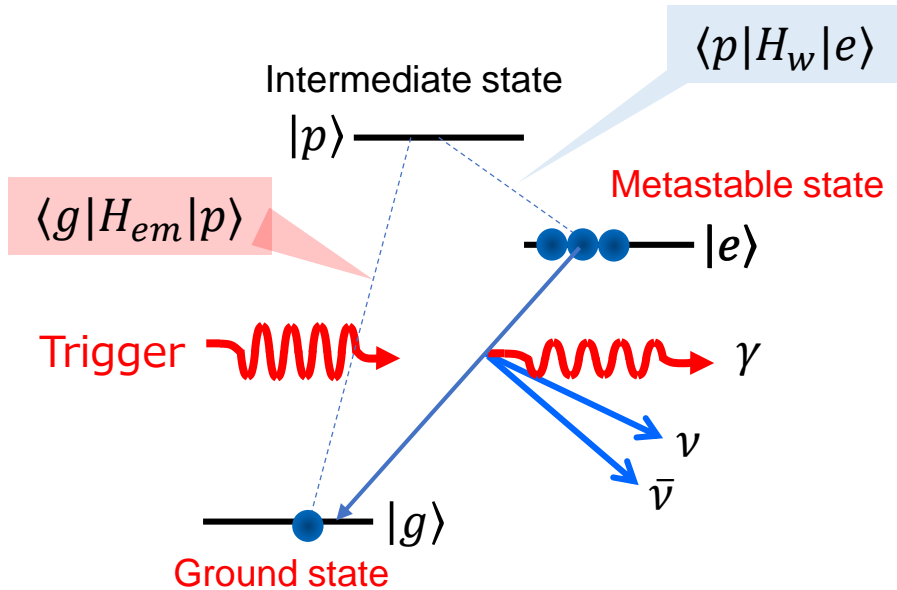
Origin of CP violation

beyond Standard Model

What should be amplified

Radiative emission of neutrino pair (RENPN)

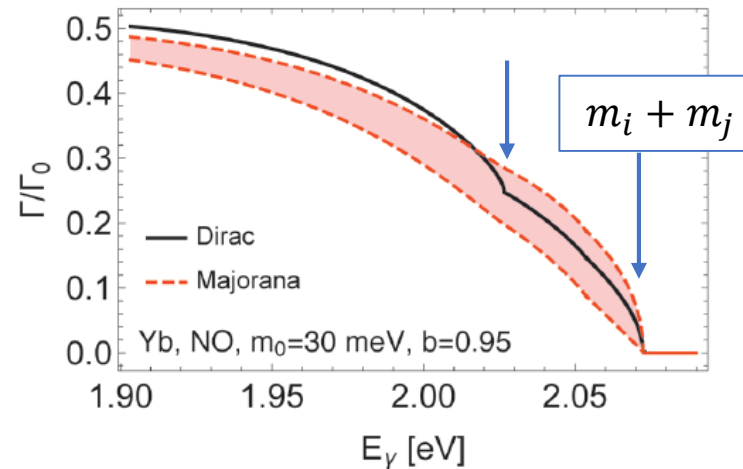
Atomic transition



$$H_w = \frac{G_F}{\sqrt{2}} \sum_{ij} \bar{\nu}_i \gamma^\alpha (1 - \gamma_5) \nu_j \bar{e} (\gamma_\alpha c_{ij} - \gamma_\alpha \gamma_5 b_{ij}) e$$

PHYSICAL REVIEW D **75**, 113007 (2007)
Neutrino pair emission from excited atoms
 M. Yoshimura
 Center of Quantum Universe and Department of Physics, Okayama University, Tsushima-naka 3-1-1, Okayama 700-8530, Japan
 (Received 24 December 2006; revised manuscript received 4 April 2007; published 25 June 2007)

photon spectrum



$$\omega_{ij} = \frac{\epsilon_{eg}}{2} - \frac{(m_i + m_j)^2}{2\epsilon_{eg}}$$

- Neutrino absolute mass (mass eigen state)
- Dirac / Majorana
- NH/IH

Energy scale **eV ~ meV** : neutrino mass scale

Low RENPN rate
 @ E ~ eV

$$\Gamma_{RENPN} \sim \alpha G_F^2 E^5 = 1.5 \times 10^{-33} [s^{-1}]$$

Neutrino Physics

- Absolute mass ?
- Dirac-type or Majorana-type ?
- CP-violating parameters ?

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

Cosmology

Why No antimatter in Universe ?

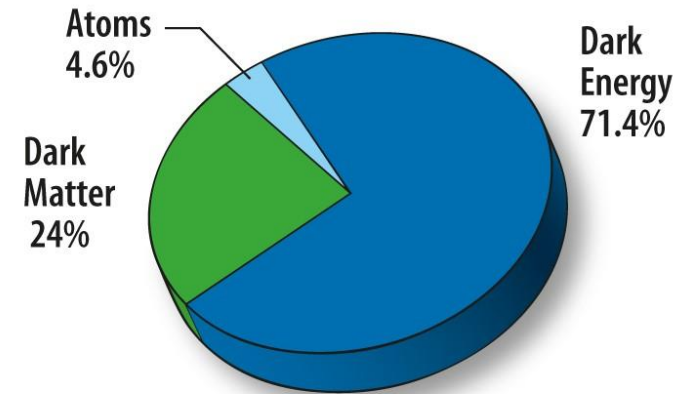
Particle Physics

Why so small mass of neutrinos ?

➔ Leptogenesis Heavy right-handed neutrino

Majorana neutrino $\nu \neq \bar{\nu}$

Dark matter



Axions

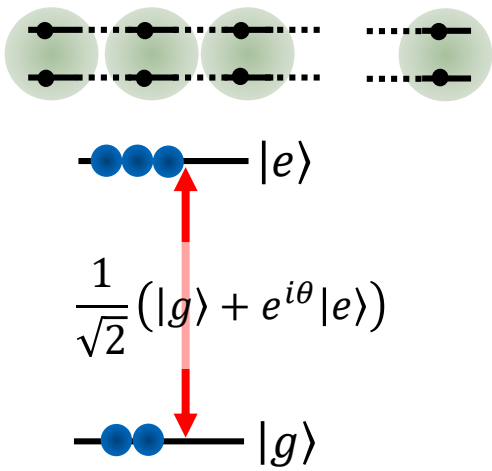
$$\mathcal{L}_a = \frac{1}{2}(\partial_\mu a)^2 - \frac{1}{2}m_a^2 a^2 - \frac{1}{4}F_{\mu\nu}F^{\mu\nu} + \frac{1}{4}g_{a\gamma\gamma}aF_{\mu\nu}\tilde{F}^{\mu\nu} \quad g_{a\gamma\gamma} = g\frac{\alpha}{\pi f_a}$$

Dark photon

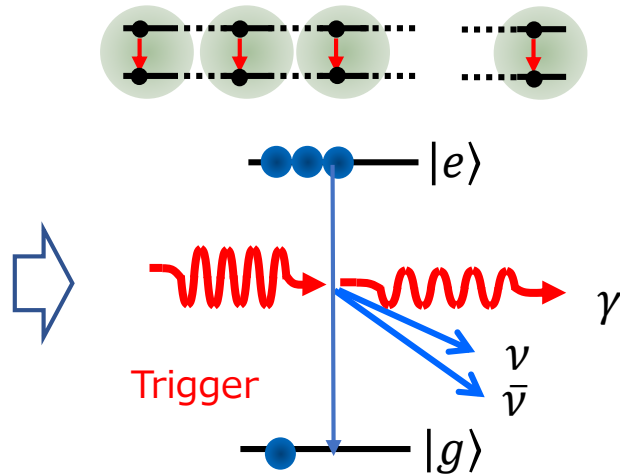
$$\mathcal{L}_{DP} = -\frac{1}{4}F_{\mu\nu}F^{\mu\nu} - \frac{1}{4}X_{\mu\nu}X^{\mu\nu} - \frac{\chi}{2}F_{\mu\nu}X^{\mu\nu} + \frac{m_X^2}{2}X_{\mu\nu}X^{\mu\nu} + j_\mu A^\mu$$

Coherence amplification

prepare "coherence"



amplified decay



$$\Gamma_{\text{RENP}} \propto \left| \sum_a^N e^{-i(\mathbf{k}_1 + \mathbf{k}_2 + \mathbf{k}_3) \cdot \mathbf{r}_a} \cdot \mathcal{M}_a(\mathbf{r}_a, t) \cdot e^{i\mathbf{k}_{ex} \cdot \mathbf{r}_a} \right|^2$$

