

Connecting theories of flavour to Kaon physics

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Outline:

1. General Introduction to the Flavour Problem
2. Effective Field Theories for BSM
3. Explicit BSM examples

Motivation

Despite the SM successes,
there are open problems:

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Hierarchy problem

dark matter/dark energy

flavour hierarchies

neutrino masses

gravity

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SM(EFT)

Λ_{EW}

Energy

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UV theory

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Λ_{UV}

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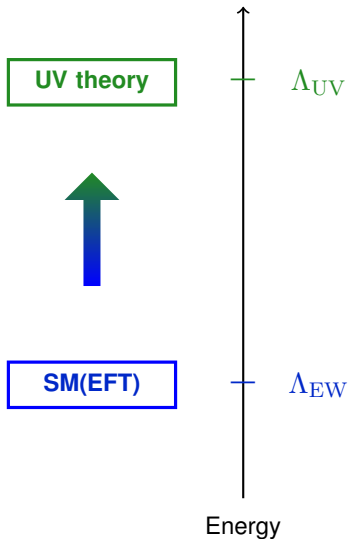
Hierarchy problem

dark matter/dark energy

flavour hierarchies

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gravity



The (two) flavour problems

1. **The SM flavour problem:** The measured Yukawa pattern doesn't seem accidental

⇒ Is there any deeper reason for that?

2. **The NP flavour problem:** If we regard the SM as an EFT valid below a certain energy cutoff Λ , why don't we see any deviations in flavour changing processes?

⇒ Which is the flavour structure of BSM physics?

The SM flavour problem

$$\mathcal{L}_{\text{Yukawa}} \supset Y_u^{ij} \bar{Q}_L^i H u_R^j$$

$$Y_u \sim y_t \begin{pmatrix} \text{light green circle} & \text{light green circle} & \text{dark green circle with } 0.003 \\ & \text{medium green circle} & \text{dark green circle with } 0.04 \\ & & 1 \end{pmatrix}$$

The SM flavour problem

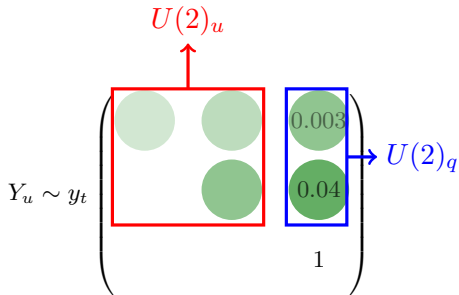
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Exact $U(2)^n$ limit

The SM flavour problem

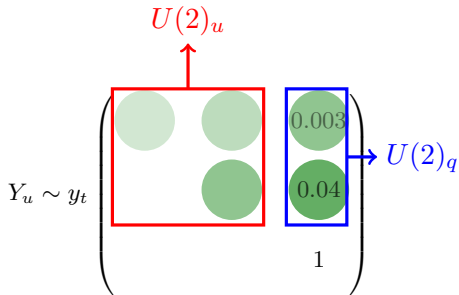
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An approximate $U(2)^n$ is acting
on the light families!

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An approximate $U(2)^n$ is acting
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The NP flavour problem

$$\mathcal{L} = \mathcal{L}_{\text{gauge}} + \mathcal{L}_{\text{Higgs}}$$

Large Flavour symmetry

Flavour degeneracy is broken

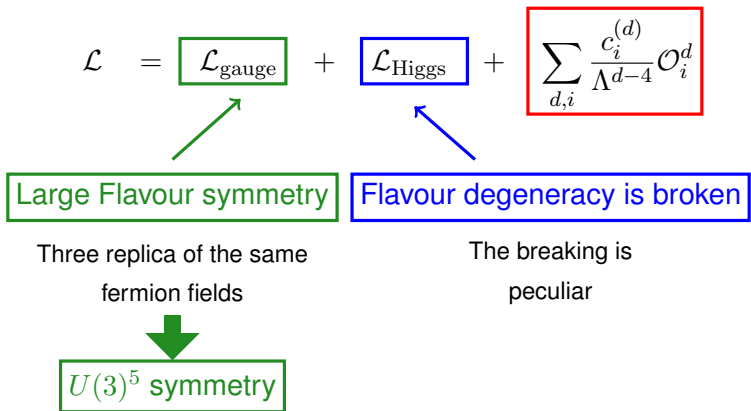
Three replica of the same
fermion fields

