

Bayesian Inference of the Reheating Temperature in Thermal Leptogenesis

Naturalness as typicality in the seesaw parameter space

NPN2026 (The Hirosawa City Center, Mito)

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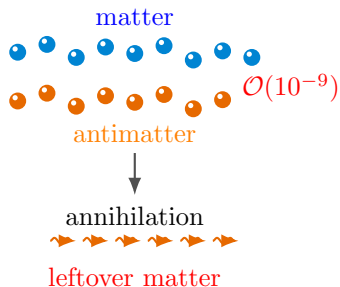
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Matter–antimatter asymmetry

In the early Universe, particles and antiparticles were almost equally abundant.



- ✓ Pair annihilation leaves only a **tiny excess**.
- ✓ Observed value:

$$\eta_B \equiv \frac{n_B - n_{\bar{B}}}{n_\gamma} \simeq 6.1 \times 10^{-10}.$$

- ✓ The Standard Model satisfies neither enough CP violation nor a strong enough departure from equilibrium.

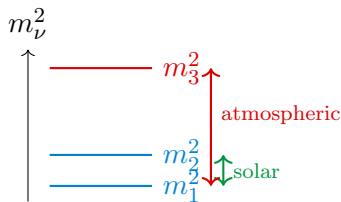
Question: Can the same new physics explain this number and neutrino masses?

Two facts pointing beyond the Standard Model

Neutrino oscillations

$$\Delta m_{21}^2 \simeq 7.4 \times 10^{-5} \text{ eV}^2$$

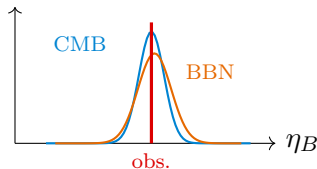
$$|\Delta m_{31}^2| \simeq 2.5 \times 10^{-3} \text{ eV}^2.$$



Baryon asymmetry

$$\Omega_b h^2 \simeq 0.022, \quad \eta_B \simeq 6.1 \times 10^{-10}.$$

likelihood



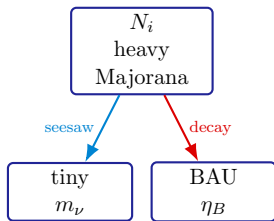
A minimal and economical extension is **SM + heavy right-handed Majorana neutrinos**.

Type-I seesaw: one extension, two targets

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + i\bar{N}_i\gamma^\mu\partial_\mu N_i - \ell_\alpha h_{\alpha i} N_i \tilde{H} - \frac{1}{2} M_i \bar{N}_i^c N_i + \text{h.c.}$$

$$m_\nu^{\text{tree}} = m_D M_R^{-1} m_D^T, \quad m_D = v h.$$

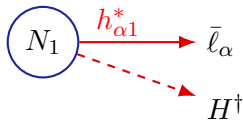
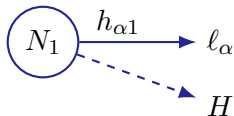
- ✓ Small m_ν follows naturally for large M_R .
- ✓ Majorana mass violates lepton number.
- ✓ Complex Yukawa matrix gives new CP phases.



thermal leptogenesis
links particle physics
and cosmology

Thermal leptogenesis in one slide

CP-violating N_1 decays

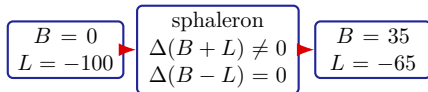


$$\Gamma(N_1 \rightarrow \ell H) \neq \Gamma(N_1 \rightarrow \bar{\ell} H^\dagger)$$

$$\varepsilon_1 = \frac{\Gamma(N_1 \rightarrow \ell H) - \Gamma(N_1 \rightarrow \bar{\ell} H^\dagger)}{\Gamma(N_1 \rightarrow \text{all})}$$

$$\eta_B \simeq 0.0096 \varepsilon_1 \kappa_f, \quad 0 \leq \kappa_f \leq 1.$$

Sphaleron redistribution



$B - L$ is conserved
in the SM plasma

$$B = \frac{28}{79}(B-L), \quad L = -\frac{51}{79}(B-L).$$

Why a reheating-temperature bound appears

η_B in the vanilla picture:

