

Search for Dark Neutrino via Vacuum Magnetic Birefringence Experiment

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Collaborators:

X. Fan (Harvard Univ.), S. Kamioka, S. Asai (Tokyo Univ.) experiment
A. Sugamoto (Ochanomizu Univ., OIJ) theory

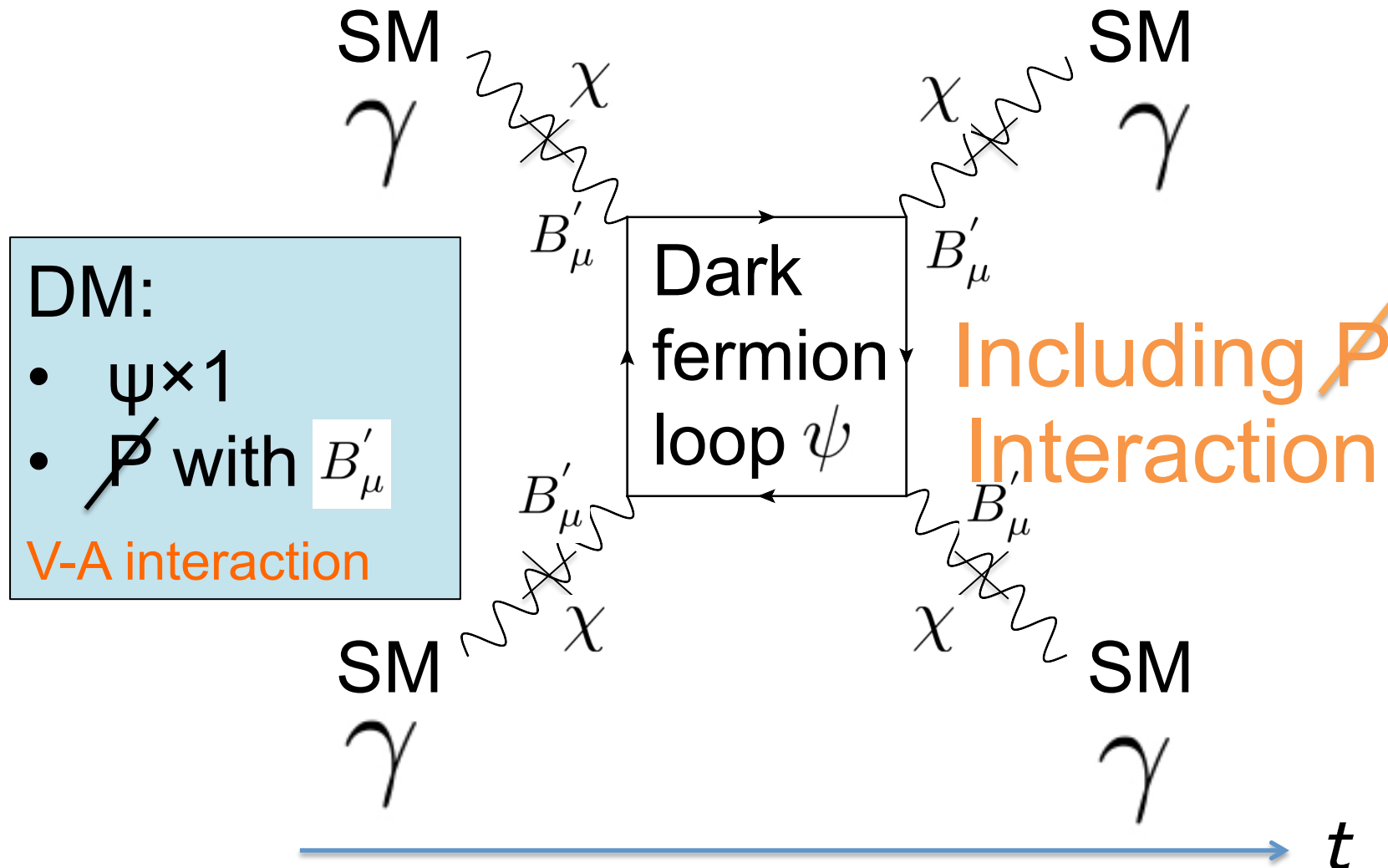
PTEP **2017** no. 12, 123B03 (2017), arXiv:1707.03609
(arXiv:1707.03308)

KEK-PH 2018
Feb. 16th 2018
KEK, Tsukuba

Including Dark Matter as New Physics

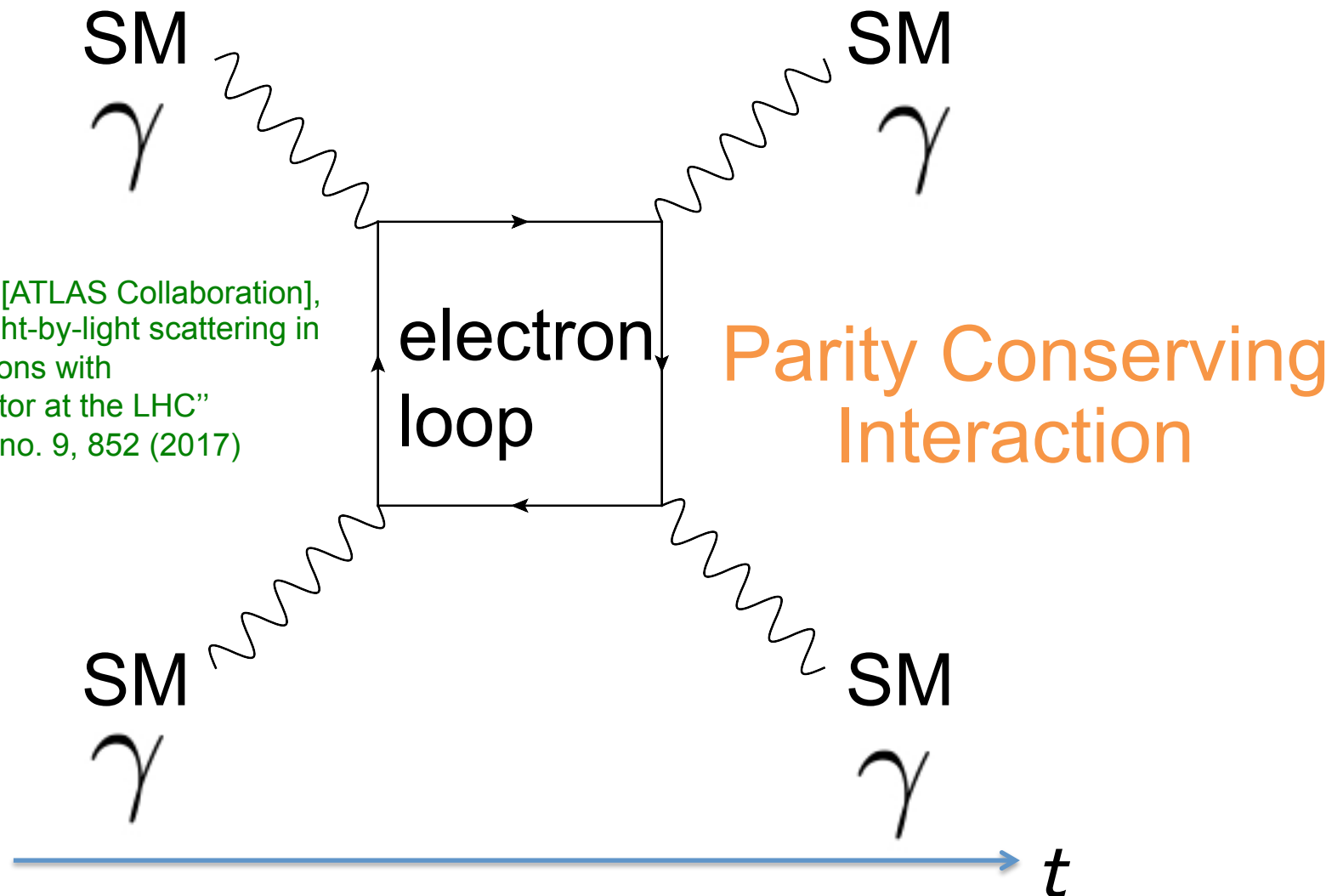
Dark Matter Search

$$\chi \ll 1$$



cf. QED interaction

M. Aaboud *et al.* [ATLAS Collaboration],
“Evidence for light-by-light scattering in
heavy-ion collisions with
the ATLAS detector at the LHC”
Nature Phys. **13**, no. 9, 852 (2017)



