

実験: $b \rightarrow c\tau\nu$

2026/9/2

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Contents

● $b \rightarrow c\tau\nu$ result and expected sensitivity

-mainly about Belle II

● Measurements:

- $R(D^{(*)})$: Ratios of $BR(B \rightarrow c\tau\nu)/BR(B \rightarrow ce\nu, B \rightarrow c\mu\nu)$

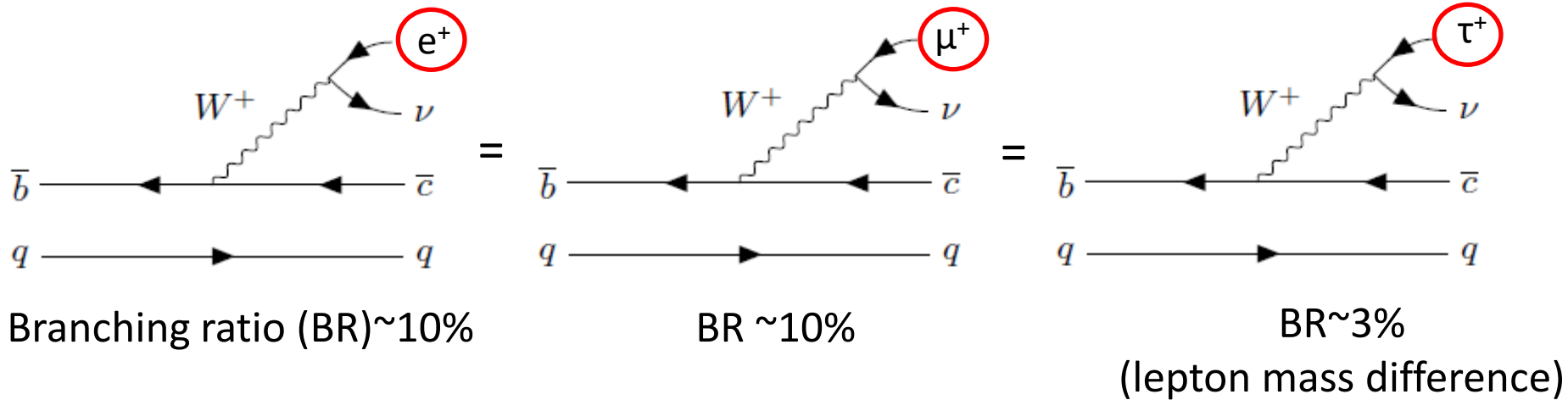
- $P_\tau(D^*)$: τ polarization

- $F_L(D^{(*)})$: D^* polarization

- $R(X), R(J/\psi), R(\Lambda_c^+)$

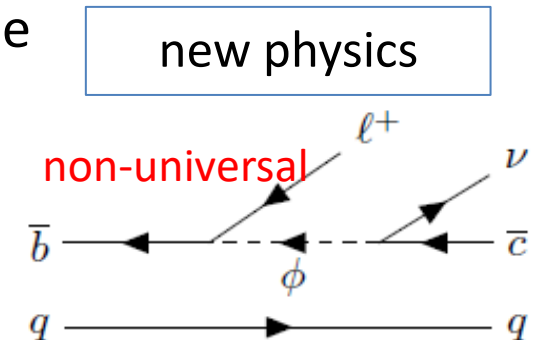
$b \rightarrow c \tau \nu$

- SM expects lepton coupling to EW gauge bosons to be flavor-universal (lepton flavor universality, LFU)



- B meson is a good probe to test LFU to search for new physics

- O(10GeV), 3 flavor(e, μ , τ) can be tested at same time
- LFU between e and μ is well ($\sim 1\%$ level) tested
- LFU between τ and $\ell(e, \mu)$: main topic today



Experimental observables

● R: ratio of $\text{BR}(b \rightarrow c\tau\nu)$ and $\text{BR}(b \rightarrow c\ell\nu, c\mu\nu)$

-cancel systematics by taking ratio

$$\mathcal{R}(D) = \frac{\mathcal{B}(B \rightarrow D\tau\nu_\tau)}{\mathcal{B}(B \rightarrow D\ell\nu_\ell)} \quad \ell=e,\mu$$

$$\mathcal{R}(D^*) = \frac{\mathcal{B}(B \rightarrow D^*\tau\nu_\tau)}{\mathcal{B}(B \rightarrow D^*\ell\nu_\ell)}$$

他にも $\mathcal{R}(X), \mathcal{R}(J/\psi), \mathcal{R}(\Lambda_c^+)$ もあるが今回はスキップ

● τ polarization ($P_\tau(D^*)$) and D^* polarization ($F_L(D^*)$) in $B \rightarrow D^*\tau\nu$ decay

$$P_\tau(D^{(*)}) = [\Gamma^+(D^{(*)}) - \Gamma^-(D^{(*)})] / [\Gamma^+(D^{(*)}) + \Gamma^-(D^{(*)})]$$

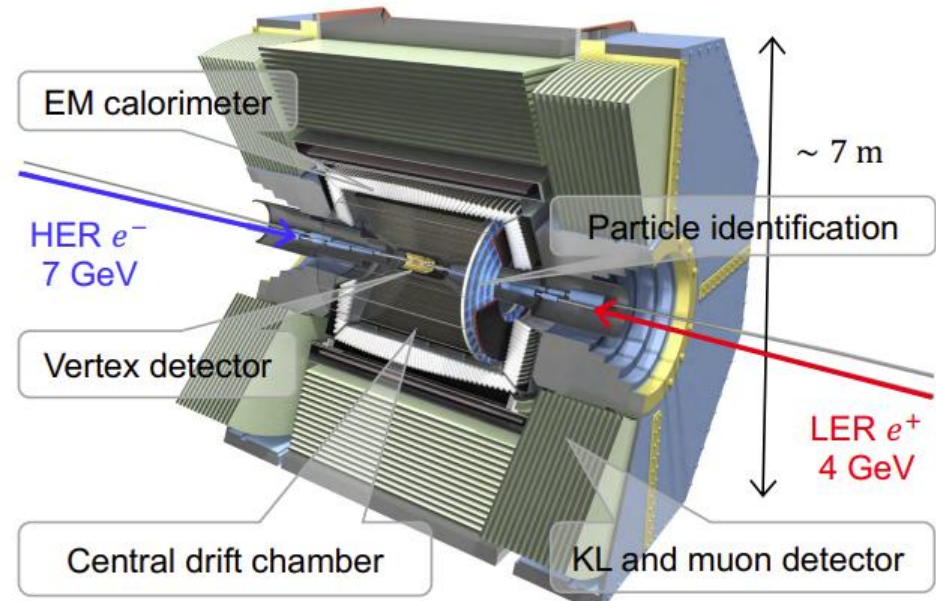
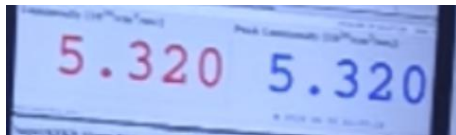
+−: τ helicity of $\pm 1/2$.

Belle II

● Belle II at SuperKEKB: on-threshold $B\bar{B}$ production from $e^+e^- \rightarrow Y(4S) \rightarrow B\bar{B}$, reconstructed with hermetic detector

● Belle II Feature:

- clean background environment
- known initial beam state
- particle identification of e, μ, π, K
- neutral particle detection
- achieved luminosity of $5.3 \times 10^{34} \text{ cm}^2 \text{ s}^{-1}$
- integrated luminosity of **808fb⁻¹** @Y(4S)



● Best experiment to measure $b \rightarrow c\tau\nu$

- τ immediately decays to one or multiple neutrino(s) ($\tau \rightarrow \mu\nu\nu$, $\tau \rightarrow \pi\nu$ etc.)
- all Belle II features are suitable for measurement with missing neutrino(s)

Analysis concept for $B \rightarrow D^{(*)}\tau\nu$

● Reconstruct $B \rightarrow D^*\tau\nu_\tau$ $B \rightarrow D^*\ell\nu_\ell$

{ -leptonic/hadronic B decay, leptonic/hadronic τ decay

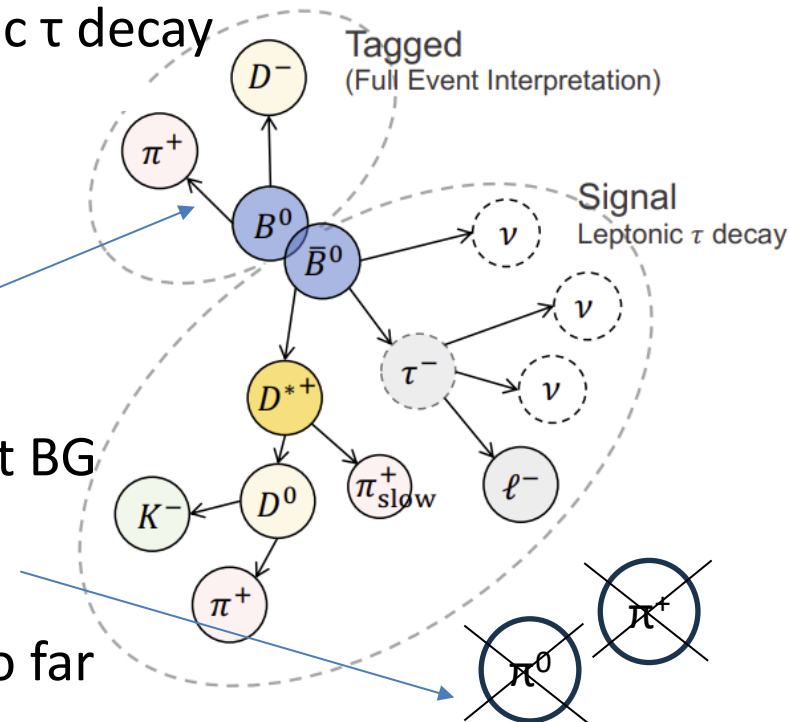
● Challenge: neutrino(s) in final state

-Fully reconstruct partner B meson (tagging)
to measure missing neutrino masses

-No remained particles except for BB to reject BG

-Major BG: $B \rightarrow D^{**}\ell\nu$, hadronic B decay

- D^{**} Branching ratio is not measured well so far



● Cancel theoretical and experimental systematics error by taking ratio of $B \rightarrow D^*\tau\nu$ and $B \rightarrow D^*\ell\nu$

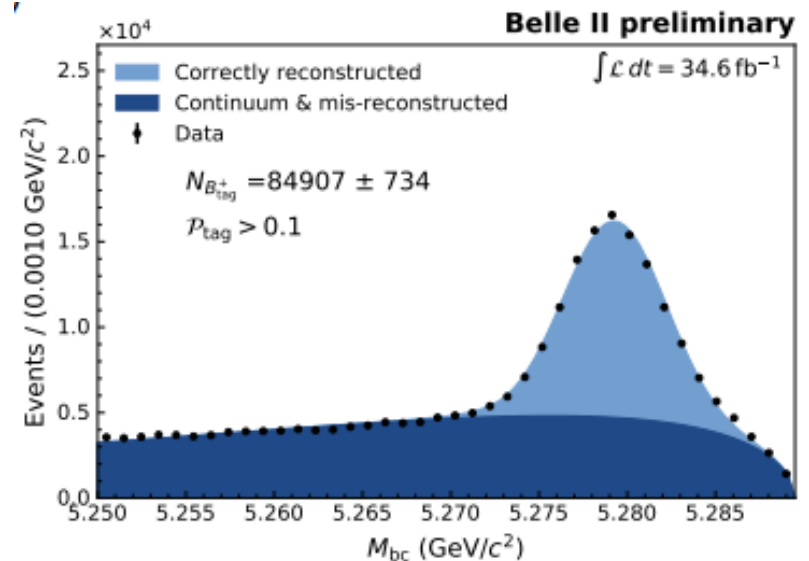
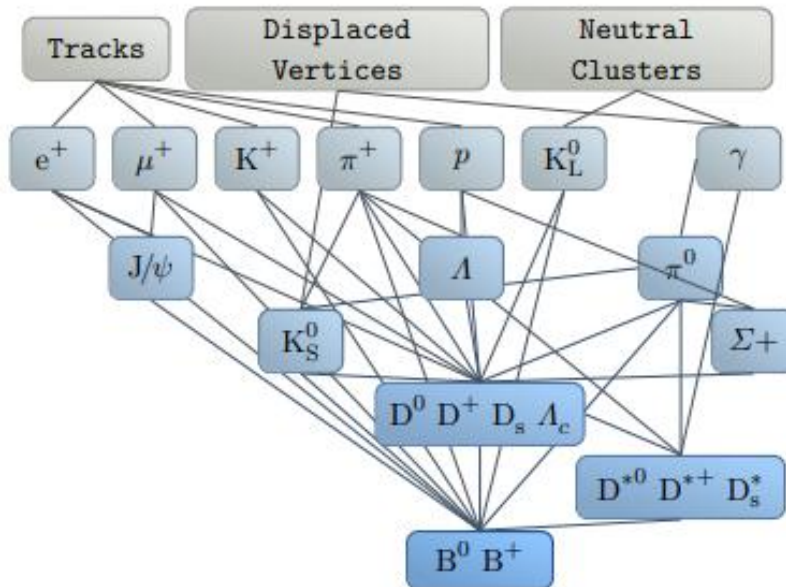
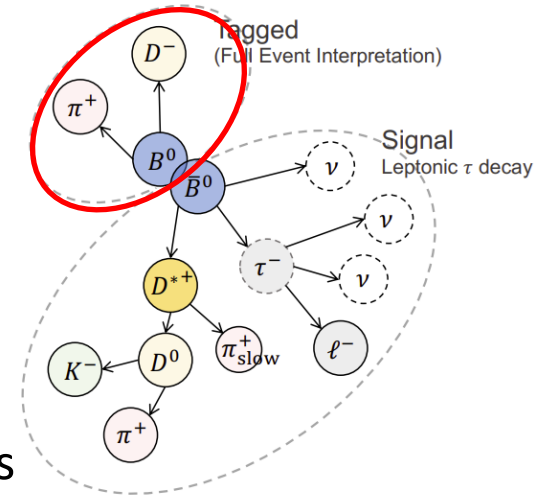
B_{tag} reconstruction