Excitation γ

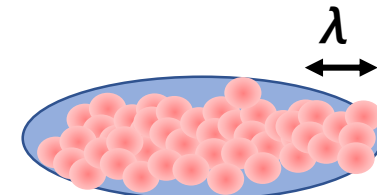
Emitted γ/ν : plane wave

Atoms: Transition matrix

if momentum conservation:

$$\mathbf{k}_{ex} - (\mathbf{k}_1 + \mathbf{k}_2 + \mathbf{k}_3) = 0$$

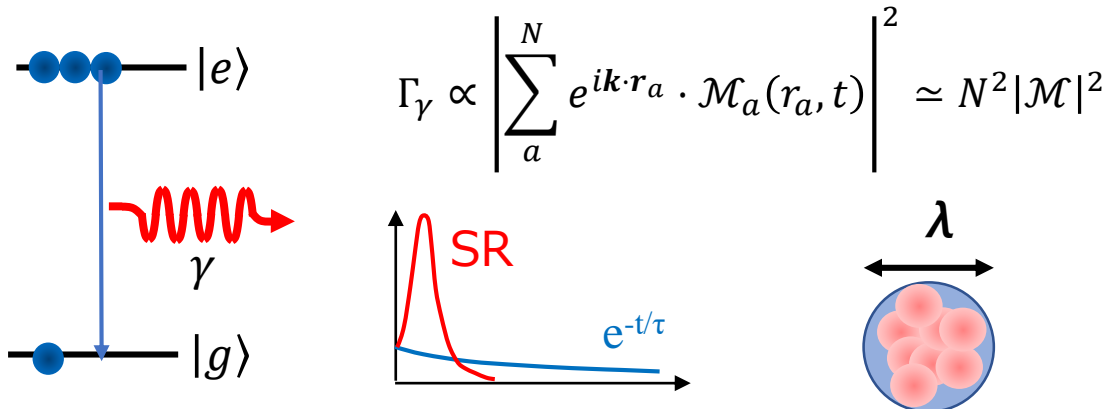
$$\Gamma_{\text{RENP}} \propto \left| \sum_a^N \mathcal{M}_a(\mathbf{r}_a, t) \right|^2 \simeq N^2 |\mathcal{M}_a|^2$$



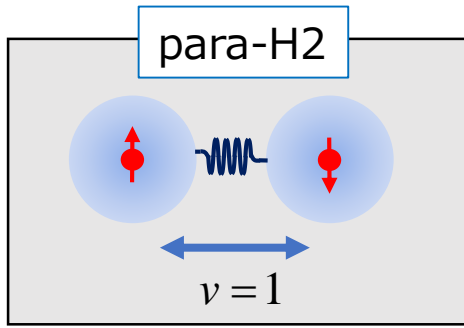
"macroscopic"

SR beyond λ !

Dicke's Superradiance



Performed the "basic" experiment of Macro-Coherence-Amplification



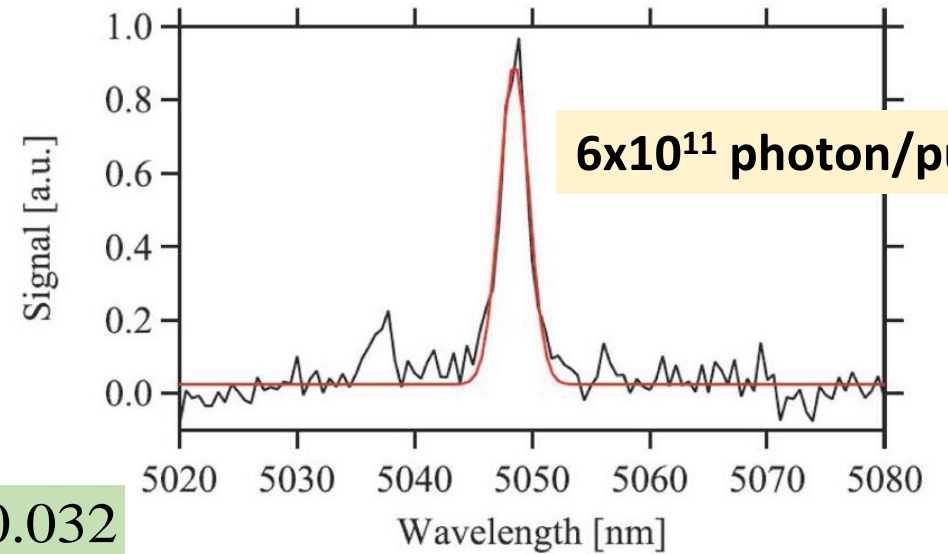
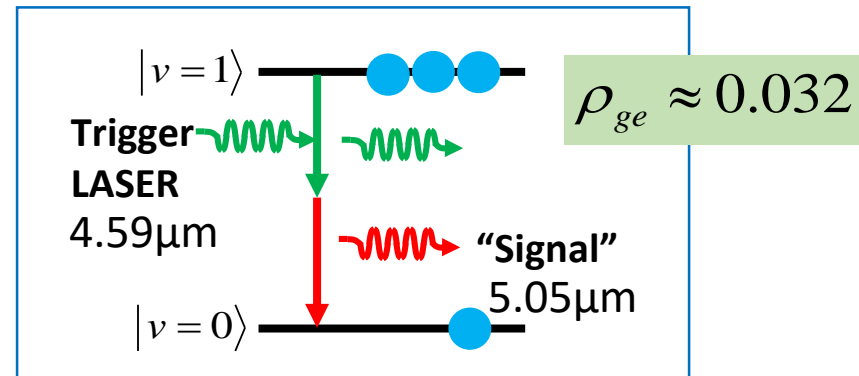
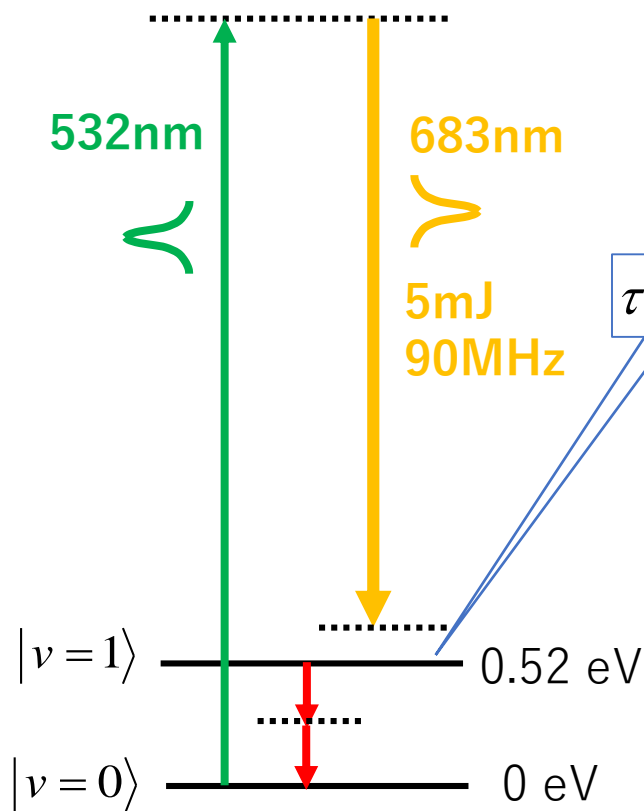
Y. Miyamoto et al.

"Observation of coherent two-photon emission from the first vibrationally excited state of hydrogen molecules"

PTEP 113C01 (2014).

"Externally triggered coherent two-photon emission from hydrogen molecules"

PTEP 081C01 (2015).



$$\text{Enhancement} = \frac{6 \times 10^{11}}{2.4 \times 10^{-7}} \approx 10^{18}$$

What's next ?

Improvements of amplification

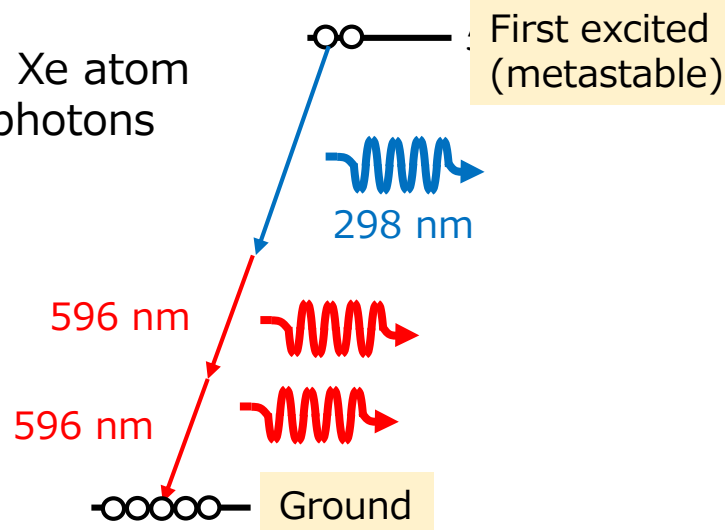
Larger N, Larger coherence ?

