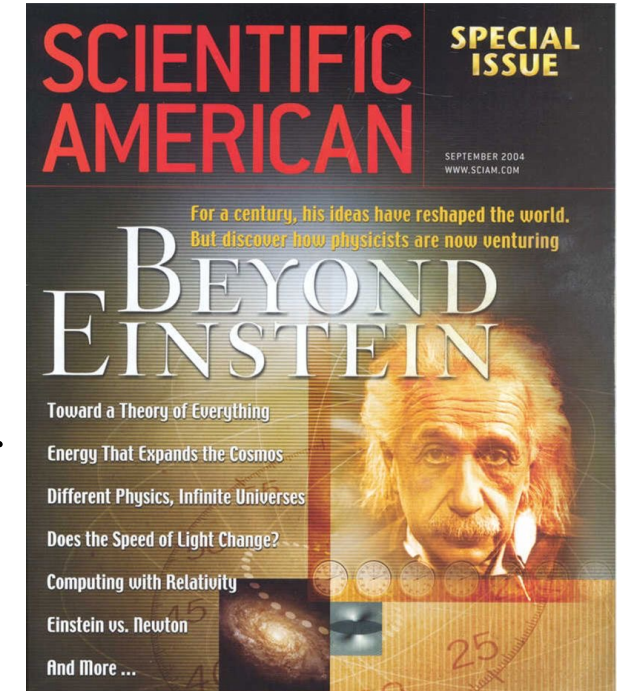


Tests of Spacetime Symmetry with Neutrinos

outline

1. Introduction
2. Tests of Lorentz violation with neutrinos
3. Tests of Lorentz violation with astrophysical neutrinos
4. Searches of ultralight dark matter with astrophysical neutrino flavor
5. Conclusion



Teppei Katori  @teppeikatori
King's College London

Q-EYES 2025, KEK, Japan, Dec. 10, 2025

Introduction

Lorentz violation

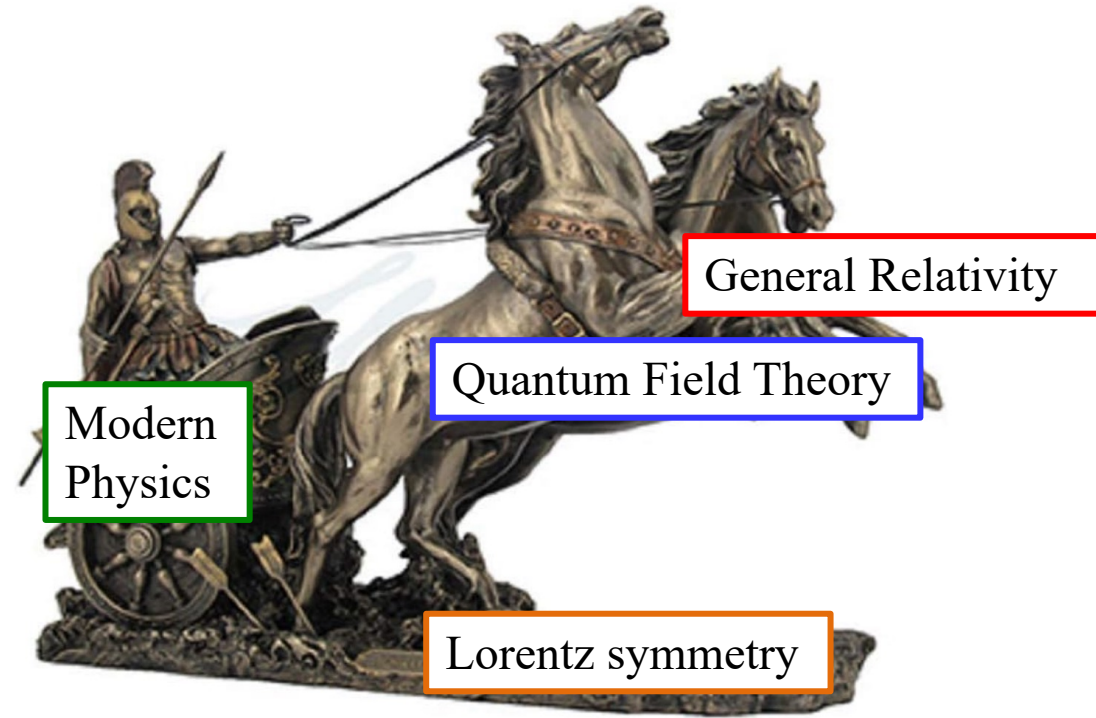
Quantum field theory and general relativity are the foundation of modern physics.

Special relativity is a basis for both quantum field theory and general relativity.

Special relativity is based on Lorentz symmetry

If the universe has a special direction, space doesn't have Lorentz symmetry and Lorentz transformation is violated → **Lorentz violation**

All fundamental physics phenomena must be experimentally tested including Lorentz symmetry



Atmospheric neutrinos

- ## Astrophysical neutrinos

- ### cf) High precision hydrogen 1S-2S transition

Fractional frequency uncertainty $\sim 4 \times 10^{-15}$

- Neutrinos are one of the best probes of fundamental symmetry tests!



Standard-Model Extension (SME)

Search of Lorentz violation is to find anomalous effects due to the couplings of background fields and ordinary fields (electrons, muons, neutrinos, etc)

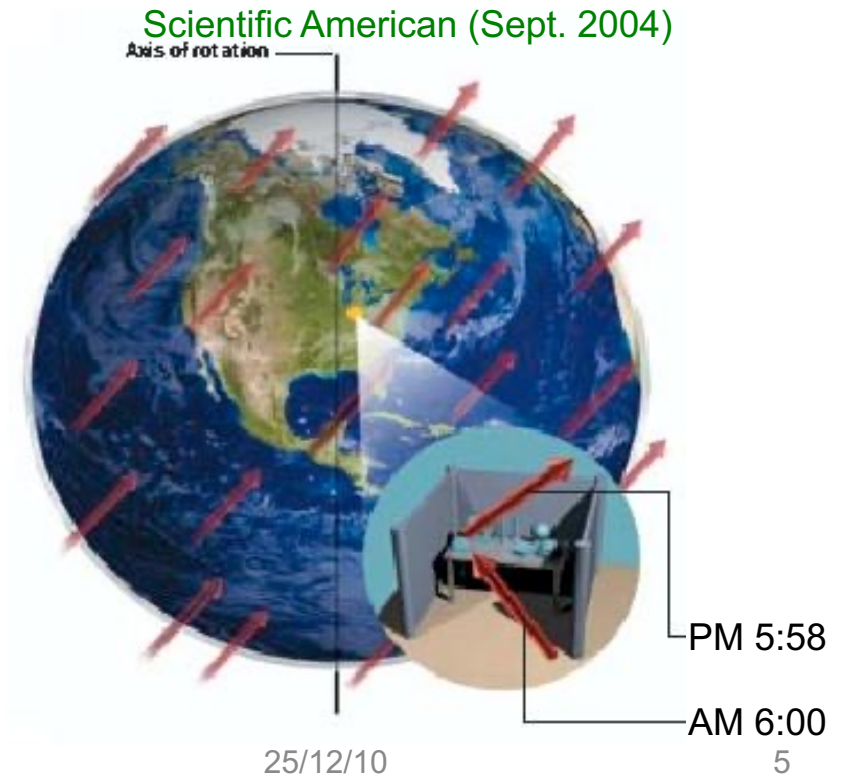
SME is an effective field theory (EFT) framework to look for Lorentz violation

e.g.) vacuum Lagrangian for fermion

$$\mathcal{L} = \underbrace{i\bar{\psi}\gamma_{\mu}\partial^{\mu}\psi - m\bar{\psi}\psi}_{\text{Standard Model}} + \underbrace{i\bar{\psi}\gamma_{\mu}a^{\mu}\psi + \bar{\psi}\gamma_{\mu}c^{\mu\nu}\psi \dots}_{\text{couplings with background fields}}$$

Physics of Lorentz violation

- Spectrum distortion,
- Sidereal time dependence,
- **Anomalous flavour conversion**, etc



Models of Lorentz violation

Long list of models including Lorentz violation

String theory, [Kostelecký and Samuel, PRD39 \(1989\) 683](#)

Ultra-light dark matter, [Graham and Rajendran, PRD88 \(2013\) 035023](#)

Quintessence, [Ando, Kamionkowski, and Mocioiu, PRD80 \(2009\) 123522](#)

Loop quantum gravity, [Gambini and Pullin, PRD59 \(1999\) 124021](#)

Non-commutative field theory, [Carroll, Harvey, Kostelecký, Lane, Okamoto, PRL87 \(2001\) 141601](#)

Hořava-Lifshitz gravity, [Pospelov and Shang, PRD85 \(2012\) 105001](#)

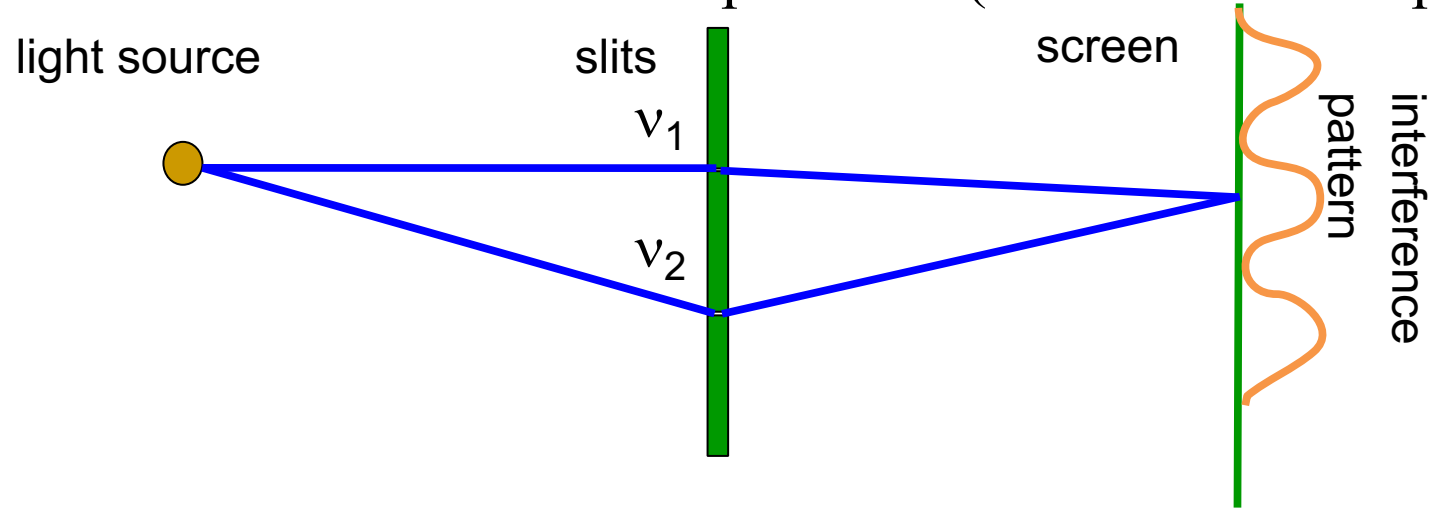
Lee-Wick theory, [Myers and Pospelov, PRL90 \(2003\) 211601](#)

etc

Tests of Lorentz Violation with Neutrinos

Neutrino oscillation experiments

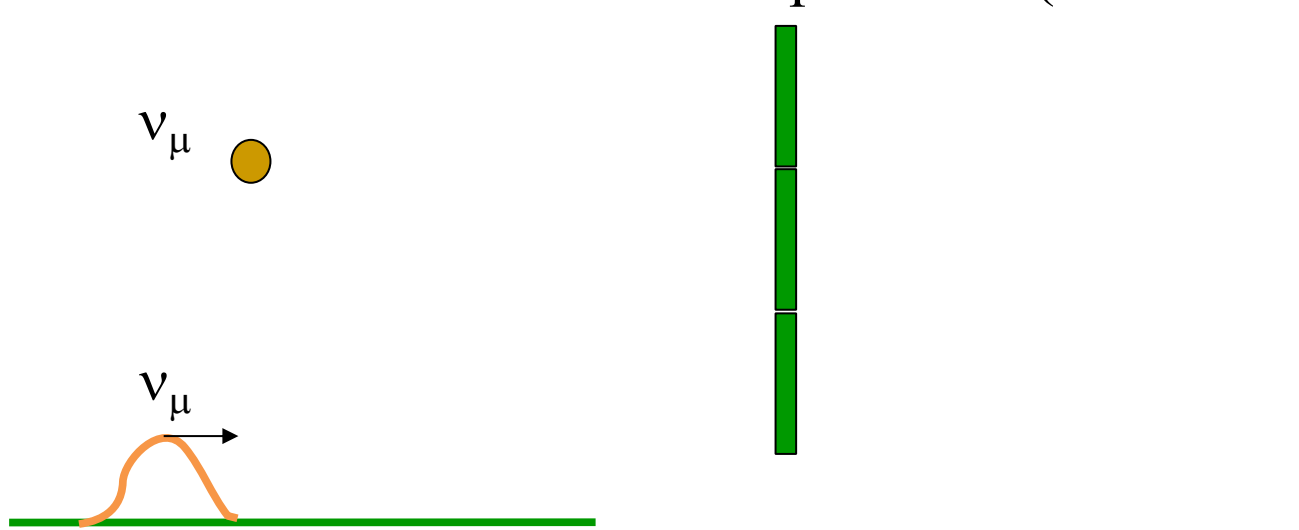
Neutrino oscillation is an interference experiment (cf. double slit experiment)



For double slit experiment, if path v_1 and path v_2 have different length, they have different phases and it causes interference.

Neutrino oscillation experiments

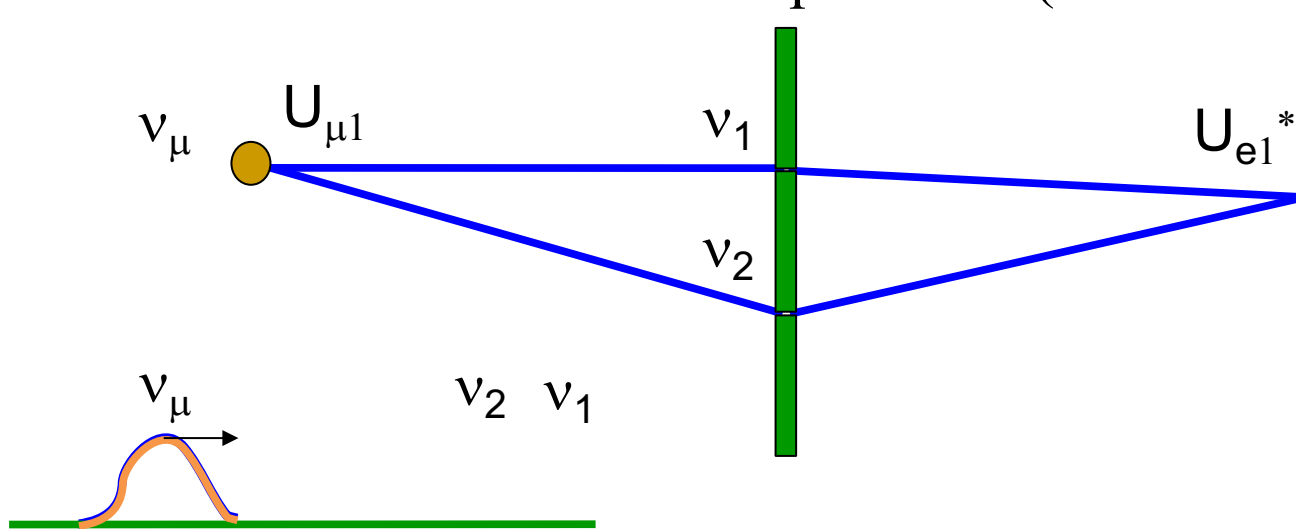
Neutrino oscillation is an interference experiment (cf. double slit experiment)



Neutrino flavour eigenstates are super-position of Hamiltonian eigenstates ν_1 and ν_2