● Reconstruct hadronic B_{tag} decays

-a few tens kind of decay modes

● Optimize selection criteria by using machine learning algorithm (Full Event Interpretation, FEI)

- Multivariate classifier to estimate B_{tag} probability
- input: vertex, momentum, particle identification of daughters

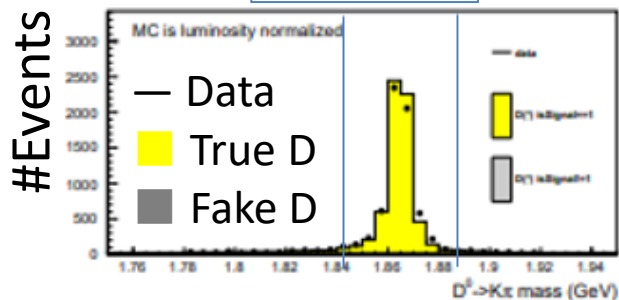


$$M_{bc} = \sqrt{E_{\text{beam}}^2 - (p_{\text{tag}}^{\text{CM}})^2}$$

D, D* reconstruction

- Use most of $D^{(*)}$ decays with large branching ratios

- 7 kind of D^0, D^+ decays
- 4 kind of D^* decays



invariant mass of D(GeV)

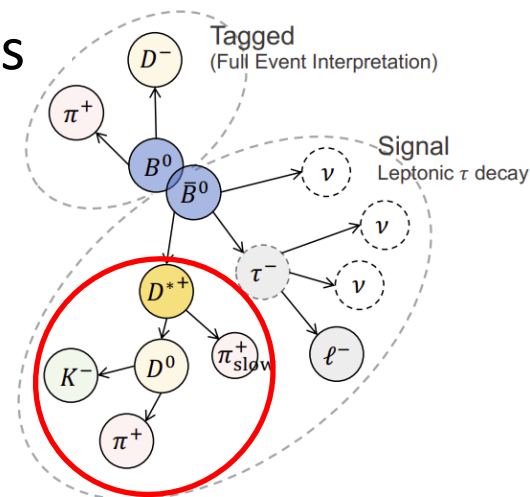
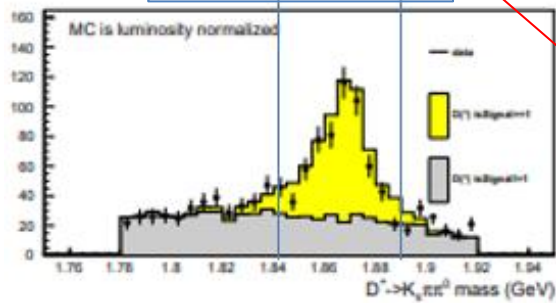
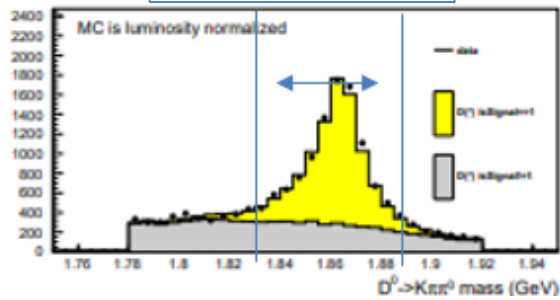
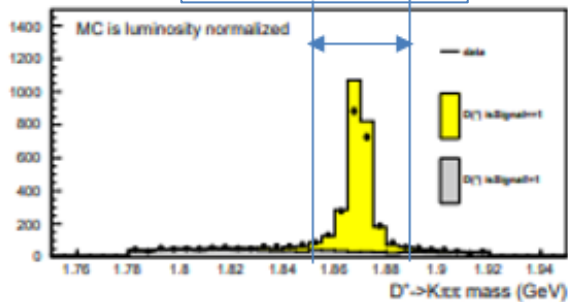


Table 3.2: List of reconstructed D^0 decay modes.

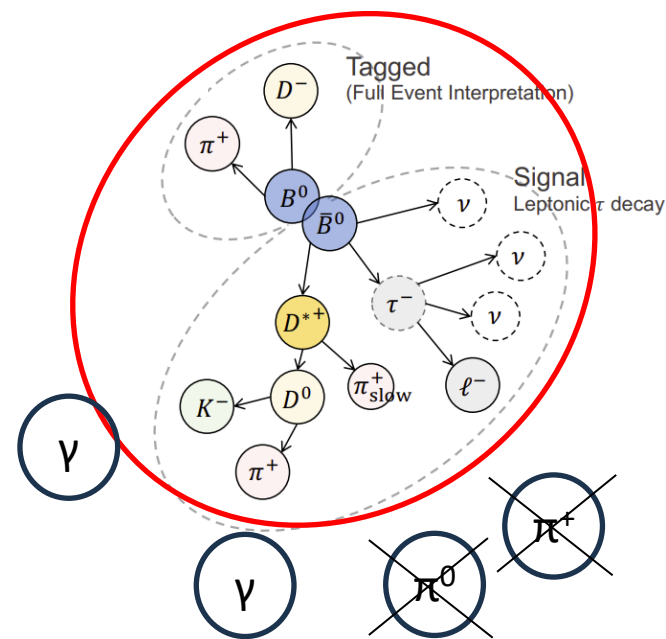
Decay	Branching ratio on PDG
$D^0 \rightarrow K^- \pi^+ \pi^0$	$(14.4 \pm 0.50)\%$
$D^0 \rightarrow K^- \pi^+ \pi^- \pi^+$	$(8.23 \pm 0.14)\%$
$D^0 \rightarrow K_S^0 \pi^+ \pi^- \pi^0$	$(5.20 \pm 0.60)\%$
$D^0 \rightarrow K^- \pi^+$	$(3.95 \pm 0.03)\%$
$D^0 \rightarrow K_S^0 \pi^+ \pi^-$	$(2.80 \pm 0.18)\%$
$D^0 \rightarrow K_S^0 \pi^0$	$(1.24 \pm 0.02)\%$
$D^0 \rightarrow K^- K^+$	$(0.41 \pm 0.01)\%$

Decay	Branching ratio on PDG
$D^+ \rightarrow K^- \pi^+ \pi^+$	$(9.38 \pm 0.16)\%$
$D^+ \rightarrow K_S^0 \pi^+ \pi^0$	$(7.36 \pm 0.21)\%$
$D^+ \rightarrow K^- \pi^+ \pi^+ \pi^0$	$(6.25 \pm 0.18)\%$
$D^+ \rightarrow K_S^0 \pi^+ \pi^- \pi^+$	$(3.10 \pm 0.09)\%$
$D^+ \rightarrow K_S^0 \pi^+$	$(1.56 \pm 0.03)\%$
$D^+ \rightarrow K^- K^+ \pi^+$	$(0.968 \pm 0.018)\%$
$D^+ \rightarrow K_S^0 K^+$	$(0.304 \pm 0.01)\%$

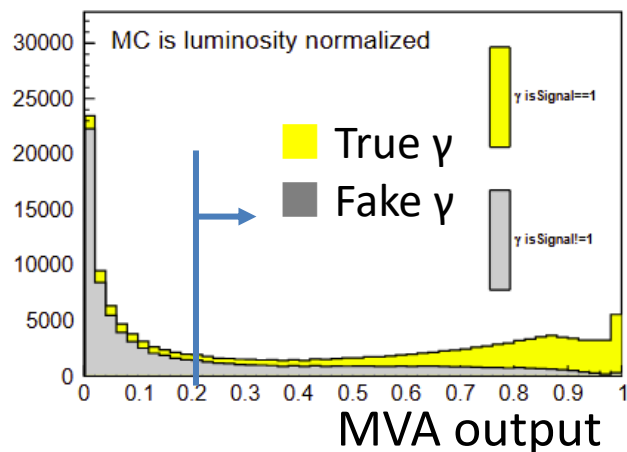
gray: newly added

Y(4S) reconstruction

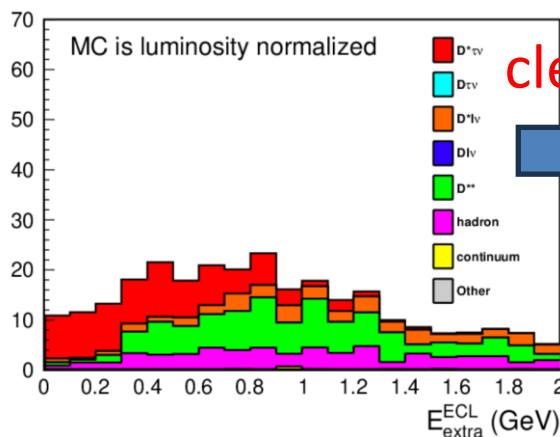
- Combine $B_{\text{tag}}, D^*, \ell$ to reconstruct Y(4S)
- $\tau \rightarrow e \nu \nu, \tau \rightarrow \mu \nu \nu$
- Require no remained charged particle, π^0
- to reject background from $B \rightarrow D^{**} \ell \nu$ etc.
- Machine learning is used to reject fake γ
(energy deposit from hadron, hadronic split-off)
to calculate sum of γ energy at rest of events (E_{ECL})



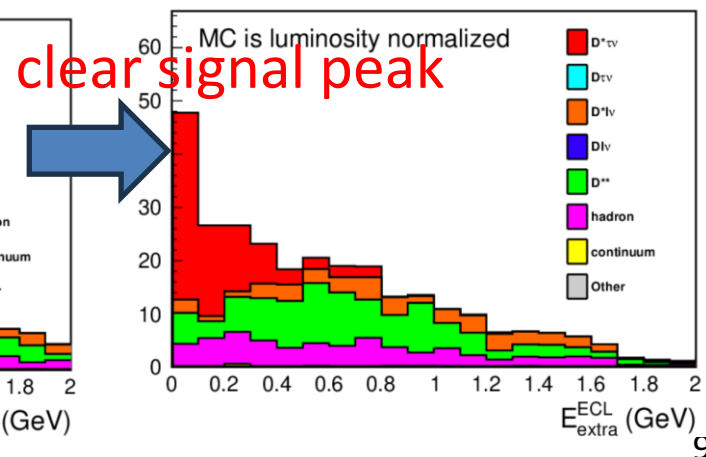
fake photon MVA



E_{ECL} without MVA



E_{ECL} with MVA



Three $R(D^{(*)})$ analysis results from Belle II

- Three results with different B_{tag} , tau decay mode @365fb⁻¹
-statistically independent results

	year	dataset	B_{tag} mode	tau decay	observable
①	2025	365fb ⁻¹	hadronic	$\tau \rightarrow e\nu\nu$ $\tau \rightarrow \mu\nu\nu$	$R(D^{(*)})$
②	2025	365fb ⁻¹	semileptonic	$\tau \rightarrow e\nu\nu$ $\tau \rightarrow \mu\nu\nu$	$R(D^{(*)+})$
③	2026	365fb ⁻¹	hadronic	$\tau \rightarrow \pi\nu$ $\tau \rightarrow \rho\nu$	$R(D^*), P_{\tau}(D^*)$

higher purity, lower statistics

lower purity, higher statistics

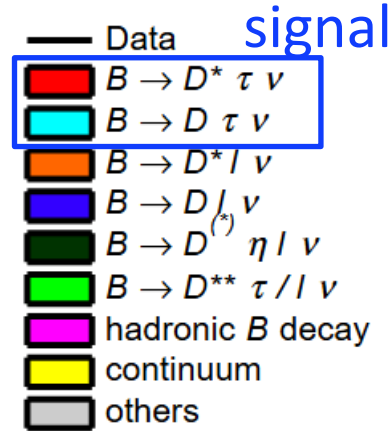
lower purity

① $R(D^{(*)})$ with hadronic tag, leptonic tau decay

● Highest purity: B_{tag} : hadronic B decay τ : $\tau \rightarrow e \nu \nu$, $\tau \rightarrow \mu \nu \nu$