The breaking is
peculiar

$U(3)^5$ symmetry

- In the SM: accidental $U(3)^5 \rightarrow \text{approx } U(2)^n$

The NP flavour problem

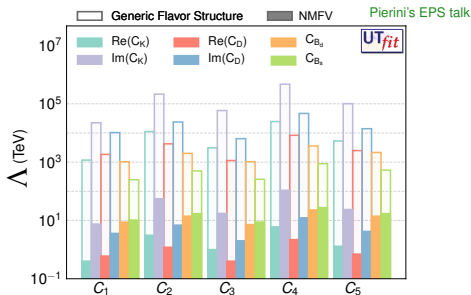
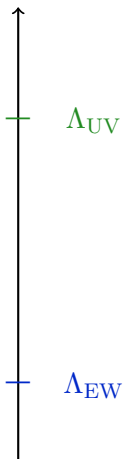


- In the SM: accidental $U(3)^5 \rightarrow$ approx $U(2)^n$
- **What happens when we switch on NP?**

The NP flavour problem

$$\mathcal{L} = \mathcal{L}_{\text{gauge}} + \mathcal{L}_{\text{Higgs}} + \sum_{d,i} \frac{c_i^{(d)}}{\Lambda^{d-4}} \mathcal{O}_i^d$$

- What is the energy scale of NP?
- Why haven't observed any violation of accidental symmetries yet?



no breaking of the $U(2)^n$ flavour symmetry at low energies

What's the problem for BSM?

B-physics

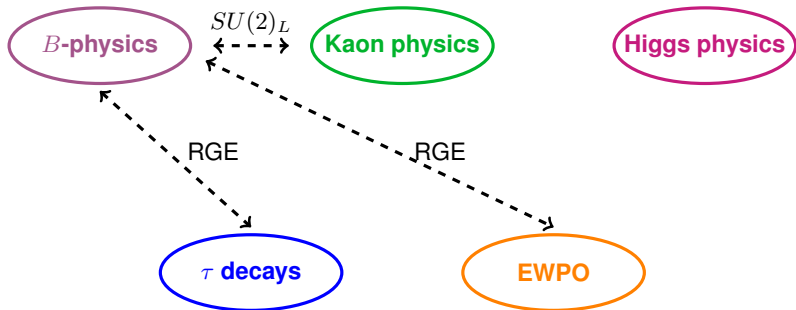
Kaon physics

Higgs physics

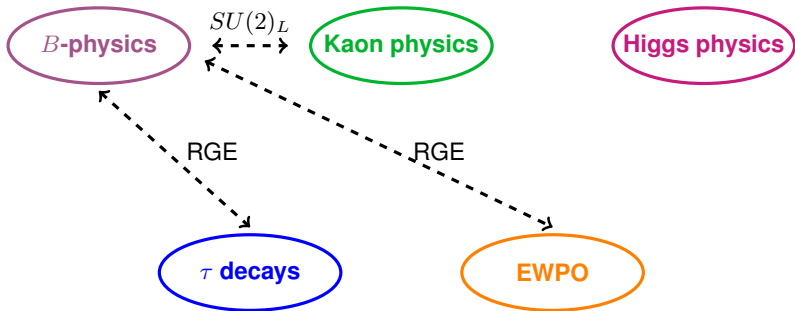
τ decays

EWPO

What's the problem for BSM?



What's the problem for BSM?