two-photon $I_{\text{sig}} \propto |E_{\text{sig}}|^2 \propto N_i^2 \cdot |\rho_{ge}^0|^2 \cdot I_{\text{trig}}$

$$\left. \begin{array}{l} \rho_{ge} \simeq 0.25 \\ n \simeq 1 \times 10^{20} [\text{cm}^{-3}] \end{array} \right\} K_{\text{enhance}} \simeq 10^{20}$$

Amplification of "weaker"-process

sample: Xe atom
three photons



"Improved" methods

Discrimination of enhanced QED background

three-photon emission $(\mathbf{d}_{ep} \cdot \mathbf{E}_a)(\mathbf{d}_{pq} \cdot \mathbf{E}_b)(\mathbf{d}_{qg} \cdot \mathbf{E}_c)$

sample: Xe atom

$$\Gamma_{3p} \sim 10^{19} \text{ Hz} \cdot \left(\frac{n}{10^{20} \text{ cm}^{-3}} \right)^3 \cdot \frac{V}{1 \text{ cm}^3} \cdot \frac{\eta_3(t)}{10^{-3}}$$

$$\Gamma_{\text{RENIP}} \sim 1 \text{ mHz} \cdot \left(\frac{n}{10^{20} \text{ cm}^{-3}} \right)^3 \cdot \frac{V}{1 \text{ cm}^3} \cdot \frac{\eta_\omega(t)}{10^{-3}}$$

Discrimination of QED-process

Photonic crystal waveguide

PTEP

Prog. Theor. Exp. Phys. 2017, 043B03 (18 pages)
DOI: 10.1093/ptep/ptx035

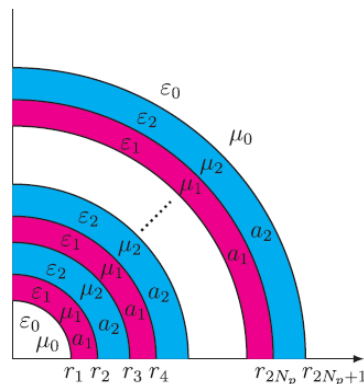
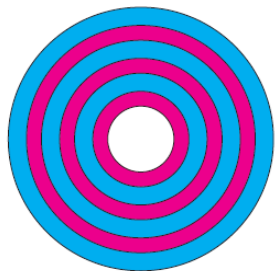
Toward background-free RENP using a photonic crystal waveguide

Minoru Tanaka^{1,*}, Koji Tsumura², Noboru Sasao³, and Motohiko Yoshimura³

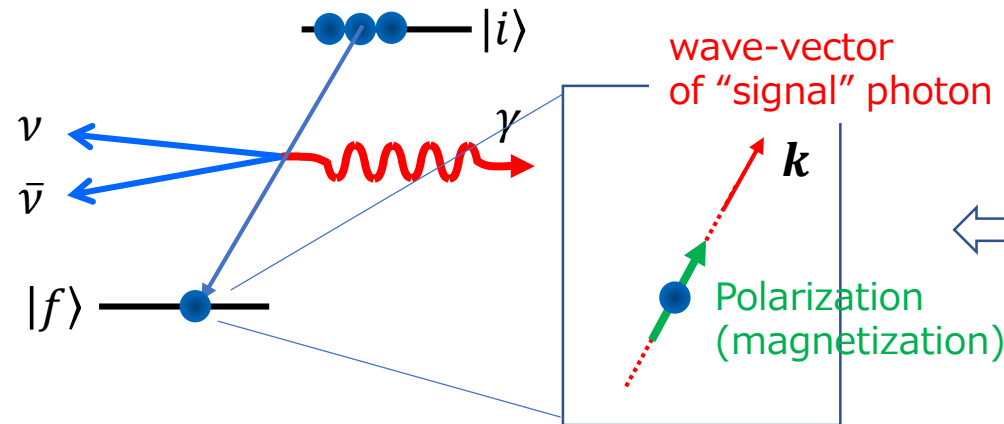
Cutoff the mode in a waveguide

Effective photon mass $> m_\nu$

➔ Large suppression of QED



Parity-violating spin component



$$\langle M \rangle \propto g\mu_B \langle f | \mathbf{k} \cdot \mathbf{S} | f \rangle \cdot |\langle f | H_w | i \rangle|^2$$

➔ Doped ion in crystals

“Parity-mixed” state

➔ Coherence amplification in Solid state (crystals)

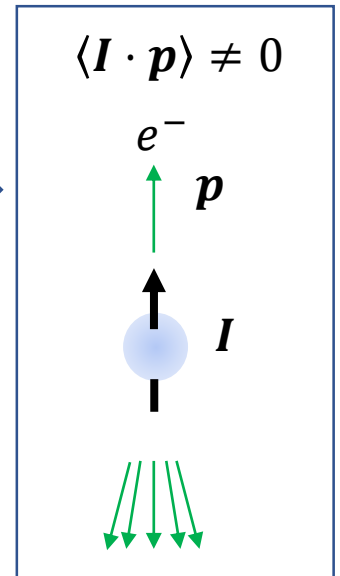
also good for N^2 -amp

PHYSICAL REVIEW D **104**, 115006 (2021)

Parity violating magnetization at neutrino pair emission using trivalent lanthanoid ions

Hideaki Hara¹, Akihiro Yoshimi¹, and Motohiko Yoshimura¹
Research Institute for Interdisciplinary Science, Okayama University,
Tsushima-naka 3-1-1, Kita-ku, Okayama 700-8530, Japan

PV in β -decay



Lanthanoid elements doped in crystals

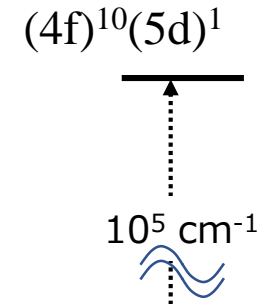
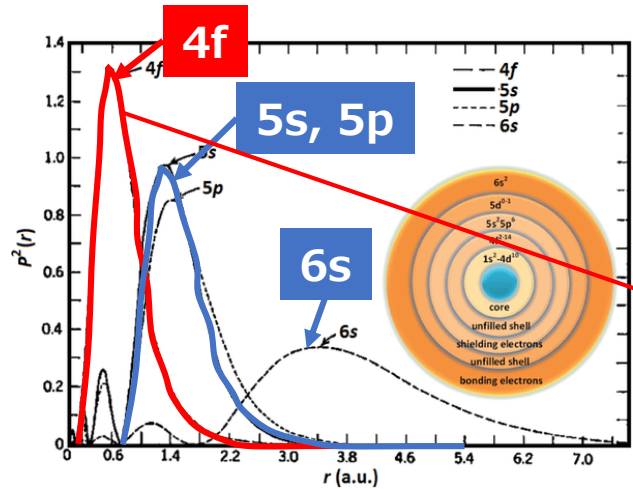
Lanthanoid ions doped in Crystal

59	60	61	62	63	64	65	66	67	68	69	70	71
Pr	Nd	Pm	Sm	Eu	Gd	Tb	Dy	Ho	Er	Tm	Yb	Lu
Praseodymium 140.90765 [Xe]4f ³ 5s ² 5.473	Neodymium 144.24 [Xe]4f ⁴ 5s ² 5.5250	Promethium (145)	Samarium 150.36 [Xe]4f ⁶ 5s ² 5.6437	Europium 151.964 [Xe]4f ⁷ 5s ² 5.6704	Gadolinium 157.25 [Xe]4f ⁷ 5d ¹ 5s ² 6.1498	Terbium 158.92534 [Xe]4f ⁹ 5s ² 5.8638	Dysprosium 162.500 [Xe]4f ¹⁰ 5s ² 5.9389	Holmium 164.93032 [Xe]4f ¹¹ 5s ² 6.0215	Erbium 167.259 [Xe]4f ¹² 5s ² 6.1077	Thulium 168.93421 [Xe]4f ¹³ 5s ² 6.1843	Ytterbium 173.04 [Xe]4f ¹⁴ 5s ² 6.2542	Lutetium 174.967 [Xe]4f ¹⁴ 5d ¹ 5s ² 6.3309