Neutrino oscillation experiments

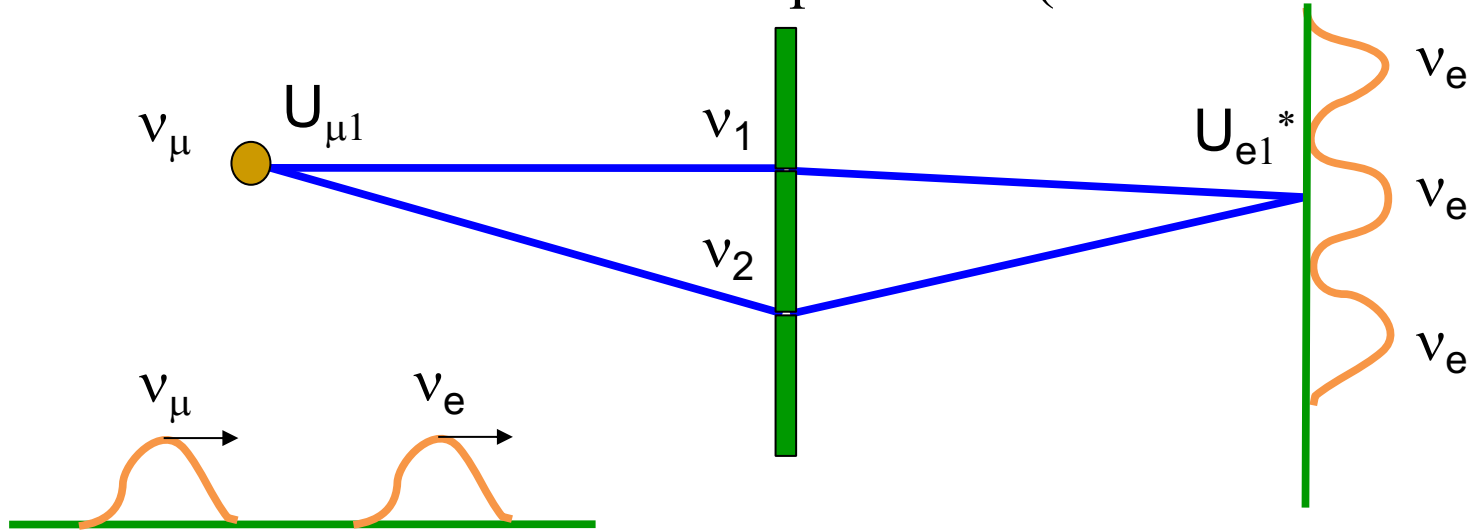
Neutrino oscillation is an interference experiment (cf. double slit experiment)



Neutrino flavour eigenstates are super-position of Hamiltonian eigenstates ν_1 and ν_2
Difference in velocities cause quantum interference

Neutrino oscillation experiments

Neutrino oscillation is an interference experiment (cf. double slit experiment)



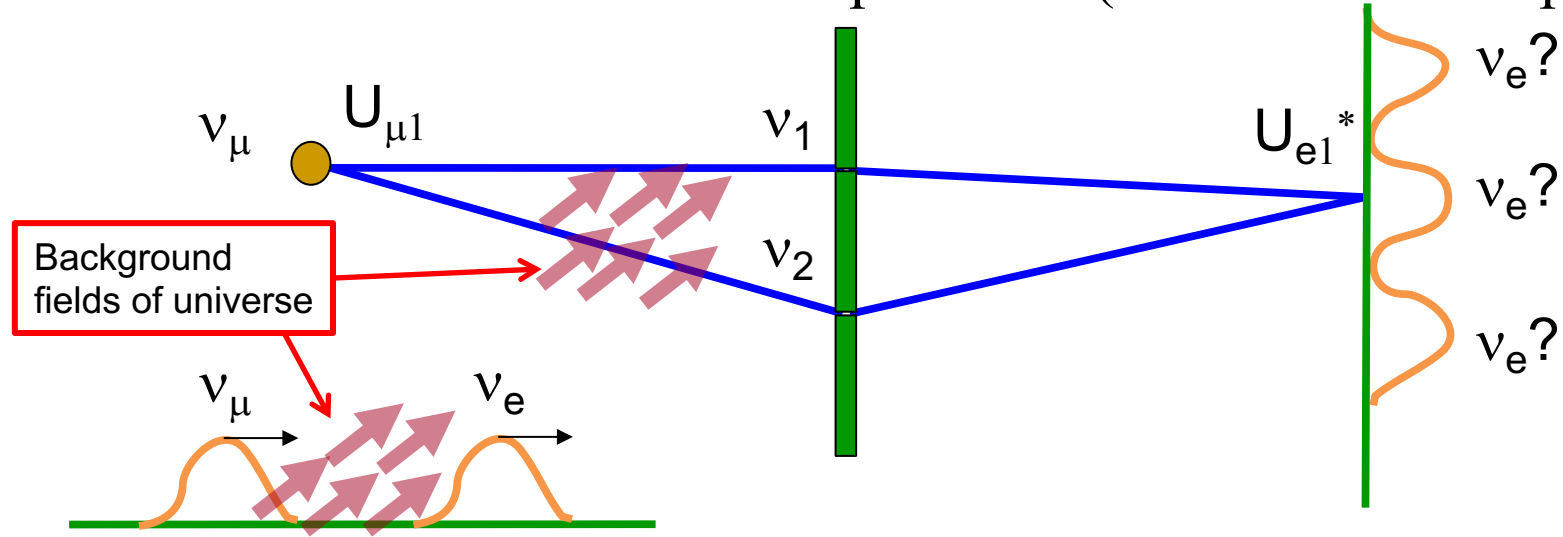
Neutrino flavour eigenstates are super-position of Hamiltonian eigenstates ν_1 and ν_2

Difference in velocities cause quantum interference

The detection may be different flavour (neutrino oscillations)

Neutrino oscillation experiments

Neutrino oscillation is an interference experiment (cf. double slit experiment)



Neutrino flavour eigenstates are super-position of Hamiltonian eigenstates ν_1 and ν_2

Difference in velocities cause quantum interference

The detection may be different flavour (neutrino oscillations)

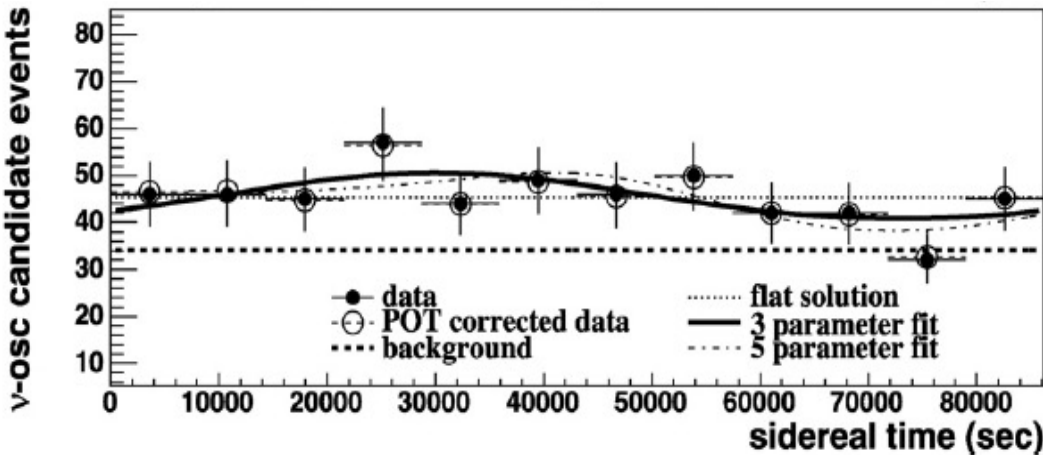
Neutrino propagation may be affected by background fields

→ anomalous neutrino oscillation results

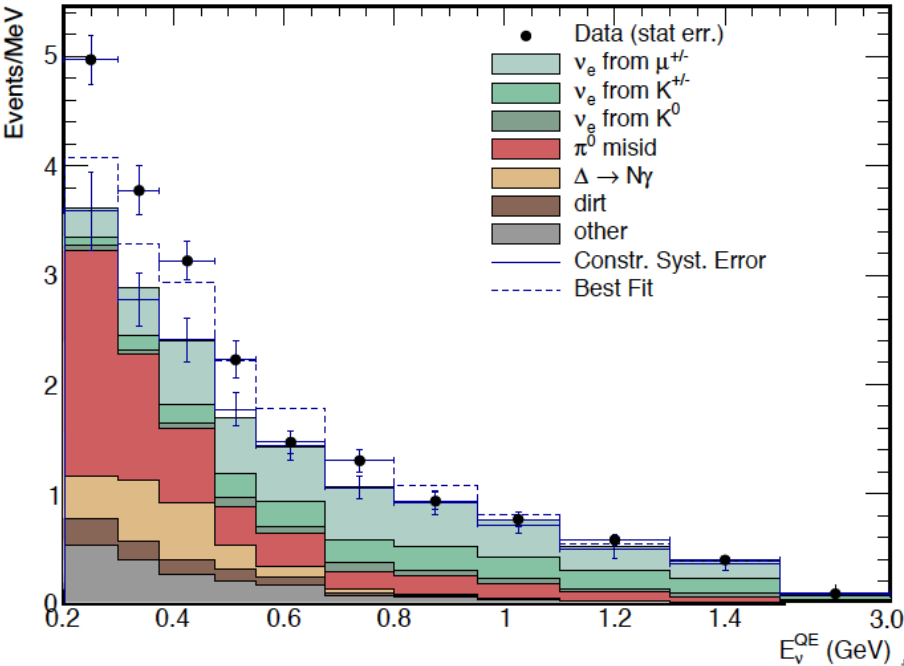
MiniBooNE ν_e appearance candidate data

Anomalous ν_e candidate low-energy excess

- Short baseline $\nu_\mu \rightarrow \nu_e$ oscillation experiment
- Data show no sidereal time dependent modulation
- set limits on SME coefficients



MiniBooNE low E ν_e excess



ν_e excess sidereal time distribution

	ν -mode BF	2σ limit	$\bar{\nu}$ -mode BF	2σ limit
$ (C)_{e\mu} $	$3.1 \pm 0.6 \pm 0.9$	< 4.2	$0.1 \pm 0.8 \pm 0.1$	< 2.6
$ (\mathcal{A}_s)_{e\mu} $	$0.6 \pm 0.9 \pm 0.3$	< 3.3	$2.4 \pm 1.3 \pm 0.5$	< 3.9
$ (\mathcal{A}_c)_{e\mu} $	$0.4 \pm 0.9 \pm 0.4$	< 4.0	$2.1 \pm 1.2 \pm 0.4$	< 3.7

SME coefficients combination (unit 10^{-20} GeV)

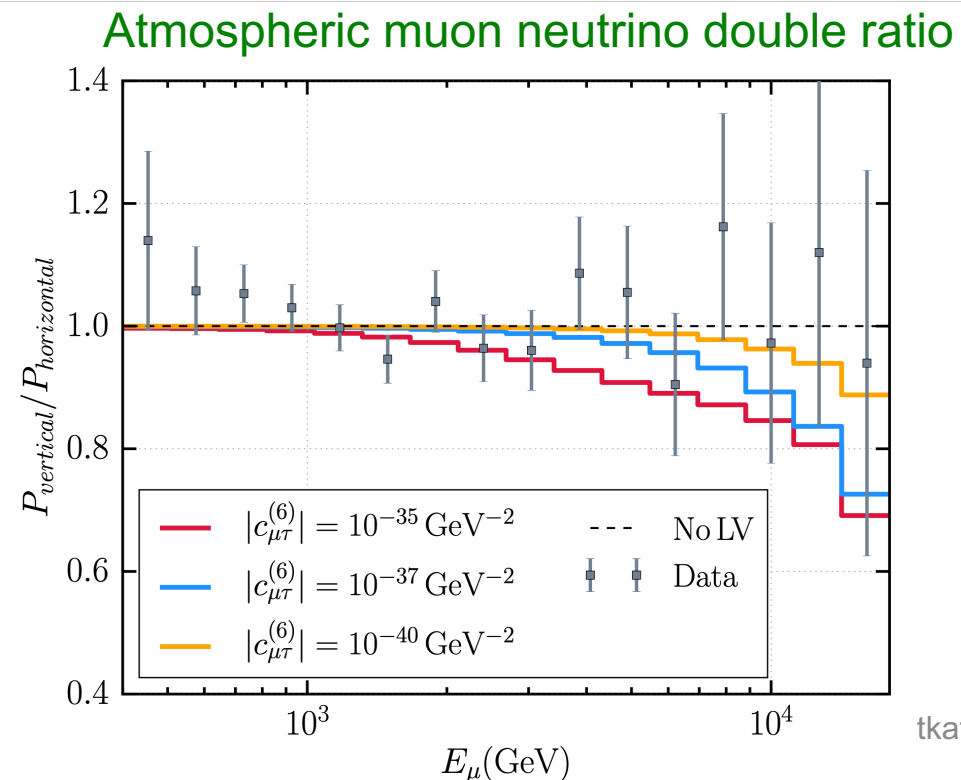
$ (C)_{e\mu} $	$\pm[(a_L)_{e\mu}^T + 0.75(a_L)_{e\mu}^Z] - \langle E \rangle [1.22(c_L)_{e\mu}^{TT} + 1.50(c_L)_{e\mu}^{TZ} + 0.34(c_L)_{e\mu}^{ZZ}]$
$ (\mathcal{A}_s)_{e\mu} $	$\pm[0.66(a_L)_{e\mu}^Y] - \langle E \rangle [1.33(c_L)_{e\mu}^{TY} + 0.99(c_L)_{e\mu}^{YZ}]$
$ (\mathcal{A}_c)_{e\mu} $	$\pm[0.66(a_L)_{e\mu}^X] - \langle E \rangle [1.33(c_L)_{e\mu}^{TX} + 0.99(c_L)_{e\mu}^{XZ}]$

SME coefficients (Lorentz violation) limits

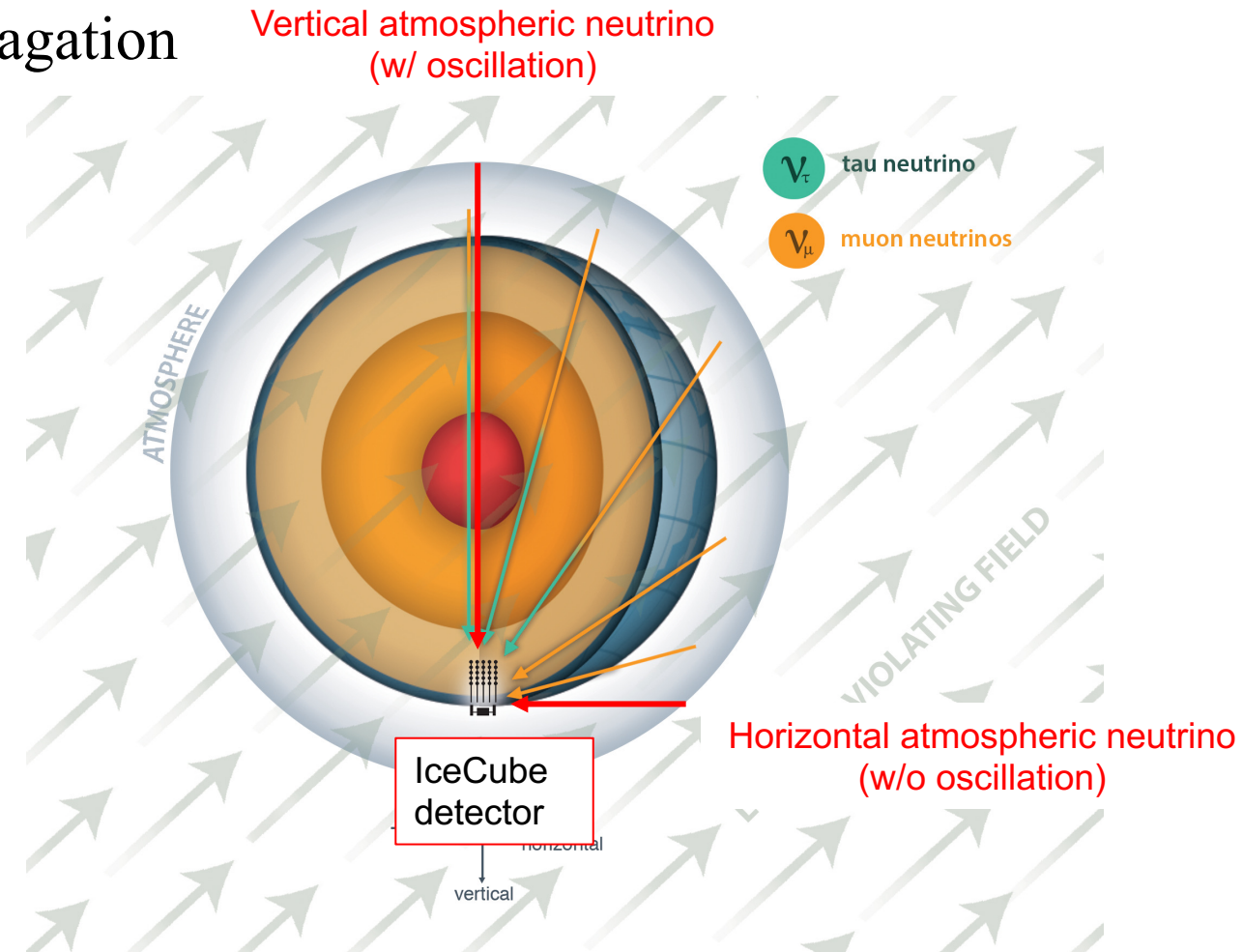
IceCube atmospheric neutrino spectrum distortion

Anomalous ν_μ disappearance

- Strong effect at high-energy and long propagation
- Data show no spectrum distortion
- set limits on SME coefficients



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Lorentz violation tests with neutrinos – Summary

Limits of all SME coefficients are summarized in tables [ArXiv:0801.0287v18](https://arxiv.org/abs/0801.0287v18)

So far, there is no compelling evidence of Lorentz violation

When do we find it???

