

# Axion-Like Particle Search in Birefringent Cavity



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**Keywords Related to Research**

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Condensed matter physics, Quantum Information

**Keywords Related to Research**

Semiconductor qubit, Quantum network, Non-equilibrium  
statistical physics

[Website](#)

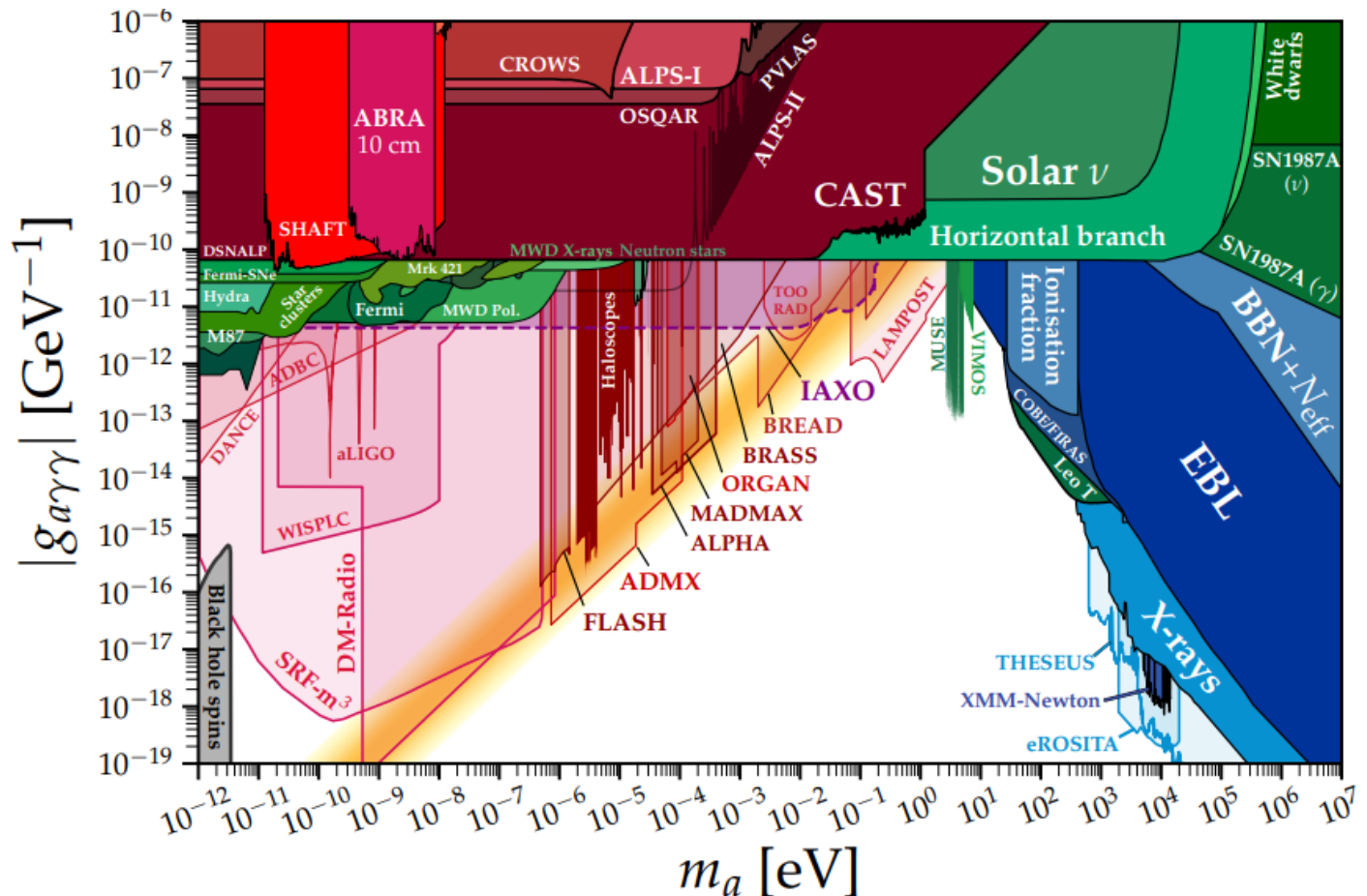


# Axion-like particle (ALP) search

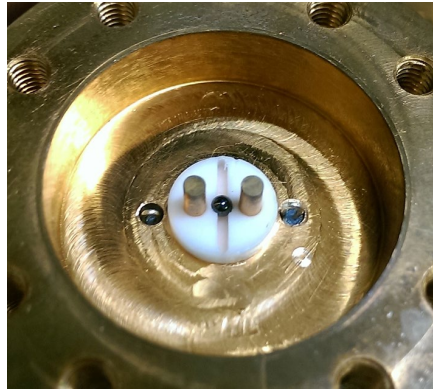
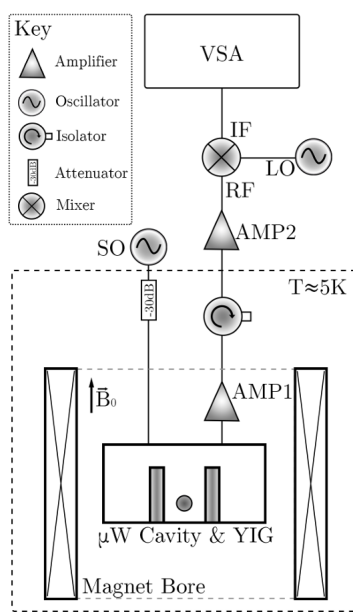
ALP is one of the candidates of the cold dark matter.

ALP is assumed to be the same interaction to the axion.