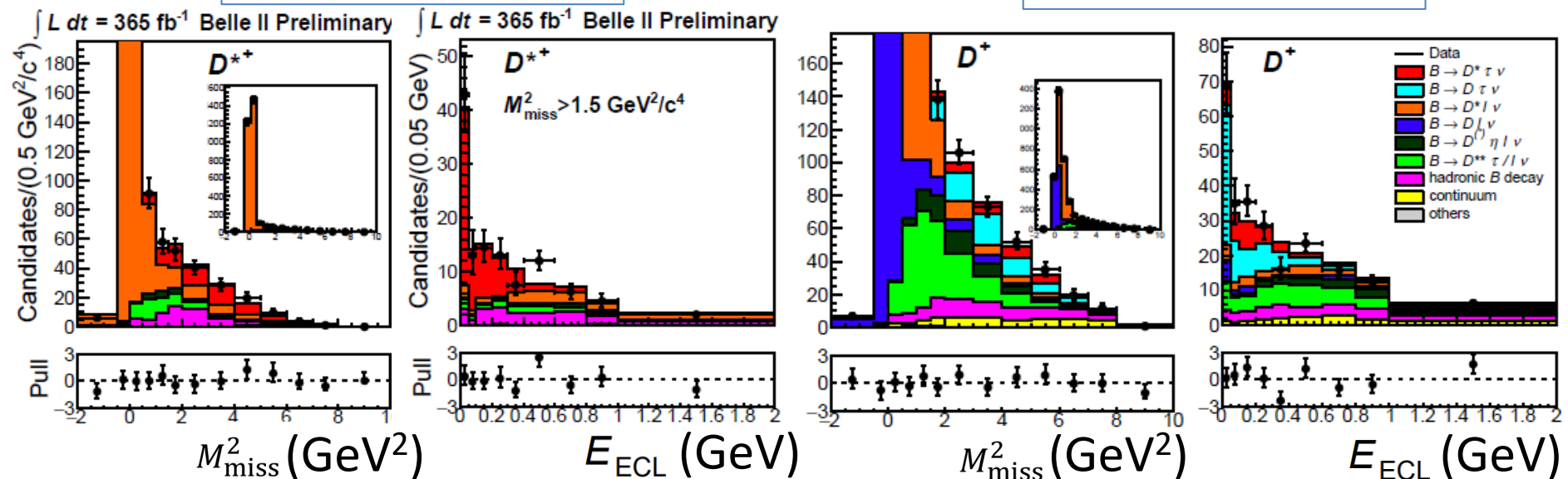
● Fitting variable:

- E_{ECL} : sum of γ energy at rest of events
- $M_{\text{miss}}^2 \equiv (p_{e^+e^-} - p_{B_{\text{tag}}} - p_{D^*} - p_{\ell})^2$: missing mass squared



$B \rightarrow D^* \tau \nu$ channel

$B \rightarrow D \tau \nu$ channel



① $R(D^{(*)})$ with hadronic tag, leptonic tau decay

● Breakdown of systematics error

- Dominant systematics is MC statistics (-_~;) } ②,③ is similar situation
- Second dominant is gap-mode (explained later)

Source	$R(D^*)$	$R(D)$	ρ
Simulation sample size	4.8%	8.4%	-0.44
gap-mode branching fraction	2.7%	3.1%	0.00
$B \rightarrow D^{**} \tau^- / (\ell^-) \bar{\nu}_\ell$ branching fractions	0.3%	1.3%	0.25
Hadronic B decay branching fractions	1.6%	1.5%	-0.26
Form factors	0.5%	0.9%	-0.70
Fraction of misreconstructed $D^{(*)}$	0.5%	1.2%	0.00
Continuum background	2.4%	2.1%	0.93
Fit biases	0.3%	1.2%	0.00
Low-momentum π^0, γ efficiency	2.2%	2.4%	0.99
Other efficiency corrections	0.7%	1.4%	0.92
B -tagging efficiency of data	0.9%	1.8%	-1.00
B -tagging efficiency of $B \rightarrow D\tau\nu$	0.1%	1.8%	1.00
M_{miss}^2 resolution	0.5%	0.8%	0.48
Total systematic uncertainty	6.7%	10.3%	-0.20
Statistical uncertainty	7.9%	12.5%	-0.40

● Result:

$$R(D^*) = 0.242 \pm 0.019(\text{stat}) \pm 0.016(\text{syst}),$$
$$R(D) = 0.439 \pm 0.055(\text{stat}) \pm 0.046(\text{syst})$$

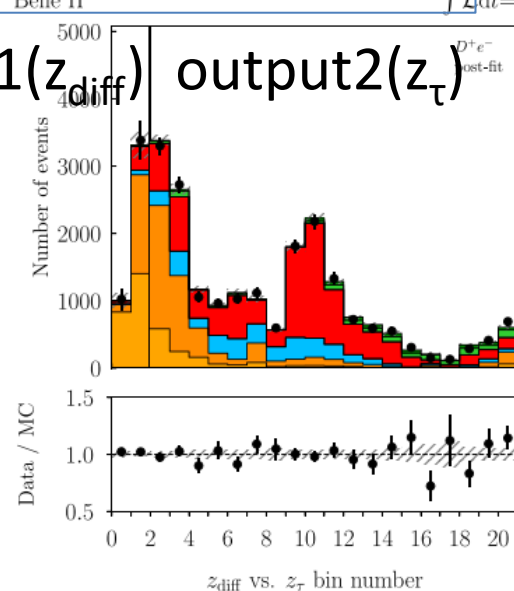
most precise
result by Belle II

② $R(D^{(*)})$ with semileptonic tag, leptonic tau decay

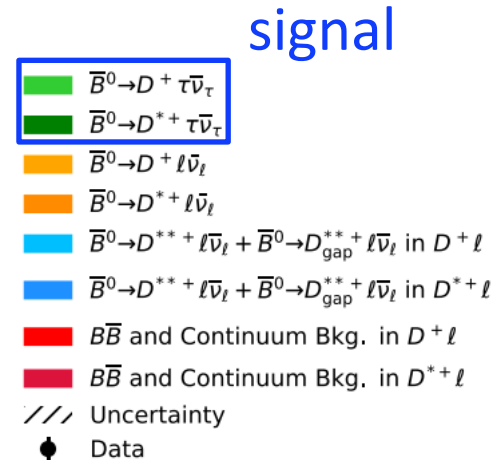
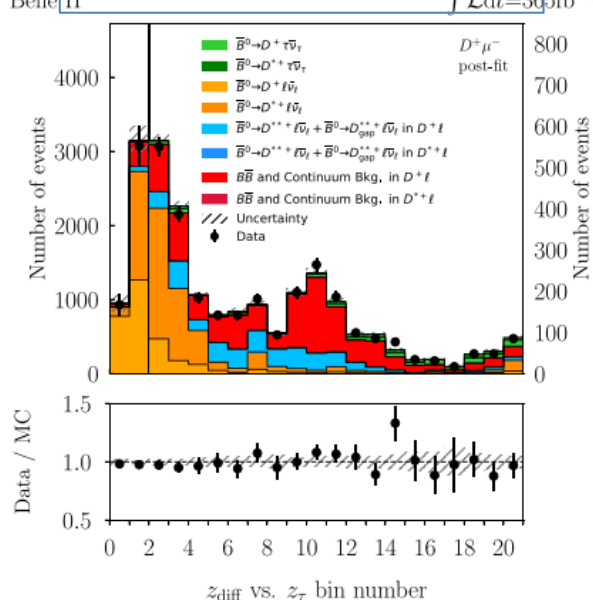
- B_{tag} : semileptonic B decay $\tau: \tau \rightarrow e\nu\nu, \tau \rightarrow \mu\nu\nu$
 - B_{tag} momentum can not be measured due to missing neutrino $\rightarrow$ MVA
- Fitting variable: 2D fitting of MVA outputs

input to MVA	meaning	importance
$\cos\theta_{BY}^{\text{sig}}$	$\cos\theta_{BY}$ of signal B	1
E_{ECL}	sum of γ energy at rest of events	2
$\cos^2\phi_B$	angle estimated from $\cos\theta_{BY}^{\text{sig}}, \cos\theta_{BY}^{\text{tag}}, \gamma^{\text{sig}}, \gamma^{\text{tag}}$	3
p_D^*	$D^{(*)}$ momentum at CMS frame	4
p_ℓ^*	signal ℓ momentum at CMS frame	5

$B \rightarrow D^{*+} \tau \nu$ channel



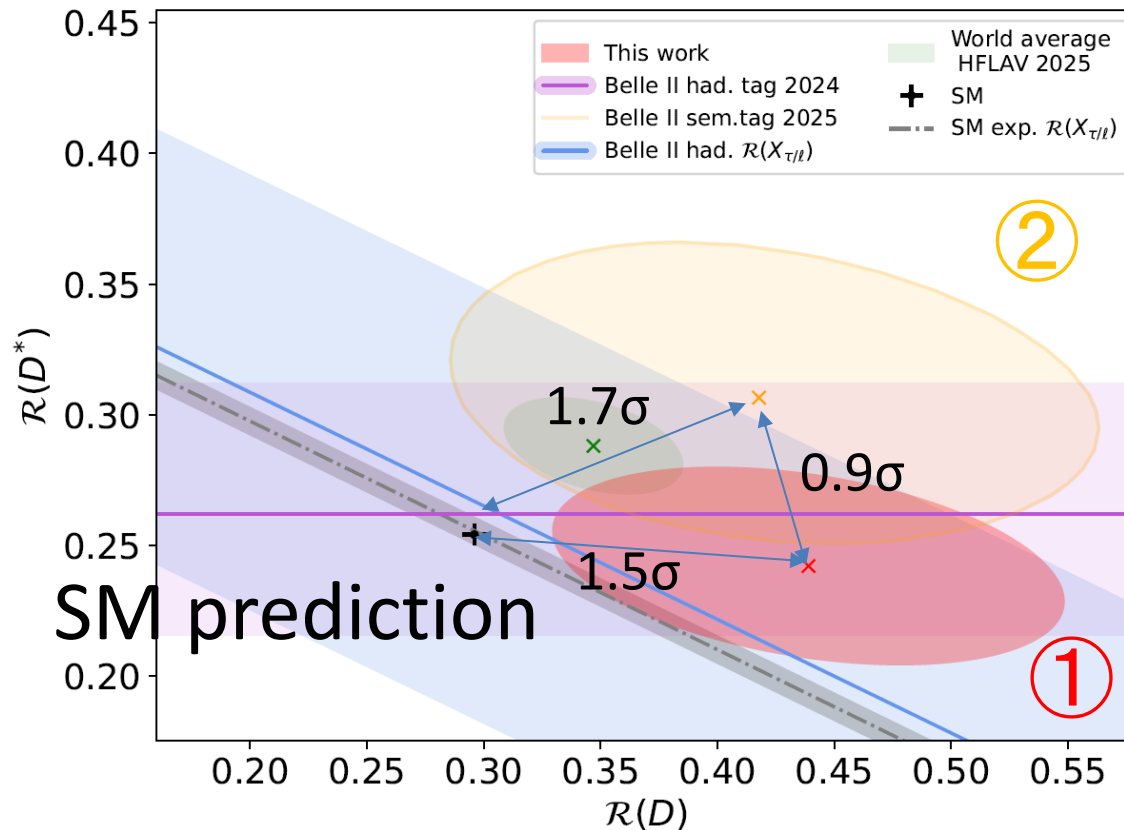
$B \rightarrow D^+ \tau \nu$ channel



Result of ① and ②

- ① hadronic tag is consistent with SM by 1.5σ
- ② semileptonic tag is consistent with SM by 1.7σ
- ① and ② are consistent by 0.9σ in each other