**How to satisfy all
the constraints
at the same time?**

Effective Field Theories for BSM

The EFT approach

- Since we haven't observed any clear sign of NP yet at low energies, we can work in an EFT context
 - ⇒ Agnostic of the nature of new physics, describe more than one UV model with the same operators
 - ⇒ Try to derive model-independent bounds
- We use the SMEFT
 - ⇒ Build all possible operators with SM fields and respecting SM symmetries
- The remnant of high-energy new physics is contained in the Wilson Coefficients
 - ⇒ With flavour, we have a lot of free degrees of freedom
 - ⇒ We need a criterium to infer their magnitude

The $U(2)^n$ symmetry for BSM

$$\begin{array}{ll} q_{3L} \sim (\mathbf{1}, \mathbf{1}) & \ell_{3L} \sim (\mathbf{1}, \mathbf{1}) \\ Q_L = (Q_L^1, Q_L^2) \sim (\bar{\mathbf{2}}, \mathbf{1}) & L_L = (\ell_L^1, \ell_L^2) \sim (\mathbf{1}, \bar{\mathbf{2}}) \end{array}$$

Unbroken $U(2)^5$

$$Y_u = y_t \begin{pmatrix} 0 & 0 \\ 0 & 1 \end{pmatrix}$$



$$\bar{q}_{3L} \Gamma q_{3L} \checkmark$$

$$\bar{q}_{3L} \Gamma Q \times$$

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Unbroken $U(2)^5$

$$Y_u = y_t \begin{pmatrix} 0 & 0 \\ 0 & 1 \end{pmatrix}$$



$$\bar{q}_{3L} \Gamma q_{3L} \checkmark$$

$$\bar{q}_{3L} \Gamma Q \times$$

Soft symmetry breaking

$$Y_u = y_t \begin{pmatrix} \Delta & V_q \\ 0 & 1 \end{pmatrix}$$



$$\bar{q}_{3L} \Gamma q_{3L} \checkmark$$

$$\bar{q}_{3L} \Gamma (V_q Q) \checkmark$$

Which operators?

$$\mathcal{L}_{\text{eff}} = -\frac{1}{\Lambda^2}(\bar{q}_{3L}\gamma_\mu\sigma^a q_{3L})(\bar{\ell}_{3L}\gamma^\mu\sigma^a \ell_{3L}) - \frac{c_{13}}{\Lambda^2}(\bar{q}_{3L}\gamma_\mu q_{3L})(\bar{\ell}_{3L}\gamma^\mu \ell_{3L})$$

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\uparrow
SU(2) triplet
 \uparrow
SU(2) singlet

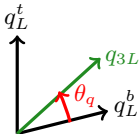
- Left-handed fields only

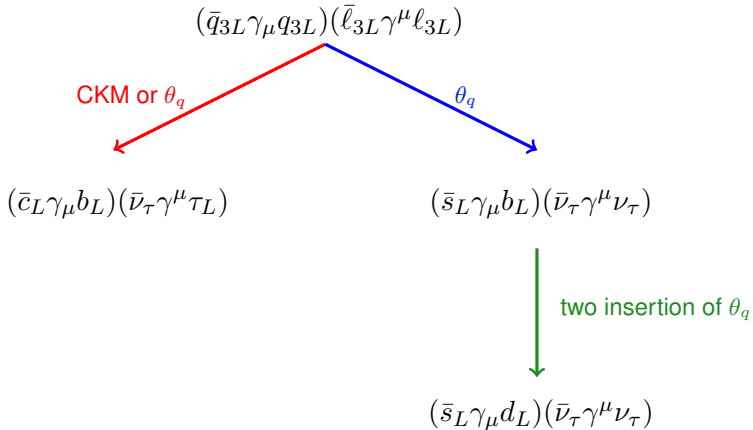
⇒ Only ones contributing to di-neutrino modes without considering right-handed ν