Need to Calculate Effective Lagrangian → Vacuum Birefringence Experiment

already
known

QED Case

W. Heisenberg, H. Euler, Z. Phys. **98**, 714 (1936)

Heisenberg-Euler Lagrangian:

$$\mathcal{L} = -\mathfrak{F} - \frac{1}{8\pi^2} \int_0^\infty ds s^{-3} \exp(-m^2 s)$$

$$\times \left[(es)^2 \mathfrak{G} \frac{\text{Re coshes} X}{\text{Im coshes} X} - 1 - \frac{2}{3} (es)^2 \mathfrak{F} \right]$$

$$= \frac{1}{2} (\mathbf{E}^2 - \mathbf{H}^2) + \frac{2\alpha^2 (\hbar/mc)^3}{45 mc^2} \times [(\mathbf{E}^2 - \mathbf{H}^2)^2 + 7(\mathbf{E} \cdot \mathbf{H})^2] + \dots$$

$$X = \sqrt{2(\mathcal{F} + i\mathcal{G})},$$

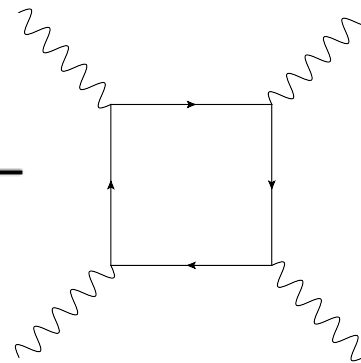
$$\mathcal{F} = \frac{1}{4} F_{\mu\nu} F^{\mu\nu} = \frac{1}{2} (\vec{H}^2 - \vec{E}^2)$$

$$\mathcal{G} = \frac{1}{4} F_{\mu\nu} \tilde{F}^{\mu\nu} = \vec{E} \cdot \vec{H}$$

$$\tilde{F}_{\mu\nu} = \frac{1}{2} \epsilon_{\mu\nu\lambda\rho} F^{\lambda\rho}$$

from J. Schwinger,
Phys. Rev. **82**, 664 (1951)

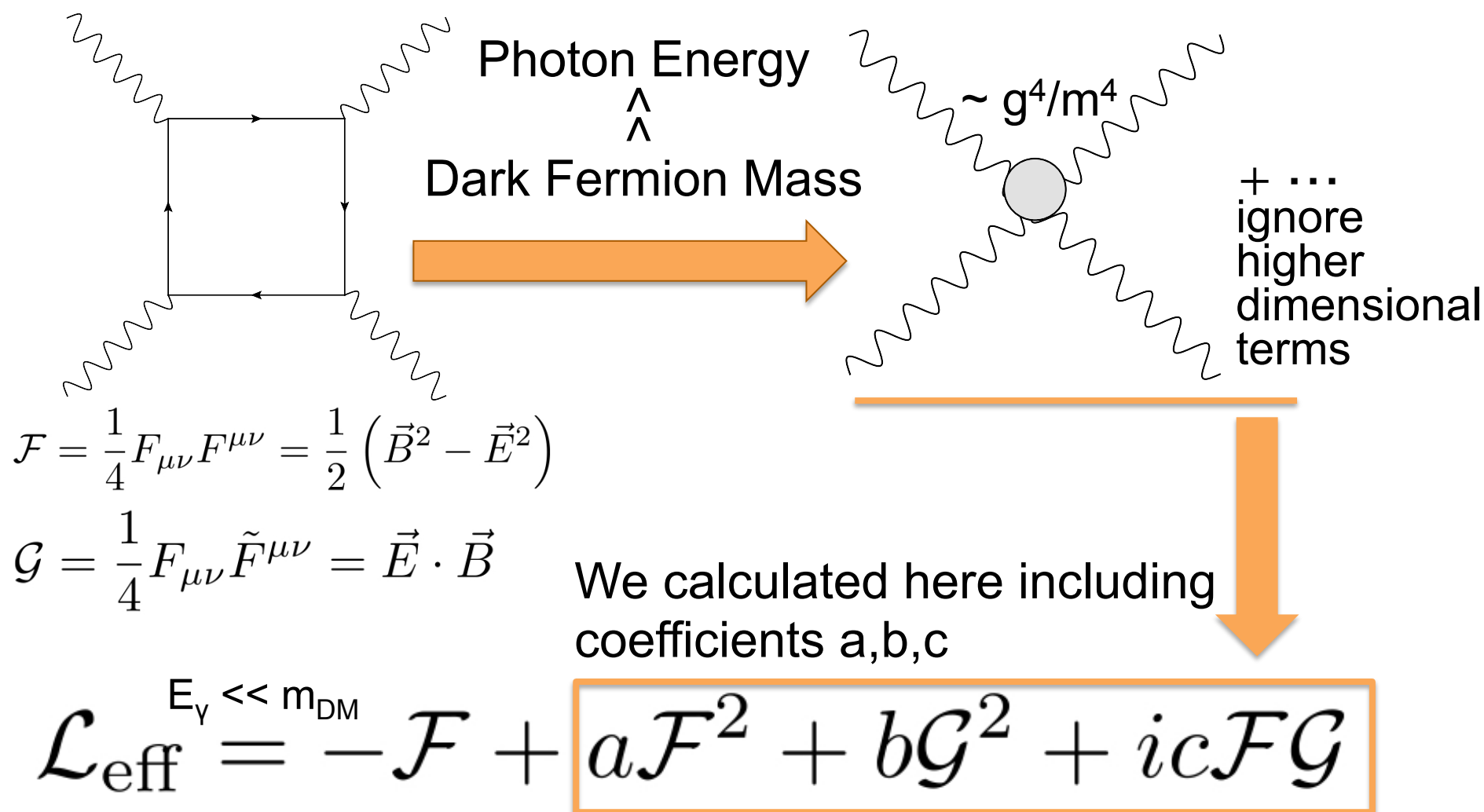
$$\mathcal{L}_{\text{eff}} = -\frac{1}{4} F_{\mu\nu}^2 + \text{diagram} + \dots$$



related to this

- constant background electromagnetic field $F_{\mu\nu}$
- electron 1-loop diagrams

Dark Sector Case (1/3)



Dark Sector Case (2/3)