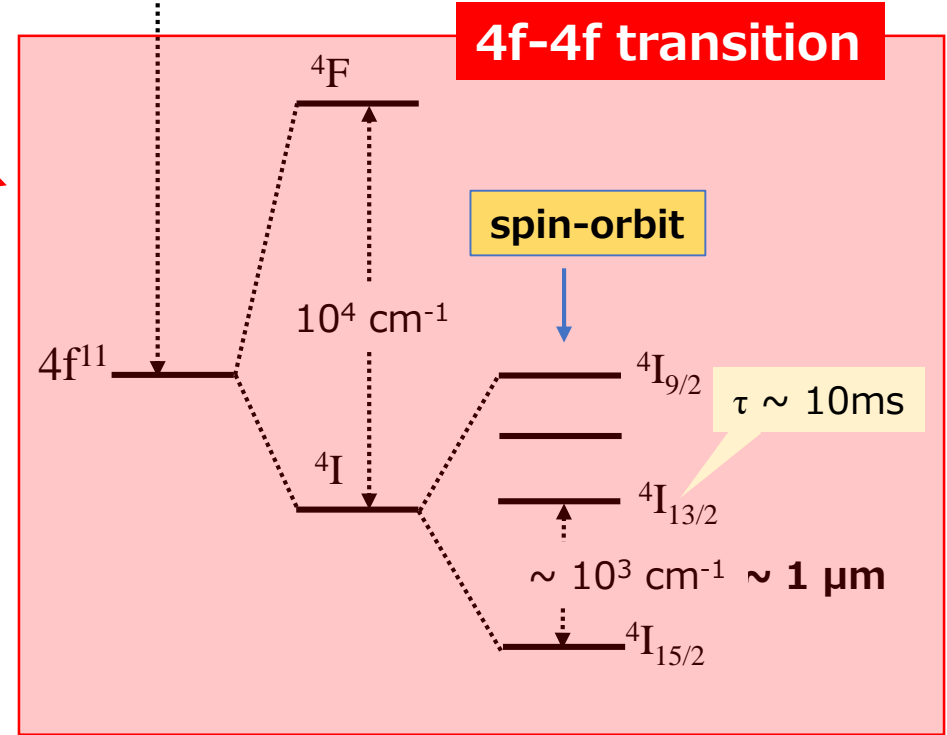
4f-electron

shielded by 5s(5p) electrons

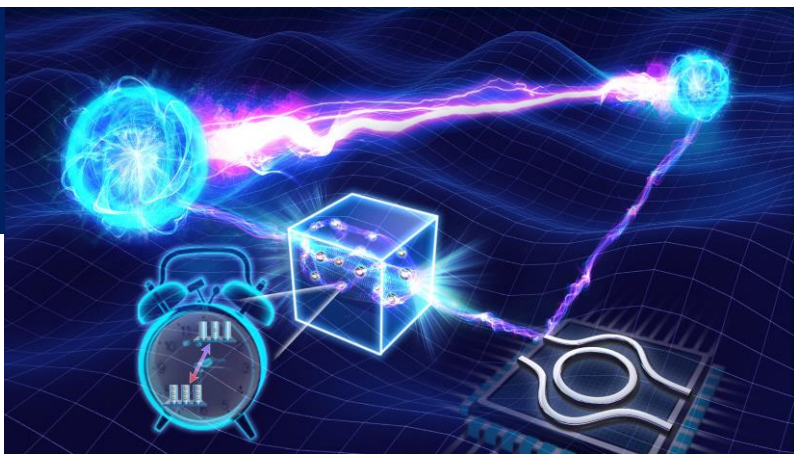
- Narrow linewidth
- Long relaxation time



The energy level of Er³⁺ doped in crystal



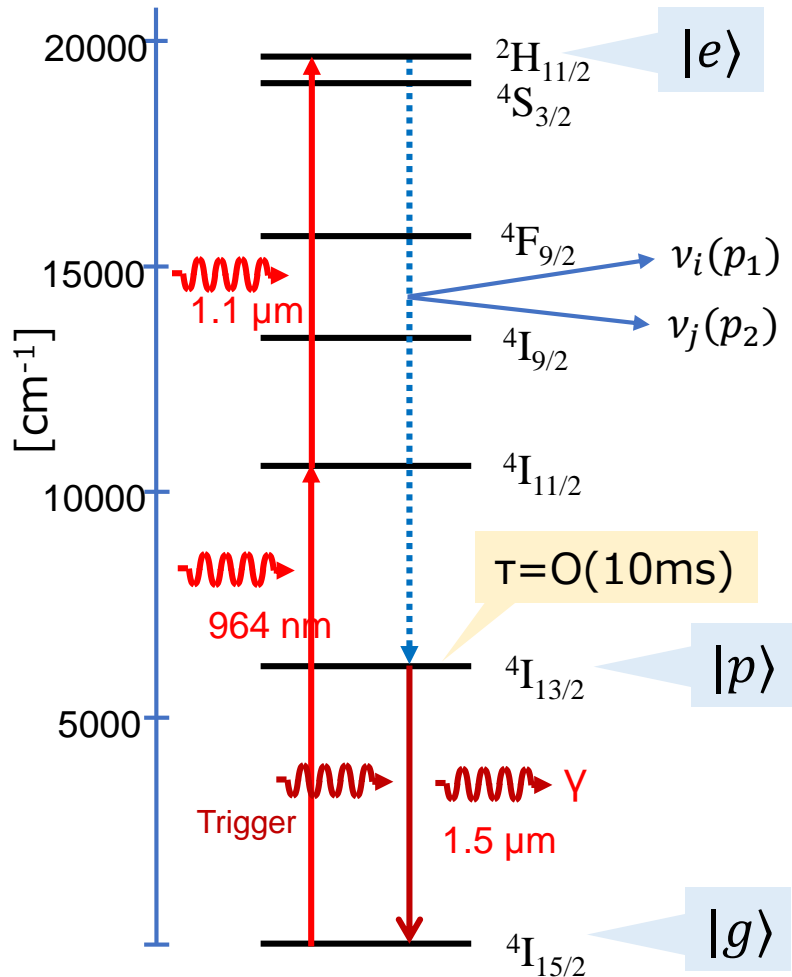
“Quantum storage of entangled photons at telecom wavelengths in a crystal” (Er:Y₂SiO₅)



Ming-Hao Jiang et al. Nature Comm. 14:6995(2023).

Proposals of MagREN

proposed scheme with $\text{Er}^{3+}:\text{LiYF}_4$



Produced magnetization

$$\Gamma_{Mag} = \frac{2G_F^2}{(2\pi)^3} h_r^2 (nV)^2 |\chi|^2 \cdot g\mu_B n \cdot (\mathbf{S}_{ep} \cdot \mathbf{v}_{ep}) \cos \theta_s \cdot \sum_{ij} G_{ij}$$

excitation/coherence

$$\propto \rho_{ee}^3 |\rho_{ep}|^2 = 10^{-2} \sim 10^{-3}$$

$$\sim 0.1 - 1 \text{ [nG]}$$

※ Accumulation time = 1 ms assumed. (spin relaxation time)

can be accumulated within spin relaxation.

$v_i v_j$ emission

atomic matrix element

$$\langle p || S || e \rangle = \frac{12}{\mu_B^2} \sum_{m', q} |\langle p, m' | M_q | e, m \rangle|^2 \approx 3.47$$

$$\langle p || v || e \rangle = \left\langle p \left| \left| \pm i \frac{\mathbf{d}_{ep}}{e} \epsilon_{ep} \right| \right| e \right\rangle$$

$$= \frac{12\epsilon_{ep}^2}{e^2} \sum_m |\langle p, m' | d_q | e, m \rangle|^2 \approx 2.79 \times 10^{-6}$$

“First-step” experiments with crystals

H. Hara,
Y. Miyamoto

PHYSICAL REVIEW RESEARCH 6, 013005 (2024)

Periodic superradiance in an Er:YSO crystal

Hideaki Hara^{1,*} Junseok Han^{1,2} Yasutaka Imai¹ Noboru Sasao¹ Akihiro Yoshimi¹ Koji Yoshimura¹
Motohiko Yoshimura¹ and Yuki Miyamoto^{1,†}

¹Research Institute for Interdisciplinary Science, Okayama University, Okayama 700-8530, Japan