~30-page limits in neutrino sector LV...

Table D51. Neutrino sector, $d = 3$ (part 4 of 6)			
Combination	Result	System	Ref.
$G_{\mu\mu}$	$(-0.3 \pm 3.0) \times 10^{-30}$ GeV	T2K	[260]
$(A_{\mu\mu})_{\text{SM}}$	$(0.4 \pm 3.2) \times 10^{-30}$ GeV	"	[260]
$(A_{\mu\mu})_{\text{NSM}}$	$(0.4 \pm 3.8) \times 10^{-30}$ GeV	"	[260]
$(B_{\mu\mu})_{\text{SM}}$	$(-1.2 \pm 2.6) \times 10^{-30}$ GeV	"	[260]
$(B_{\mu\mu})_{\text{NSM}}$	$(2.0 \pm 3.1) \times 10^{-30}$ GeV	"	[260]
$ C_{\mu\mu} ^2$	$(10.7 \pm 2.6 \pm 1.3) \times (10^{-19} \text{ GeV})^2$	LSND	[261]
$ C_{\mu\mu} ^2 + \frac{1}{2}[(A_{\mu\mu})_{\text{SM}}^2 + \frac{1}{2}(B_{\mu\mu})_{\text{SM}}^2]$	$(9.9 \pm 2.3 \pm 1.4) \times (10^{-19} \text{ GeV})^2$	"	[261]
$ C_{\mu\mu} ^2 + \frac{1}{2}[(A_{\mu\mu})_{\text{SM}}^2 + \frac{1}{2}(B_{\mu\mu})_{\text{SM}}^2]$	$(10.5 \pm 2.4 \pm 1.4) \times (10^{-19} \text{ GeV})^2$	"	[261]
$ C_{\mu\mu} ^2 + \frac{1}{2}[(A_{\mu\mu})_{\text{SM}}^2 + \frac{1}{2}(B_{\mu\mu})_{\text{SM}}^2]$	$< 6.5 \times 10^{-30}$ GeV	SNO	[251]
$ C_{\mu\mu} ^2$	$< 2.8 \times 10^{-30}$ GeV	"	[251]
$ C_{\mu\mu} ^2$	$< 1.5 \times 10^{-30}$ GeV	"	[251]
$ C_{\mu\mu} ^2$	$< 1.7 \times 10^{-30}$ GeV	"	[251]
$(a_{\mu\mu})_{\text{SM}}$	$(-5.6 \pm 8.0) \times 10^{-30}$ GeV	Daya Bay	[252]
$(a_{\mu\mu})_{\text{NSM}}$	$(-0.9 \pm 8.0) \times 10^{-30}$ GeV	"	[252]
$(a_{\mu\mu})_{\text{SM}}$	$< 4.1 \times 10^{-30}$ GeV	Super-Kamiokande	[253]
$(a_{\mu\mu})_{\text{NSM}}$	$< 2.8 \times 10^{-30}$ GeV	"	[253]
$ \text{Re}(a_{\mu\mu})_{\text{SM}} , \text{Im}(a_{\mu\mu})_{\text{SM}} $	$< 7.8 \times 10^{-30}$ GeV	Double Chooz	[256]
$ \text{Re}(a_{\mu\mu})_{\text{SM}} , \text{Im}(a_{\mu\mu})_{\text{SM}} $	$< 4.4 \times 10^{-30}$ GeV	"	[256]
$ \text{Re}(a_{\mu\mu})_{\text{SM}} , \text{Im}(a_{\mu\mu})_{\text{SM}} $	$< 9.0 \times 10^{-30}$ GeV	"	[256]
$ \text{Re}(a_{\mu\mu})_{\text{SM}} , \text{Im}(a_{\mu\mu})_{\text{SM}} $	$< 2.7 \times 10^{-30}$ GeV	"	[256]
$ \text{Re}(a_{\mu\mu})_{\text{SM}} , \text{Im}(a_{\mu\mu})_{\text{SM}} $	$< 7.8 \times 10^{-30}$ GeV	"	[256]
$ \text{Re}(a_{\mu\mu})_{\text{SM}} , \text{Im}(a_{\mu\mu})_{\text{SM}} $	$< 6.6 \times 10^{-30}$ GeV	"	[256]
$ \text{Re}(a_{\mu\mu})_{\text{SM}} , \text{Im}(a_{\mu\mu})_{\text{SM}} $	$< 7.0 \times 10^{-30}$ GeV	"	[256]
$ \text{Re}(a_{\mu\mu})_{\text{SM}} , \text{Im}(a_{\mu\mu})_{\text{SM}} $	$< 5.4 \times 10^{-30}$ GeV	"	[256]
$ \text{Re}(a_{\mu\mu})_{\text{SM}} , \text{Im}(a_{\mu\mu})_{\text{SM}} $	$< 5.4 \times 10^{-30}$ GeV	"	[256]
$ \text{Re}(a_{\mu\mu})_{\text{SM}} , \text{Im}(a_{\mu\mu})_{\text{SM}} $	$< 2 \times 10^{-30}$ GeV	Lepton, SU(2) _L invariance	[239]*
$ \text{Re}(a_{\mu\mu})_{\text{SM}} , \text{Im}(a_{\mu\mu})_{\text{SM}} $	$< 4 \times 10^{-30}$ GeV	"	[239]*
$ \text{Re}(a_{\mu\mu})_{\text{SM}} , \text{Im}(a_{\mu\mu})_{\text{SM}} $	$< 8.2 \times 10^{-30}$ GeV	SNO	[251]
$ \text{Re}(a_{\mu\mu})_{\text{SM}} , \text{Im}(a_{\mu\mu})_{\text{SM}} $	$< 8.4 \times 10^{-30}$ GeV	"	[251]
$ \text{Re}(a_{\mu\mu})_{\text{SM}} , \text{Im}(a_{\mu\mu})_{\text{SM}} $	$< 2.9 \times 10^{-30}$ GeV	"	[251]
$ \text{Re}(a_{\mu\mu})_{\text{SM}} , \text{Im}(a_{\mu\mu})_{\text{SM}} $	$< 3.2 \times 10^{-30}$ GeV	"	[251]
$(a_{\mu\mu})_{\text{SM}}$	$(9.4 \pm 45) \times 10^{-30}$ GeV	Daya Bay	[252]
$(a_{\mu\mu})_{\text{NSM}}$	$(-9.4 \pm 45) \times 10^{-30}$ GeV	"	[252]
$ \text{Re}(a_{\mu\mu})_{\text{SM}} , \text{Im}(a_{\mu\mu})_{\text{SM}} $	$< 1.9 \times 10^{-30}$ GeV	Super-Kamiokande	[262]*
$ \text{Re}(a_{\mu\mu})_{\text{SM}} , \text{Im}(a_{\mu\mu})_{\text{SM}} $	$< 4.8 \times 10^{-30}$ GeV	T2K	[263]
$ \text{Re}(a_{\mu\mu})_{\text{SM}} , \text{Im}(a_{\mu\mu})_{\text{SM}} $	$< 6.3 \times 10^{-30}$ GeV	Super-Kamiokande	[264]*

Spectral distortion

Super-Kamiokande
PRD91(2015)052003

Daya Bay
PRD98(2018)092013

AMANDA
PRD79(2009)102005

IceCube
Nature Physics
14(2018)961

Sidereal variation

LSND
PRD72(2005)076004

MiniBooNE
PLB718(2013)1303

MINOS ND
PRL101(2008)151601

MINOS FD
PRL105(2010)151601

T2K ND
PRD95(2017)111101

IceCube
PRD82(2010)112003

Double Chooz
PRD86(2013)112009

SNO
PRD98(2018)112013

Flavor ratio

IceCube
Nature Physics, 18(2022)1287

Seasonal variation

SNO
PRD98(2018)112013

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When do we find Lorentz violation???

Lorentz violation is motivated by Planck scale theories, so it is suppressed with the power of Planck mass ($\sim 10^{19} \text{ GeV}$)

$$\sim \frac{1}{M_{Pl}}, \left(\frac{1}{M_{Pl}}\right)^2, \text{etc}$$

In effective field theory, **non-renormalizable operators** are the signature of new physics, dimension analysis guides target sensitivity to look for Lorentz violation.

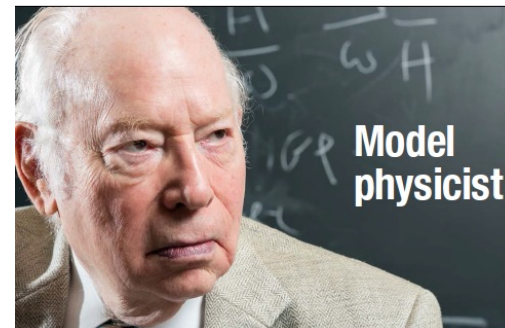
dimension-5 LV operator, $a^{(5)} < 10^{-19} \text{ GeV}^{-1}$

dimension-6 LV operator, $c^{(6)} < 10^{-38} \text{ GeV}^{-2}$

etc

These numbers can be used as a guidance to design new experiments

Steven Weinberg
([CERN Courier Nov. 2017](#))



“We don’t know anything about non-renormalizable interaction terms, but I’ll swear they are there!”

Tests of Lorentz violation with astrophysical neutrinos

Terrestrial experiments

- controlled, high-precision

So far, no compelling evidence of Lorentz violation

Atmospheric, astrophysical, and cosmological experiments

- not controlled, low-precision
- extreme systems (high energy, long propagation, etc)
- **more sensitive to nonrenormalizable operators**

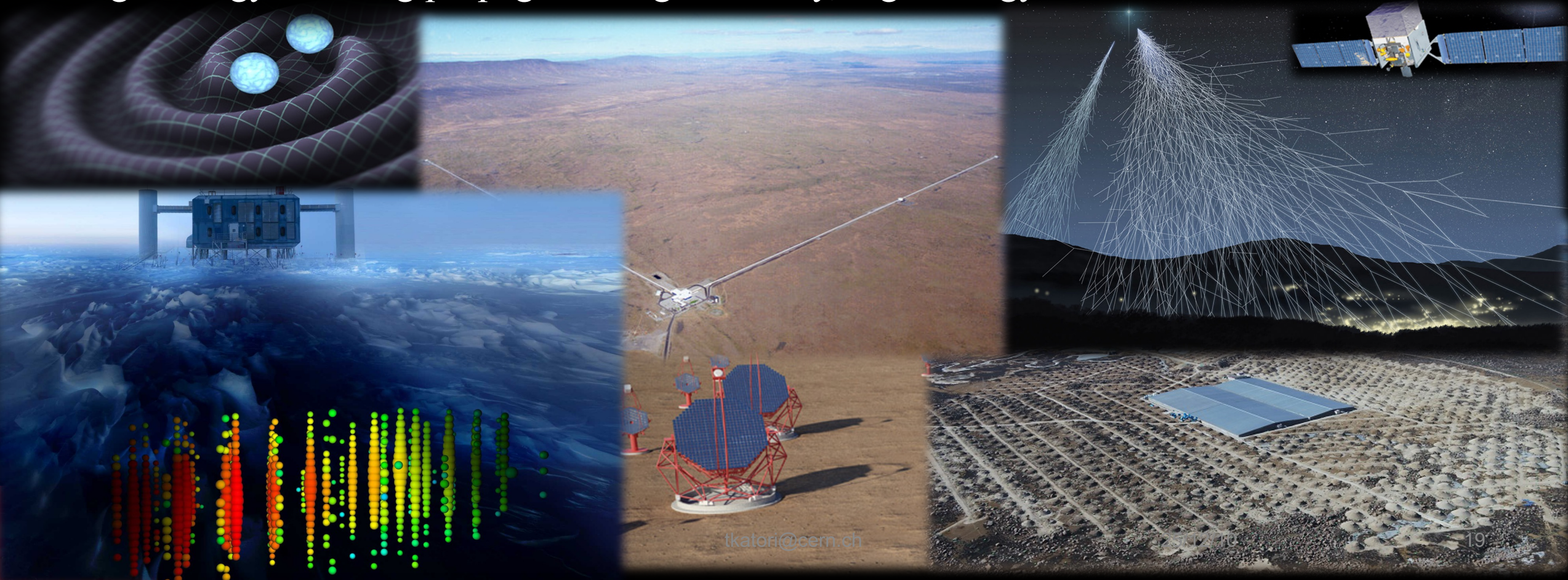
Tests of Lorentz Violation with Astrophysical Neutrinos

Lorentz violation in Astrophysics

Highest energy particles – ultra-high-energy cosmic rays

Longest propagating waves – gravitational waves, cosmic microwave background

High-energy and long propagation – gamma-ray, high-energy neutrinos



Review

Quantum gravity phenomenology at the dawn of the multi-messenger era—A review



Contents lists available at [ScienceDirect](https://www.sciencedirect.com)

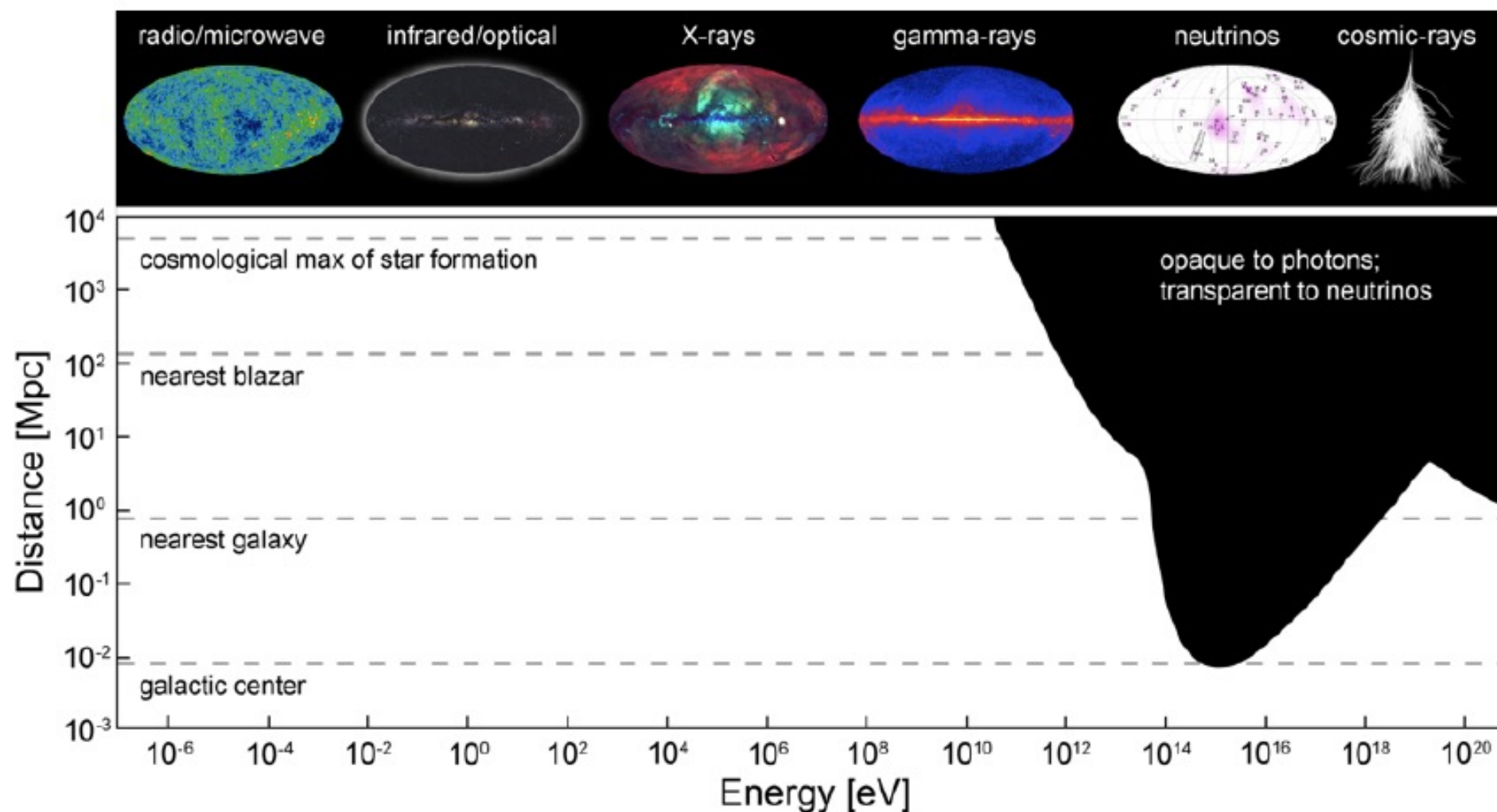
Progress in Particle and Nuclear Physics

journal homepage: www.elsevier.com/locate/ppnp



High-energy astrophysical neutrinos

Neutrinos are the highest-energy (>100 TeV) longest-baseline ($> \text{Mpc}$) quantum system