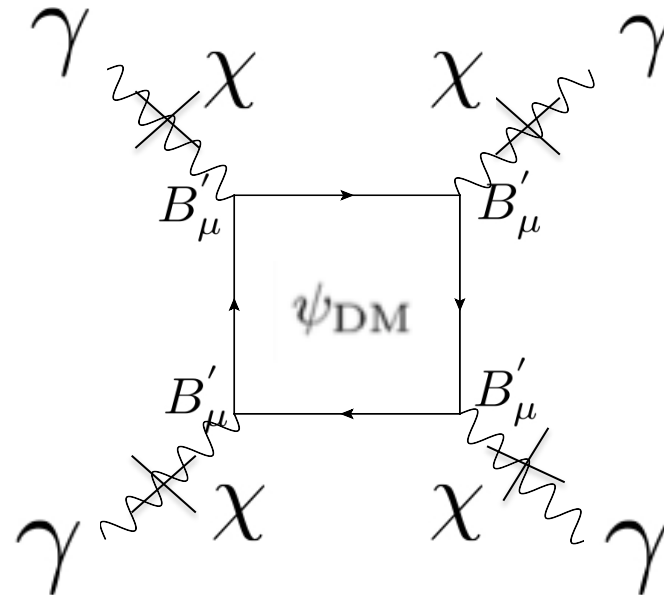
$$\tilde{A}^\mu = A_{\text{SM}}^\mu + \chi B'^\mu \quad \chi \ll 1$$

photon in our
theory
(massless)

ordinary
photon in
SM

extra U(1)
gauge boson

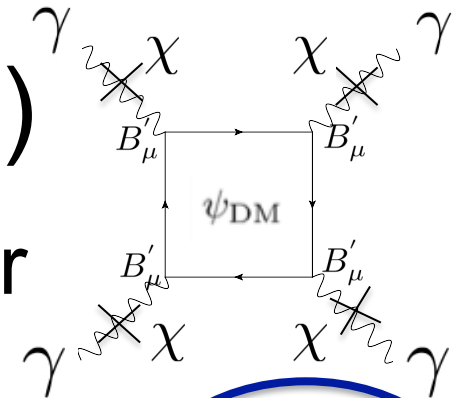
$$\mathcal{L} = \bar{\psi}_{\text{DM}} [\gamma^\mu (i\partial_\mu - (g_V + g_A \gamma_5) B'_\mu) - m_{\text{DM}}] \psi_{\text{DM}}$$



Dark Sector Case (3/3)

- Effective Lagrangian of Fourth Order

Our work: PTEP **2017** no. 12, 123B03 (2017)



$$\mathcal{L}_{\text{eff}} = -\mathcal{F} + \chi^4 (a\mathcal{F}^2 + b\mathcal{G}^2 + ic\mathcal{F}\mathcal{G})$$

$$\mathcal{F} = \frac{1}{4} F_{\mu\nu} F^{\mu\nu} = \frac{1}{2} (\vec{B}^2 - \vec{E}^2) \quad \mathcal{G} = \frac{1}{4} F_{\mu\nu} \tilde{F}^{\mu\nu} = \vec{E} \cdot \vec{B}$$

$$a = \frac{1}{(4\pi)^2 m^4} \left(\frac{8}{45} g_V^4 - \frac{4}{5} g_V^2 g_A^2 - \frac{1}{45} g_A^4 \right)$$

$$b = \frac{1}{(4\pi)^2 m^4} \left(\frac{14}{45} g_V^4 + \frac{34}{15} g_V^2 g_A^2 + \frac{97}{90} g_A^4 \right)$$

$$c = \frac{1}{(4\pi)^2 m^4} \left(\frac{4}{3} g_V^3 g_A + \frac{28}{9} g_V g_A^3 \right) \quad \begin{array}{l} c=0 \text{ when} \\ g_A \text{ or } g_V \text{ is 0} \end{array}$$

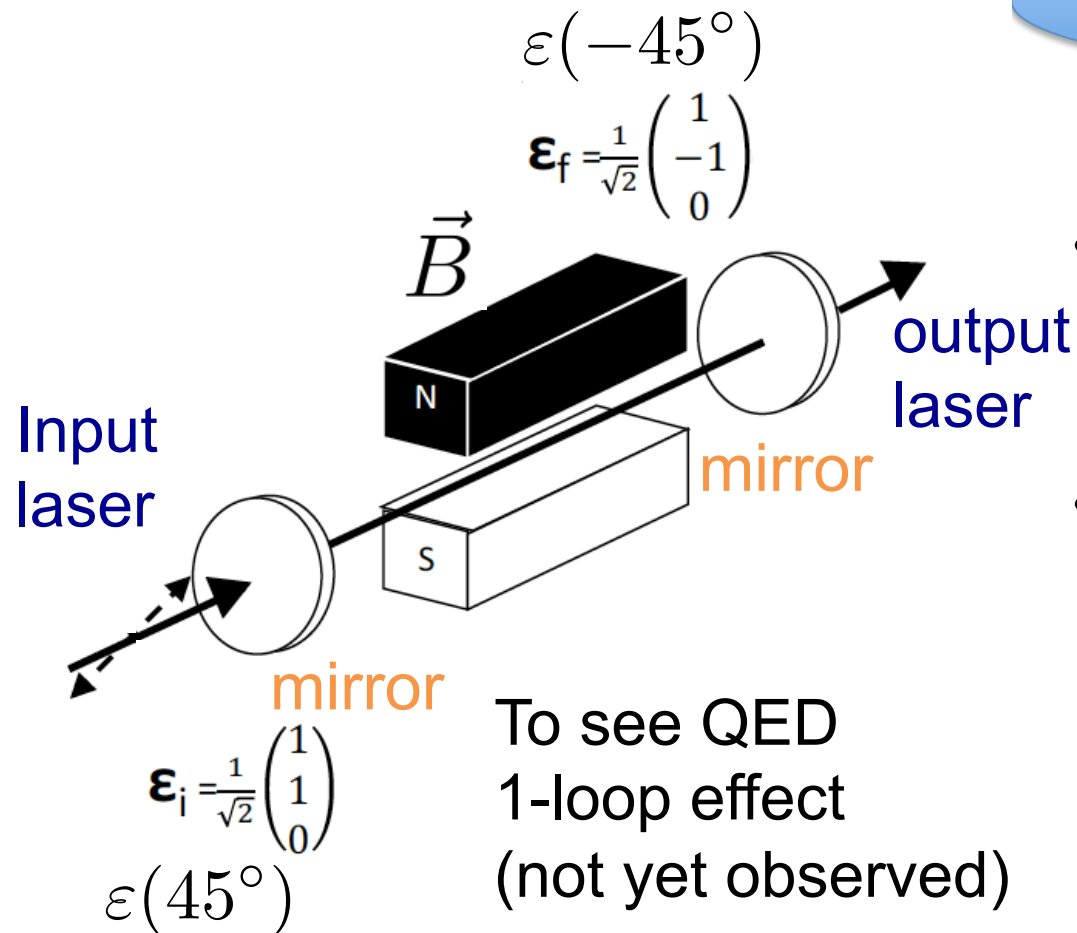
We followed a method developed by Schwinger J. Schwinger,
Phys. Rev. **82**, 664 (1951)

Vacuum Magnetic Birefringence Experiment (1/5)

X. Fan *etal.* Eur. Phys. J. D **71**, no. 11, 308 (2017)

- OVAL (Observing Vacuum with Laser) experiment

Conventional



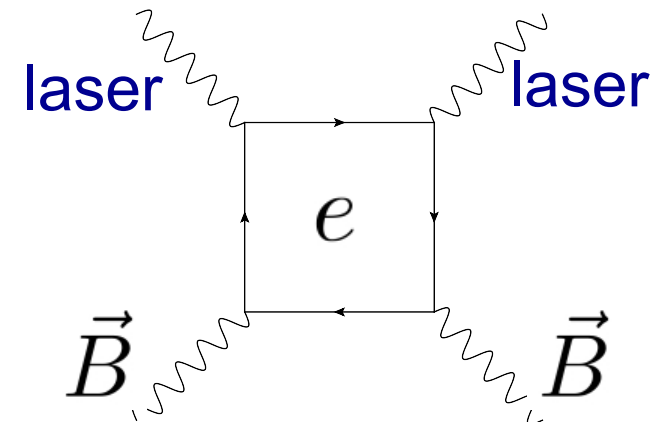
Tabletop experiment

Eur. Phys. J. D (2014) **68**: 16

- BMV experiment

Eur. Phys. J. C (2016) **76**: 24

- PVLAS experiment



Vacuum Magnetic Birefringence Experiment (2/5)