Belle II preliminary



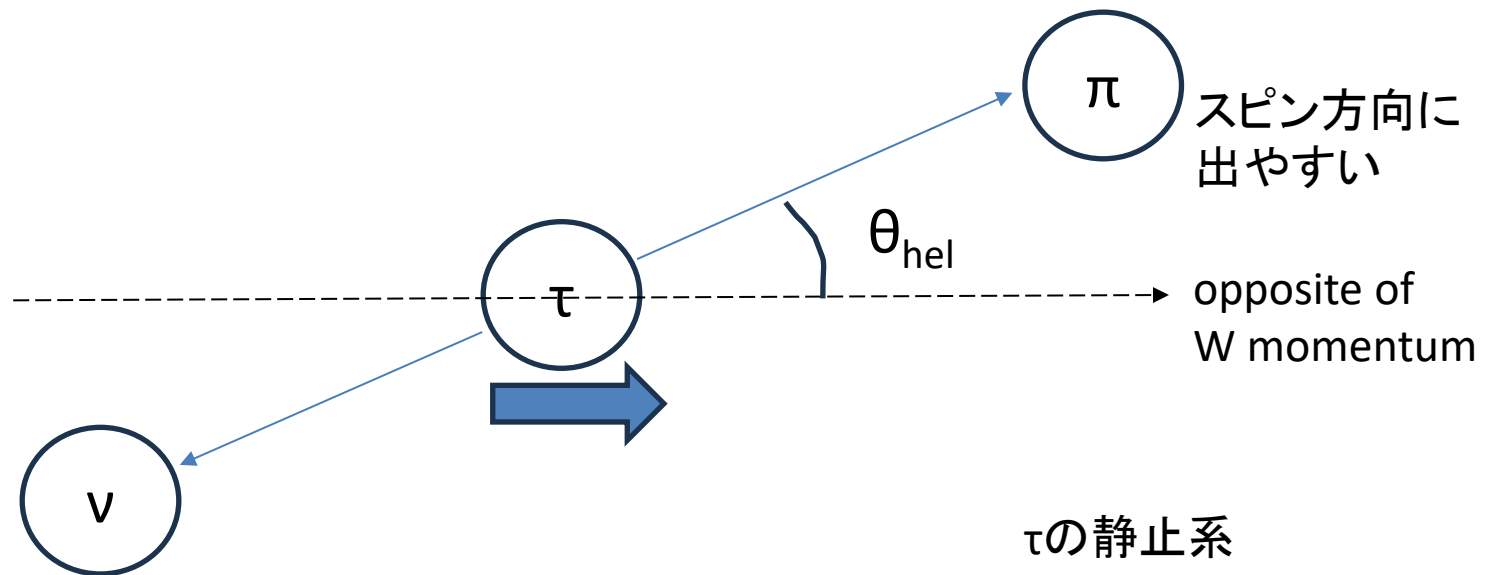
B→D(*)τν 偏極度測定

-新物理のモデルの中には、D*やτの偏極度に影響を与えるものがある

+−: τ helicity of ±1/2.

-τの偏極度: $P_\tau(D^{(*)}) = [\Gamma^+(D^{(*)}) - \Gamma^-(D^{(*)})] / [\Gamma^+(D^{(*)}) + \Gamma^-(D^{(*)})]$

-微分崩壊分岐比: $\frac{1}{\Gamma(D^{(*)})} \frac{d\Gamma(D^{(*)})}{d\cos\theta_{\text{hel}}} = \frac{1}{2} \left[1 + \alpha \boxed{P_\tau(D^{(*)})} \cos\theta_{\text{hel}} \right]$



-τ→ℓννでは2個ニュートリノがありスピンの情報が損失するため、
τ→πν、ρνが用いられる. ただしBG大.

③ $R(D^{(*)})$ with hadronic tag, hadronic tau decay

● low purity, low stat. B_{tag} : hadronic B decay τ : $\tau \rightarrow \pi \nu$, $\tau \rightarrow \rho \nu$ ($\rho^- \rightarrow \pi^- \pi^0$)

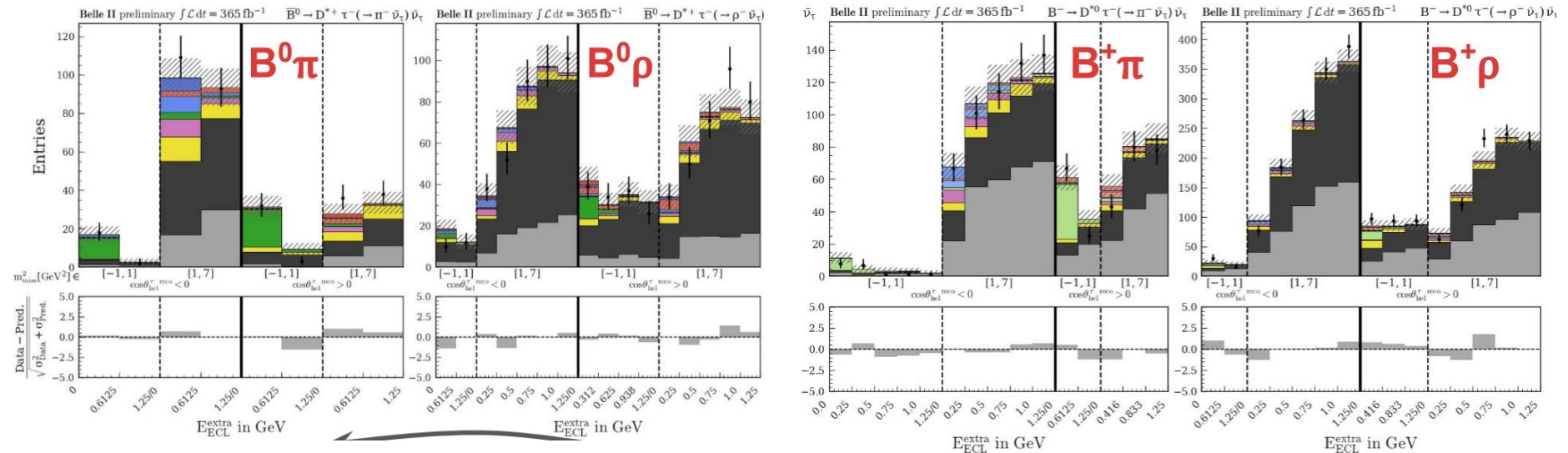
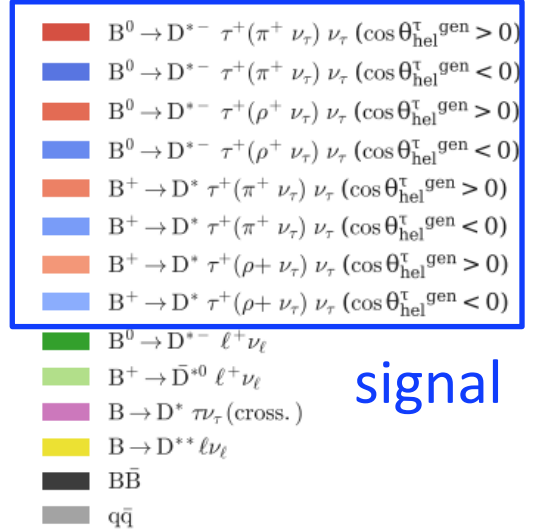
● Fitting variable: E_{ECL} , M_{miss}^2 , $\cos \theta_{\text{hel}}^\tau$

- M_{miss}^2 : $<1, >1 \text{ GeV}^2$ の 2bin

- $\cos \theta_{\text{hel}}^\tau$: $<0, >0$ の 2bin

● dominant BG: $B \rightarrow D^* + \text{hadron}$, $B \rightarrow D^* D_{(s)}(K)$

- evaluation by sideband



Result of ③

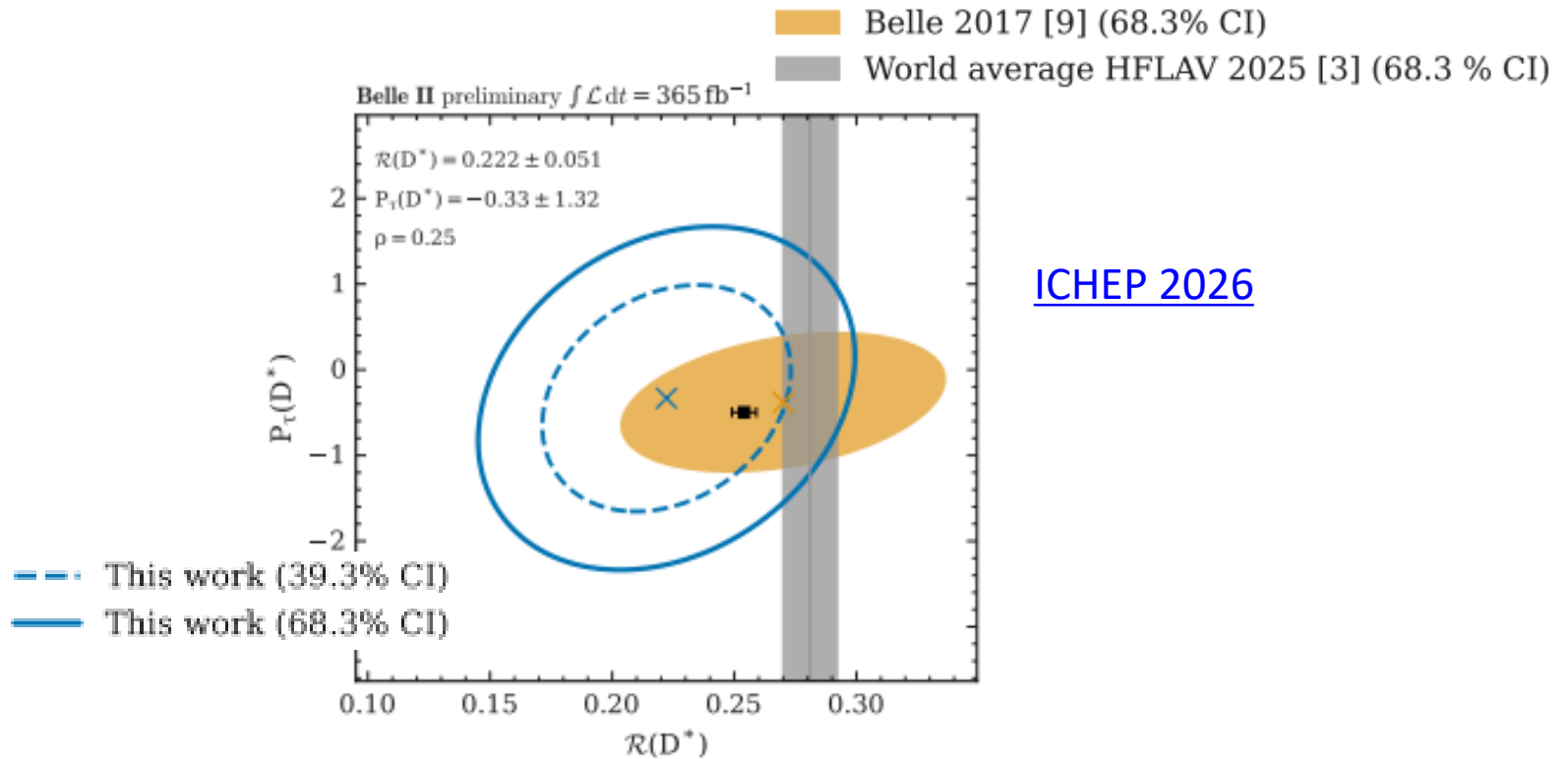
$R(D^*)$ is not so precise

● Result:

$$R(D^*) = 0.222 \pm 0.041 \text{ (stat)} \pm 0.030 \text{ (syst)}$$
$$P_\tau(D^*) = -0.33 \pm 1.15 \text{ (stat)} \pm 0.65 \text{ (syst)}$$

first polarization result from Belle II

● Consistent with SM by 0.68σ

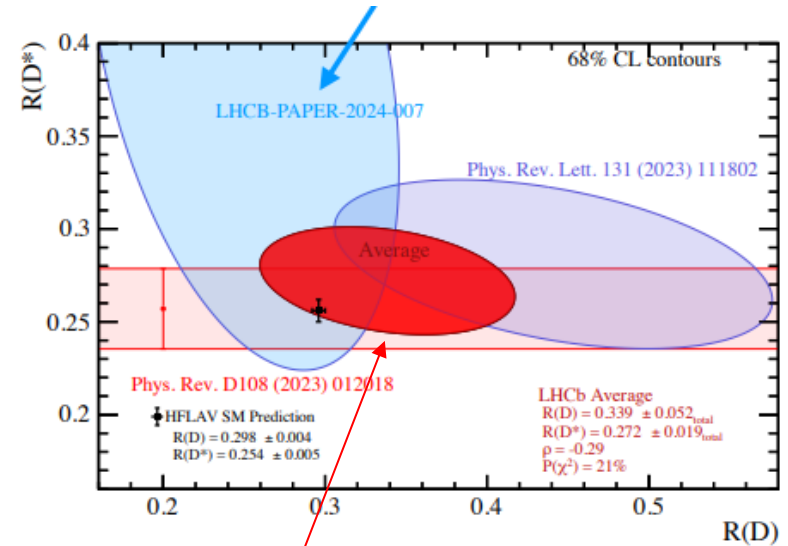


Results from LHC, Babar

R(D^(*)) by LHCb

- LHCbから3つの測定 ($R(J/\psi)$, $R(\Lambda_c^+)$ も)
- D⁰ or D⁺, τ の崩壊モード, fit変数が異なる
- LHCb^bは $B \rightarrow D^* \pi \pi \pi$ との比をとって誤差削減.