High-energy, long propagating neutrinos

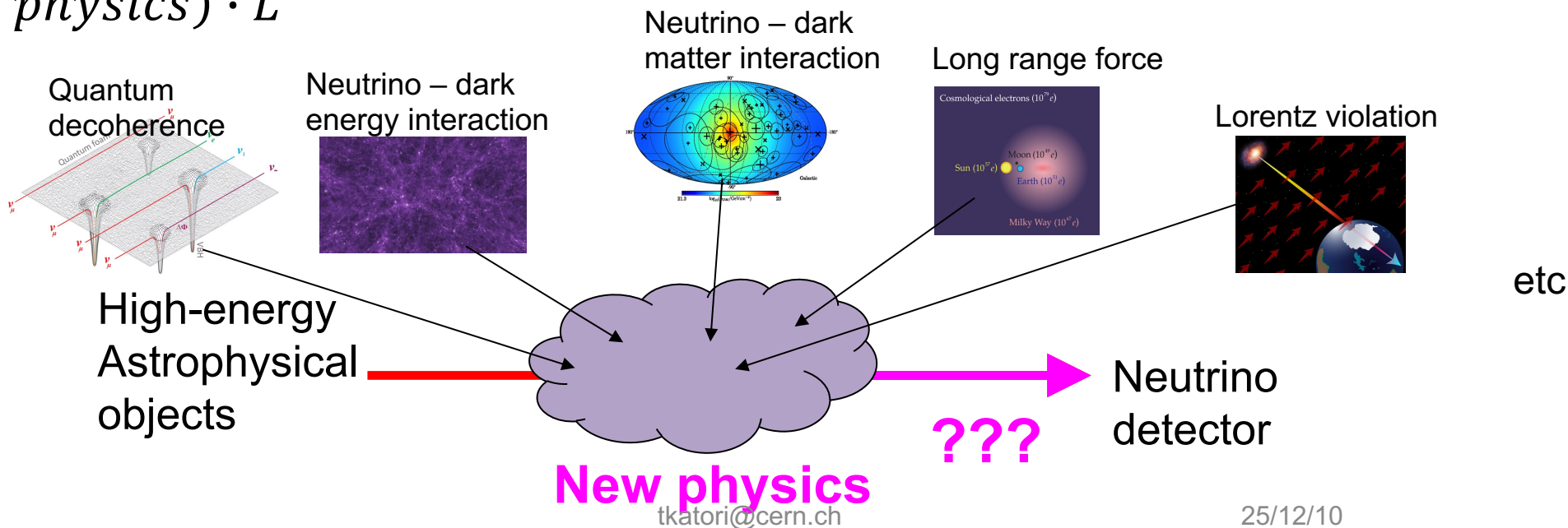
High-energy astrophysical neutrinos

- Long baseline accumulates new physics effect
- High energy enhances new physics effect
- Quantum interference magnify a small effect

$$H \sim \frac{m^2}{2E} + V(\text{new physics})$$

$$P \sim V(\text{new physics}) \cdot L$$

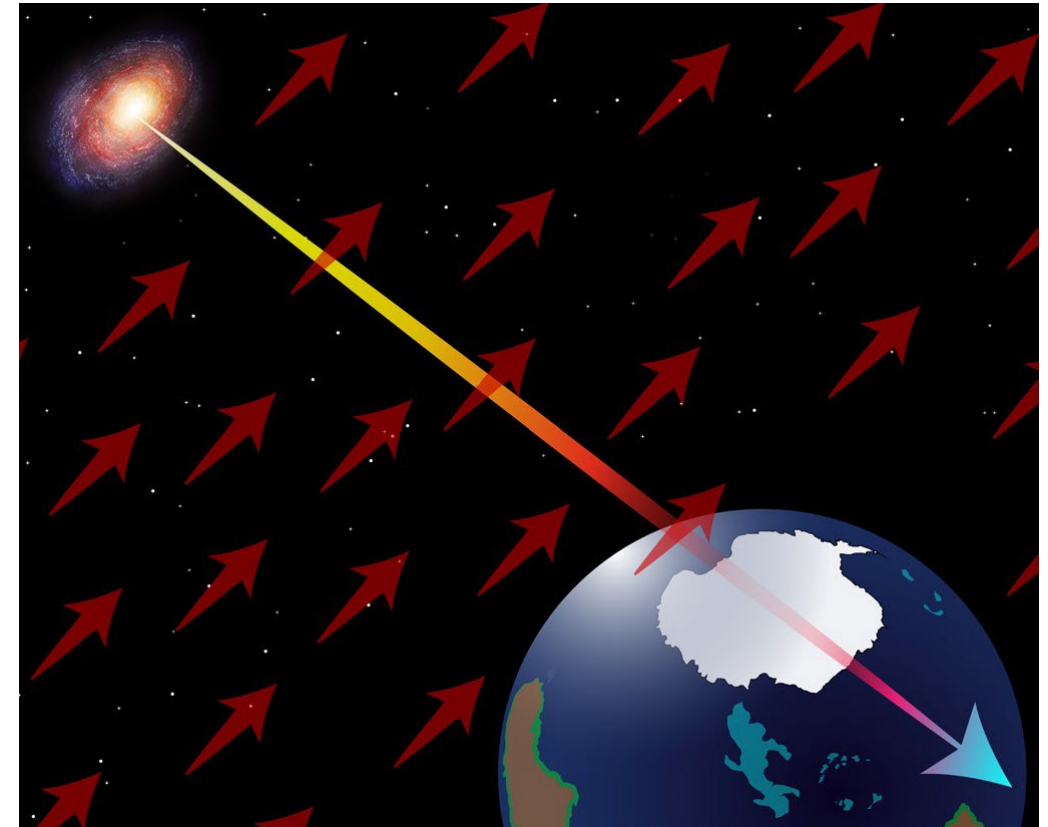
Energy spectrum, arrival time, **flavor** are affected by production, **propagation**, detection of neutrinos



High-energy, long propagating neutrinos

Violation of Lorentz invariance

- Theoretically motivated (long list of models)
- Neutrino interacting with new fields in vacuum
- Matter potential in vacuum, but very small
- Energy spectrum, arrival time, **flavor** are affected
- Astrophysical neutrino flavor physics



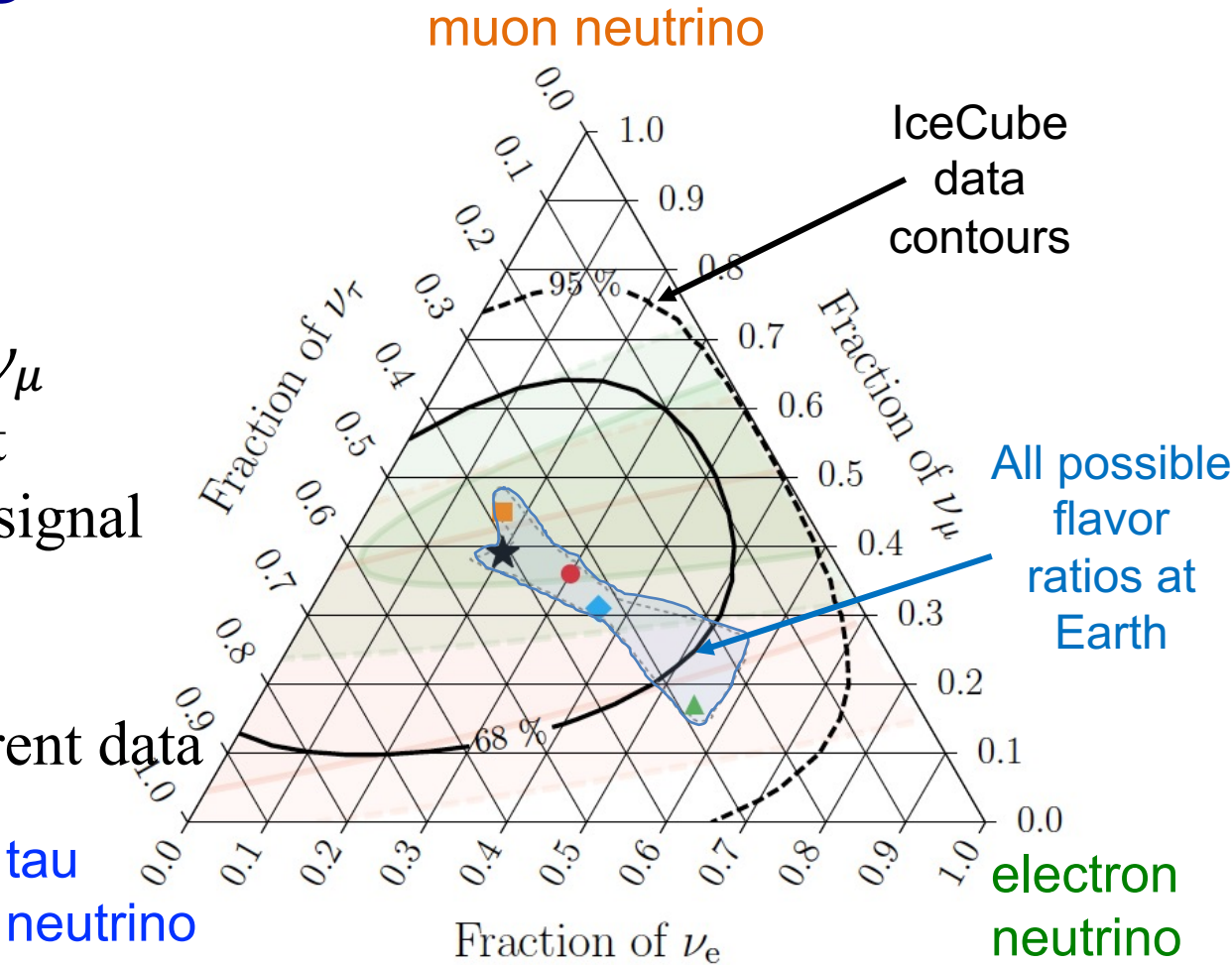
High-energy, long propagating neutrinos

Astrophysical neutrino flavor physics

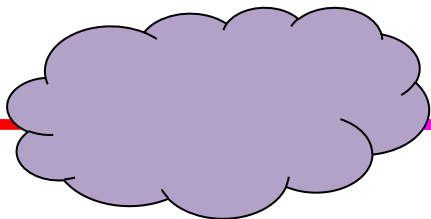
- Flavor triangle
- Spectrum integrated flavor ratio ($\nu_e : \nu_\mu : \nu_\tau$)
- Standard production models include ν_e and ν_μ
- Flavor ratio observables on Earth is different
- Deviation from this “island” is new physics signal

Data contour covers most of flavor triangle

- New physics cannot be discovered from current data
- Limits are set on vacuum operators



High-energy
Astrophysical
objects



Flavor mixing

???

Ne
det

- HESE with ternary topology ID
- ★ Best fit: 0.20 : 0.39 : 0.42
- Global Fit (IceCube, APJ 2015)
- Inelasticity (IceCube, PRD 2019)
- 3ν-mixing 3σ allowed region

$\nu_e : \nu_\mu : \nu_\tau$ at source $\rightarrow$ on Earth:	
■	0:1:0 $\rightarrow$ 0.17 : 0.45 : 0.37
●	1:2:0 $\rightarrow$ 0.30 : 0.36 : 0.34
▲	1:0:0 $\rightarrow$ 0.55 : 0.17 : 0.28

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HESE 7.5-yr flavor Lorentz violation search

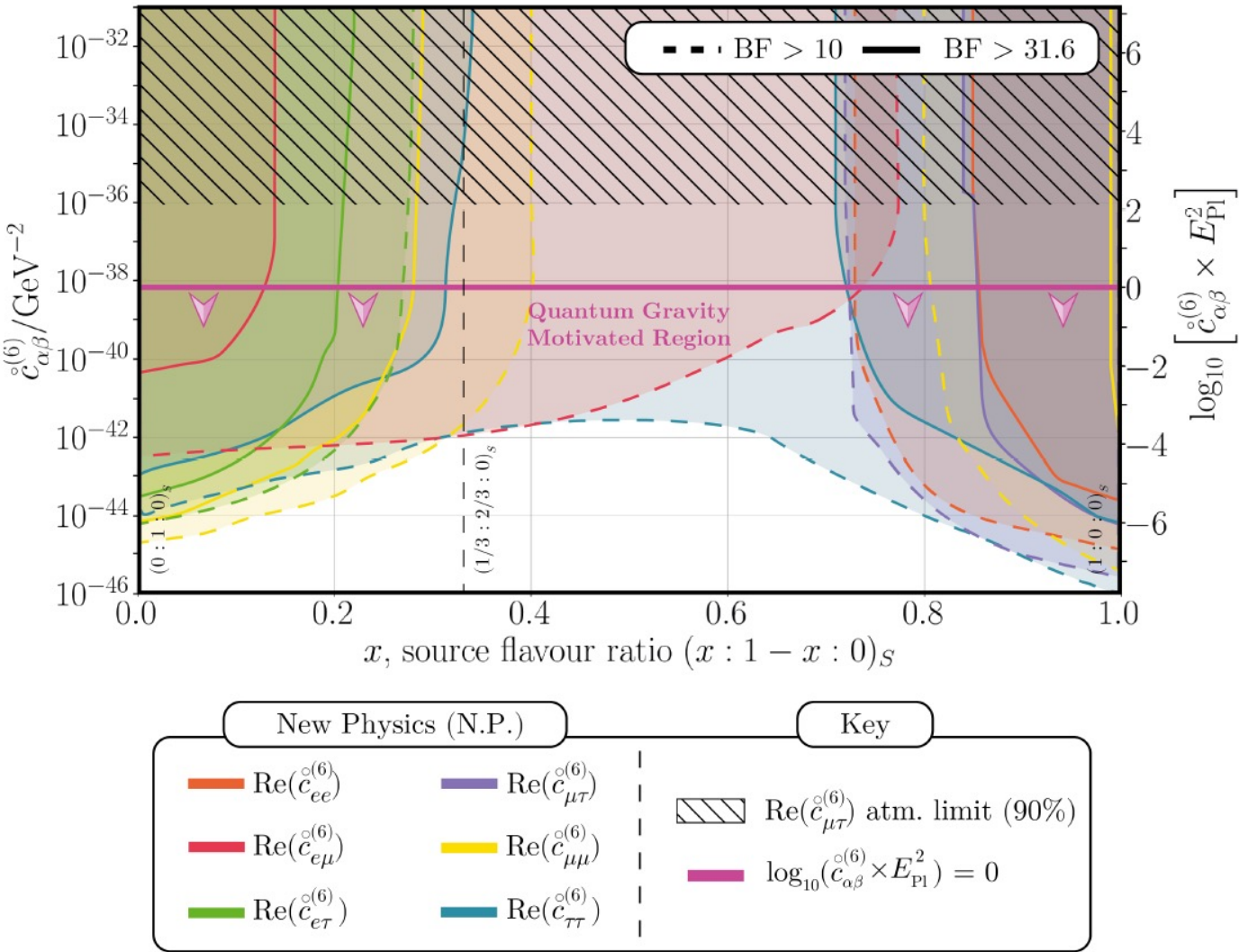
dim-6 new physics operator limit

60 HESE events in 60 TeV – 2 PeV

IceCube data start to explore quantum gravity-motivated signal region for some parameters

$$c^{(6)} \leq \frac{1}{M_{Planck}^2} \sim 10^{-38} GeV^{-2}$$

dim coefficient limit (BF> 10.0)		
3	$Re(\overset{\circ}{a}_{\tau\tau}^{(3)})$	$2 \times 10^{-26} GeV$
4	$Re(\overset{\circ}{c}_{\tau\tau}^{(4)})$	2×10^{-31}
5	$Re(\overset{\circ}{a}_{\tau\tau}^{(5)})$	$2 \times 10^{-37} GeV^{-1}$
6	$Re(\overset{\circ}{c}_{\tau\tau}^{(6)})$	$3 \times 10^{-42} GeV^{-2}$
7	$Re(\overset{\circ}{a}_{\tau\tau}^{(7)})$	$3 \times 10^{-47} GeV^{-3}$
8	$Re(\overset{\circ}{c}_{\tau\tau}^{(8)})$	$2 \times 10^{-52} GeV^{-4}$