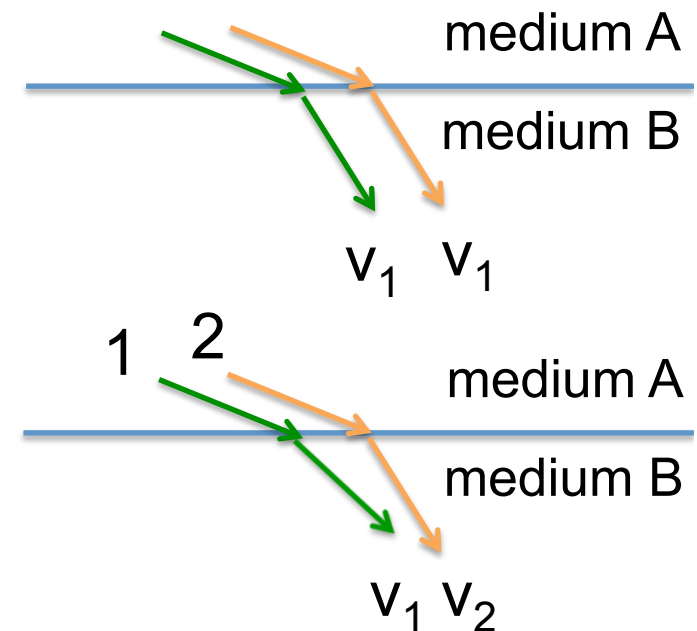
- refractive index: n
- phase velocity: v
 $\rightarrow n = 1/v$

refractive:

changing phase velocity of the light

birefringence:

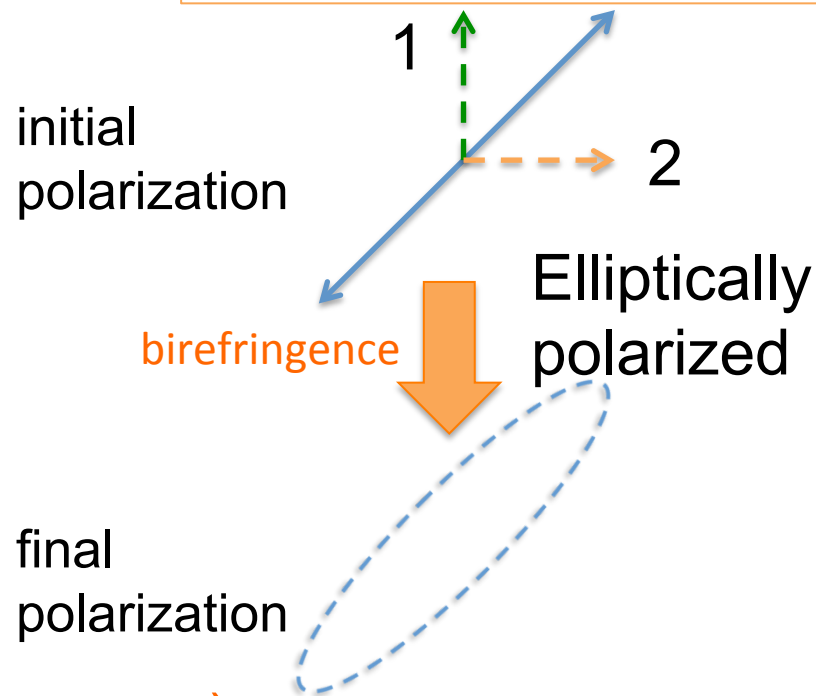
changing phase velocity of 2 light polarizations in different ways



Vacuum Magnetic Birefringence Experiment (3/5)

To detect birefringence,
we observe a difference of polarization state

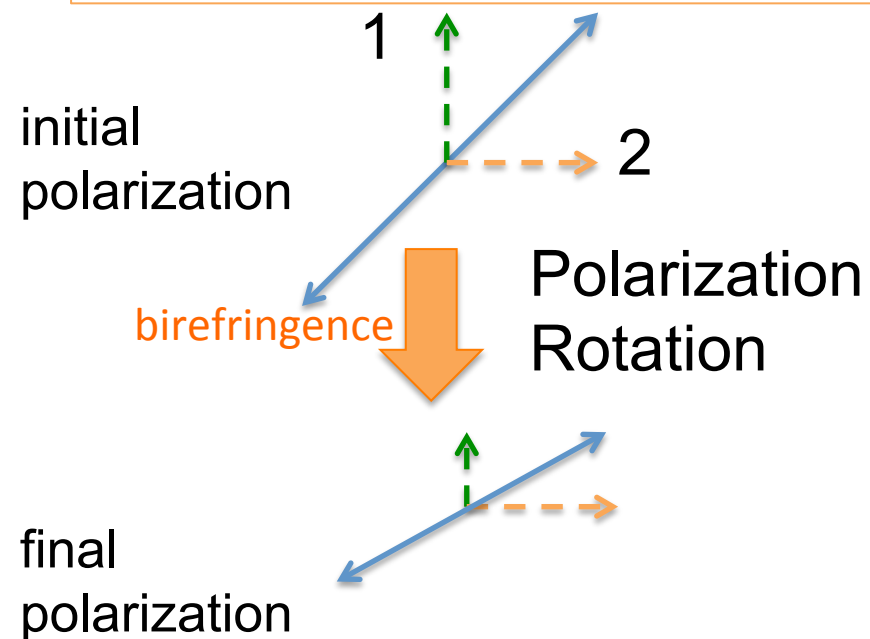
1) Ellipticity



ex)

- QED
- dark sector in our model

2) Direction of the long axis of an ellipse

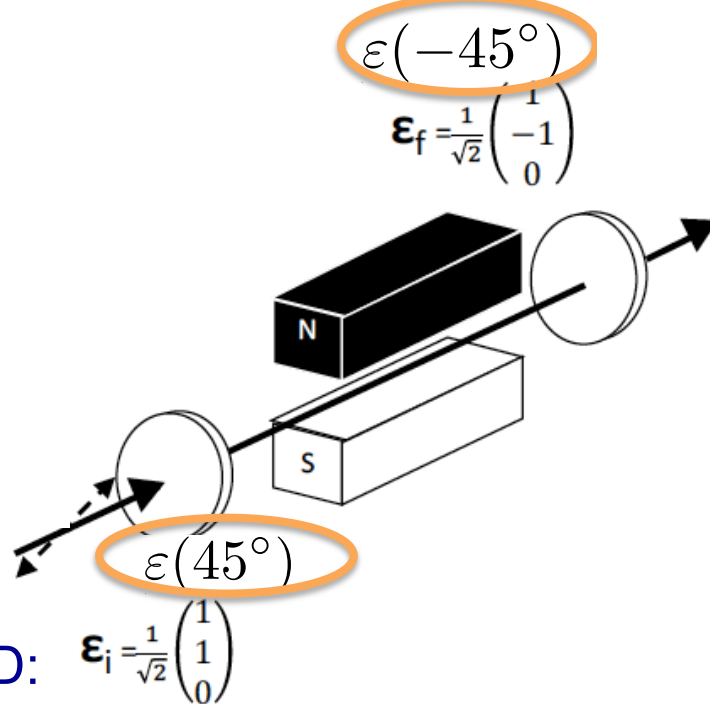


ex) dark sector in our model
with ~~ρ~~

Vacuum Magnetic Birefringence Experiment (4/5)