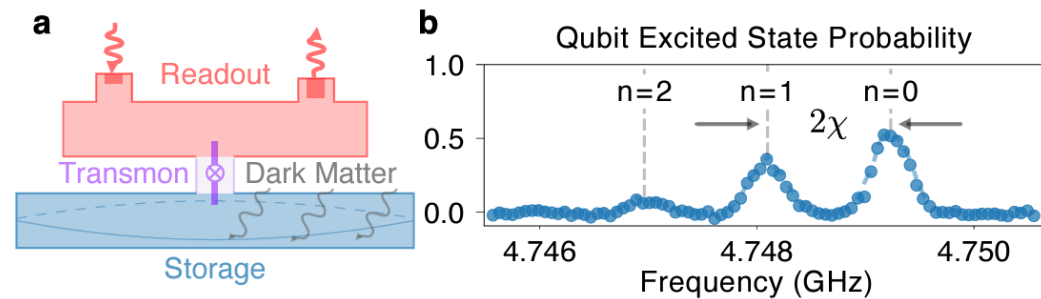
Quantum sensing technique is one the candidates of the detection.



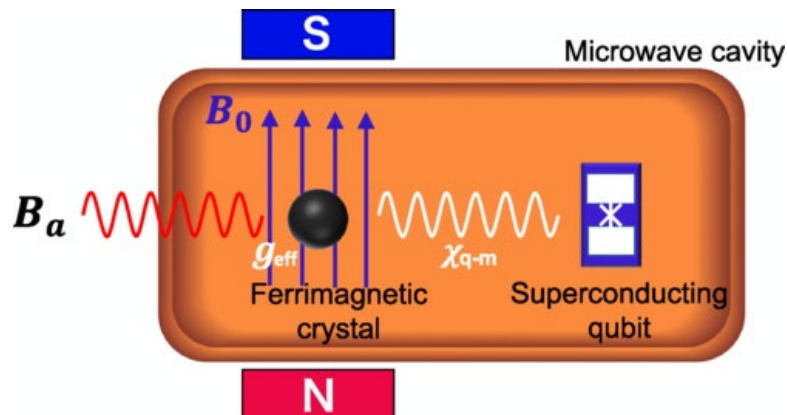
# ALP search w/ quantum sensors (microwave region)



Flower+ Physics of the Dark Universe 2019 (Michael E. Tobar G)

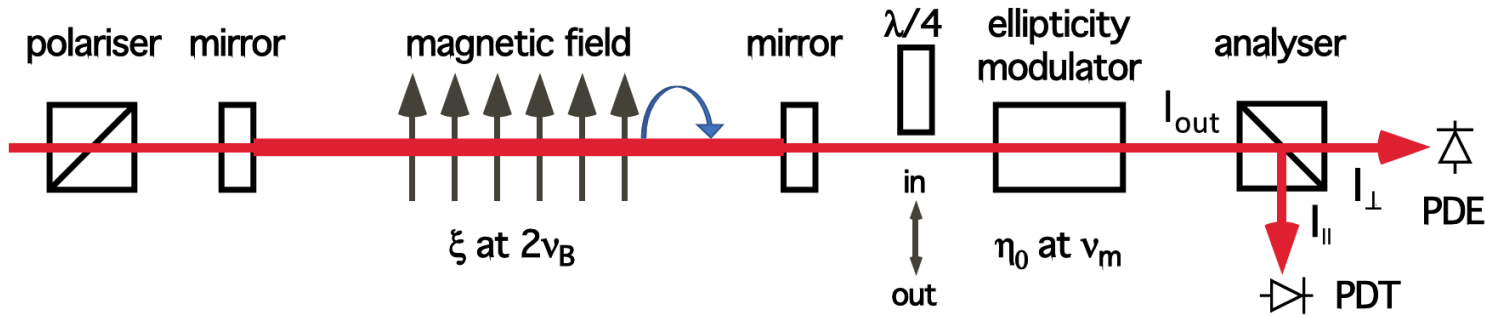


Dixit+ PRL 2021 (Chicago)