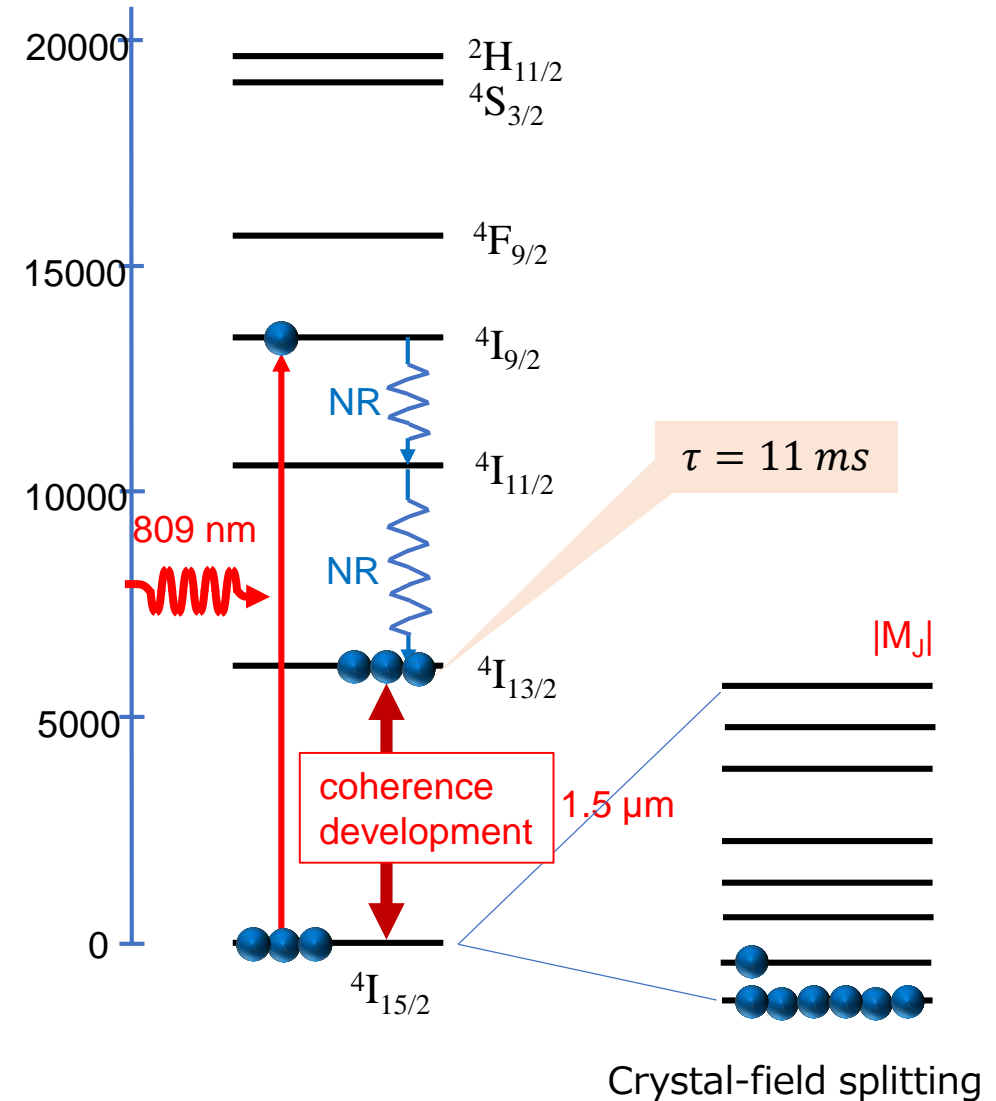
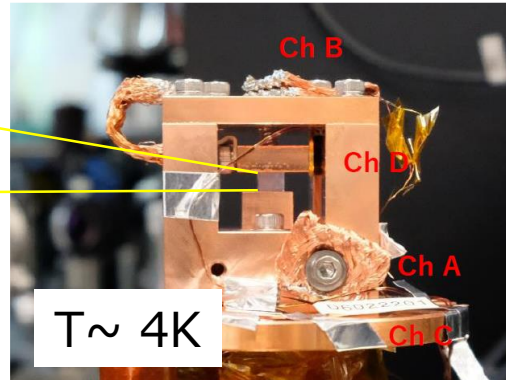
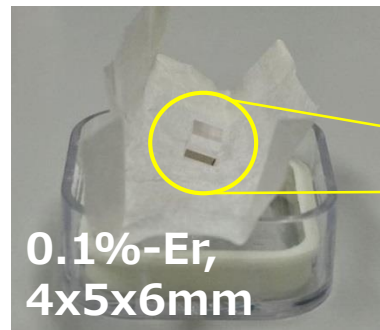
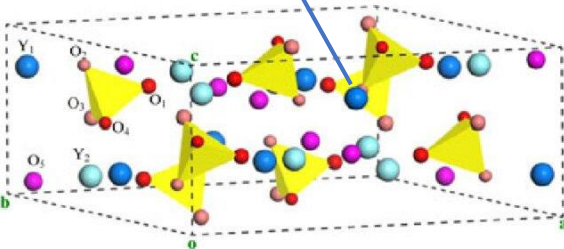
²Department of Physics and Astronomy & Institute of Applied Physics, Seoul National University, Seoul 08826, Korea

Superradiance in crystal

Er³⁺:Y₂SiO₅: good condition for “4f-e”-coherence

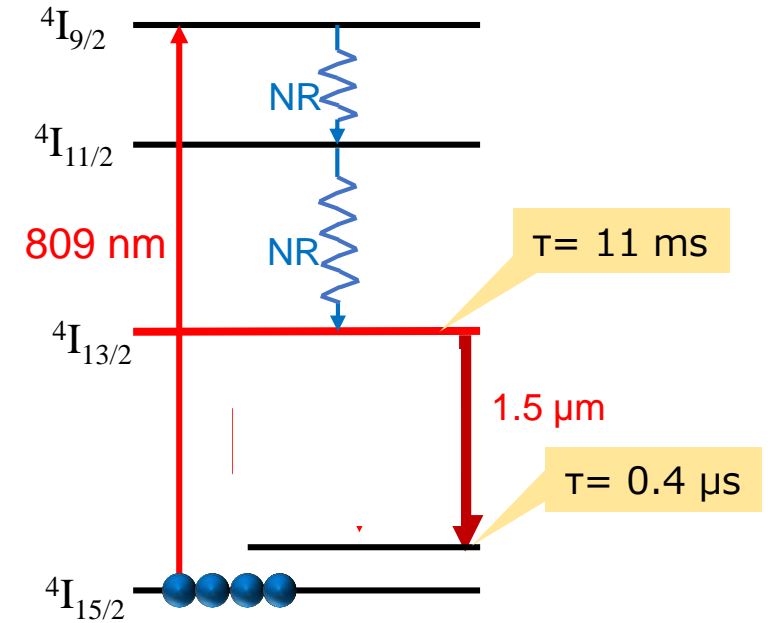
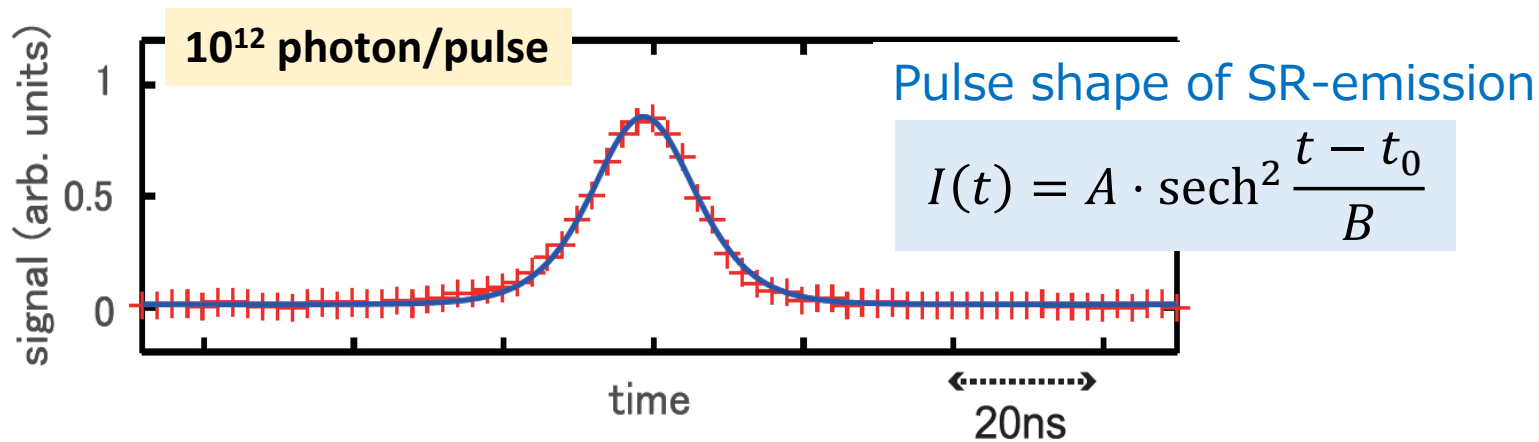
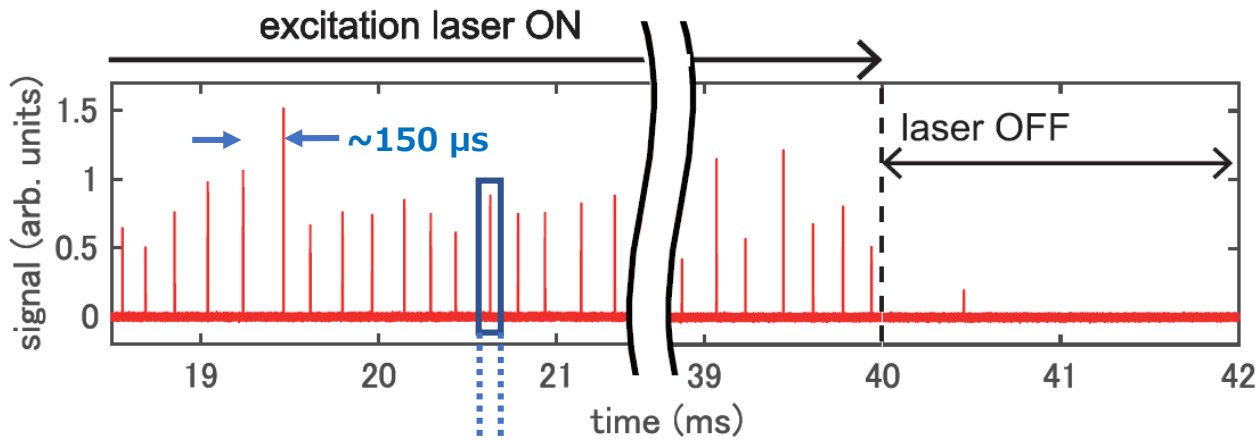
→ Coherence developed in the crystal environment