To detect ~~P~~ interaction, we propose a new method

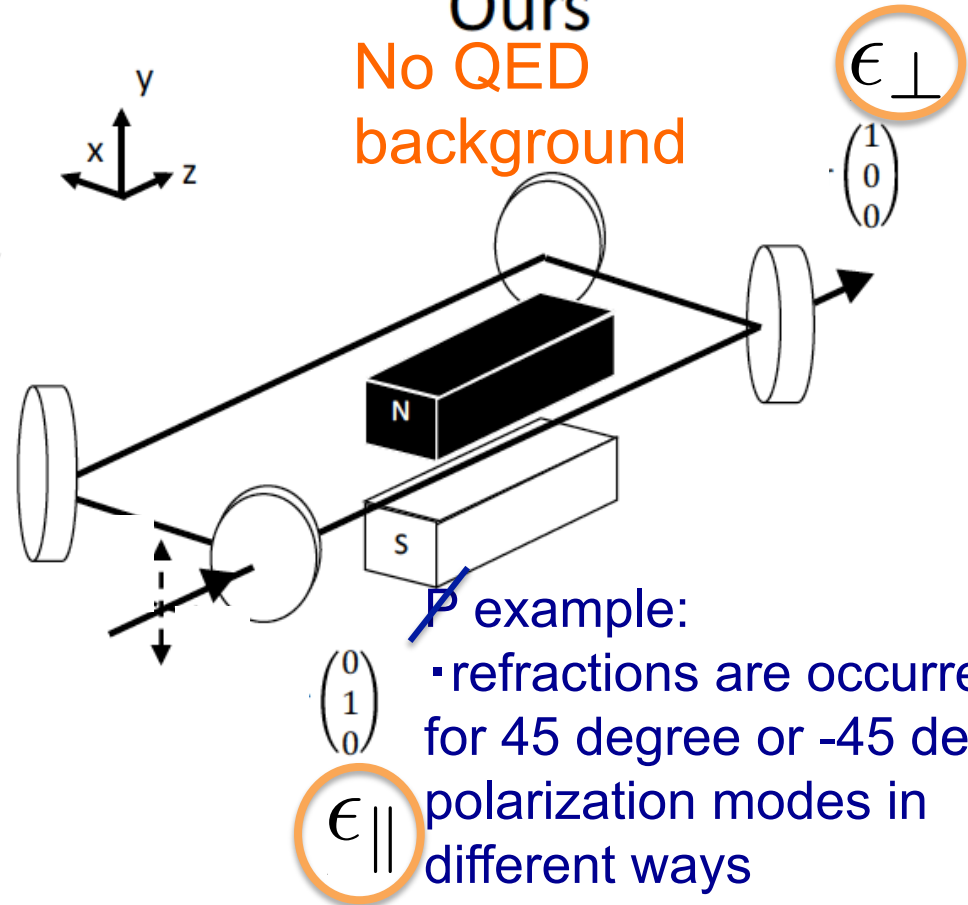
Conventional



- refractions are occurred for parallel (from magnetic field) or perpendicular polarization modes in different ways
- Polarization with 45 degrees includes both modes.
- > We detect -45 degrees to see reflections

Ours

No QED background



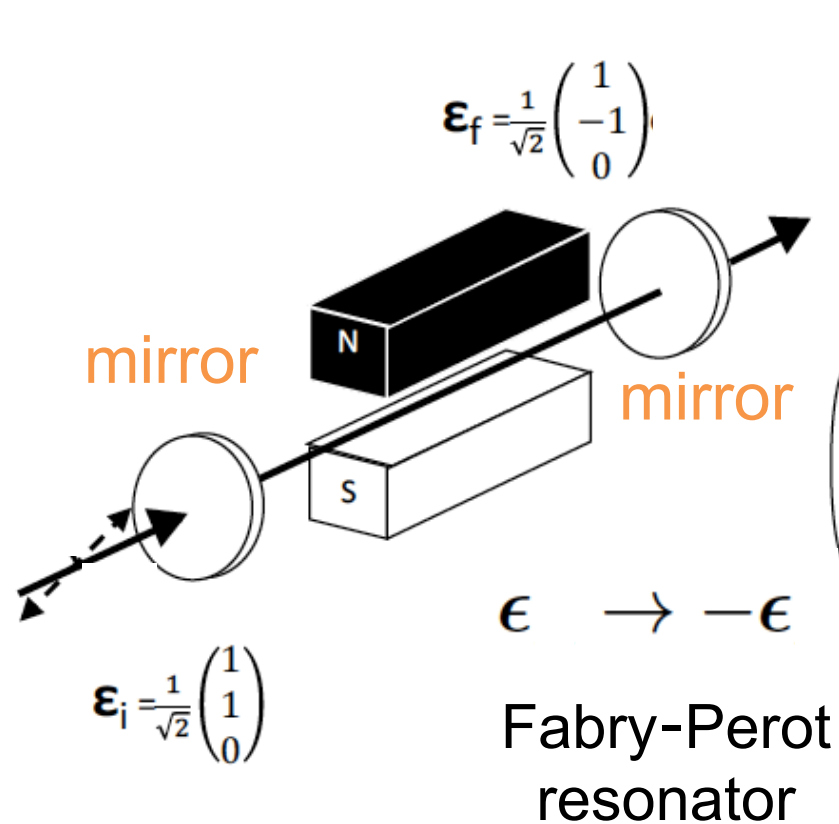
~~P~~ example:

- refractions are occurred for 45 degree or -45 degree polarization modes in different ways
- Polarization with parallel includes both modes.
- > We detect perpendicular to see reflections

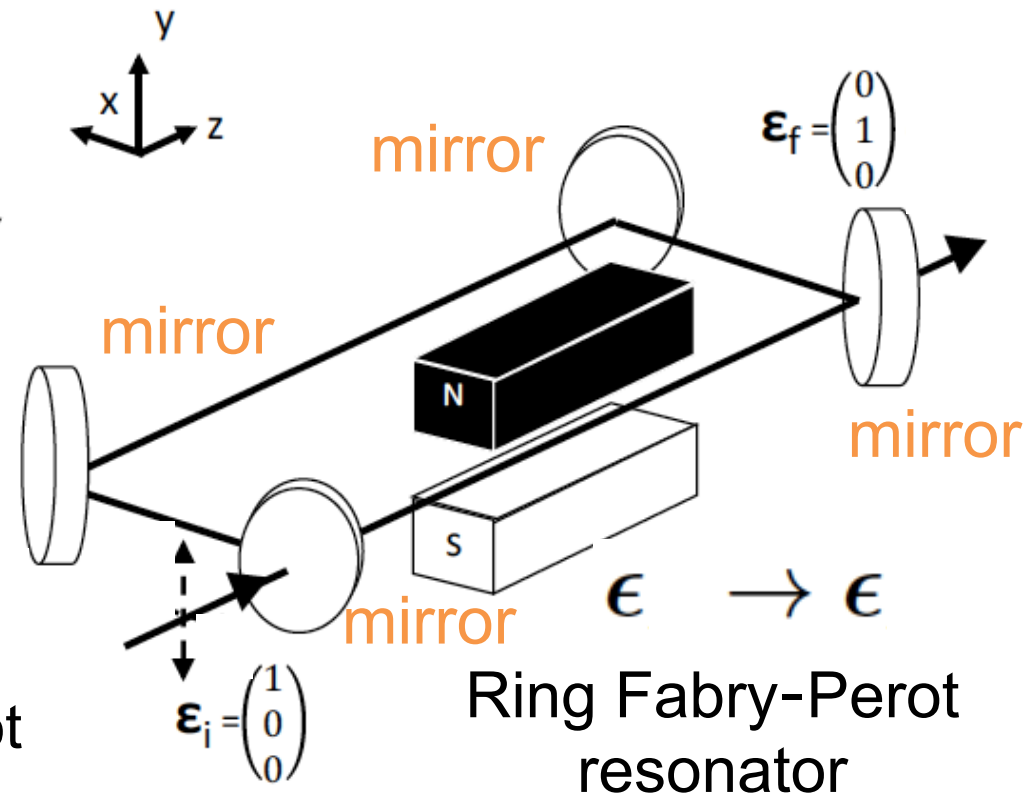
Vacuum Magnetic Birefringence Experiment (5/5)