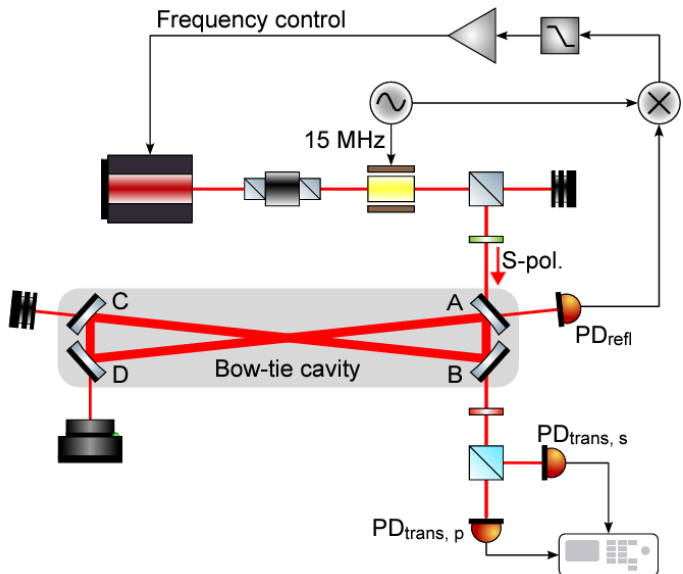
Ikeda, YS+ PRD 2022

# ALP search w/ polarized light

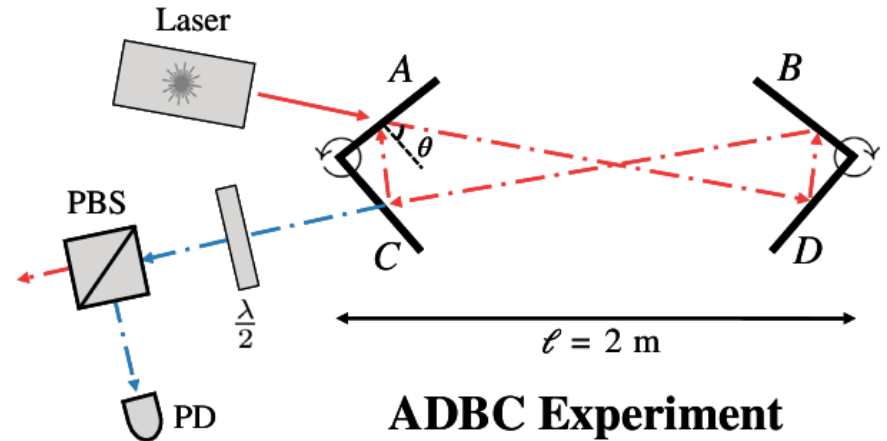


PVLAS experiment @ Ferrara, Italy

## DANCE Experiment



Oshima+ PRD 2023

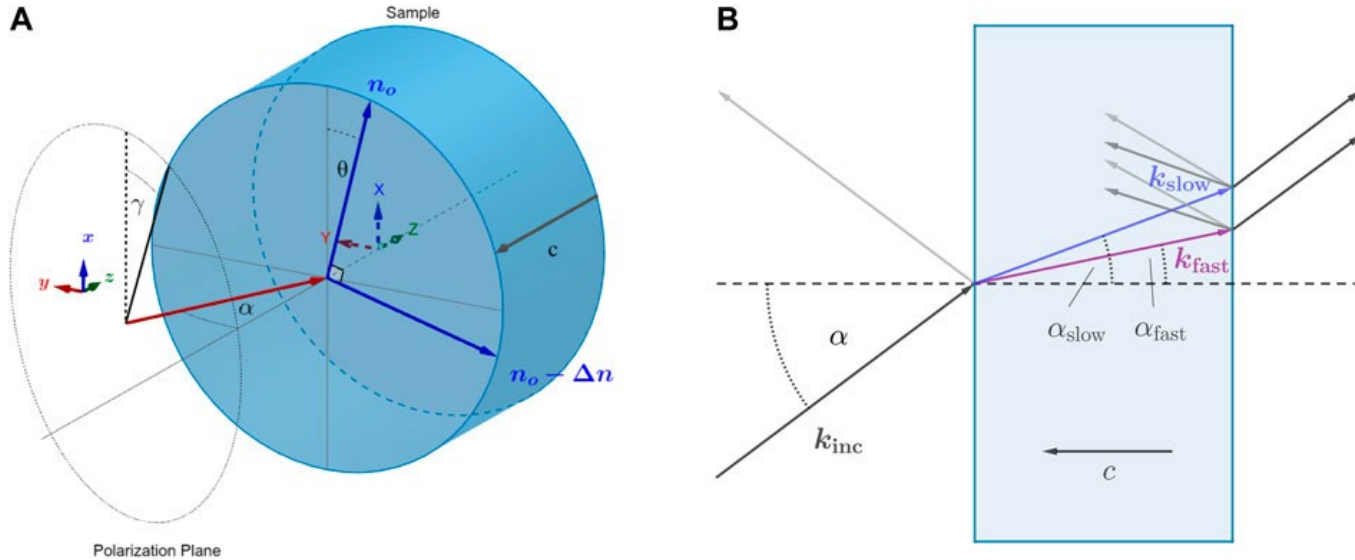


ADBC Experiment

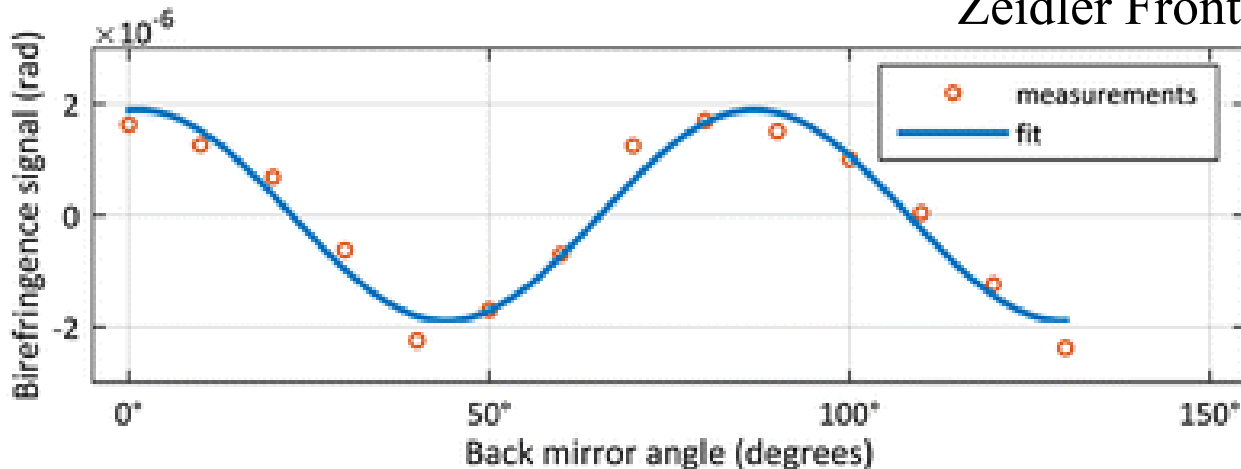
Liu+ PRD 2019

# Problem on polarization

## (Alignment mismatched) Mirror-induced birefringence

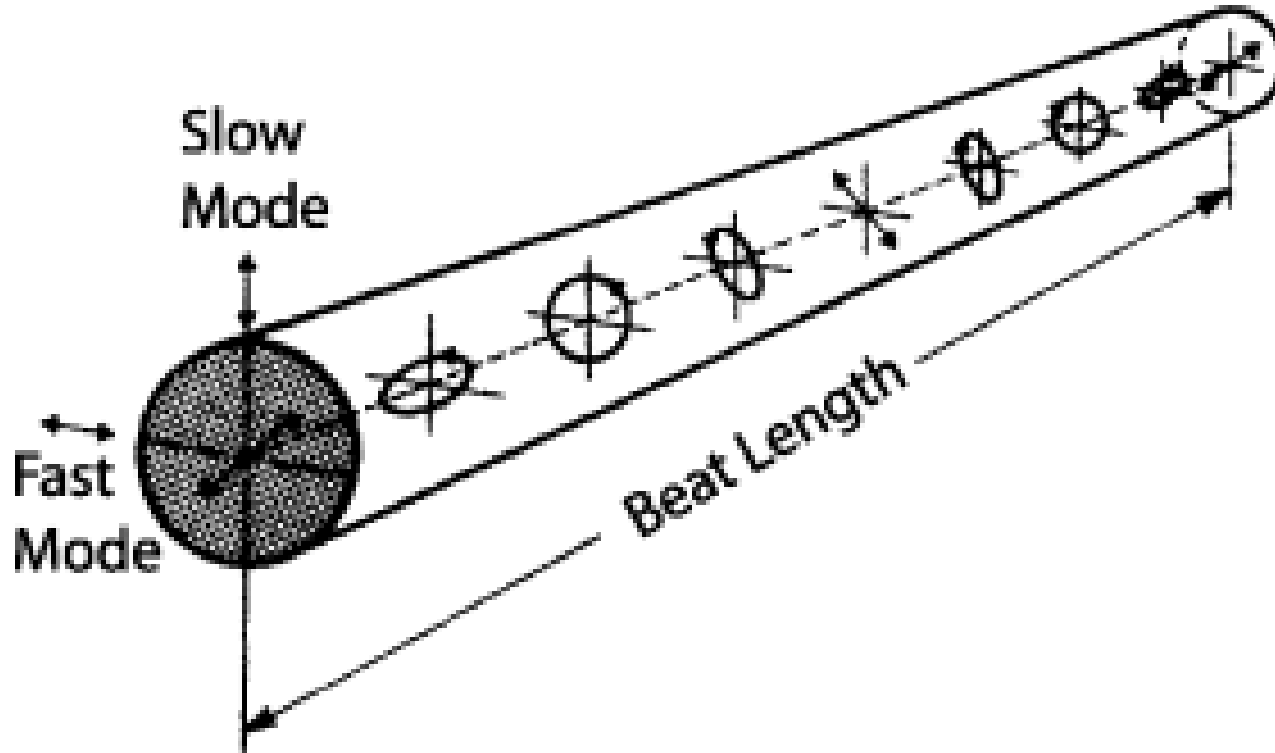