Y → Er



“First-step” experiments with crystals

CW excitation to metastable level Output pulse of $\lambda=1.5 \mu\text{m}$



Spontaneous formation of atomic coherence

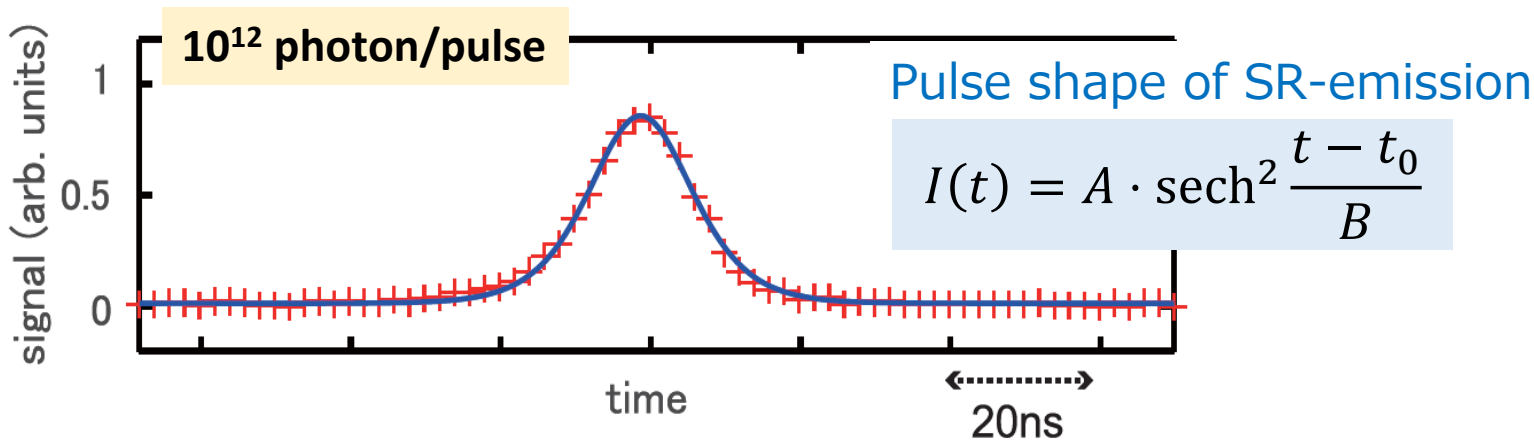
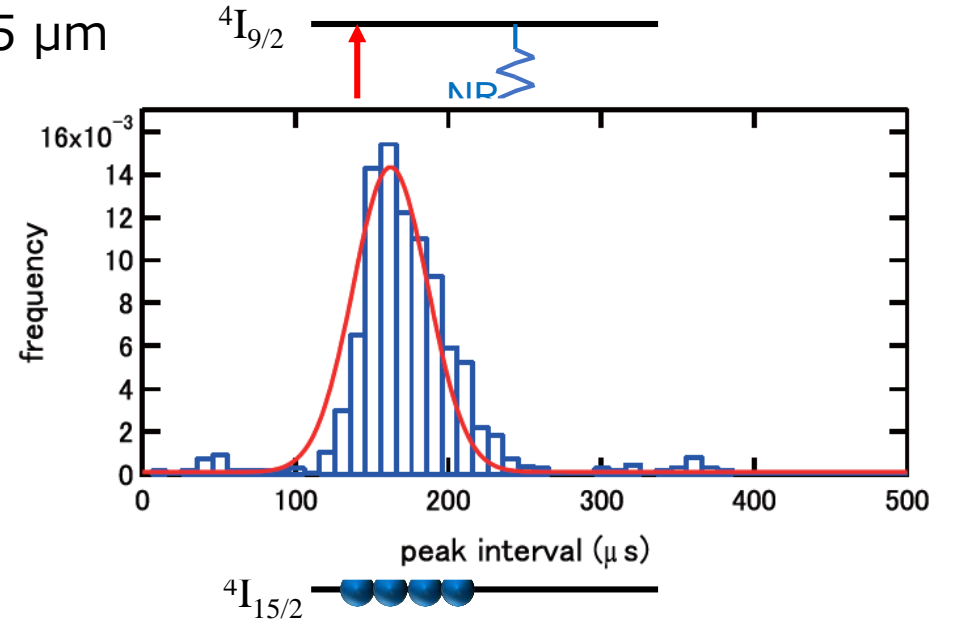
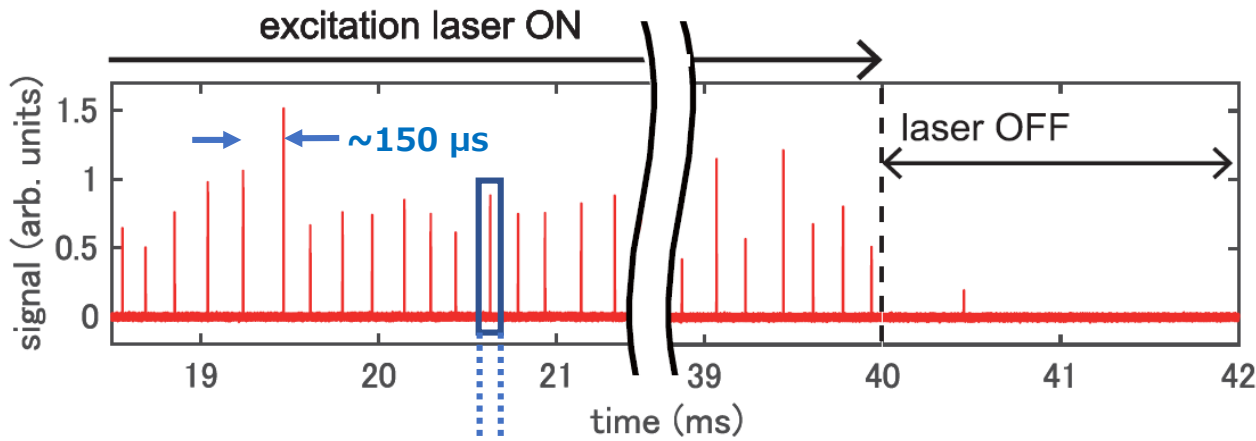
with inhomogeneously broadened ($\sim 1 \text{ GHz}$) Er-ion

More controllable SR?

for example, “triggered SR”

"First-step" experiments with crystals

CW excitation to metastable level Output pulse of $\lambda=1.5 \mu\text{m}$



Spontaneous formation of atomic coherence

with inhomogeneously broadened ($\sim 1 \text{ GHz}$) Er-ion

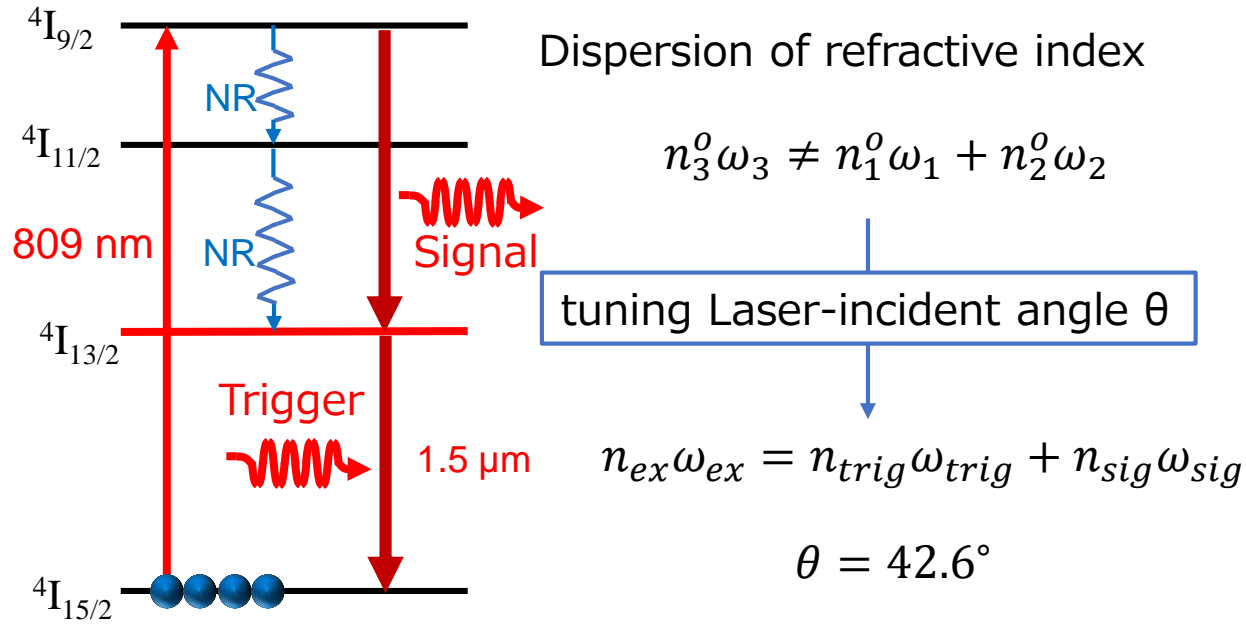
More controllable SR?