- どの測定も系統誤差が支配的
- BG, MC stat., form factor. 今後は？



- LHCb の結果のみだと、SMと68%CLでコンシステント

paper	D崩壊	τ 崩壊	dataset	fit variable	R(D [*]) ±stat±syst.	R(D) ±stat±syst.
LHCb^a 2023	D ⁰ →K π	$\tau \rightarrow \mu \nu \nu$	RUN1 3fb ⁻¹	$M_{\text{miss}}^2, E^*_\ell, q^2$	$0.281 \pm 0.018 \pm 0.024$	$0.441 \pm 0.060 \pm 0.066$
LHCb^b 2023	D ⁰ →K π	$\tau \rightarrow \pi \pi \pi (\pi^0) \nu$	RUN1 3fb ⁻¹	M_{miss}^2 , tau decay time, BDT	$0.247 \pm 0.015 \pm 0.015 \pm 0.012$	--
LHCb^c 2024	D ⁺ →K $\pi \pi$	$\tau \rightarrow \mu \nu \nu$	RUN2 2fb ⁻¹	$M_{\text{miss}}^2, E^*_\ell, q^2$	$0.402 \pm 0.081 \pm 0.085$	$0.249 \pm 0.043 \pm 0.047$

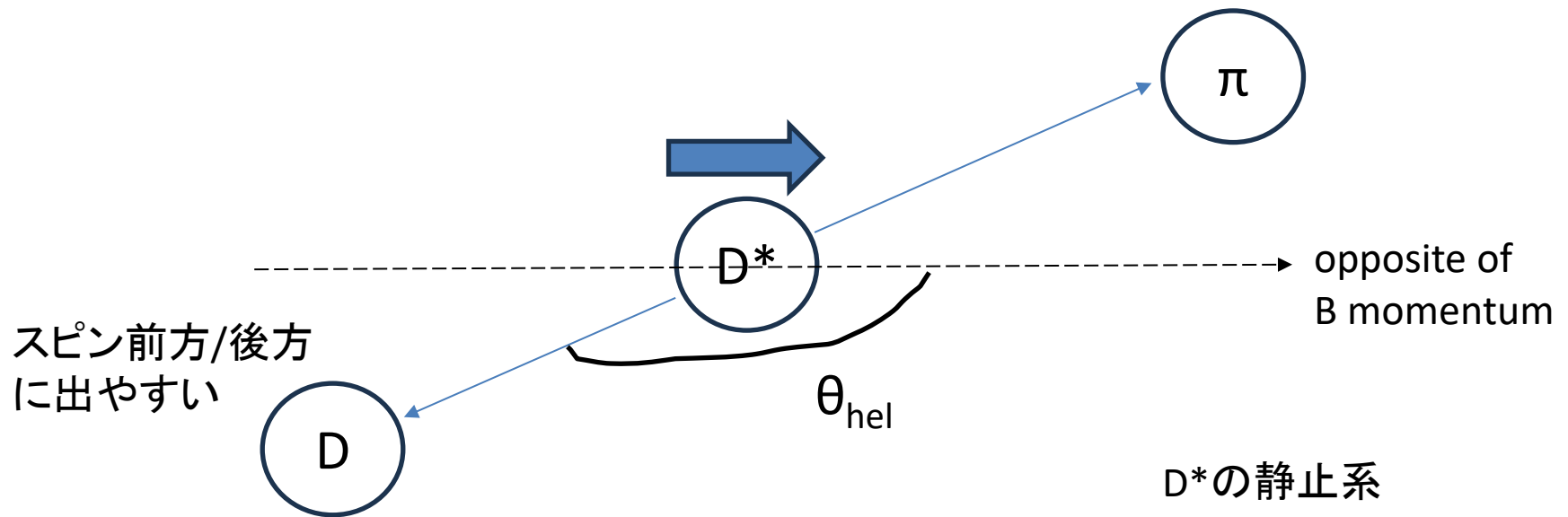
external BR

-LHCb^b 2023 BDT: neutral particles around 3 π to identify BG from 3 π system from Ds⁺ decays

B → D* τ ν D* 偏極度測定

-D(*) longitudinal polarization: $F_L^{D^*}$

-微分崩壊分岐比: $\frac{1}{\Gamma} \frac{d\Gamma}{d\cos\theta_{\text{hel}}} = \frac{3}{4} (2F_L^{D^*} \cos^2 \theta_{\text{hel}} + (1 - F_L^{D^*}) \sin^2 \theta_{\text{hel}})$



$B \rightarrow D^* \tau \nu$ D^* 偏極度測定 @LHCb

-LHCb run1 + partial run2 (5fb^{-1}) を使った解析

-[LHCb^b 2023](#) の $R(D^*)$ 解析を拡張: $\cos\theta_{\text{hel}}$ をフィット変数に追加

Measured values of $F_L^{D^*}$:

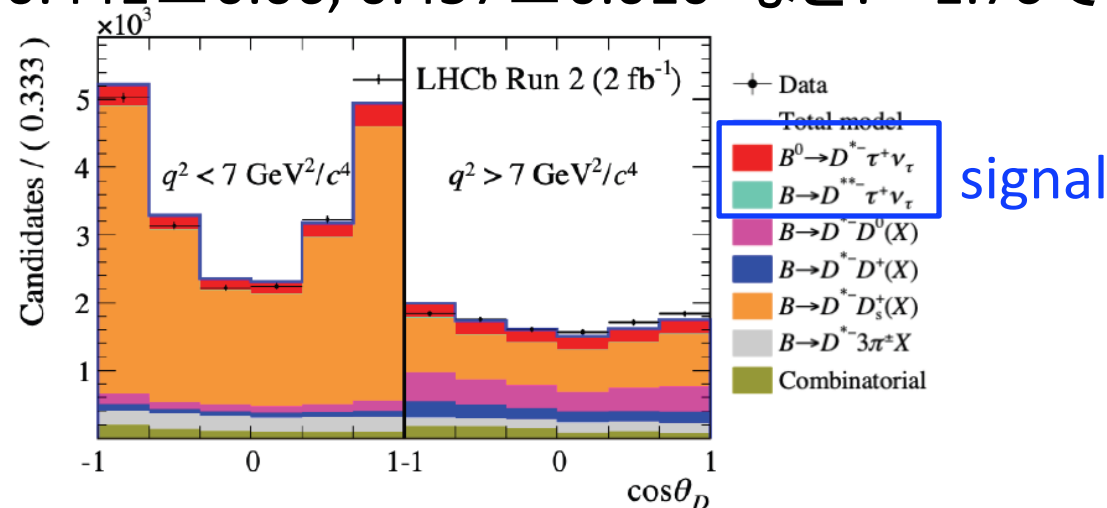
$$q^2 < 7 \text{ GeV}^2/c^4 : 0.51 \pm 0.07 (\text{stat}) \pm 0.03 (\text{syst})$$

$$q^2 > 7 \text{ GeV}^2/c^4 : 0.35 \pm 0.08 (\text{stat}) \pm 0.02 (\text{syst})$$

$$q^2 \text{ whole range} : 0.43 \pm 0.06 (\text{stat}) \pm 0.03 (\text{syst})$$

arxiv.2311.05224

SM model: $F_L^{D^*} = 0.441 \pm 0.06, 0.457 \pm 0.010$ など. $\sim 1.7\sigma$ で一致.



-Belle IIでも同様の D^* 偏極度測定は可能(現在進行中)

$R(D^{(*)})$ semileptonic tag by Babar

- $R(D^{(*)})$ measurement with semileptonic tag by Babar @426fb⁻¹ has been available as doctor thesis, but not published since 2022
- Presentation at [2026 Moriond](#) and [2025 workshop](#)
- "Journal paper in preparation: submission anticipated over next few month"
- very roughly say, analysis method is similar to semileptonic tag @ Belle II

New preliminary BABAR results, using its full dataset

$$R(D) = 0.316 \pm 0.062 \text{ (stat)} \pm 0.019 \text{ (syst)}$$

$$R(D^*) = 0.226 \pm 0.022 \text{ (stat)} \pm 0.012 \text{ (syst)}$$

$$\rho = -0.82$$

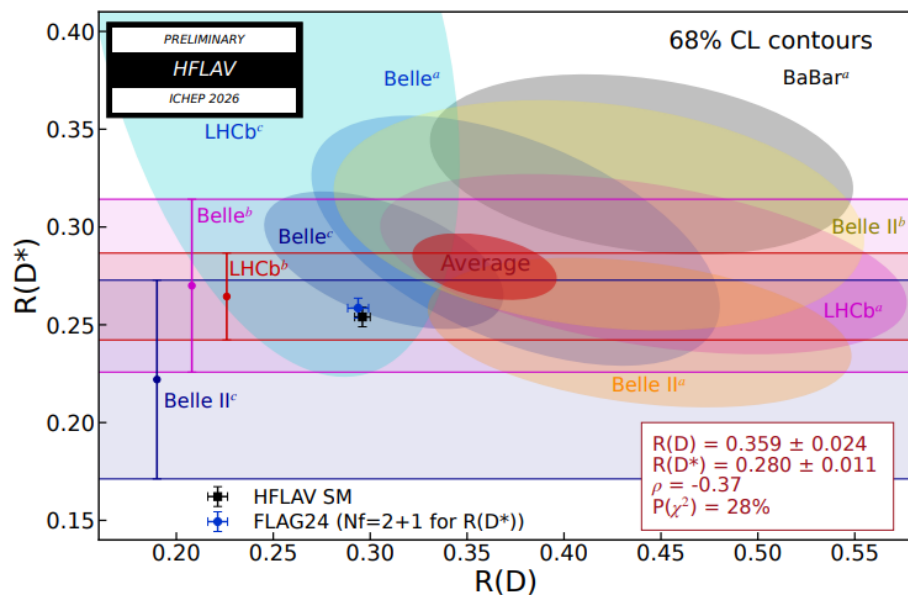
→ Consistent with SM expectations at $\sim 1.5 \sigma$

→ New world average consistent with SM expectations at 2σ

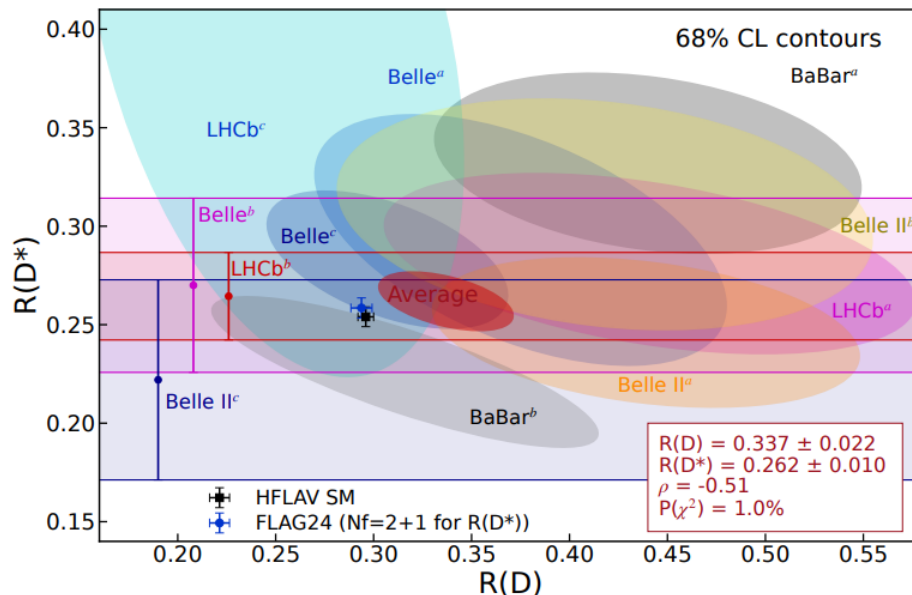
Global average

- Global average is 3.7σ (2.0σ) different from SM prediction without (with) Babar 2026 Moriond
- Consistency between experiments ($P(\chi^2)=1.0\%$) is low with Babar.