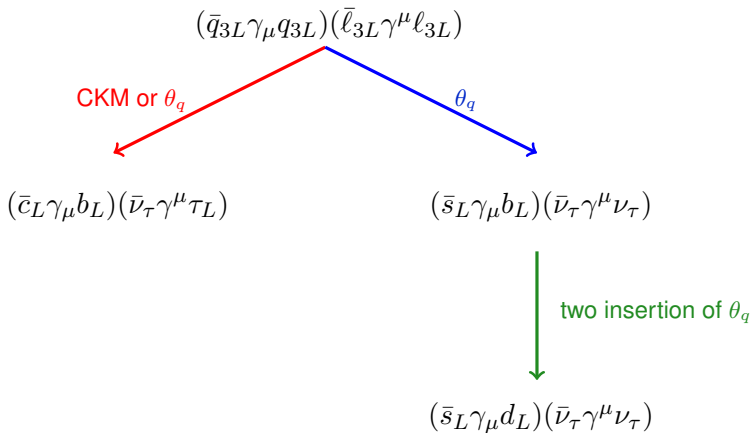
- $q_{3L} \equiv q_L^b + \theta_q e^{i\phi_q} \hat{V}_q^\dagger \cdot Q_L$

$$q_L^b = \begin{pmatrix} V_{j3}^* u_L^j \\ b_L \end{pmatrix} \quad Q_L^i = \begin{pmatrix} V_{ji}^* u_L^j \\ d_L^i \end{pmatrix} \quad \hat{V}_q \equiv (V_{td}^*, V_{ts}^*)$$

⇒ θ_q and ϕ_q are small mixing angles

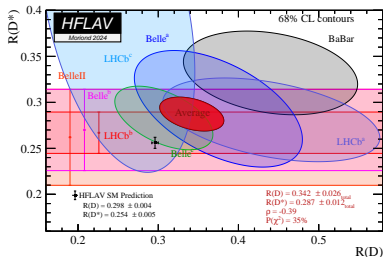






**Correlations among all these modes
is essential to prove NP scenarios**

Observables: $R_{D^{(*)}}$



$$R_{D^{(*)}} = \frac{\mathcal{B}(B \rightarrow D^{(*)} \tau \bar{\nu})}{\mathcal{B}(B \rightarrow D^{(*)} \ell \bar{\nu})}$$

- Test of Lepton Flavour Universality between the 3rd and light lepton families
- Ratios allow cancelling hadronic uncertainties and experimental uncertainties

$$\Delta R_{D^{(*)}} = \left[\frac{R_{D^{(*)}}}{R_{D^{(*)}}^{\text{SM}}} - 1 \right] \approx 2R_0(1 - \theta_q \cos \phi_q) \quad R_0 = \frac{1}{\Lambda^2} \frac{1}{\sqrt{2}G_F}$$

Observables: $B^+ \rightarrow K^+ \nu \bar{\nu}$

[2311.14647]

Hadronic Tagging

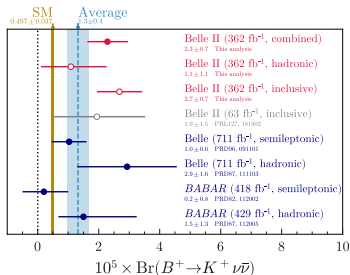
$$\mathcal{B}(B^+ \rightarrow K^+ \nu \bar{\nu}) = (1.1^{+0.9+0.8}_{-0.8-0.5}) \times 10^{-5}$$

Inclusive Tagging

$$\mathcal{B}(B^+ \rightarrow K^+ \nu \bar{\nu}) = (2.7 \pm 0.5 \pm 0.5) \times 10^{-5}$$

Combined

$$\mathcal{B}(B^+ \rightarrow K^+ \nu \bar{\nu}) = (2.7 \pm 0.5^{+0.5}_{-0.4}) \times 10^{-5}$$



3.5 σ evidence wrt background only

2.7 σ tension wrt SM

Observables: $B^+ \rightarrow K^+ \nu \bar{\nu}$

- From the theory point of view, the $B^+ \rightarrow K^+ \nu \bar{\nu}$ mode is very clean
 - No charm pollution
 - Pollution from $B \rightarrow \tau(\rightarrow K\nu)\bar{\nu}$, but removable experimentally
 - Very precise, already hitting the wall with precision

$$\frac{\mathcal{B}(B \rightarrow K^{(*)} \nu \bar{\nu})}{\mathcal{B}(B \rightarrow K^{(*)} \nu \bar{\nu})_{\text{SM}}} = \left[\frac{2}{3} + \frac{1}{3} \left| 1 - \frac{\pi s_w^2 \Delta R_{D^{(*)}}}{2\alpha X_t (1 - \theta_q \cos \phi_q)} \theta_q e^{i\phi_q} (1 - c_{13}) \right|^2 \right]$$