for example, "triggered SR"

On-going experiments with crystals

Junseok Han

For coherence generation in Er:YLF



Dispersion of refractive index

$$n_3^0 \omega_3 \neq n_1^0 \omega_1 + n_2^0 \omega_2$$

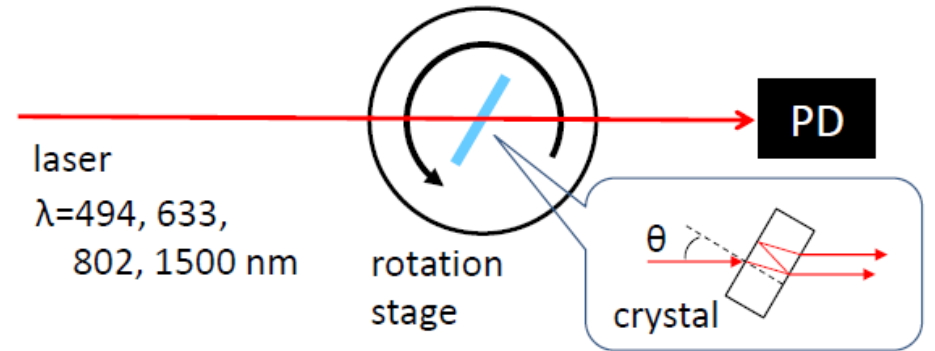
tuning Laser-incident angle θ

$$n_{ex} \omega_{ex} = n_{trig} \omega_{trig} + n_{sig} \omega_{sig}$$

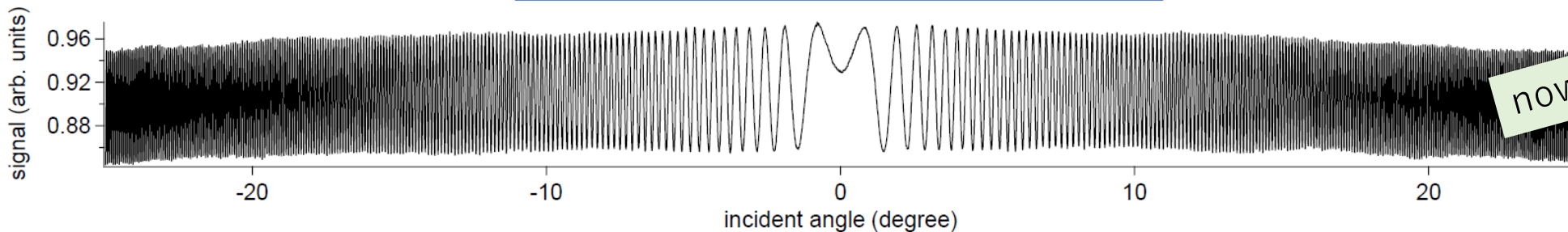
$$\theta = 42.6^\circ$$

Measurement of refractive index

required precision ; 10^{-5}

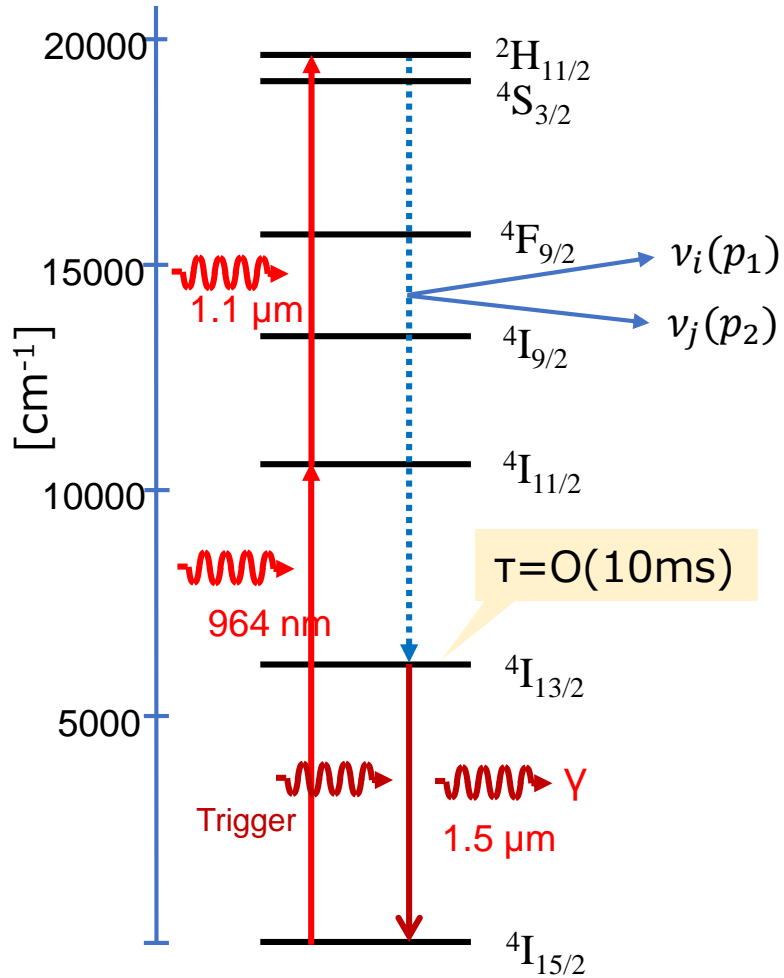


Transmitted intensity for YLF crystal



now in progress

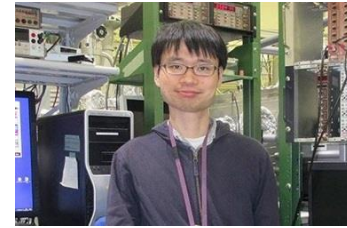
RENK scheme with Er:YLF



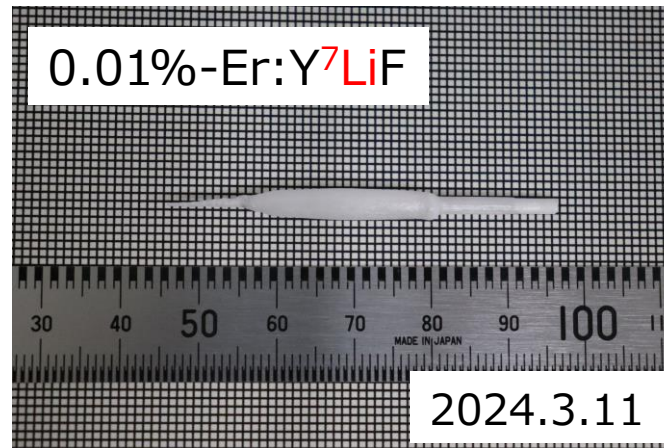
Fabrication of Er:YLF

0.1%, 0.01%-Er:YLF

Micro Pulling down method
@ Tohoku University



Low-concentration <0.1%
Isotope-enriched ^7Li



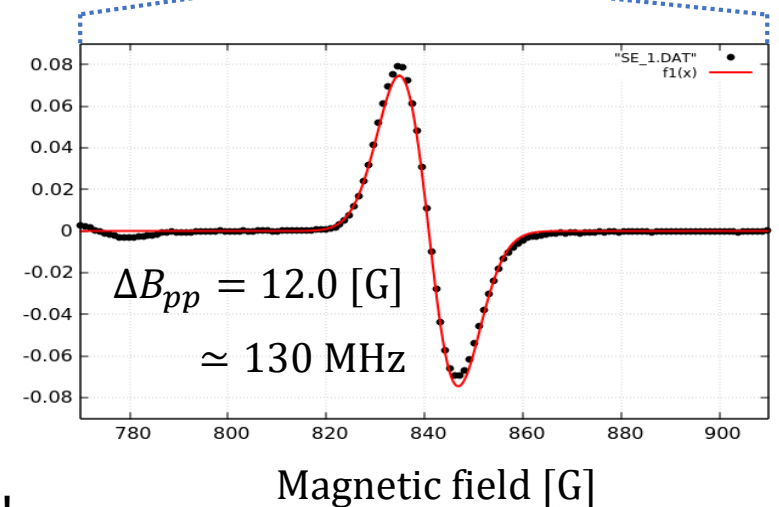
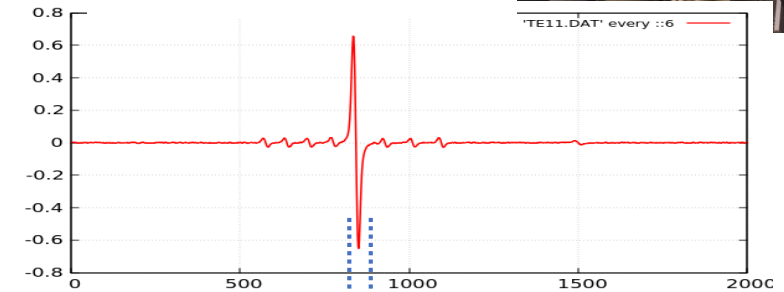
→ go to Narrower-width!