3.7 σ without Babar 2026 Moriond



2.0 σ with Babar 2026 Moriond



<https://hflav-eos.web.cern.ch/hflav-eos/semi/ichep26/html/RDsDsstar/RDRDs.html>

Belle II prospect

future Belle II sensitivity

-At present analysis, major error sources are statistic and MC statistics.
Sensitivity will improve by increasing them.

-Present precision

analysis	year	dataset	tag	τ decay	precision (stat.+sys.)
①	2025	365fb^{-1}	hadronic	hadronic	$R(D^*):10\%$ $R(D):16\%$
②	2025	365fb^{-1}	semileptonic	leptonic	$R(D^*):13\%$ $R(D):22\%$
③	2026	365fb^{-1}	hadronic	hadronic	$R(D^*):23\%$ $P_\tau(D^*): \pm 1.3$

-Near future sensitivity with 808fb^{-1}

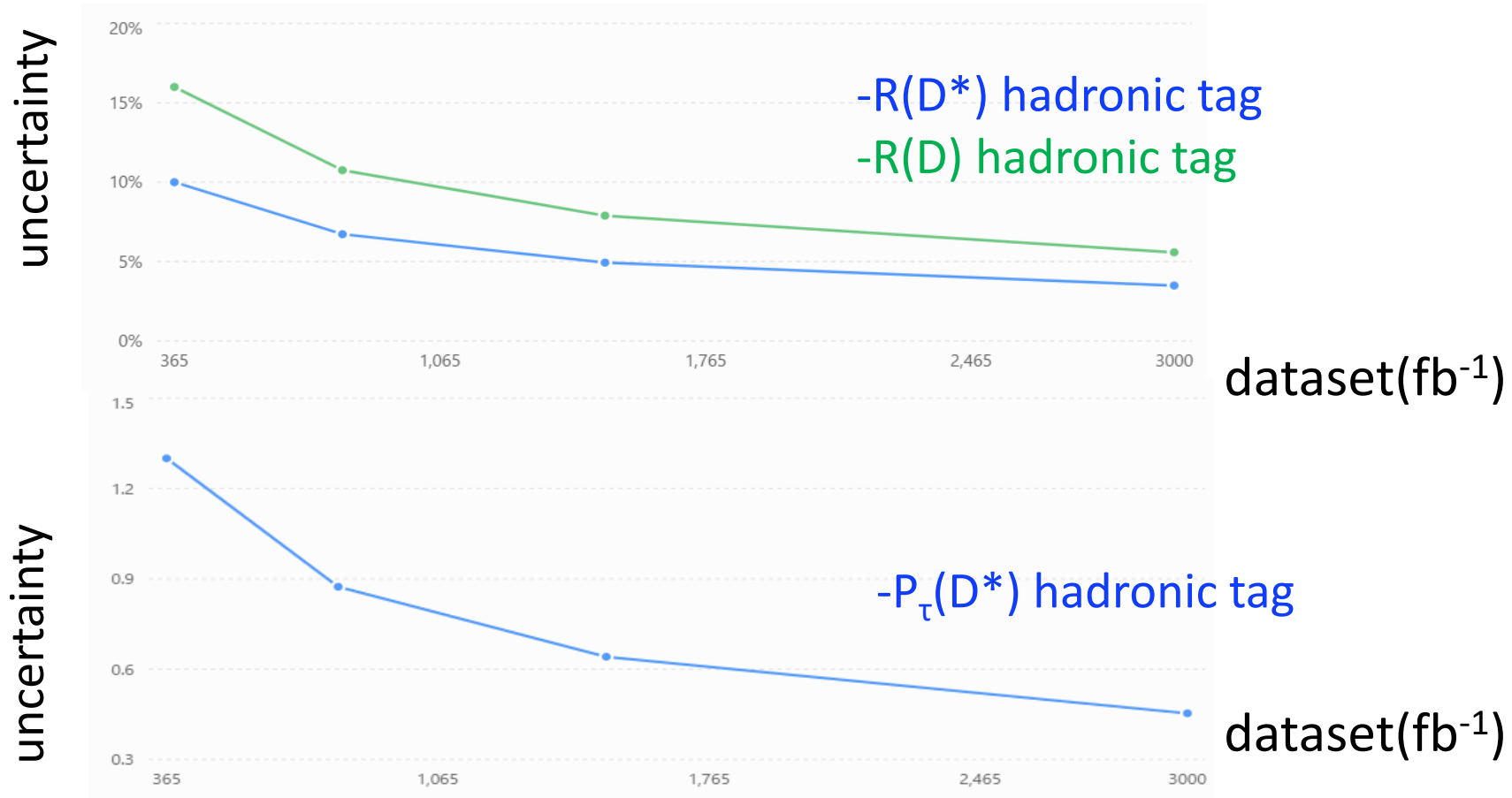
(✂my private number by hand calculation, just scaling $\sqrt{808/365}$)

	year	dataset	tag	τ decay	sensitivity
①	2027-28	808fb^{-1}	hadronic	hadronic	$R(D^*):7\%$ $R(D):11\%$, q^2 , $F_L(D^*)$
②	2027-28	808fb^{-1}	semileptonic	leptonic	$R(D^*):9\%$ $R(D):15\%$
③	2027-28	808fb^{-1}	hadronic	leptonic	$R(D^*):23\%$ $P_\tau(D^*): \pm 0.90$
④	?	?	inclusive	leptonic	$R(D^*):? \%$ $F_L(D^*): ?$

future Belle II sensitivity

-More future sensitivity

(✂ my private number by hand calculation, just scaling $\sqrt{N}$)



-I personally think more improvement of analysis method is possible

-ML for hadronic tag, add more D^* channels for semileptonic tag, partial reconstruction of B_{tag} , combined analysis of all analysis, etc..

new measurement: q^2 dependent $R(D^{(*)})$

-new physics can change q^2 distribution of $R(D^{(*)})$ Phys. Rev. D 91, 114028

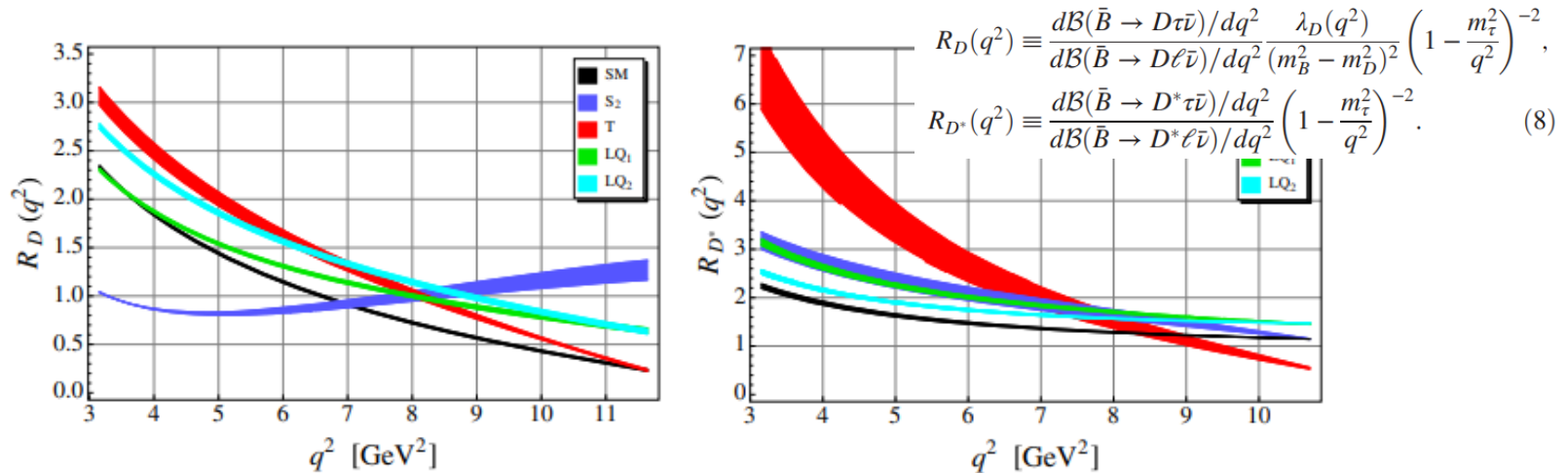


FIG. 4 (color online). The $R_{D^{(*)}}(q^2)$ distributions, predicted in the SM (black) and various NP scenarios listed in Sec. II: S_2 (blue), T (red), LQ_1 (green), and LQ_2 (cyan). The width of each curve is due to the theoretical errors in the hadronic form factor parameters.

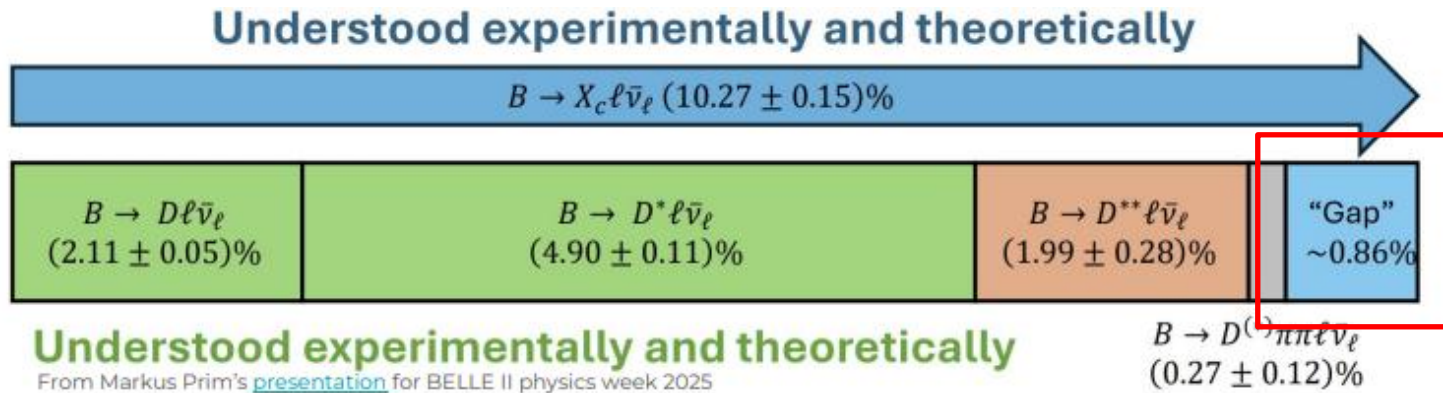
-Analysis of q^2 dependent $R(D^{(*)})$ is on-going at Belle II
 -targeting 2027-2028

new measurement: $B \rightarrow D^{(*)} \eta \ell \nu$

● Next leading systematics is modeling of gap mode in $B \rightarrow X \ell \nu$

-~0.86% unmeasured decay

-for now, we are using $B \rightarrow D^{(*)} \eta \ell \nu$ to model it



Full Gap [slide at last JPS](#)

● We are measuring $\text{BR}(B \rightarrow D^{(*)} \eta \ell \nu)$

-targeting winter 2026

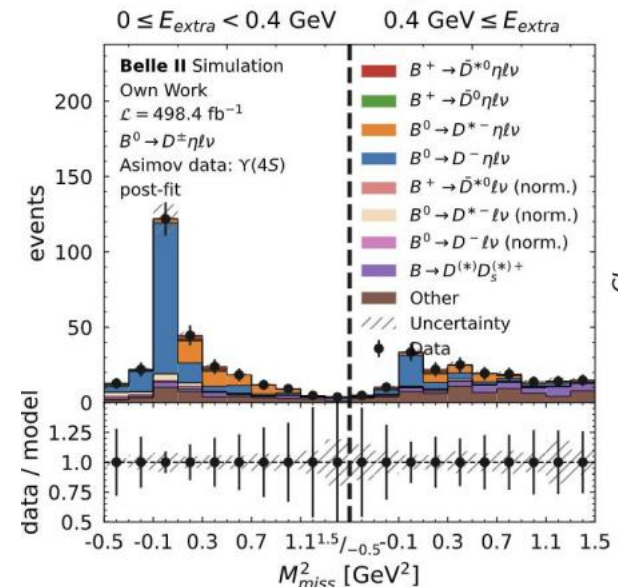
-expected Asimov sensitivity is ~0.1%

$$\mathcal{B}(B^0 \rightarrow D^\pm \eta \ell \nu) = (0.88 \pm 0.10_{\text{stat.}})\%$$

$$\mathcal{B}(B^0 \rightarrow D^{*\pm} \eta \ell \nu) = (0.88 \pm 0.11_{\text{stat.}})\%$$