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Direct connection with $b \rightarrow c \tau \bar{\nu}$

distinguishes among UV models

Kaon decays

$$\frac{\mathcal{B}(K^+ \rightarrow \pi^+ \nu \bar{\nu})}{\mathcal{B}(K^+ \rightarrow \pi^+ \nu \bar{\nu})_{\text{SM}}} = \frac{2}{3} + \left| \frac{1}{3} + \frac{\Delta R_{D^{(*)}} \theta_q^2 (1 - c_{13})}{2(\alpha/\pi) C_{sd,\tau}^{\text{SM,eff}} (1 - \theta_q \cos \phi_q)} \right|^2$$

$$\frac{\mathcal{B}(K_L \rightarrow \pi^0 \nu \bar{\nu})}{\mathcal{B}(K_L \rightarrow \pi^0 \nu \bar{\nu})_{\text{SM}}} = \frac{2}{3} + \left| \frac{1}{3} - \frac{\Delta R_{D^{(*)}} \theta_q^2 (1 - c_{13})}{2(\alpha/\pi) (X_t/s_w^2) (1 - \theta_q \cos \phi_q)} \right|^2$$

- Same proportionality to $\Delta R_{D^{(*)}}$ as in $B \rightarrow K \nu \bar{\nu}$
- Same CKM structure as in the SM
- We have a large interference also for the $K_L \rightarrow \pi^0 \nu \bar{\nu}$ decay

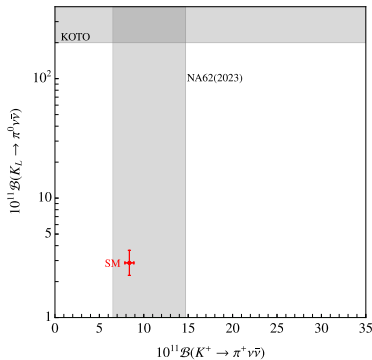
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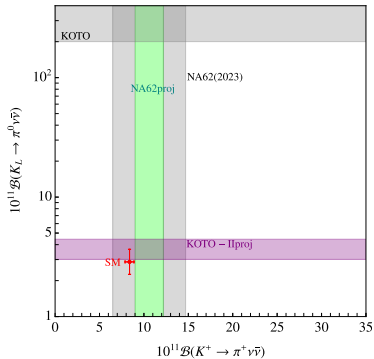
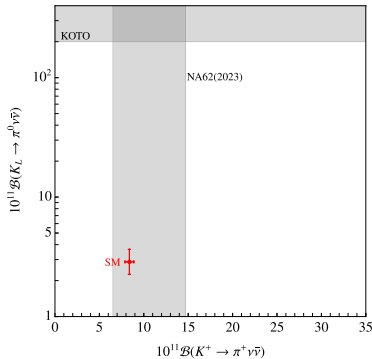
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The BSM reach of Kaon decays



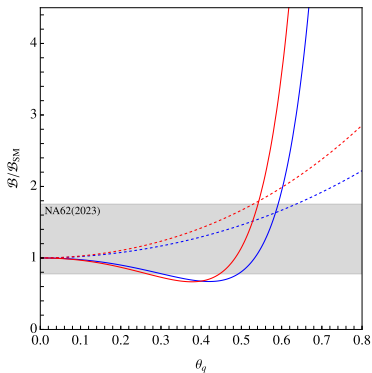
- Currently, the NA62 limits are not enough to ping down a specific parametric window
- KOTO-II sensitivity at 25% of the measured branching fraction
 - Hypothesis: $\mathcal{B}(K_L \rightarrow \pi^0 \nu \bar{\nu})_{\text{exp}} = 1.3 \mathcal{B}(K_L \rightarrow \pi^0 \nu \bar{\nu})_{\text{SM}}$
- NA62 projection at 15% with current \mathcal{B} measured central value