Zeidler Front. Astron. Space Sci. 2022



Westberg+ APB 2017

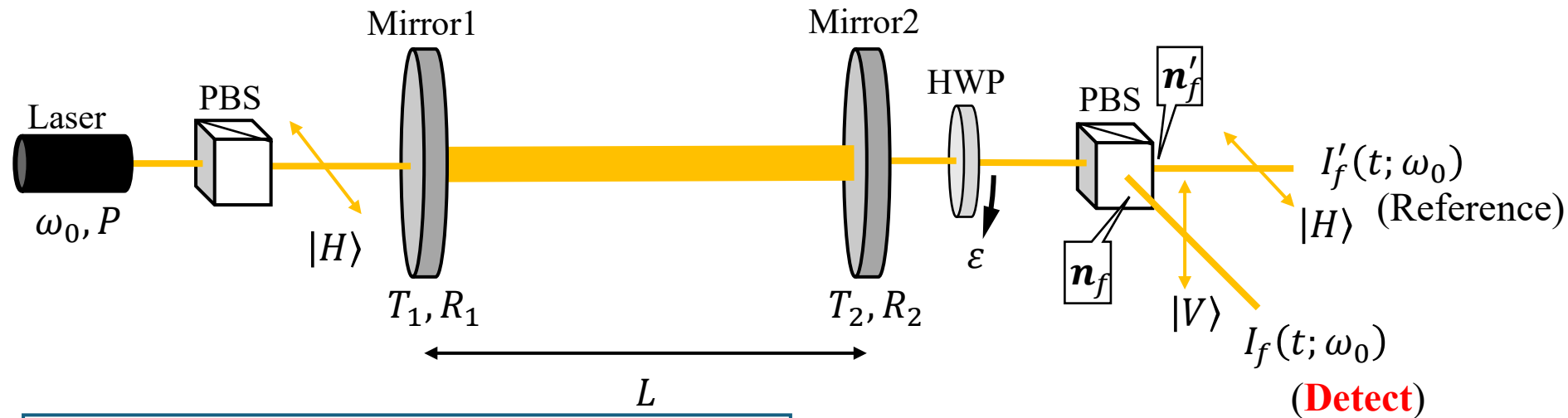
# Birefringence through material



Fast mode / axis: relatively low refractive index  
Slow mode / axis: relatively high refractive index

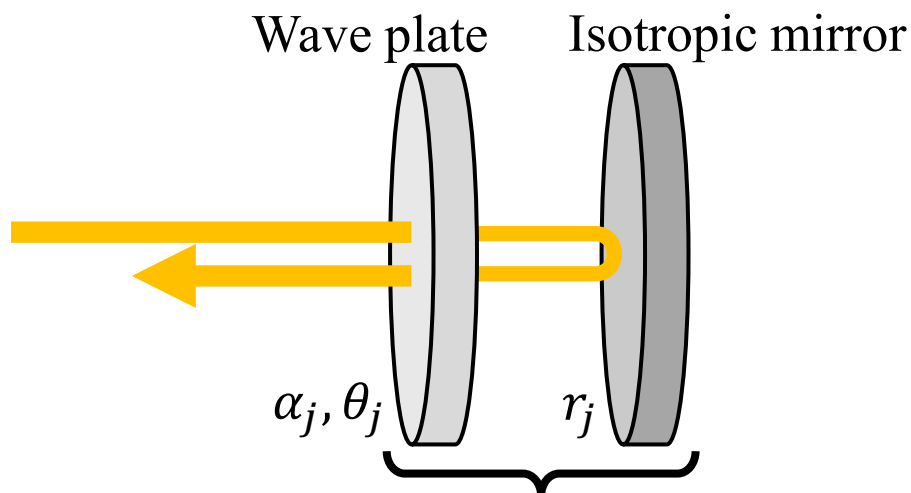
The polarization is slightly changed due to the material transmitting.