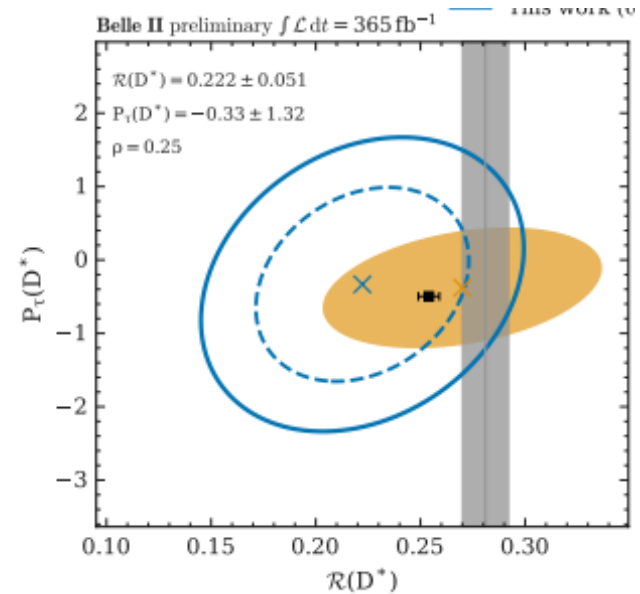
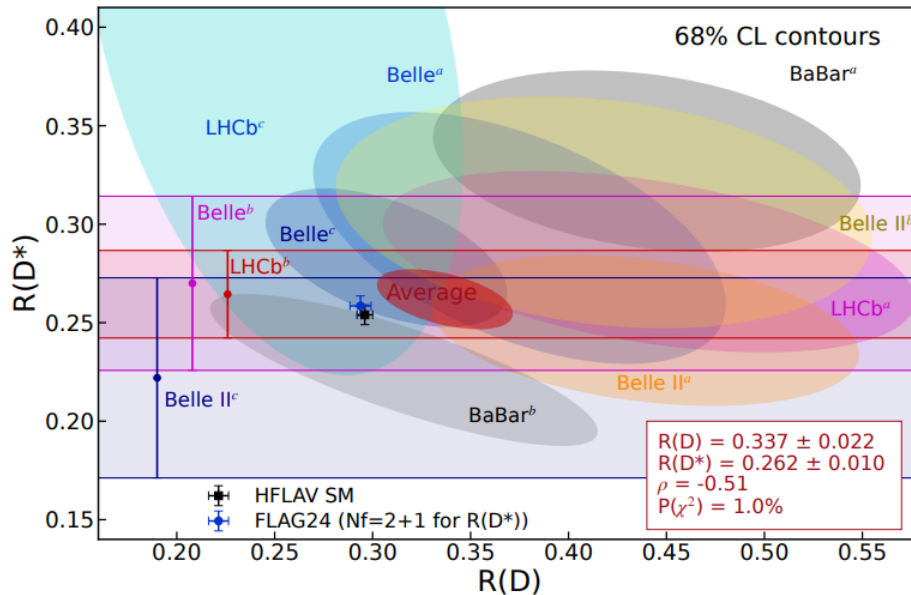
$$\mathcal{B}(B^\pm \rightarrow D^0 \eta \ell \nu) = (0.92 \pm 0.08_{\text{stat.}})\%$$

$$\mathcal{B}(B^\pm \rightarrow D^{*0} \eta \ell \nu) = (0.92 \pm 0.09_{\text{stat.}})\%$$



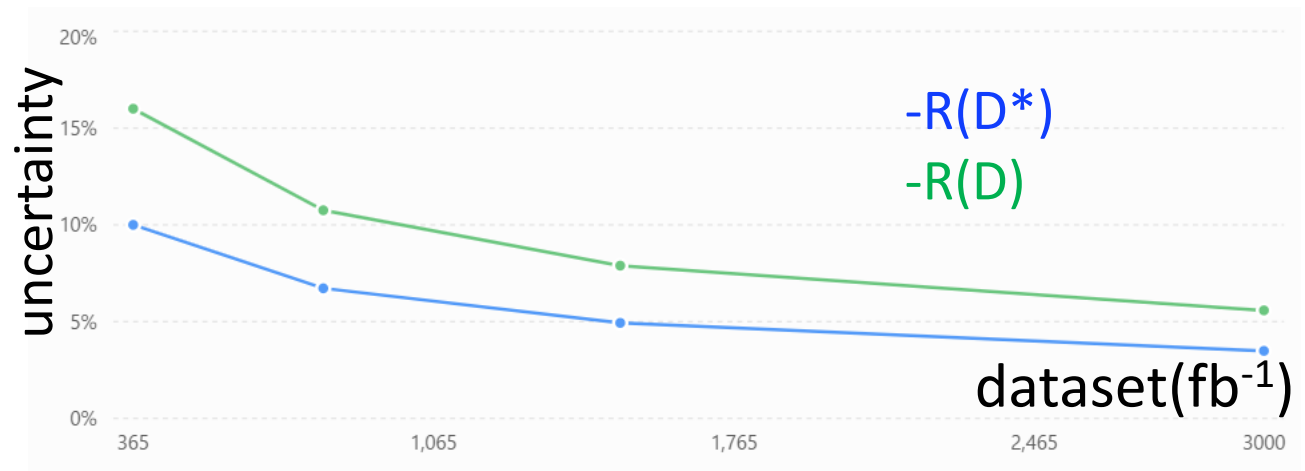
Summary

● Measurement of $b \rightarrow c \tau \nu$: result of $R(D^{(*)})$, $P_\tau(D^*)$



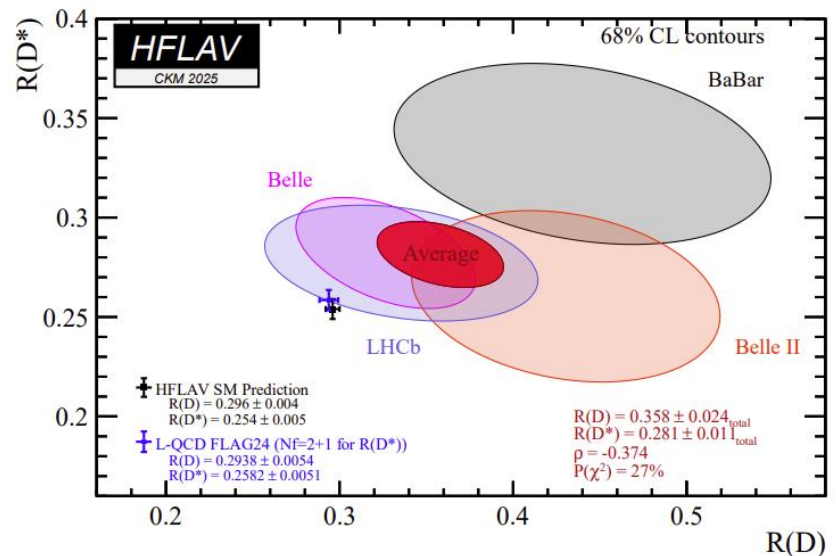
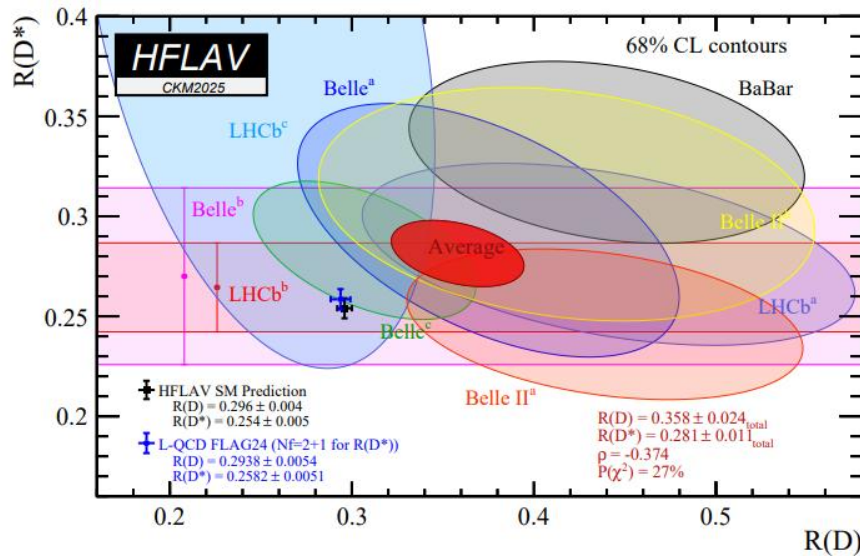
● Expected sensitivity by Belle II in future

- q^2 dependence
- $B \rightarrow D^{(*)} \eta \ell \nu$



backup

R(D(*)) 測定状況 2025

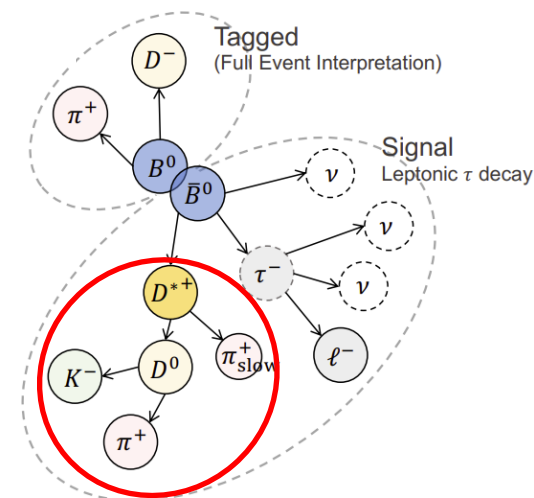


paper	tag手法	τ 崩壊	#BB events	R(D*), R(D)
Babar 2012	hadronic	leptonic	471×10^6	$0.332 \pm 0.024 \pm 0.018, 0.440 \pm 0.058 \pm 0.042$ (灰色)
Belle^a 2015	hadronic	leptonic	772×10^6	$0.293 \pm 0.038 \pm 0.015, 0.375 \pm 0.064 \pm 0.026$ (青)
Belle^b 2017	hadronic	hadronic	772×10^6	$0.270 \pm 0.035^{+0.028}_{-0.025}$ (ピンク棒線)
Belle^c 2020	semileptonic	leptonic	772×10^6	$0.283 \pm 0.018 \pm 0.014, 0.307 \pm 0.037 \pm 0.016$ (緑)
Belle II ^a 2025	semileptonic	leptonic	387×10^6	$0.306 \pm 0.034 \pm 0.018, 0.418 \pm 0.074 \pm 0.051$ (黄色)
Belle II ^b 2025	hadronic	leptonic	387×10^6	$0.242 \pm 0.019 \pm 0.016, 0.439 \pm 0.055 \pm 0.046$ (赤)
paper	D崩壊	τ 崩壊	dataset	R(D*), R(D)
LHCb^a 2023	$D^0 \rightarrow K\pi$	leptonic($\mu\nu\nu$)	RUN1 3fb^{-1}	$0.281 \pm 0.018 \pm 0.024, 0.441 \pm 0.060 \pm 0.066$ (紫)
LHCb^b 2023	$D^0 \rightarrow K\pi$	$\tau \rightarrow \pi\pi\pi(\pi^0)\nu$	RUN1 3fb^{-1}	$0.267 \pm 0.012 \pm 0.019$ (赤棒線)
LHCb^c 2024	$D^+ \rightarrow K\pi\pi$	leptonic($\mu\nu\nu$)	RUN2 2fb^{-1}	$0.402 \pm 0.081 \pm 0.085, 0.249 \pm 0.043 \pm 0.047$ (水色)