$$\eta_B \simeq 0.0096 \varepsilon_1 \kappa_f$$

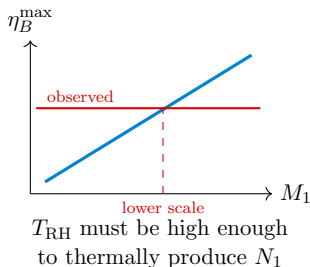
For hierarchical heavy neutrinos,

$$|\varepsilon_1| \leq \frac{3M_1}{16\pi v^2} (m_3 - m_1).$$

Davidson–Ibarra bound

Therefore, the maximal baryon asymmetry scales linearly with M_1 :

$$\eta_B^{\max} = \text{Constant} \times M_1.$$



Conventional estimates give a scale around

$$M_1, T_{\text{RH}} \gtrsim 10^{9-10} \text{ GeV},$$

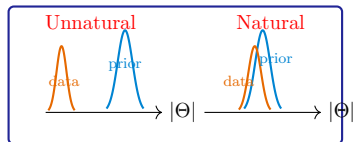
depending on hierarchy, flavor, and degeneracy.

Our question: typicality, not only existence

A low T_{RH} point may exist after tuning parameters.

Question:

How typical is successful leptogenesis at each (M_0, T_{RH}) ?



Naturalness = overlap of likelihood and prior.

- ✓ Prior expresses “anarchy-like” flavor ignorance.
- ✓ Likelihood imposes oscillation data and η_B .
- ✓ Evidence measures overlap between prior volume and data.

Bayesian setup

$$\pi(Y, M) = \frac{8}{\pi^{15} Y_0^{18} M_0^{12}} \exp \left[-\frac{\text{tr}(Y^\dagger Y)}{Y_0^2} - \frac{\text{tr}(M^\dagger M)}{M_0^2} \right].$$

$$L(x) = \prod_i \frac{1}{\sqrt{2\pi}\sigma_i} \exp \left[-\frac{(x_i - x_i^{\text{obs}})^2}{2\sigma_i^2} \right].$$

$$x_i = \{\sin^2 \theta_{ij}, \delta_{\text{CP}}, \Delta m_{31}^2, \Delta m_{21}^2 / \Delta m_{31}^2, \eta_B\}.$$

Without leptogenesis

$$Z_{Y_0, M_0} = \int dY dM L_\nu(Y, M) \pi(Y, M),$$

With thermal leptogenesis

$$Z_{M_0, T} = \left\langle \exp \left[-\frac{(\eta_B^{\text{th}} - \eta_B^{\text{obs}})^2}{2(\Delta\eta_B)^2} \right] \right\rangle_0.$$

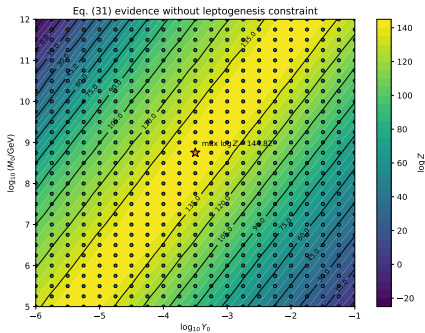
The average is over the analytically reduced seesaw measure after imposing low-energy neutrino data.

Result I: natural seesaw scale

- ✓ First, ignore the η_B constraint.
- ✓ Evidence tests whether neutrino data prefer a particular seesaw scale.
- ✓ In the scale-invariant limit, the analytic calculation predicts no sharp M_0 preference.

$$\tilde{Z}(M_0) = \text{const.}$$

The numerical contour is consistent with **no typical seesaw mass scale** from oscillation data alone.



Result II: natural leptogenesis scale

Evidence to be evaluated on

$$10^8 \text{ GeV} < M_0 < 10^{14} \text{ GeV},$$

$$10^8 \text{ GeV} < T_{\text{RH}} < 10^{14} \text{ GeV}.$$

- ✓ Draw Monte Carlo points once from the reduced measure.
- ✓ Reuse them for each (M_0, T_{RH}) and average the η_B likelihood.
- ✓ Perturbativity condition:
 $|Y_{\alpha i}| < \sqrt{4\pi}$.

Take-home message

Low- T_{RH} solutions may exist, but they are not typical in the seesaw parameter space.