To detect ~~P~~ interaction, we propose a new method

Conventional



Ours



~~P~~ is reduced if only 2 mirrors ¹¹

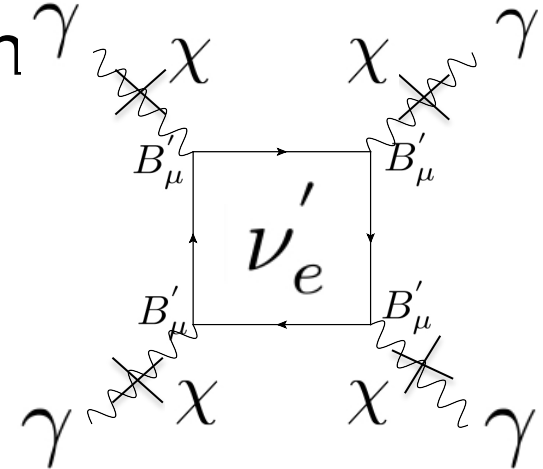
Dark neutrino

$$\mathcal{L} = \bar{\psi}_{\text{DM}} [\gamma^\mu (i\partial_\mu - (g_V + g_A \gamma_5) B'_\mu) - m_{\text{DM}}] \psi_{\text{DM}}$$

We assume $g_A = -g_V (= |e|)$ to obtain
the experimental constraint

↓

V – A current: **Dark neutrino**



We examine the case, having both the electron and the lightest DS neutrino. For the DS search, QED forms the background to the DS signal.

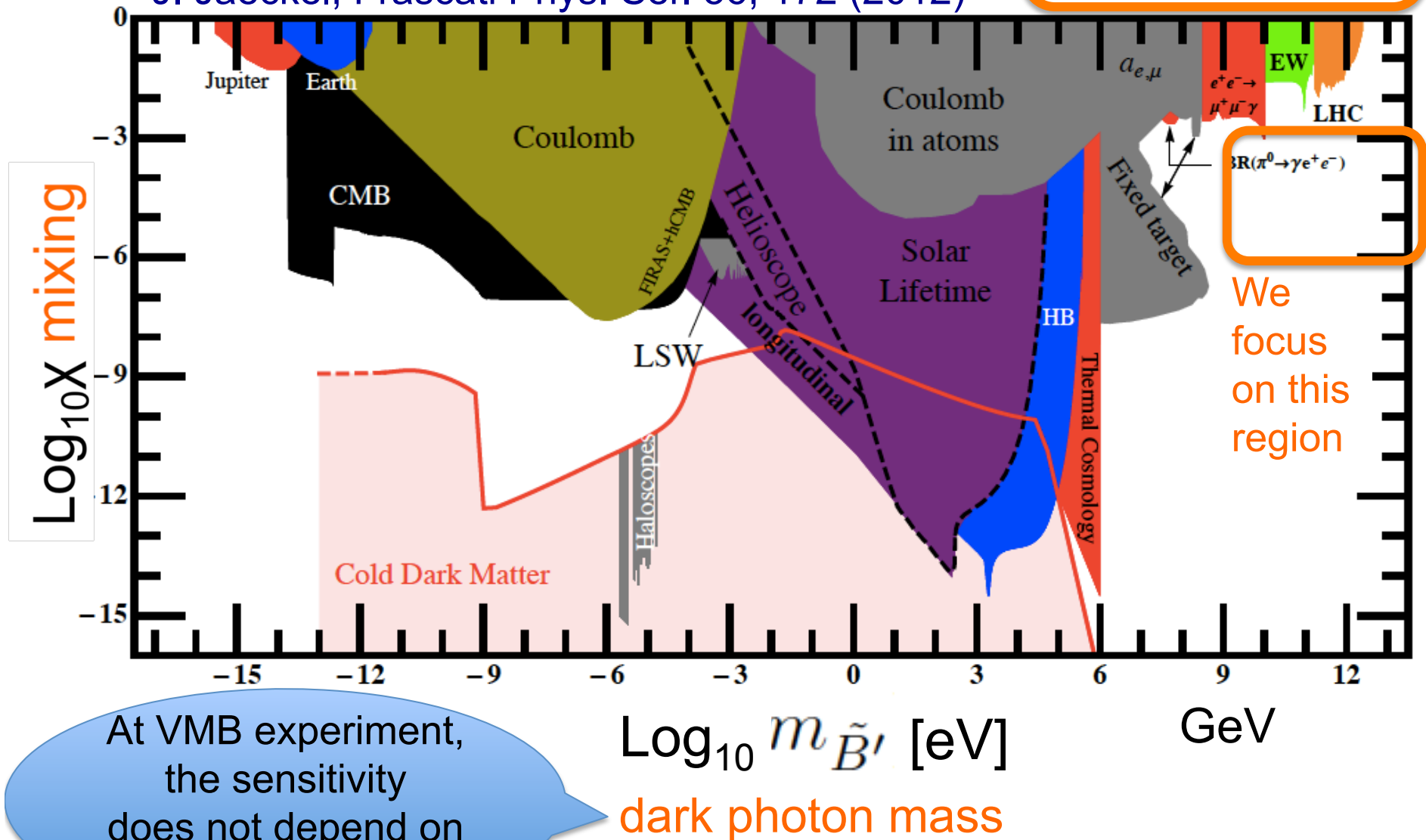
$$a = a_{\text{QED}} + \chi^4 a_{\text{DS}\nu'}, \quad b = b_{\text{QED}} + \chi^4 b_{\text{DS}\nu'}, \quad \text{and} \quad c = \chi^4 c_{\text{DS}\nu'}$$