Lorentz violation limits from tabletop to cosmology



Physics MMA

Lower dimension operators → searches by tabletop experiments
 Higher dimension operators → searches by astrophysical observations

$$H \sim \frac{m^2}{2E} + a^{(3)} - E \cdot c^{(4)} + E^2 \cdot a^{(5)} - E^3 \cdot c^{(6)} \dots$$



torsion pendulum



optical resonator



comagnetometer



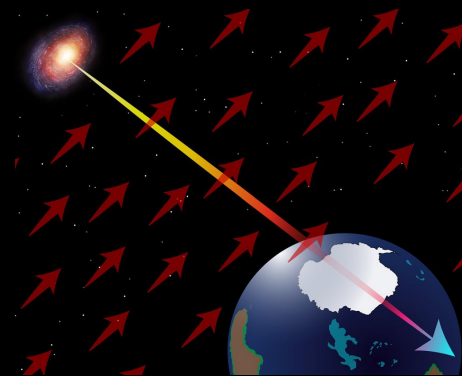
vacuum birefringence



UHECRs

dim.	method	type	sector	limits	ref.
$\frac{a^{(3)}}{a^{(3)}}$	CMB polarization	astrophysical	photon	$\sim 10^{-43}$ GeV	[2]
	He-Xe comagnetometer	tabletop	neutron	$\sim 10^{-34}$ GeV	[3]
	torsion pendulum	tabletop	electron	$\sim 10^{-31}$ GeV	[4]
	muon g-2	accelerator	muon	$\sim 10^{-24}$ GeV	[5]
	neutrino mixing	astrophysical	neutrino	$\sim 10^{-26}$ GeV	[1]
$\frac{c^{(4)}}{c^{(4)}}$	GRB vacuum birefringence	astrophysical	photon	$\sim 10^{-38}$	[6]
	Laser interferometer	LIGO	photon	$\sim 10^{-22}$	[7]
	Sapphire cavity oscillator	tabletop	photon	$\sim 10^{-18}$	[8]
	Ne-Rb-K comagnetometer	tabletop	neutron	$\sim 10^{-29}$	[9]
	trapped Ca^+ ion	tabletop	electron	$\sim 10^{-19}$	[10]
$\frac{a^{(5)}}{a^{(5)}}$	neutrino mixing	astrophysical	neutrino	$\sim 10^{-31}$	[1]
	GRB vacuum birefringence	astrophysical	photon	$\sim 10^{-34}$ GeV ⁻¹	[6]
	ultra-high-energy cosmic ray	astrophysical	proton	$\sim 10^{-22}$ to 10^{-18} GeV ⁻¹	[11]
$\frac{c^{(6)}}{c^{(6)}}$	neutrino mixing	astrophysical	neutrino	$\sim 10^{-37}$ GeV ⁻¹	[1]
	GRB vacuum birefringence	astrophysical	photon	$\sim 10^{-31}$ GeV ⁻²	[6]
	ultra-high-energy cosmic ray	astrophysical	proton	$\sim 10^{-42}$ to 10^{-35} GeV ⁻²	[11]
	gravitational Cherenkov radiation	astrophysical	gravity	$\sim 10^{-31}$ GeV ⁻²	[12]
	neutrino mixing	astrophysical	neutrino	$\sim 10^{-42}$ GeV ⁻²	[1]

Astrophysical neutrino flavour Lorentz violation limits



Weak interaction
 + Small mass
 + Quantum mixing
 = macroscopic quantum system you cannot disturb

Tests of Lorentz Violation with Astrophysical Neutrinos – Summary

Astrophysical neutrinos have high potential to look for Lorentz violation. But there are many unknowns;

- Energy spectrum
- Production time
- Source information
- Foreground

etc

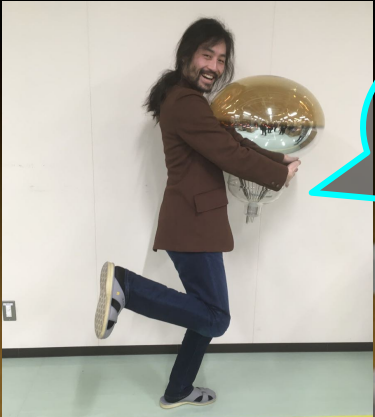
So far, astrophysical neutrino data are low statistics, and further data are needed to search Lorentz violation...

Hyper-Kamiokande and IceCube-Gen2

Summer
2024-2045
IceCube team



New international neutrino astronomy projects around the world



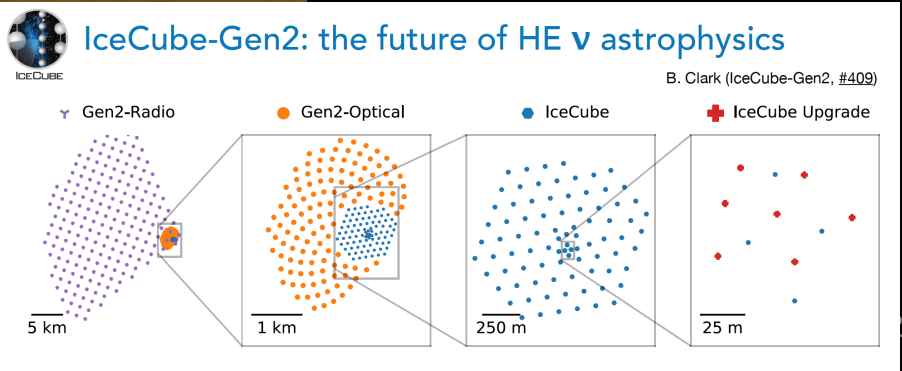
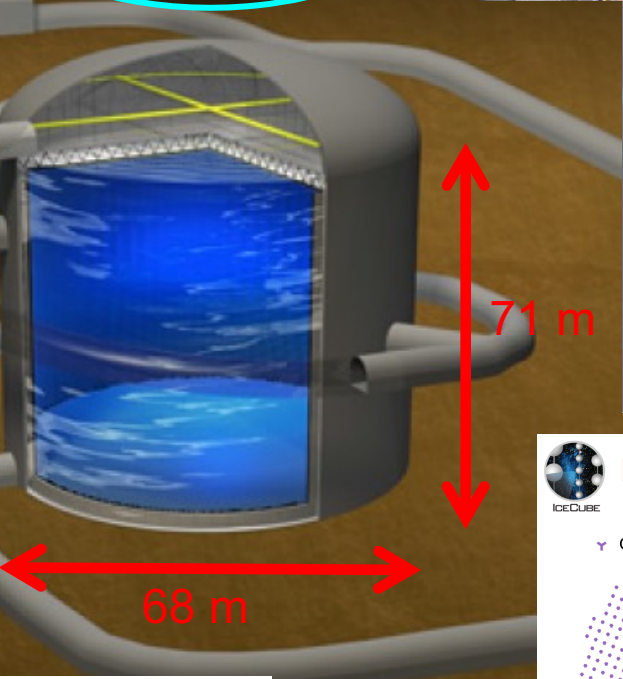
Hyper-K
construction
is ongoing



Gen2-Optical (~8 Gton)
Gen2-Radio (~500 Gton, >10 PeV)
IceCube-Upgrade (~8 Mton, >3 GeV)



The first stage of
Gen2 (IceCube
upgrade) is
ongoing



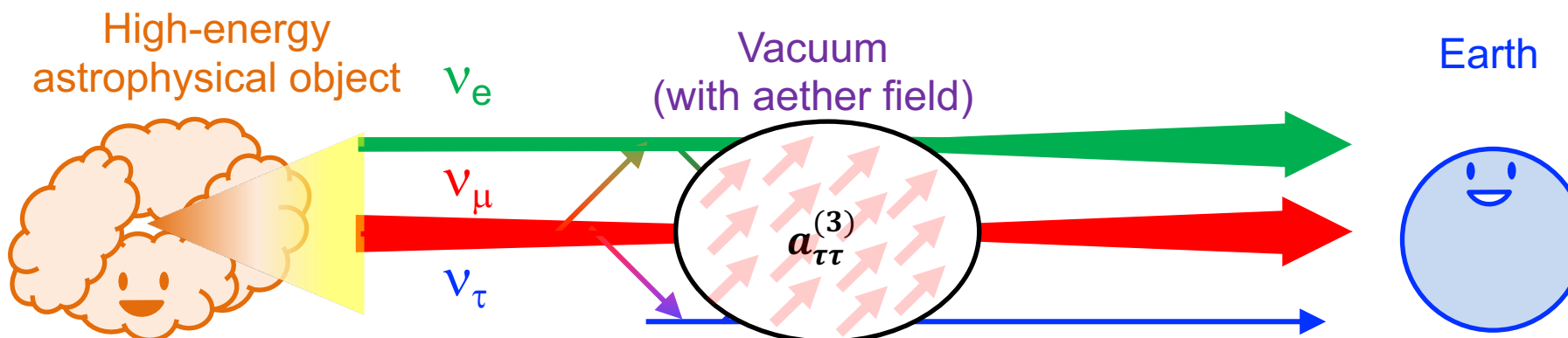
Searches of Ultralight Dark Matter with Astrophysical Neutrino Flavour

Astrophysical neutrino flavour physics

IceCube Lorentz violation analysis set a limit on $a_{\tau\tau}^{(3)}$

- Try to reinterpret this limit $a_{\tau\tau}^{(3)}$ as a limit of **neutrino-ultralight dark matter interaction**

$$h_{eff} \sim \frac{1}{2E} U^\dagger M^2 U + a_{\alpha\beta}^{(3)} \dots \sim \frac{1}{2E} \begin{pmatrix} m_{ee}^2 & m_{e\mu}^2 & m_{\tau e}^2 \\ m_{e\mu}^{2*} & m_{\mu\mu}^2 & m_{\mu\tau}^2 \\ m_{\tau e}^{2*} & m_{\mu\tau}^{2*} & m_{\tau\tau}^2 \end{pmatrix} + \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & a_{\tau\tau}^{(3)} \end{pmatrix} \dots$$

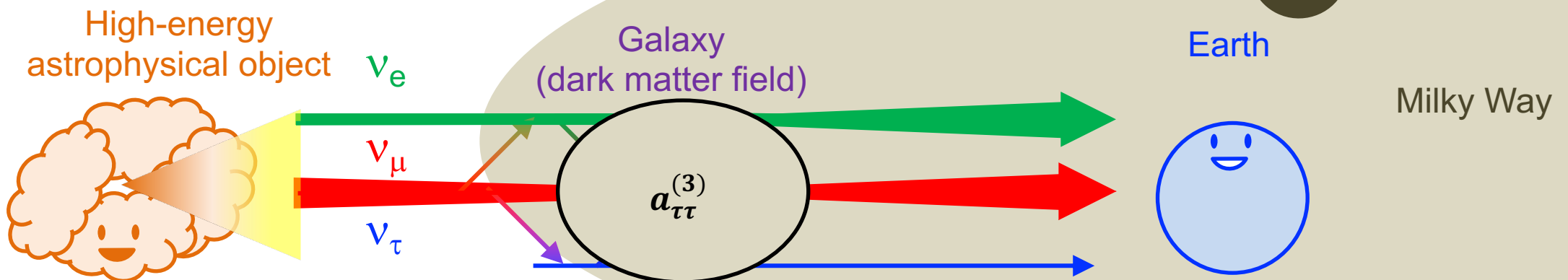


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Ultralight dark matter coupling with neutrinos

Different dark matter models provide different effective Hamiltonian

ex) Relativistic ultra-light dark matter model

$$h_{eff} \sim \frac{1}{2E} U^\dagger M^2 U + V_{\tau\tau}$$

1. Axion dark matter model

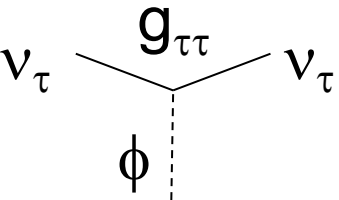
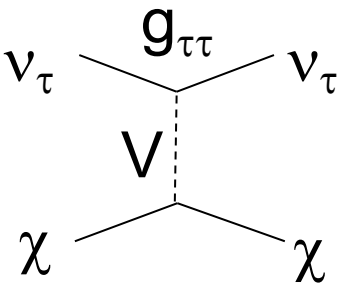
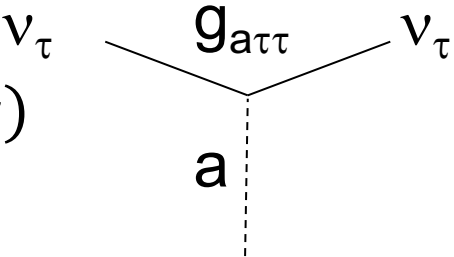
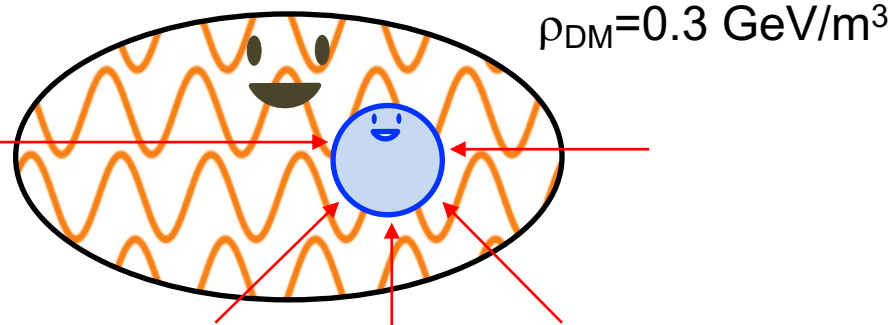
$$V_{\tau\tau}(t) = g_{a\tau\tau} m_a a_0 \sin(m_a t)$$

2. Vector and axial vector dark matter coupling model

$$V_{\tau\tau}(t) = g_{\tau\tau} \sqrt{2\rho_{DM}}/m_A \sin(m_A t)$$

(3. Scalar ultralight dark matter model correct neutrino mass)