# Fabry-Perot type cavity w/ Birefringence

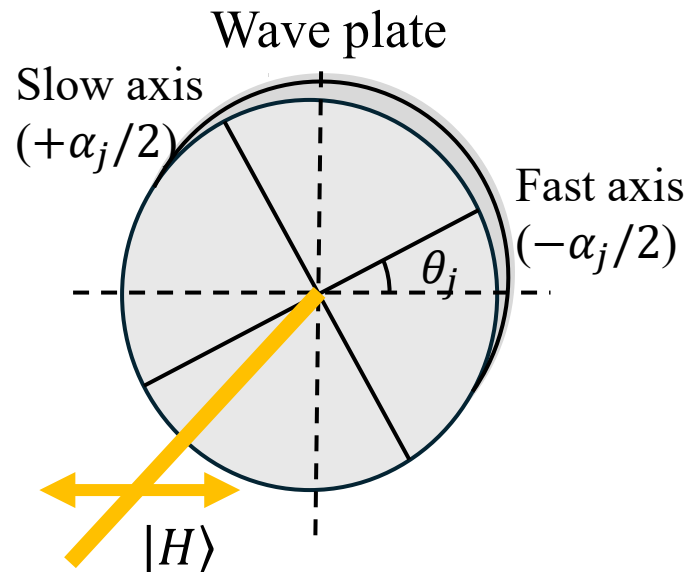


Description of birefringent mirror

Brandi+ APB 1997

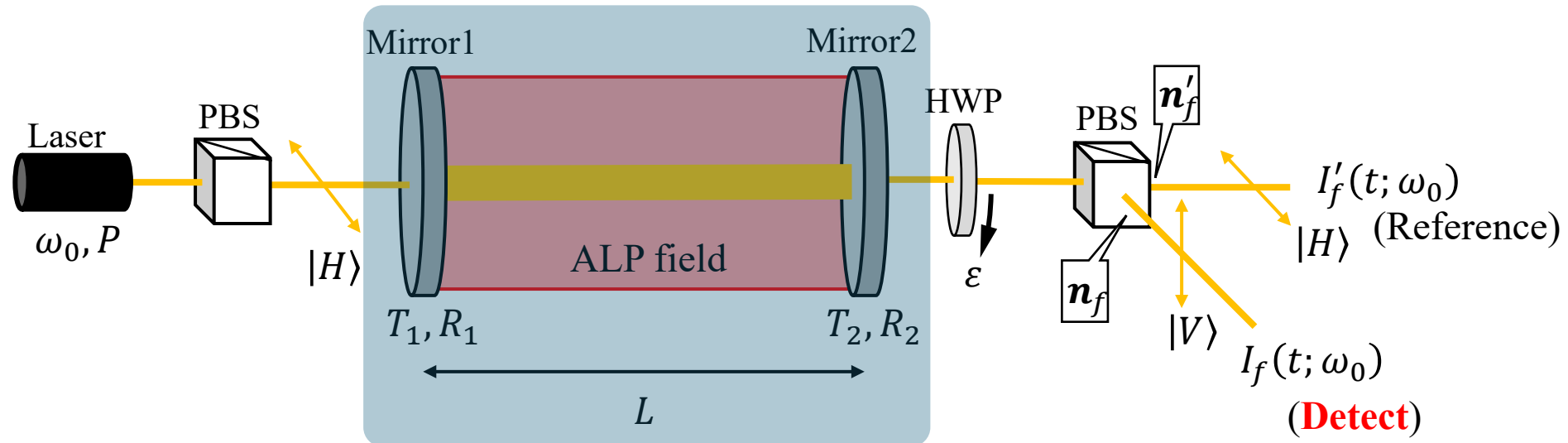


Anisotropic (birefringent) mirror

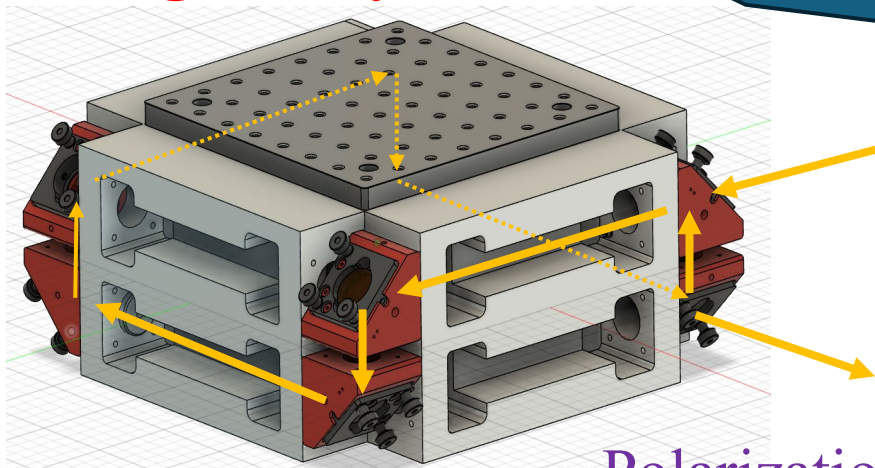




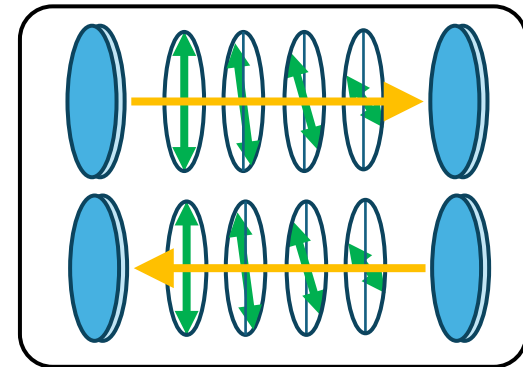
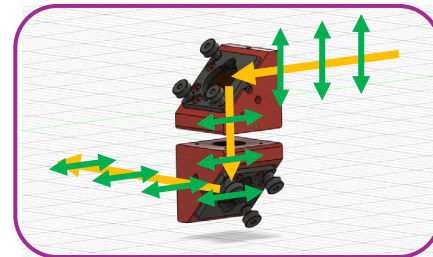
# Our proposed setup



## Ring cavity



In FB-type cavity, the polarized effect due to ALP field is cancelled.