Allowed region

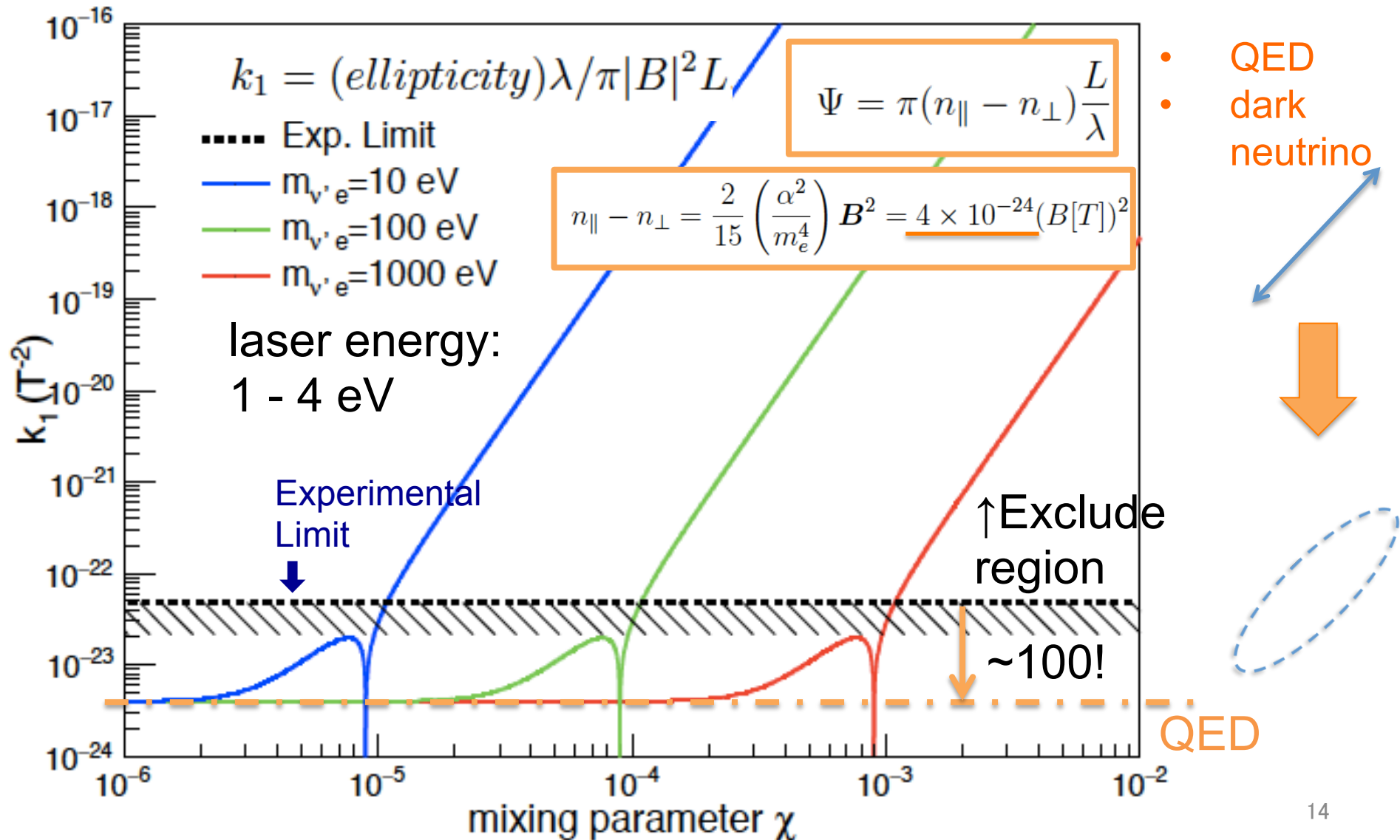
J. Jaeckel, Frascati Phys. Ser. 56, 172 (2012)

$$10^{-6} \leq \chi \leq 10^{-3}$$

$$m_{\tilde{B}'} \geq 1 \text{ GeV}$$

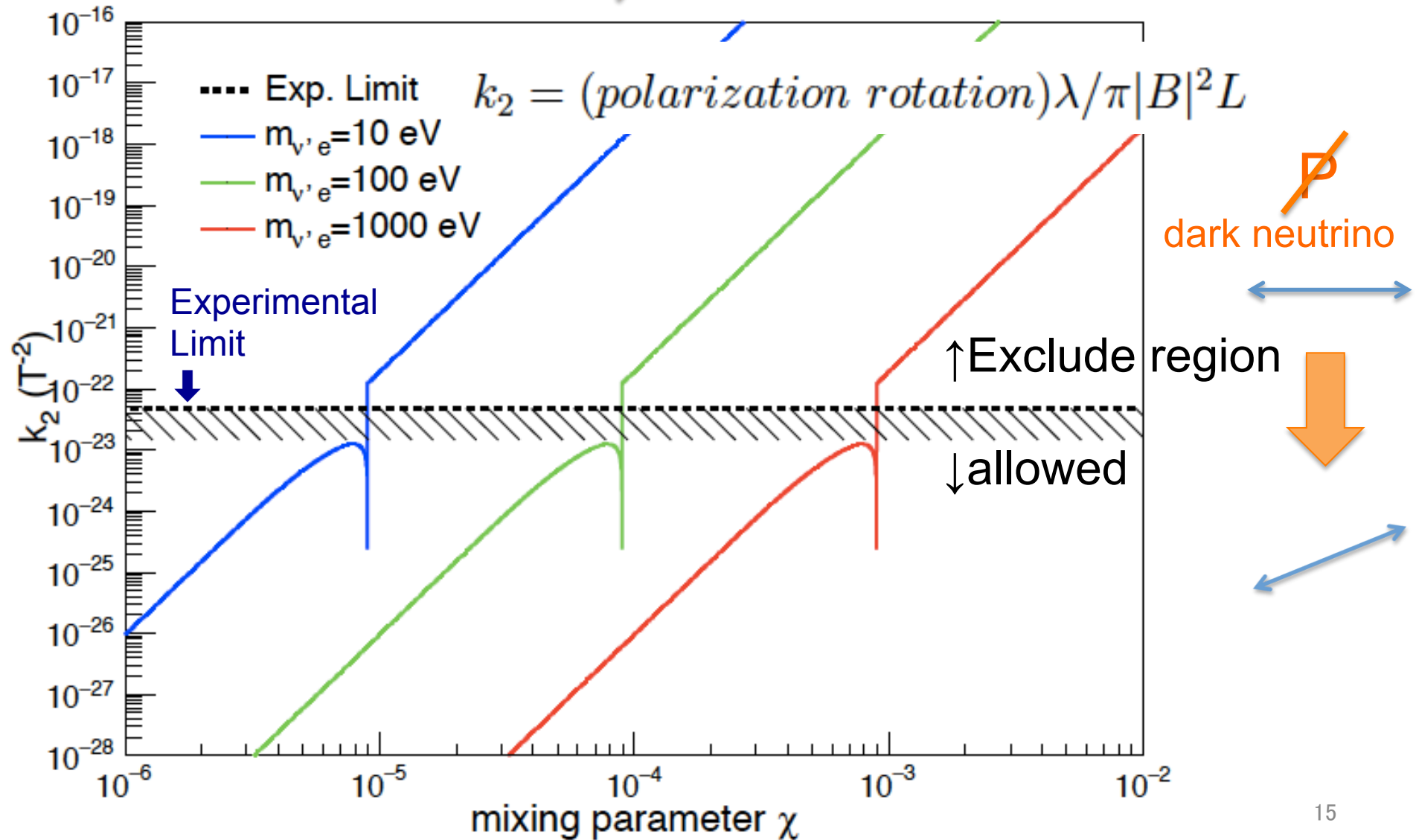


Conventional, QED/Dark neutrino



New set up, dark neutrino only

~~P~~ No QED background



Summary

1. We considered Parity violated dark sector model, and derived generalized Heisenberg-Euler formula
2. Our focus lay on light-by-light scattering effective Lagrangian of fourth order and gave a result:

$$\mathcal{L}_{\text{eff}} = -\mathcal{F} + a\mathcal{F}^2 + b\mathcal{G}^2 + ic\mathcal{F}\mathcal{G}$$

$$\mathcal{F} = \frac{1}{4}F_{\mu\nu}F^{\mu\nu} = \frac{1}{2}(\vec{B}^2 - \vec{E}^2) \quad \mathcal{G} = \frac{1}{4}F_{\mu\nu}\tilde{F}^{\mu\nu} = \vec{E} \cdot \vec{B}$$

$$a = \frac{1}{(4\pi)^2 m^4} \left(\frac{8}{45} g_V^4 - \frac{4}{5} g_V^2 g_A^2 - \frac{1}{45} g_A^4 \right)$$

$$b = \frac{1}{(4\pi)^2 m^4} \left(\frac{14}{45} g_V^4 + \frac{34}{15} g_V^2 g_A^2 + \frac{97}{90} g_A^4 \right)$$

$$c = \frac{1}{(4\pi)^2 m^4} \left(\frac{4}{3} g_V^3 g_A + \frac{28}{9} g_V g_A^3 \right)$$

3. We focused on Vacuum Magnetic Birefringence Experiment to probe the dark sector and proposed new polarization state and the ring resonator in stead of the usual Fabry-Perot resonator to measure the Parity violated term

Backup

Search for Dark Neutrino via Vacuum Magnetic Birefringence Experiment 20'