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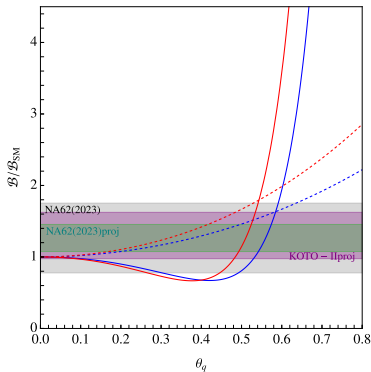
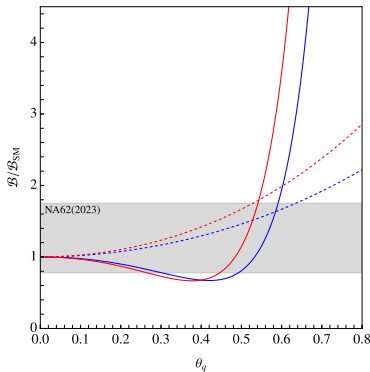
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The BSM reach of Kaon decays



- Blue lines: $K^+ \rightarrow \pi^+ \nu \bar{\nu}$, red lines: $K_L \rightarrow \pi^0 \nu \bar{\nu}$
- $\Delta R_{D^{(*)}}$ fixed to its central value
- filled: $c_{13} = 0$ $\phi_q = 0$, dashed $c_{13} = 2$ $\phi_q = \pi$
- “Model” allows for large modifications, NA62 and KOTO-II updates are **essential** to constrain the parameter space

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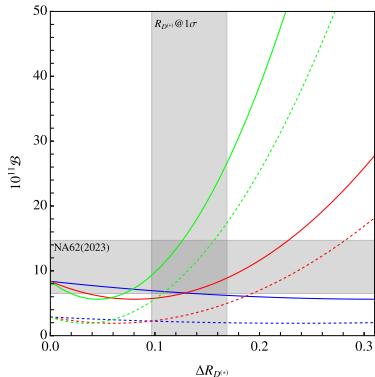


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Correlation with B -physics

If In this setup, the relative shift to fit R_D and R_{D^*} is the same

$$\Delta R_{D^{(*)}} = \left[\frac{R_{D^{(*)}}}{R_{D^{(*)}}^{\text{SM}}} - 1 \right] = 0.133 \pm 0.036$$

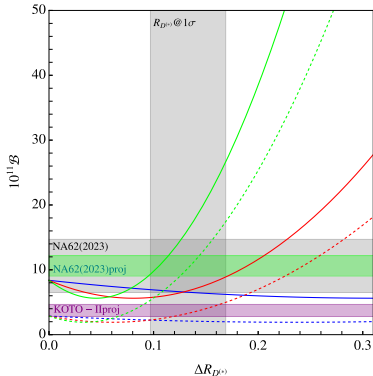


- Filled lines: $K^+ \rightarrow \pi^+ \nu \bar{\nu}$, Dashed lines: $K_L \rightarrow \pi^0 \nu \bar{\nu}$
- In all scenarios $c_{13} = 0$ $\phi_q = 0$
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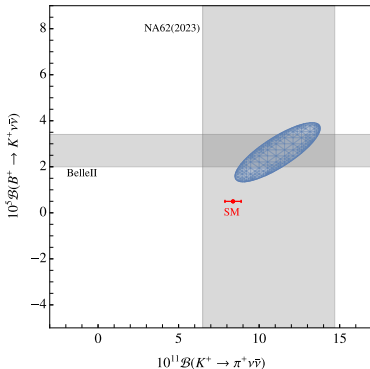
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KOTO-II is essential to select the parameter space