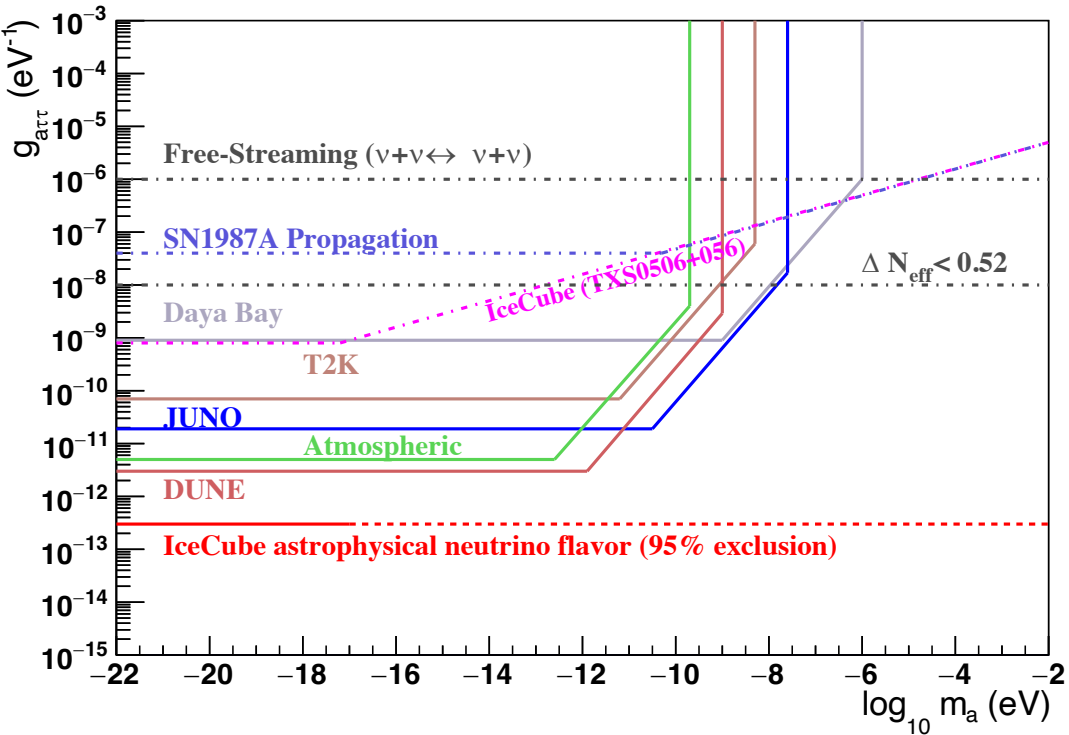
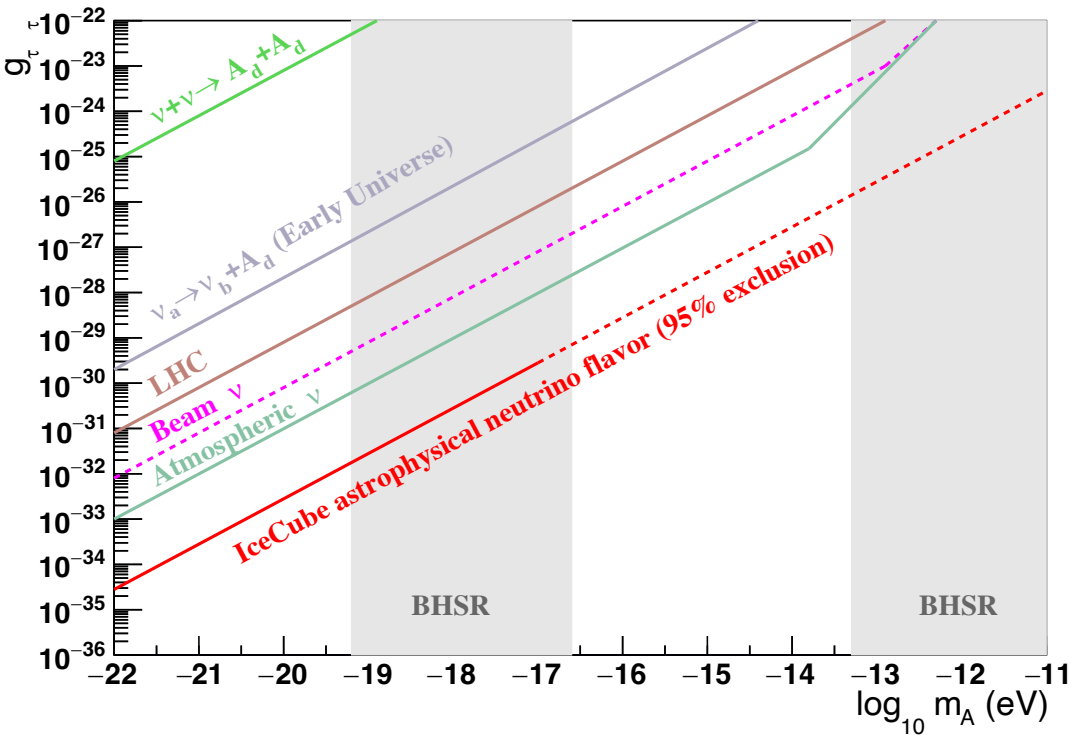
[Krnjaic, Machado, Necib, PRD97\(2018\)075017](#)



Ultralight dark matter coupling with neutrinos

Left: Vector and axial-vector coupling with dark matter: $g_{\tau\tau} < 3 \times 10^{-33} \left(\frac{m_{DM}}{10^{-20} \text{eV}} \right)$

Right: Axion dark matter coupling limit: $g_{a\tau\tau} < 3 \times 10^{-13} \text{eV}^{-1} \left(\frac{m_{DM}}{10^{-20} \text{eV}} \right)$



Conclusion

Lorentz violation is motivated from Planck-scale theories

There is a worldwide effort to look for Lorentz violation, using various state-of-the-art techniques including neutrinos, but so far, no compelling evidence of Lorentz violation

Lorentz violation occurs in various models including ultralight dark matter

Thank you for your attention!



Backup

Flavor new physics search with effective operators

Standard Model Extension (SME) is an effective field theory to look for Lorentz violation

Standard Model

New physics

$$L = i\bar{\psi}\gamma^\mu\partial_\mu\psi - m\bar{\psi}\psi + \bar{\psi}\gamma^\mu a_\mu \psi + \bar{\psi}\gamma^\mu c_{\mu\nu}\partial^\nu\psi \dots$$

Effective Hamiltonian can be written from here

Standard Model

New physics
(renormalizable)

higher dimension operator
(non-renormalizable)

$$h_{eff} \sim \frac{1}{2E} U^\dagger M^2 U + a_{\alpha\beta}^{(3)} - E c_{\alpha\beta}^{(4)} + E^2 a_{\alpha\beta}^{(5)} - E^3 c_{\alpha\beta}^{(6)} \dots$$

$E^3 c_{\alpha\beta}^{(6)} = E^3 \begin{pmatrix} c_{ee}^{(6)} & c_{e\mu}^{(6)} & c_{\tau e}^{(6)} \\ c_{e\mu}^{(6)*} & c_{\mu\mu}^{(6)} & c_{\mu\tau}^{(6)} \\ c_{\tau e}^{(6)*} & c_{\mu\tau}^{(6)*} & c_{\tau\tau}^{(6)} \end{pmatrix}$

IceCube is sensitive to higher dimension operators

dimension-6 operator natural scale: $c^{(6)} \sim \frac{1}{M_{Planck}^2} \sim 10^{-38} GeV^{-2}$

Flavor new physics search with effective operators

We start from isotropic model of nonminimal SME

$$h_{eff} \sim \frac{1}{2E} U^\dagger M^2 U + a_{\alpha\beta}^{(3)} - E c_{\alpha\beta}^{(4)} + E^2 a_{\alpha\beta}^{(5)} - E^3 c_{\alpha\beta}^{(6)} + E^4 a_{\alpha\beta}^{(7)} - E^5 c_{\alpha\beta}^{(8)} \dots$$

Neutrino oscillation formula is written with mixing matrix elements and eigenvalues

$$P_{\alpha \rightarrow \beta}(E, L) = 1 - 4 \sum_{i>j} \text{Re}(V_{\alpha i}^* V_{\beta i}^* V_{\alpha j} V_{\beta j}) \sin^2 \left(\frac{\lambda_i - \lambda_j}{2} L \right) + 2 \sum_{i>j} \text{Im}(V_{\alpha i}^* V_{\beta i}^* V_{\alpha j} V_{\beta j}) \sin \left((\lambda_i - \lambda_j) L \right)$$

However, astrophysical neutrinos propagate O(100Mpc) $\rightarrow$ lost coherence

$$P_{\alpha \rightarrow \beta}(E, \infty) \sim 1 - 2 \sum_{i>j} \text{Re}(V_{\alpha i}^* V_{\beta i}^* V_{\alpha j} V_{\beta j}) = \sum_i |V_{\alpha i}|^2 |V_{\beta i}|^2$$

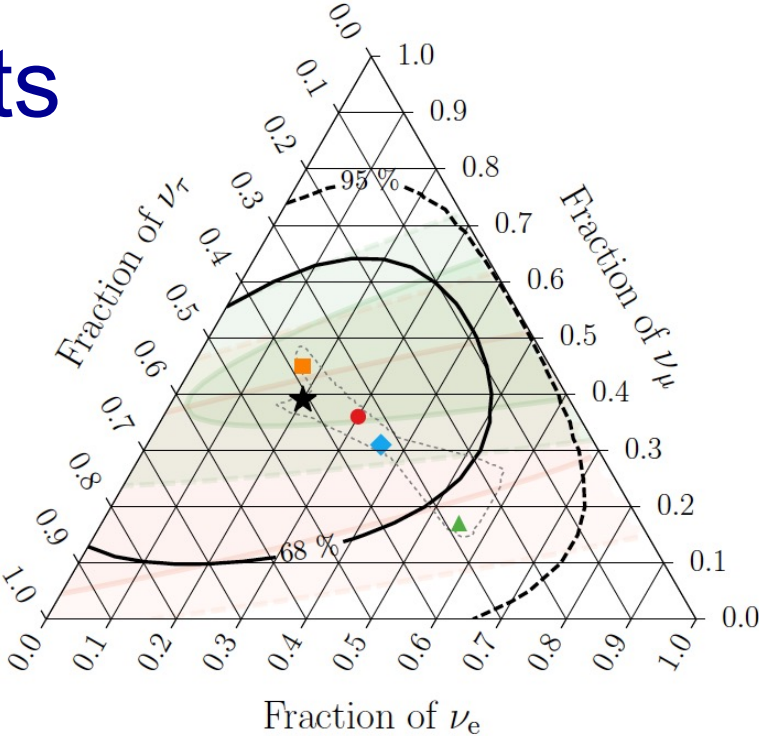
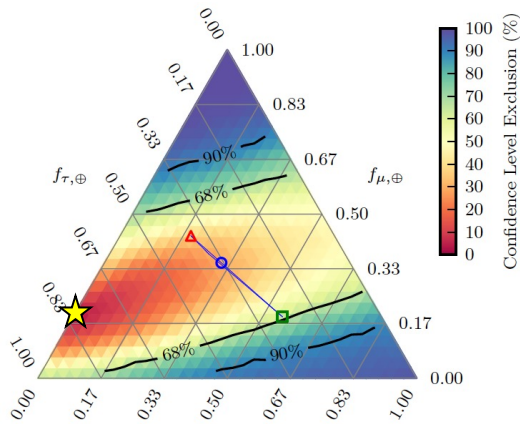
Finally, fraction of neutrino flavour b on the earth is

$$\alpha_\beta^\oplus \sim \int_{E_{min}}^{E_{max}} \sum_\alpha P_{\alpha \rightarrow \beta}(L \rightarrow \infty, E) \phi_\alpha(E) dE$$

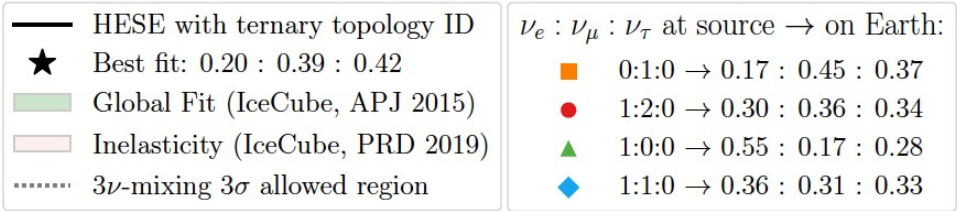
$\rightarrow$ Information of small Lorentz violation is encoded on **neutrino mixing probability**,
by measuring (tasting) **astrophysical neutrino flavours**, you can explore Lorentz violation

IceCube flavor ratio measurements

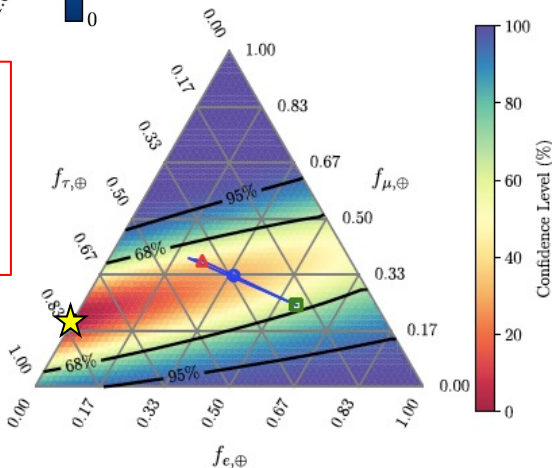
IceCube
1st flavour ratio result
(0.0:0.2:0.8)



IceCube
2nd flavour ratio result
(0.5:0.5:0.0)



IceCube
3rd flavour ratio result
(0.0:0.2:0.8)



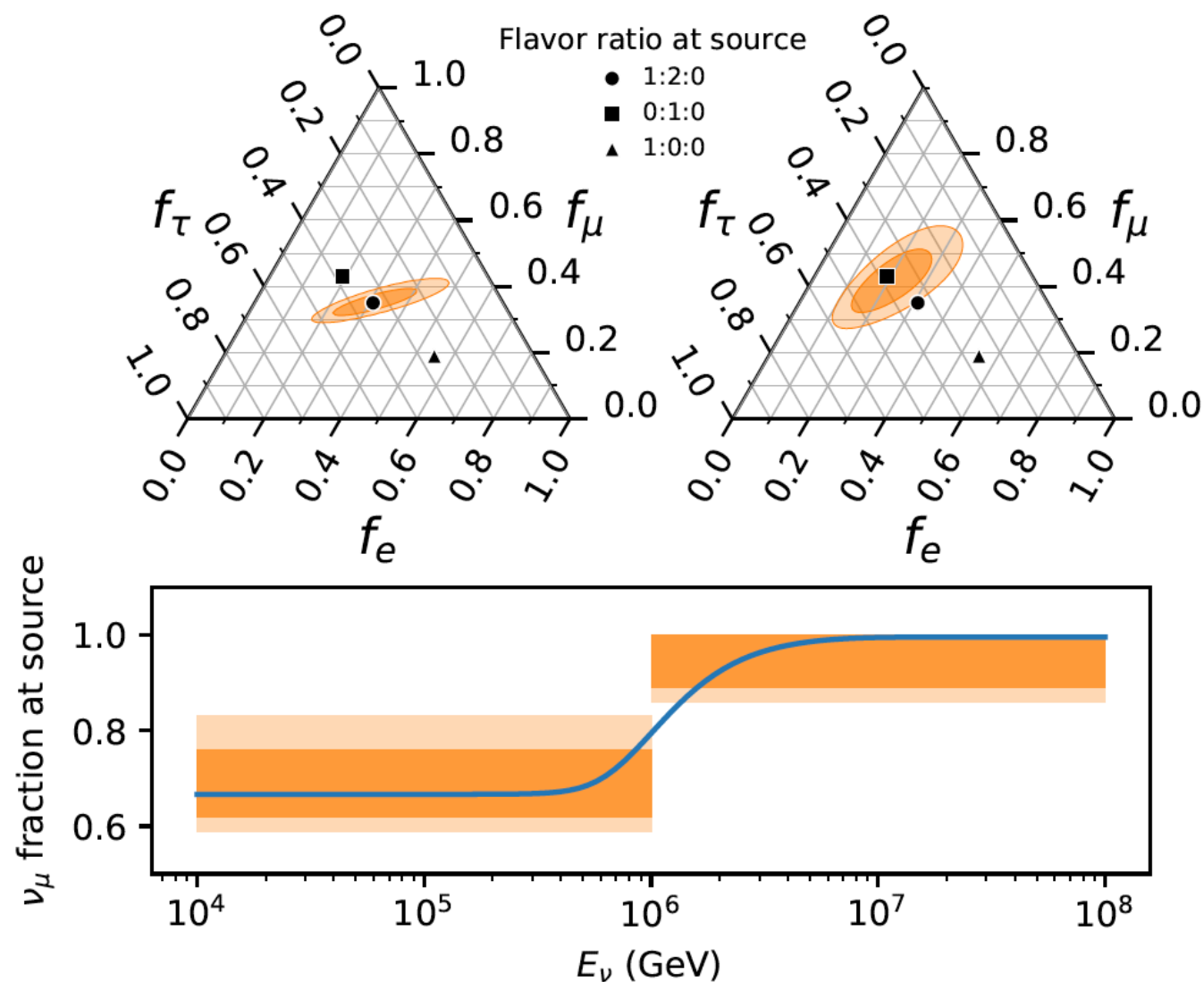
2018 flavour ratio measurement

- Likelihood is very shallow and fit often confuses between ν_e and ν_τ
- Flavour ratio result has some power to distinguish ν_e and ν_τ