We consider a dark matter model where a dark matter candidate couples to photons via an extra $U(1)$ mediator and assume that this dark matter candidate is a fermion and can couple to the mediator with parity violation. We derived a low energy effective Lagrangian including a parity violated term for light-by-light scattering by integrating out the dark matter fermion. Our focus lies on Vacuum Magnetic Birefringence Experiment to probe the dark sector. We propose the ring resonator (3-4 mirrors) with an appropriate polarization state of light instead of a usual Fabry-Perot resonator (2 mirrors) with a conventional polarization state of light to measure the Parity violated term. We assume that a dark neutrino is a dark matter, i.e. V-A current, and give constraints on model parameters from a current experimental limit. PTEP 2017 no. 12, 123B03 (2017) (arXiv: 1707.03308 [hep-ph]), arXiv:1707.03609 [hep-ph]

Dark Matter Model (1/3)

SM + $U'(1)_{Y'}$ + 1 Complex Scalar

$$\mathcal{L}_S = \left| \left(i\partial_\mu - g_1 Y_s B_\mu - g'_1 Y'_s \textcircled{B'_\mu} \right) \textcircled{S(x)} \right|^2$$

spontaneously broken  $\langle S \rangle = v_s / \sqrt{2}$

$$\mathcal{L}_{\text{mixing}} = \frac{1}{2} m_{B'}^2 \left(\varepsilon^2 B_\mu B^\mu + 2\varepsilon B_\mu B'^\mu + B'_\mu B'^\mu \right)$$

$$m_{B'} = g'_1 Y'_s v_s \quad \varepsilon \equiv \frac{g_1 Y_s}{g'_1 Y'_s}$$

$$m_{B'} = g'_1 Y'_s v_s$$

Dark Matter Model (2/3)

$$\varepsilon \equiv \frac{g_1 Y_s}{g'_1 Y'_s}$$

$$\mathcal{L}_{\text{mixing}} = \frac{1}{2} m_{B'}^2 \left(\varepsilon^2 B_\mu B^\mu + 2\varepsilon B_\mu B'^\mu + B'_\mu B'^\mu \right)$$

mass diagonalization



$$(m_{\tilde{A}})^2 = 0, \quad (m_{\tilde{Z}})^2 = \frac{1}{4} v^2 (g_1^2 + g_2^2) + \varepsilon^2 \frac{g_1^2}{g_1^2 + g_2^2 - \alpha'} (m_{B'})^2, \quad \text{and}$$

$$(m_{\tilde{B}'})^2 = (m_{B'})^2 \left(1 + \varepsilon^2 \frac{g_2^2 - \alpha'}{g_1^2 + g_2^2 - \alpha'} \right).$$

$$\tilde{A}_\mu = \frac{g_1 A_\mu^3 + g_2 B_\mu}{\sqrt{g_1^2 + g_2^2}} - \varepsilon \frac{g_2}{\sqrt{g_1^2 + g_2^2}} B'_\mu$$

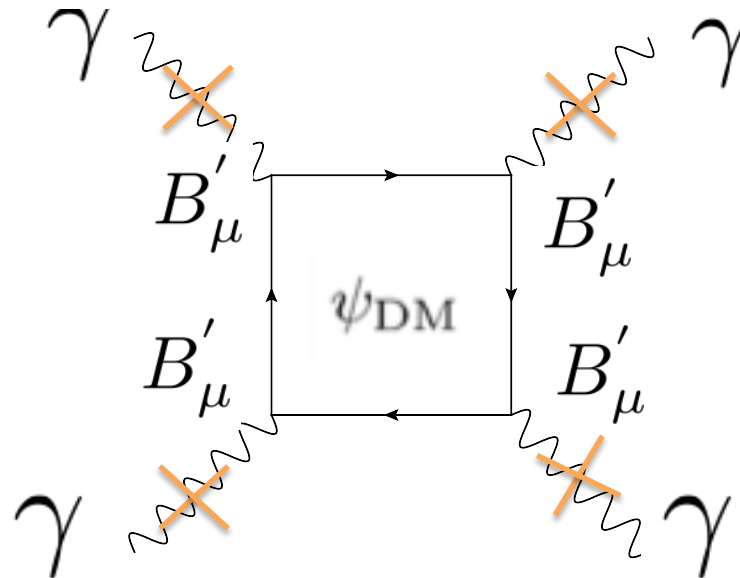
We assume $\varepsilon \ll 1$

Dark Matter Model (3/3) $\varepsilon \equiv \frac{g_1 Y_s}{g'_1 Y'_s}$

$$\tilde{A}_\mu = \frac{g_1 A_\mu^3 + g_2 B_\mu}{\sqrt{g_1^2 + g_2^2}} - \varepsilon \frac{g_2}{\sqrt{g_1^2 + g_2^2}} B'_\mu \chi$$

$$\mathcal{L}'_{\text{eff}} = \chi^4 \left\{ a \mathcal{F}^2 + b \mathcal{G}^2 + ic \mathcal{F}\mathcal{G} \right\}$$

$$S_\psi(m) = \int d^4x \bar{\psi}_{\text{DM}} \left[\gamma^\mu \left(i\partial_\mu - (g_V + g_A \gamma_5) B'_\mu \right) - m \right] \psi_{\text{DM}}$$

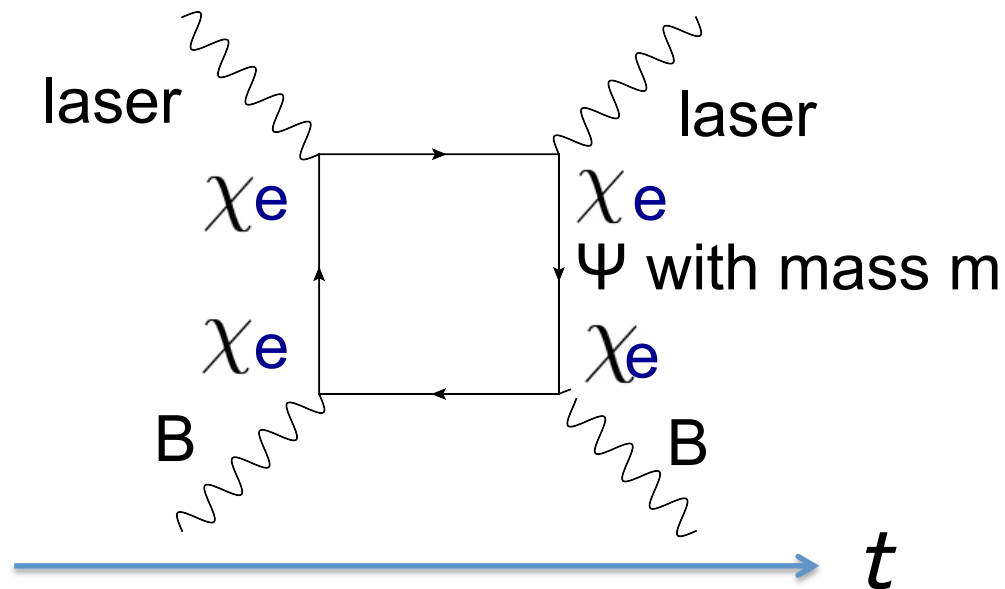


2 conditions

$$\frac{h\nu_{\text{laser}}}{1 \text{ eV}} \ll mc^2$$

$$\frac{\hbar \chi e |\mathbf{B}|}{10 \text{ Tesla, (1 Tesla} \sim 200 \text{ eV}^2)} \ll m^2 c^2$$

10 Tesla, (1 Tesla $\sim 200 \text{ eV}^2$)



Vacuum Magnetic Birefringence Experiment: laser beam energy

beam energy 1.16 eV @OVAL experiment

For 2 mirrors system: 1 ~ 4 eV

laser energy itself:

m eV ~ 10 k eV are available

thanks to X-ray Free Electron Laser