Polarization-dependent path cavity

# Signal-to-Noise Ratio (SNR)

$$\text{SNR} = \frac{\sqrt{2}}{\left| C_f^{(0)} \right|} \left| C_f^{(0)*} C_f^{(+)} + C_f^{(0)} C_f^{(-)*} \right| \sqrt{\frac{P T_{\text{obs}}}{\hbar \omega_0}}$$

$$C_f^{(0)} = e^{i\omega_0 L} e^{-i\theta \mathbf{n} \cdot \boldsymbol{\sigma}} \times \begin{pmatrix} \frac{1}{1-r_1 r_2 e^{2i\omega_0 L} e^{-i\alpha}} & 0 \\ 0 & \frac{1}{1-r_1 r_2 e^{2i\omega_0 L} e^{i\alpha}} \end{pmatrix} \times e^{i\theta \mathbf{n} \cdot \boldsymbol{\sigma}} T_1 \begin{pmatrix} 1 \\ 0 \end{pmatrix}.$$

$$C_f^{(\pm)} = \frac{1}{2} g e^{i\omega_0 L} (1 - e^{\pm i m_a L}) \times \left\{ \frac{\mathbf{u}_F^{(\pm)}}{1 - r_1 r_2 e^{2i(\omega_0 \pm m_a) L} e^{-i\alpha}} + \frac{\mathbf{u}_S^{(\pm)}}{1 - r_1 r_2 e^{2i(\omega_0 \pm m_a) L} e^{i\alpha}} + \frac{\mathbf{v}_F^{(\pm)}}{1 - r_1 r_2 e^{2i\omega_0 L} e^{-i\alpha}} + \frac{\mathbf{v}_S^{(\pm)}}{1 - r_1 r_2 e^{2i\omega_0 L} e^{i\alpha}} \right\}$$

$$\mathbf{u}_F^{(\pm)} := \mathbf{b}_F + \frac{i\Xi_{\pm} - \Sigma_{\pm}}{1 - e^{\pm 2im_a L}} \mathbf{a}_F - \frac{\Sigma_{\pm}}{1 - e^{\pm 2im_a L} e^{-2i\alpha}} \mathbf{a}_S,$$

$$\mathbf{u}_S^{(\pm)} := \mathbf{b}_S + \frac{i\Xi_{\pm} + \Sigma_{\pm}}{1 - e^{\pm 2im_a L}} \mathbf{a}_S + \frac{\Sigma_{\pm}}{1 - e^{\pm 2im_a L} e^{2i\alpha}} \mathbf{a}_F,$$

$$\mathbf{v}_F^{(\pm)} := \frac{-1}{1 - e^{\pm 2im_a L}} \left[ i\Xi_{\pm} + \frac{e^{2im_a L} (e^{2i\alpha} - 1)}{1 - e^{\pm 2im_a L} e^{2i\alpha}} \Sigma_{\pm} \right] \mathbf{a}_F,$$

$$\mathbf{v}_S^{(\pm)} := \frac{-1}{1 - e^{\pm 2im_a L}} \left[ i\Xi_{\pm} - \frac{e^{2im_a L} (e^{-2i\alpha} - 1)}{1 - e^{\pm 2im_a L} e^{-2i\alpha}} \Sigma_{\pm} \right] \mathbf{a}_S$$

$$\Xi_{\pm} := \sigma_y + e^{\pm im_a L} R_1 \sigma_y R_1^{-1},$$

$$\Sigma_{\pm} := \frac{1}{2} \left[ \left( \frac{\partial}{\partial \alpha} \Gamma \right)_{\alpha=0}, \Xi_{\pm} \right],$$

$$\mathbf{a}_{F/S} := e^{-i\theta \mathbf{n} \cdot \boldsymbol{\sigma}} \frac{1 \pm \sigma_z}{2} e^{i\theta \mathbf{n} \cdot \boldsymbol{\sigma}} T_1 \begin{pmatrix} 1 \\ 0 \end{pmatrix},$$

$$\mathbf{b}_{F/S} := e^{-i\theta \mathbf{n} \cdot \boldsymbol{\sigma}} \frac{1 \pm \sigma_z}{2} e^{i\theta \mathbf{n} \cdot \boldsymbol{\sigma}} (-i\sigma_y) T_1 \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