Energy dependence of flavor ratio

Muon neutrino increases at higher energy

Future higher-statistics flavor measurement

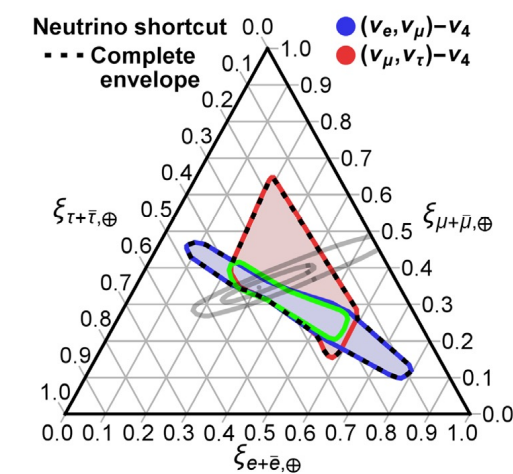
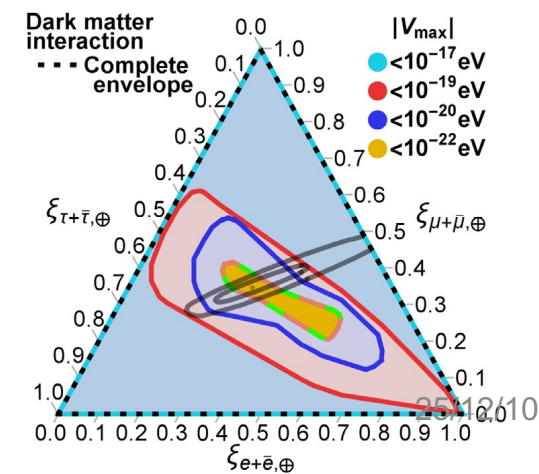
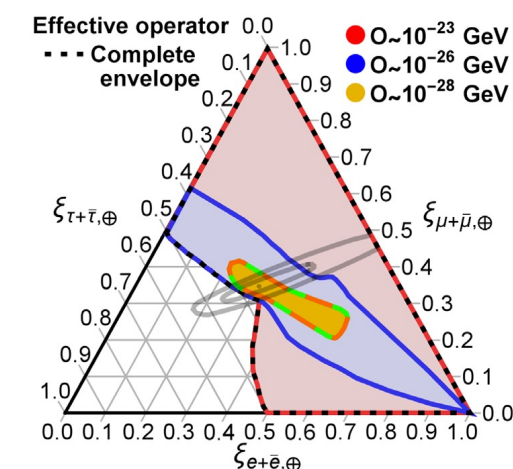
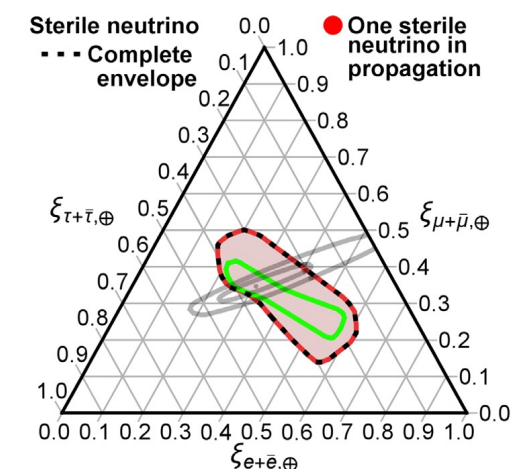
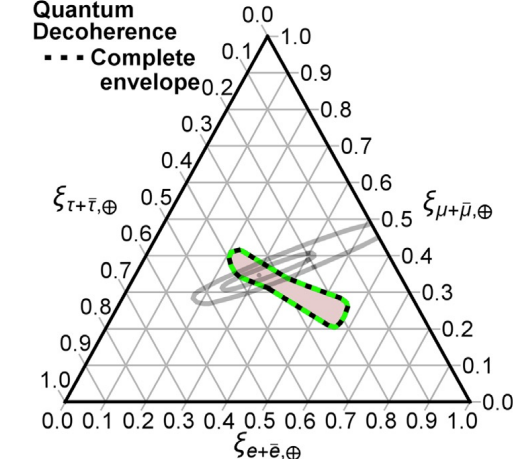
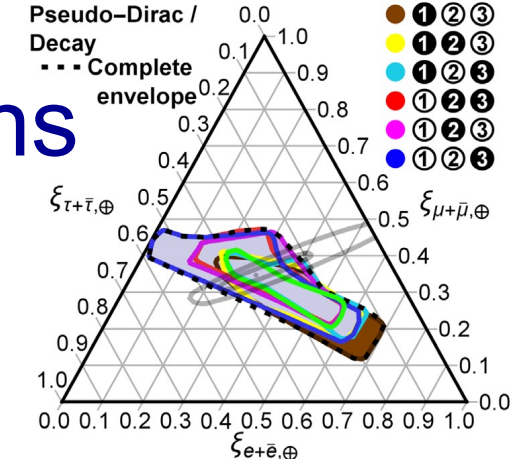


New physics flavor ratio predictions

New physics models have different flavor ratios

Effective operator

- It includes Lorentz violation
- Assuming all possible standard production models, $(\nu_e:\nu_\mu:\nu_\tau) = (x:1-x:0)$, it covers 2/3 of the phase space.



High-energy, long propagating neutrinos - summary

High energy astrophysical neutrinos have amazing new physics sensitivity, and it will increase more

Multi-messenger astronomy

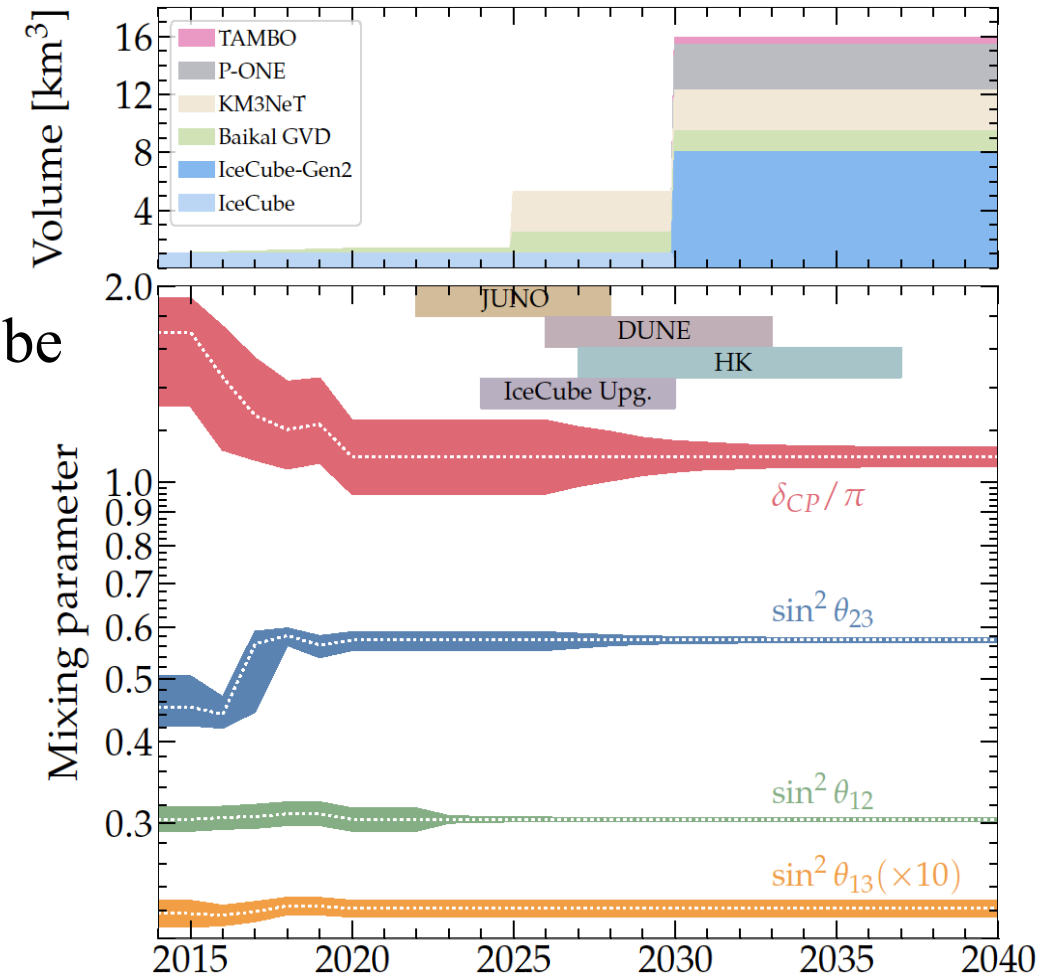
- High-energy astrophysical neutrino model errors will be reduced (spectrum, flavor, direction, time)

New neutrino telescopes

- Higher statistics to reach higher energy events

Neutrino physics

- Oscillation parameter errors will be reduced



Time varying ultra-light dark matter coupling with neutrinos

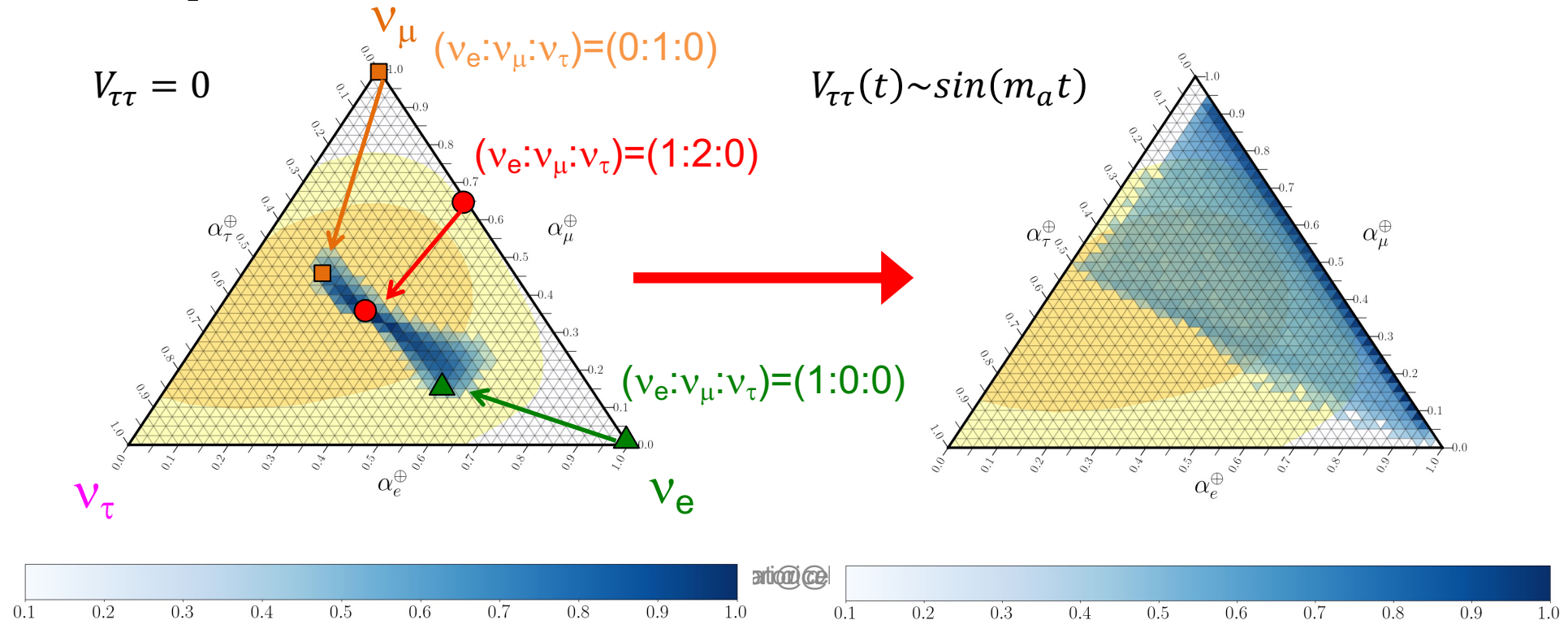
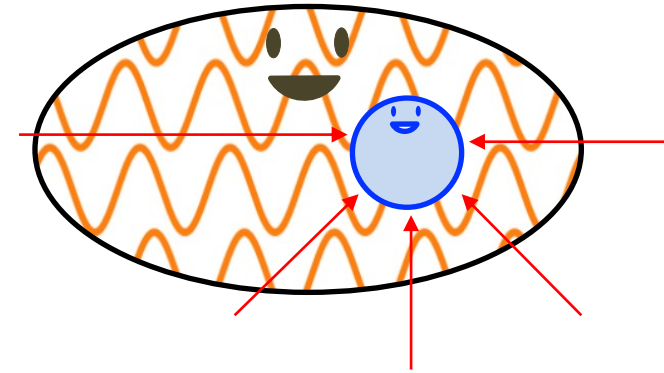
On average, dark matter potential is zero.

$$V_{\tau\tau}(t) = g_{a\tau\tau} m_a a_0 \sin(m_a t) \xrightarrow{t \rightarrow \infty} 0$$

However, dark matter potential smear flavour ratio for each neutrino

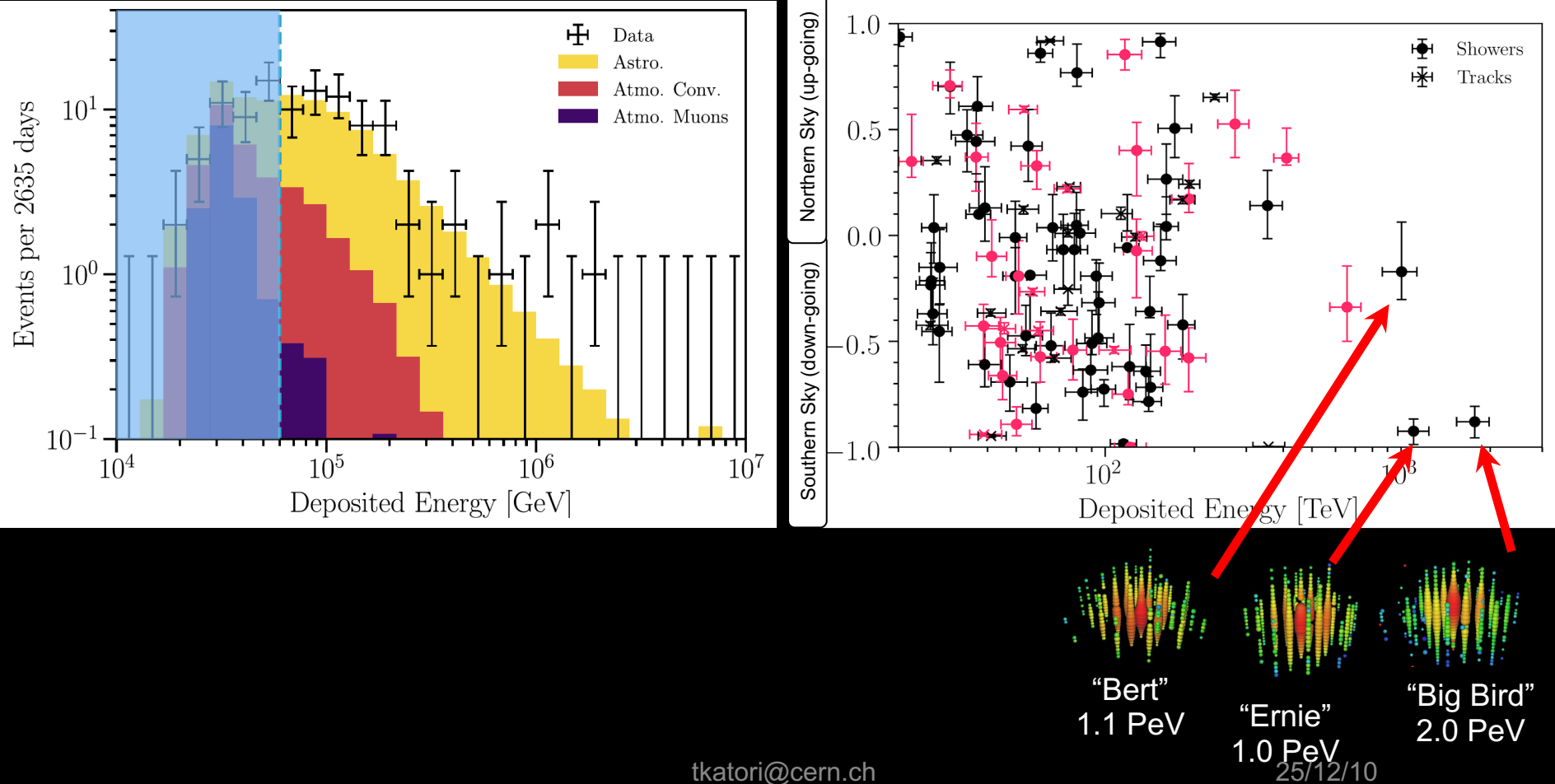
We calculate flavour prediction points with oscillating dark matter potential which smears predicted flavour ratio