Fit to di-neutrino modes

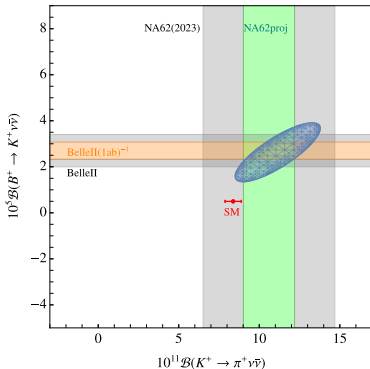
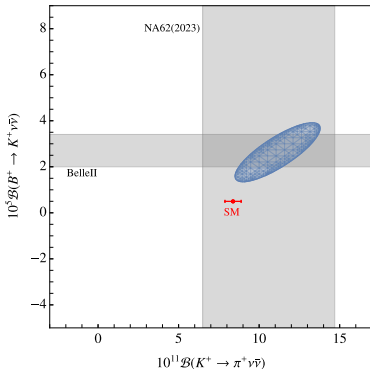


- Fit assuming the current central value for $\Delta R_{D^{(*)}}$ and $c_{13} = 0.5$
⇒ Excellent fit quality
- We predict

$$\mathcal{B}(K_L \rightarrow \pi^0 \nu \bar{\nu}) = (6.7 \pm 1.8) \times 10^{-11}$$

testable at 2σ at KOTO-II

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Explicit BSM examples

Which NP particle?

1) Colourless Mediators

- $W' + Z'$: tension with high- p_T searches with $\tau_L \tau_L$ or $b_L b_L$ final states

[Greljo, Isidori, Marzocca, '15]

- Solutions with right-handed neutrino are motivated and help to ease the tension with $b \rightarrow c \tau \nu$ data but they are most likely to be excluded from high- p_T

[Greljo, Camalich, Ruiz-Álvarez, '18]

2) Leptoquark Mediators

Model	$R_{K^{(*)}}$	$R_{D^{(*)}}$	$R_{K^{(*)}}$ & $R_{D^{(*)}}$
S_1	\times^*	\checkmark	\times^*
R_2	\times^*	\checkmark	\times
\widetilde{R}_2	\times	\times	\times
S_3	\checkmark	\times	\times
U_1	\checkmark	\checkmark	\checkmark
U_3	\checkmark	\times	\times

$$S_1 \sim (\overline{\mathbf{3}}, 1, 1/3)$$

$$S_3 \sim (\overline{\mathbf{3}}, 3, 1/3)$$

$$U_1 \sim (\mathbf{3}, 1, 2/3)$$

[Angelescu, Bečirević, Faroughy, Sumensari, '18]

Flavour Non-Universal New Physics

Dvali, Shifman, '00

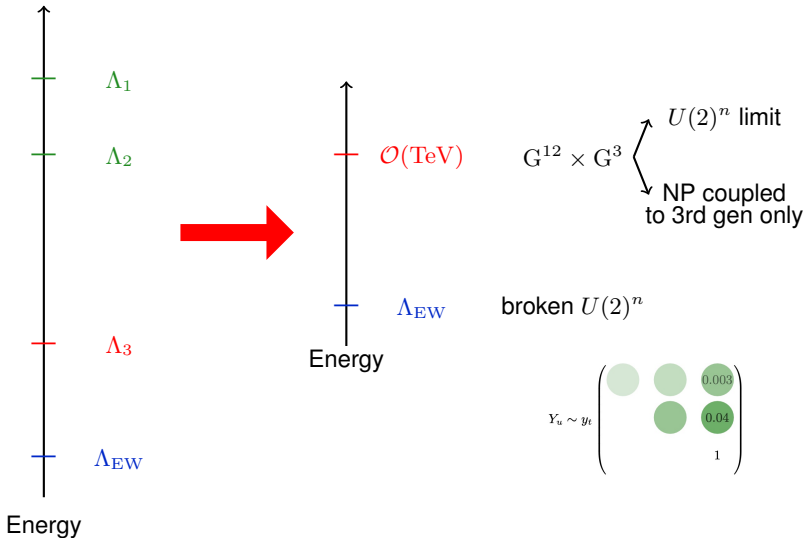
Panico, Pomarol, '16

MB, Cornella, Fuentes-Martin, Isidori '17

Allwicher, Isidori, Thomsen '20

Barbieri, Cornella, Isidori, '21

Davighi, Isidori '21



The Pati-Salam Leptoquark

$$G_i = \text{SU}(4)^i \times \text{SU}(2)_L^i \times \text{SU}(2)_R^i$$

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$$G_{12} \times G_3 \Rightarrow \text{SM} + U_1 + Z'$$