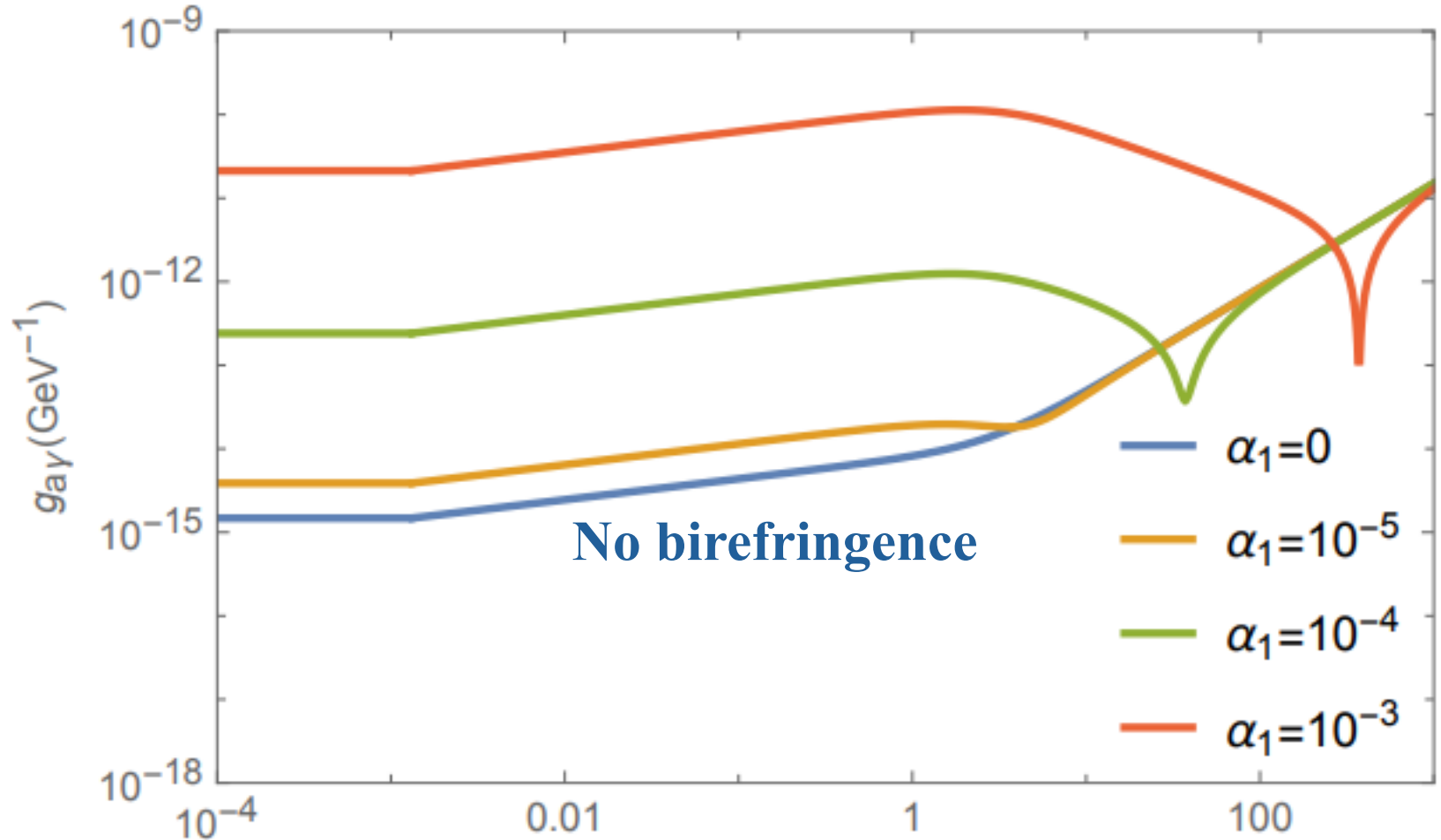
$$T_{\text{obs}} = \begin{cases} T_{\text{obs}} & (T_{\text{obs}} \lesssim \tau) \\ (T_{\text{obs}} \tau)^{1/2} & (T_{\text{obs}} \gtrsim \tau) \end{cases} \quad \text{Axion coherence time} \quad \tau = 10^6 \frac{2\pi}{m_a}$$