$$\rho_{\text{DM}} = 0.3 \text{ GeV/m}^3$$



High-energy astrophysical neutrinos

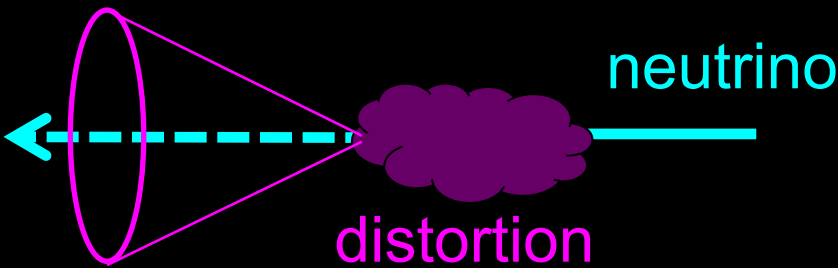
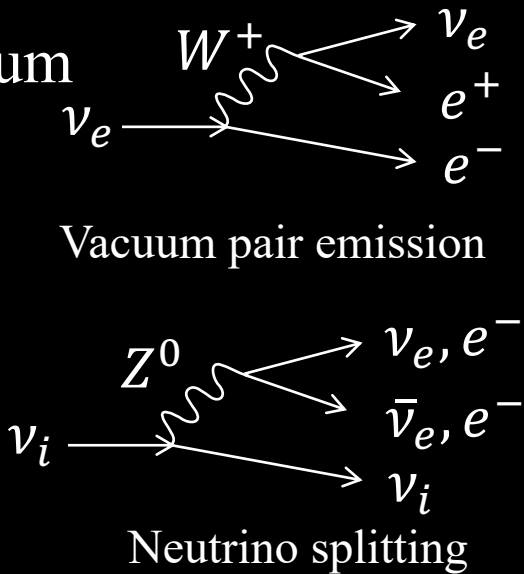
60TeV- 2PeV astrophysical neutrinos are observed by IceCube Neutrino Observatory
high-energy starting event (HESE) sample



Test of Spacetime properties with Astrophysical neutrinos

Lorentz violation = Media in vacuum

- Spectrum distortion (energy)
- Time of Flight (time)
- Anomalous mixing (flavour)

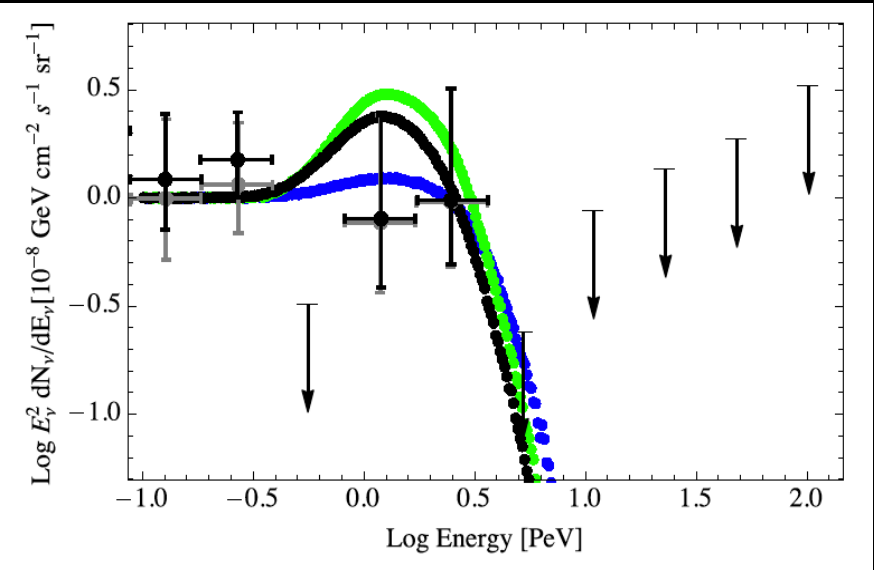


Lorentz violating field cause radiation in vacuum

- High-energy neutrinos are attenuated
- KM3NeT 220 PeV neutrino (KM3-230213A)

$$\delta \equiv c_v^2 - 1 < 4 \times 10^{-22}$$

Diffuse neutrino spectrum distortion



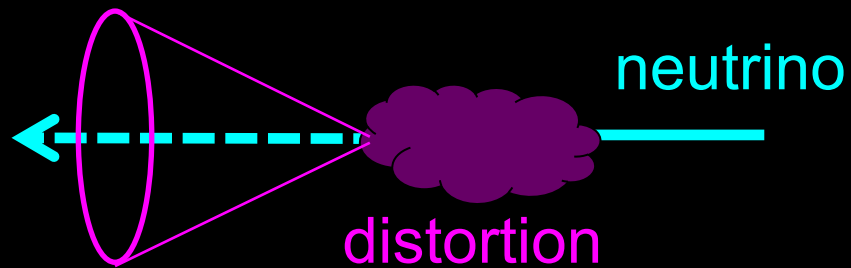
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Spectrum distortion happen by other scenarios

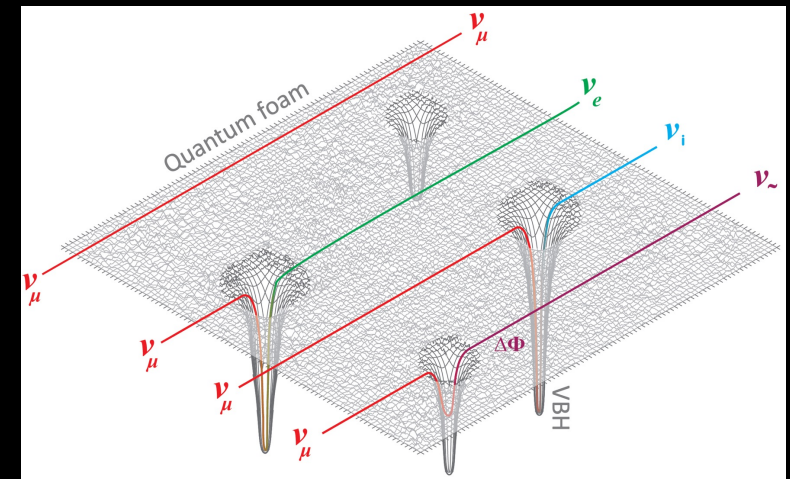
- “missing” neutrinos by micro black-hole (neutrino-loss quantum decoherence)
- Strong limits from SN1987A (cf. neutrino decay)



Lorentz violating field cause radiation in vacuum

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Test of Spacetime properties with Astrophysical neutrinos

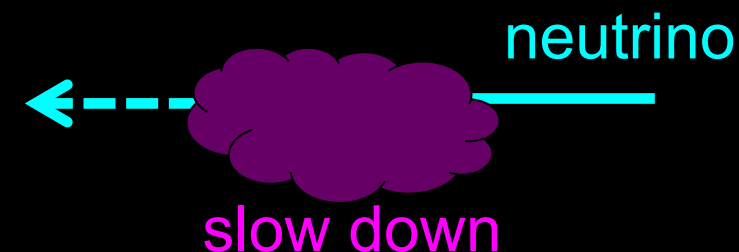
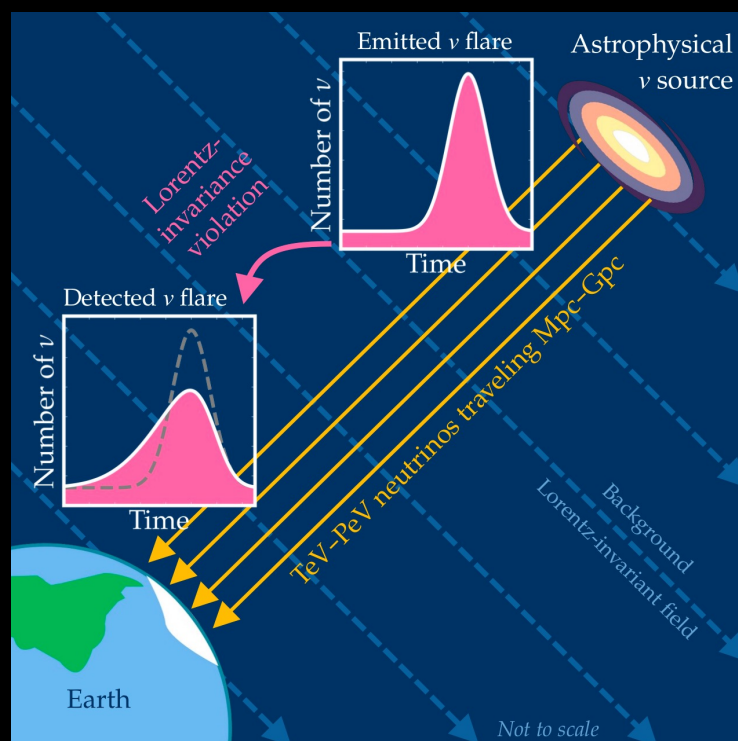
New physics search

- Spectrum distortion (energy)
- **Time of Flight (time)**
- Anomalous mixing (flavour)

Modified dispersion due to quantum foam
 cause unexpected delay/advance for neutrinos

- Neutrino time-of-flight ($a^{(5)}$ =CPT odd)

$$\delta v \sim E a^{(5)} + E^2 c^{(6)} + \dots$$



Time distribution is modified due to
 Lorentz violation (energy-dependent)

Test of Spacetime properties with Astrophysical neutrinos

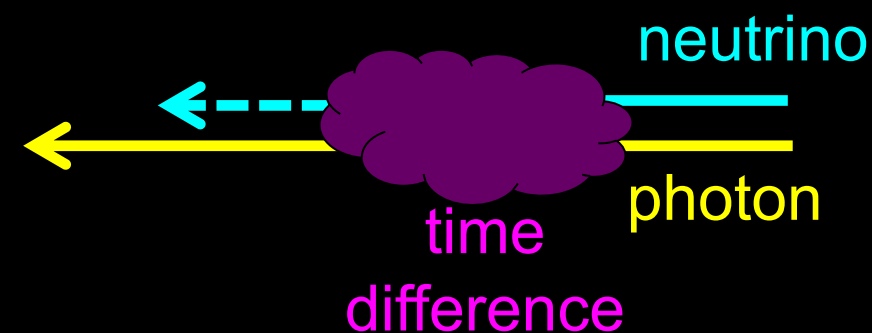
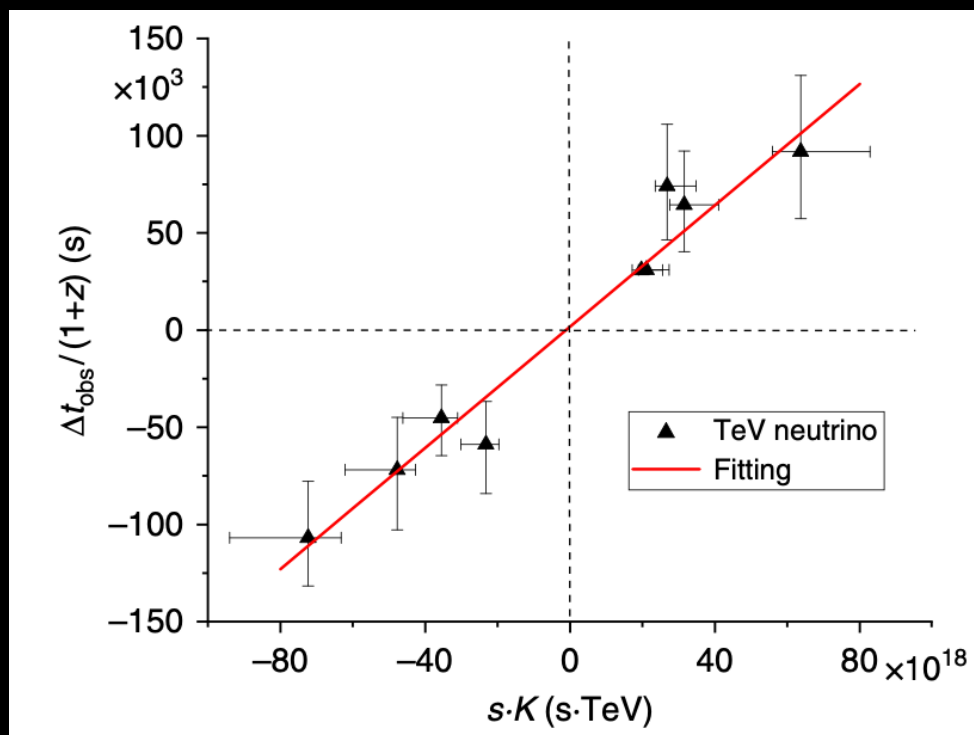
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Neutrinos and gamma-ray bursts may
have coincidence with Lorentz violation

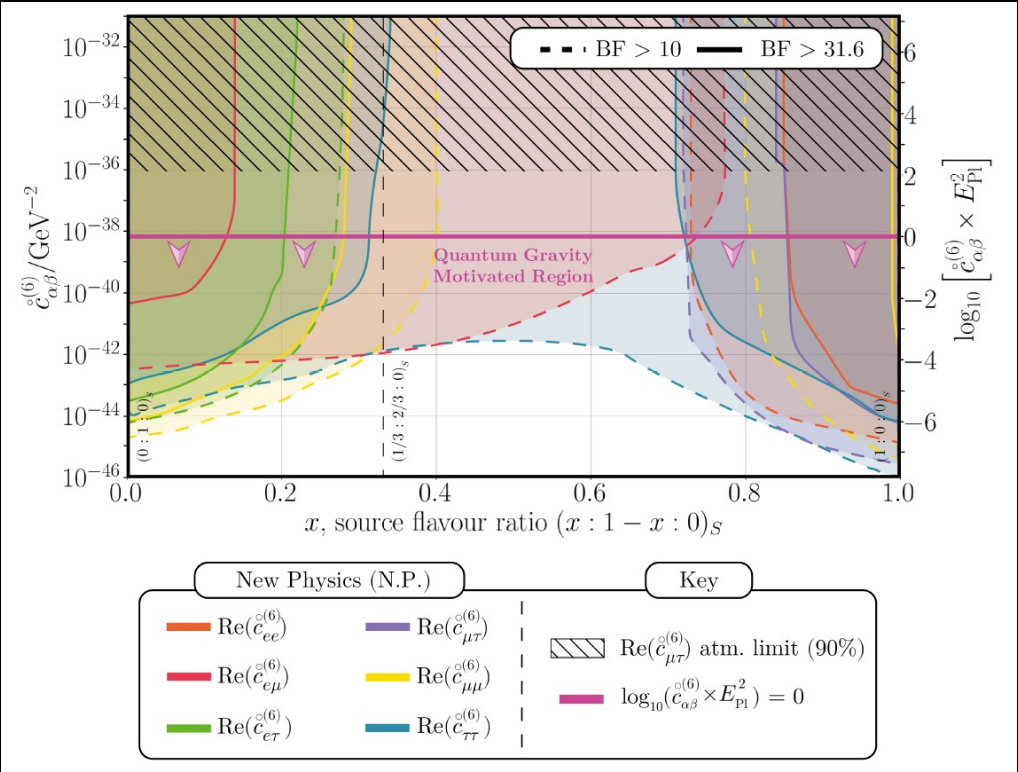
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Flavour effect

- Macroscopic quantum effect and sensitive to small effects
 - Sensitive to the target signal region of Lorentz violation
- ($< 10^{-38} \text{ GeV}^{-2}$ for dim-6 operators)



Flavour
change



Mixing

Neutrino