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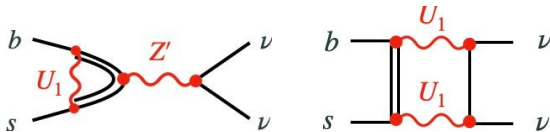
$$G_{12} \times G_3 \Rightarrow \text{SM} + U_1 + Z'$$

Large couplings to third generation

+other (heavy) states that depend on the details of the model in the UV

Phenomenology

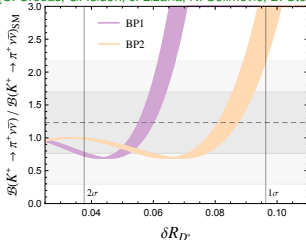
- The Z' mediates neutral meson mixing at tree-level
 \Rightarrow Suppressed parametrically
- The U_1 LQ has tree level matching $c_{13} = 1$, no tree-level contribution to $s \rightarrow d\nu\bar{\nu}$
- However, there are loop contributions



$$\Delta C_\tau \approx V_{us}^* V_{ud}$$

- The loop doesn't preserve the $U(2)$ CKM structure
- The contribution to $K_L \rightarrow \pi\nu\bar{\nu}$ is negligible

[O. Crosas, G. Isidori, J. Lizana, N. Selimović, B. Stefaneke, '22]

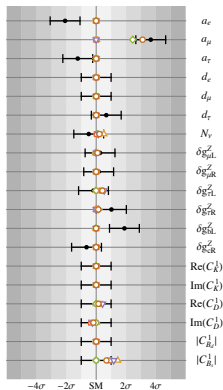
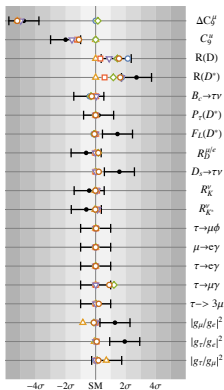


The scalar leptoquarks $S_1 + S_3$

- Scalar leptoquarks don't require a UV completion
- They both contribute at tree-level to $s \rightarrow d\nu\bar{\nu}$ transitions such as

$$c_{13}|_{S_1} = \frac{1}{2} \quad c_{13}|_{S_3} = \frac{1}{2}$$

- Sweet spot to connect to $B^+ \rightarrow K^+ \nu\bar{\nu}$



[V. Gherardi, D. Marzocca, E. Venturini, '20]

Conclusions

- Flavour physics has exciting prospects in the search for New Physics
- Understanding the origin of the Flavour Puzzle might hint at what structure new physics couplings have
- Correlations among different observables are crucial to studying the viability of classes of models
 - ⇒ Di-neutrino modes are one of the golden modes where to look for new physics signals
 - ⇒ The complementarity between measurements $B^+ \rightarrow K^+ \nu \bar{\nu}$, $K^+ \rightarrow \pi^+ \nu \bar{\nu}$ and $K_L \rightarrow \pi^0 \nu \bar{\nu}$ are essential to ping down specific scenarios

Appendix

Flavour Non-Universal New Physics

Dvali, Shifman, '00

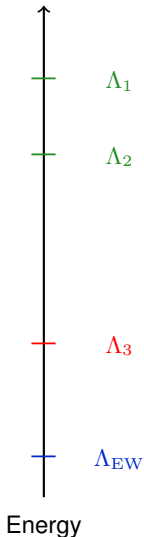
Panico, Pomarol, '16

MB, Cornella, Fuentes-Martin, Isidori '17

Allwicher, Isidori, Thomsen '20

Barbieri, Cornella, Isidori, '21

Davighi, Isidori '21



Basic idea:

- 1st and 2nd have small masses and small couplings to NP because they are generated by dynamics at a heavier scale
- 3rd generation is linked to dynamics at lower scales and has stronger couplings

Flavour deconstruction:

fermion families interact with different gauge groups and flavour hierarchies emerge as accidental symmetries