Common parameters

$$L = 10.64 \text{ m}, \lambda = 1064 \text{ nm},$$

$$P = 100 \text{ W}, T_{\text{obs}} = 1 \text{ yr}$$

# Sensitivity in birefringent cavity (In the case of the perfect alignment)

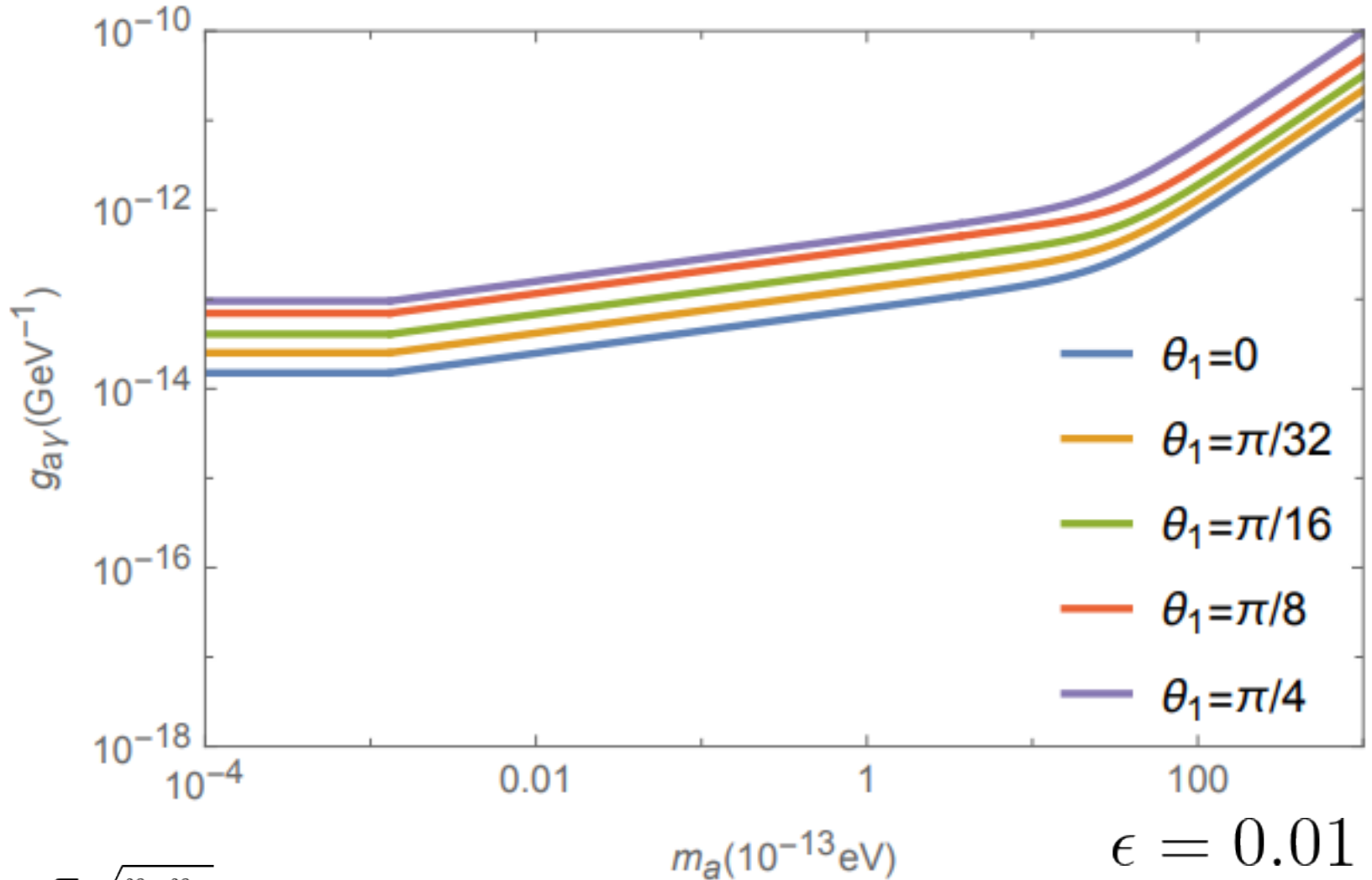


$$\mathcal{F} = \frac{\pi\sqrt{r_1 r_2}}{1 - r_1 r_2} = 10^5 \quad \epsilon = 0.01 \quad m_a(10^{-13}\text{eV}) \quad \alpha_1 = \alpha_2$$

The resonance effect to detect the ALP with polarized light is observed.

# Sensitivity with birefringence

(In the case of the imperfect alignment)

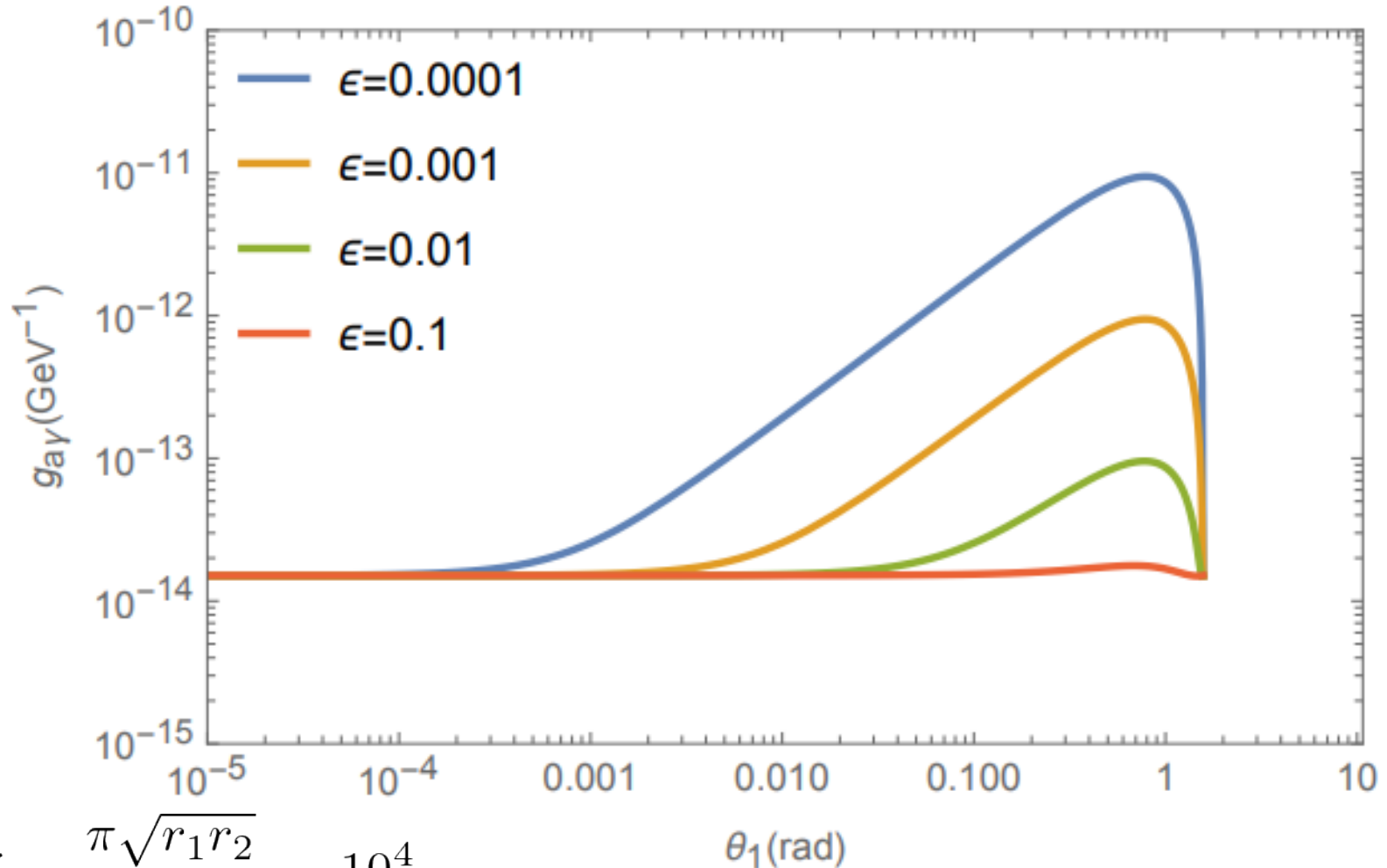


$$\mathcal{F} = \frac{\pi \sqrt{r_1 r_2}}{1 - r_1 r_2} = 10^4$$

$$\alpha_1 = \alpha_2 = 10^{-5}$$

# Sensitivity with birefringence

## Post-selection angle dependence



$$\mathcal{F} = \frac{\pi \sqrt{r_1 r_2}}{1 - r_1 r_2} = 10^4$$

$$m_a = 10^{-16} \text{ eV}$$

$$\alpha_1 = \alpha_2 = 10^{-5} \quad \theta_1 = \theta_2$$

# Conclusion

T. Kuramoto et al., in preparation.

1. Axion-like particle detection with polarized light plus ring cavity was proposed.
2. We study the birefringence effect in this situation.
  - Post-selection angle tuning will cover the sensitivity against to the birefringence.



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