Electron spin resonance

@ $T = 5.0 \text{ K}$



0.01%-Er:Y $^{\text{nat}}$ LiF



→ $T_1 \sim O(1) \text{ ms @ 5K}$

- Principle

- Generate coherence between Cs levels $|i\rangle$ and $|f\rangle$
- Transition induced by photons (γ_{dm}) of axion- B_{ext} scattering or dark-photon.
- Detect signal photons (γ_s) via $|e\rangle \rightarrow |g\rangle$

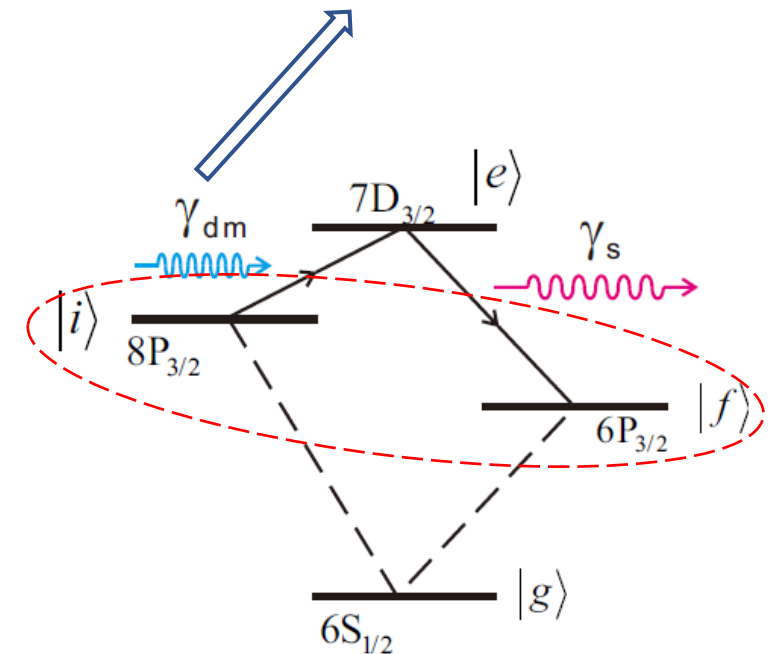
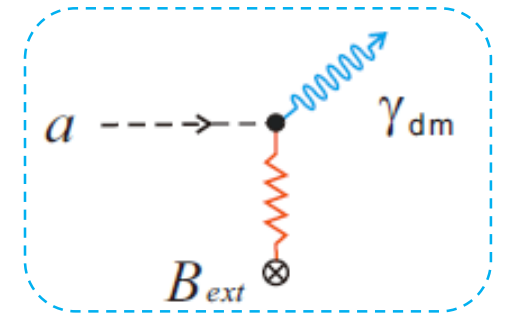
- Signal rate

- $\Gamma \sim 10$ Hz
 - $N_p = 10^{14}$, $B_{ext} = 1$ T for axion
 - $N_p = 10^{10}$, $\chi = 10^{-12}$ for dark-photon

- Backgrounds

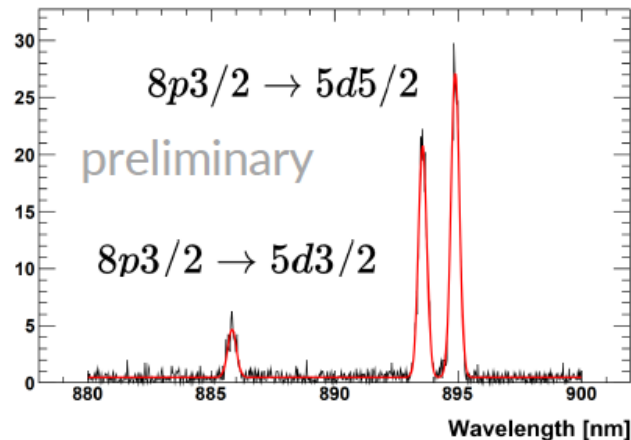
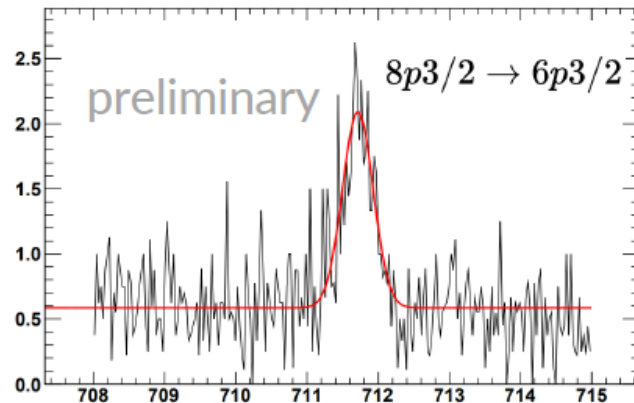
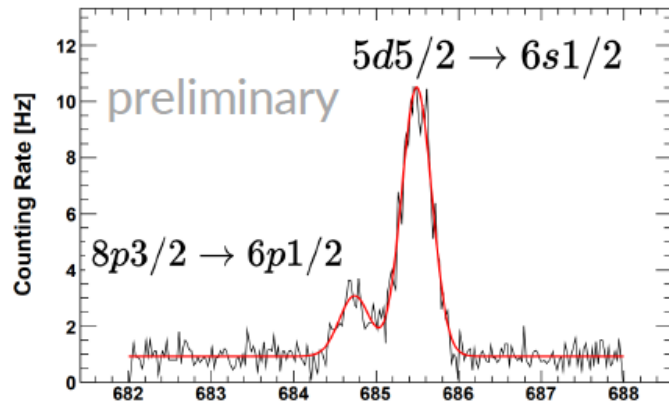
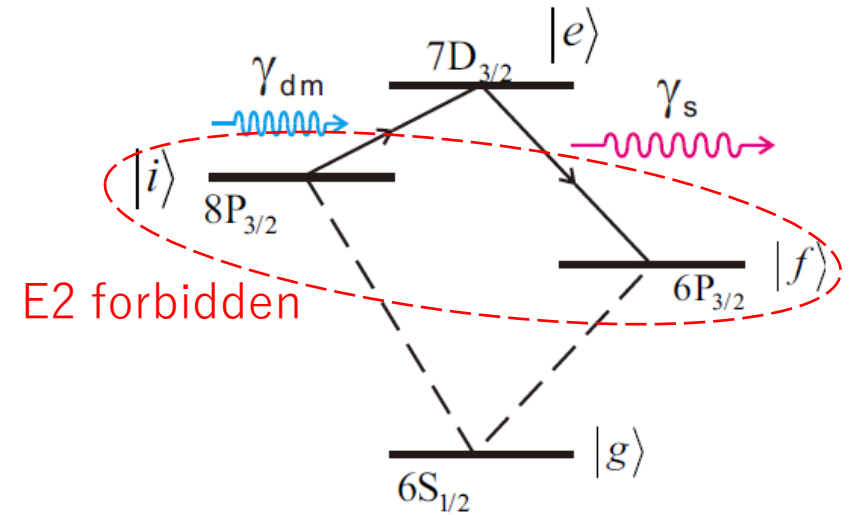
- Black body: need to cool down below $T < 4$ K
- Detector dark counts < 1 Hz or less

Axion dark-matter



Dark-matter search with cold Cs

- Key feature: **coherence**
 - How to confirm it experimentally?
 - Measure the forbidden transition rate $|i\rangle - |f\rangle$ and compare with theoretical expectation.
 - Necessary matrix elements are measured.
- Near-future plan
 - Coherence measurement at 4K.
 - Blackbody detection at $>4\text{K}$.
 - Dark photon search/axion search



poster
presentation
by Jing Wang

Summary

- RENP process is a unique key for neutrino physics
- Macro-coherence amplification is important for neutrino / DM - physics
- Amplification of 2-photon emission with pH_2 ; 10^{18}
- Coherence in Lanthanoid-ion doped in crystals is useful

{ Estimation of PV-magnetization,
Superradiance experiment in Er:YSO crystals
Preparation of coherence generation in crystals