D, D* reconstruction

-Use most of D(*) decays with large branching ratios

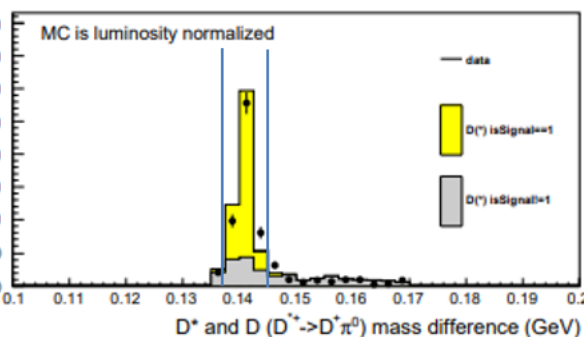
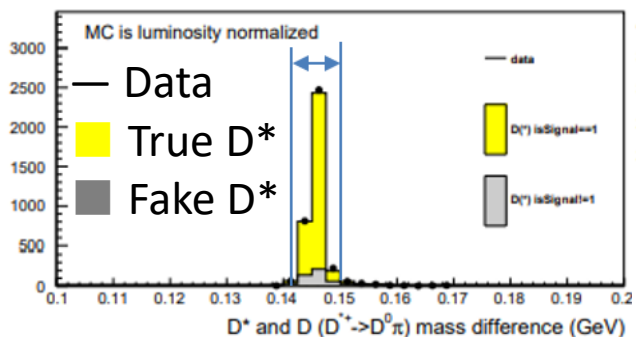
-4 kind of D* decays



$$D^{*+} \rightarrow D^0 \pi^+$$

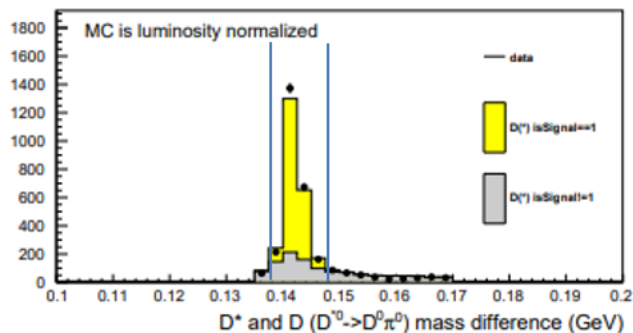
#Events

$$D^{*+} \rightarrow D^+ \pi^0$$

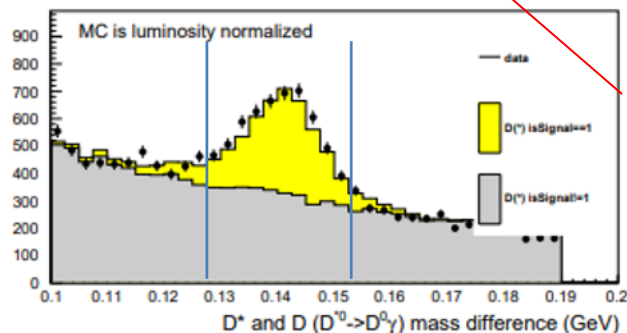


mass difference of D* and D(GeV)

$$D^{*0} \rightarrow D^0 \pi^0$$



$$D^{*0} \rightarrow D^0 \gamma$$



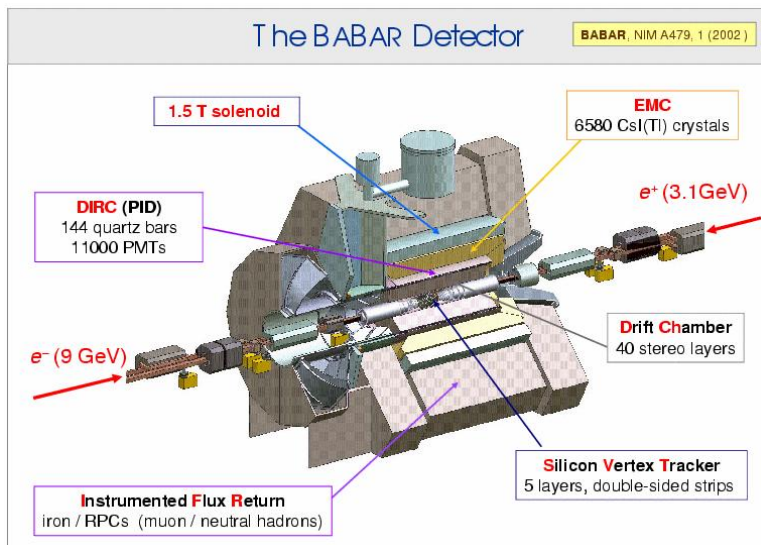
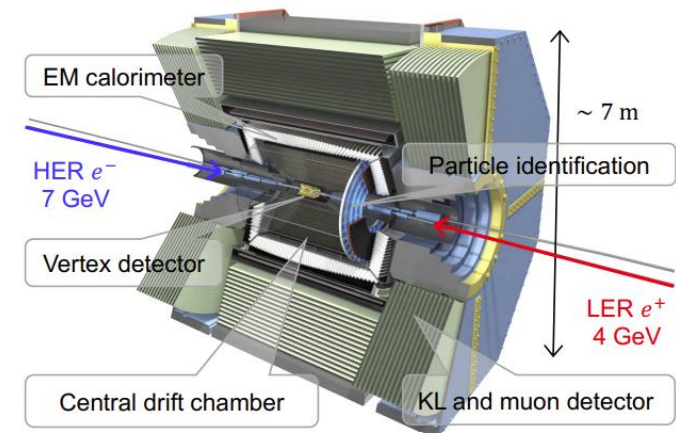
Decay	Branching ratio on PDG
$D^{*+} \rightarrow D^0 \pi^+$	$(67.7 \pm 0.5)\%$
$D^{*+} \rightarrow D^+ \pi^0$	$(30.7 \pm 0.5)\%$
$D^{*0} \rightarrow D^0 \pi^0$	$(64.7 \pm 0.9)\%$
$D^{*0} \rightarrow D^0 \gamma$	$(35.3 \pm 0.9)\%$

gray: newly added

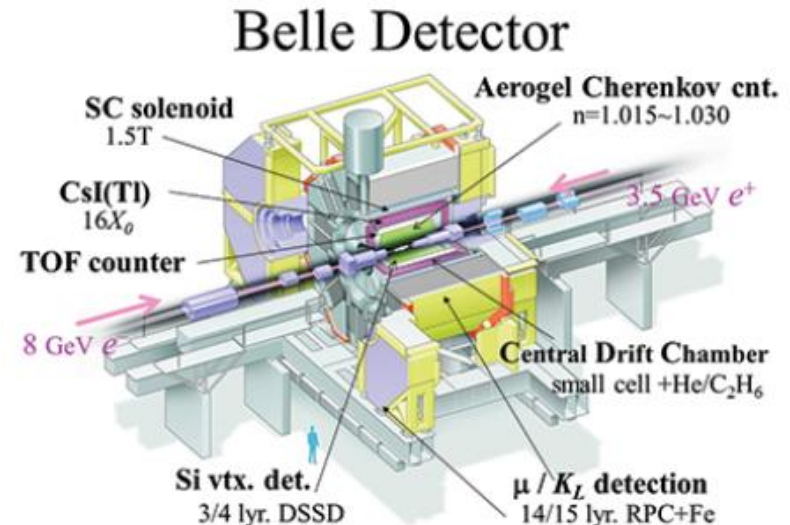
Babar, Belle, Belle II experiments

-on-threshold BB production from $e^+e^- \rightarrow \Upsilon(4S) \rightarrow B\bar{B}$

- nearly 4π coverage with excellent PID
- clean background environment
- known initial beam state
- number of BB events for analysis: $O(10^8)$
 471×10^6 (Babar), 772×10^6 (Belle), 198×10^6 (Belle II)



https://www.ippp.dur.ac.uk/~krauss/Lectures/QuarksLeptons/Detector/Typical_Detector.html



<https://ihepa.phys.ufl.edu/the-belle-and-belle-ii-experiments-at-kekb/>

B_{tag}再構成 @Belle II

-ハドロン崩壊するB_{tag}を再構成

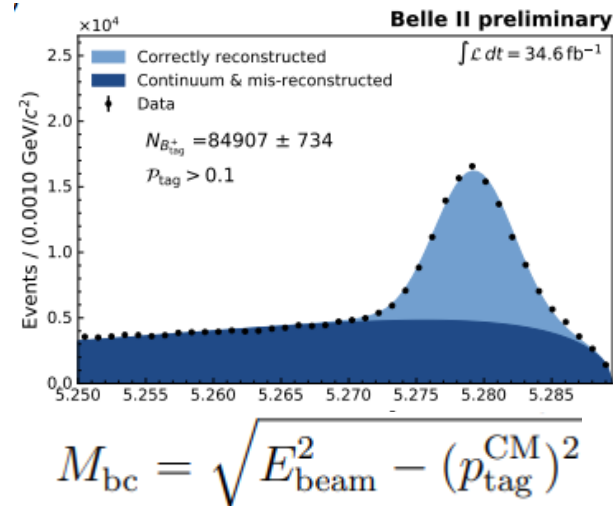
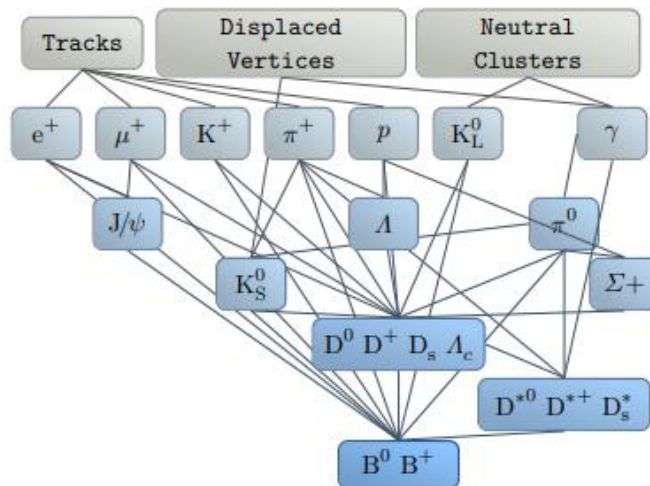
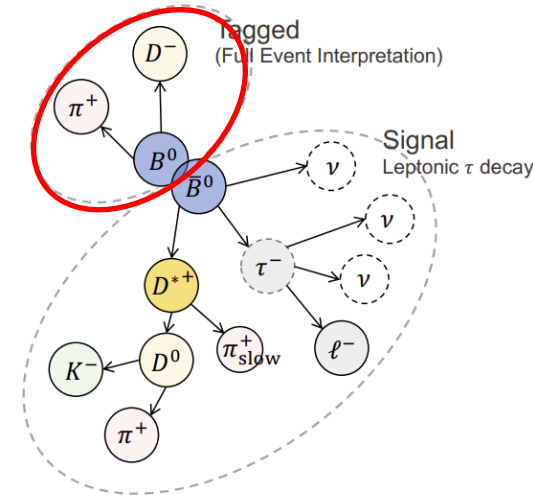
-崩壊の種類が多く(数十)、1つ1つ最適化するのは大変

-Belle II: Full Event Interpretation (FEI)アルゴリズム

-荷電粒子飛跡、中性クラスターを総当たりで組み合わせ

-Multivariate classifierでBの信号確率を計算

学習の入力情報: 娘粒子の生成点, 運動量, 粒子識別



$$M_{bc} = \sqrt{E_{beam}^2 - (p_{tag}^{CM})^2}$$

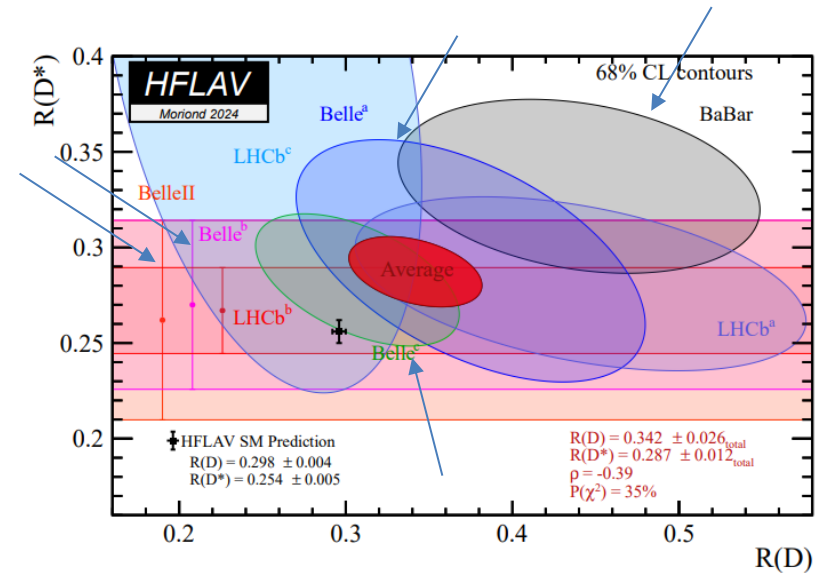
-B_{tag}に対する検出効率 ~0.27%, purity ~15%

-Belleより約2倍検出効率が向上

ハドロン崩壊分岐比
が小さいため 統計勝負₃₄

R(D(*)) 測定 @Belle, Babar

- 基本的な測定手法はBelle IIと同様
- tag手法, fit変数などが異なる
- どの測定も統計誤差が支配的
- 今後Belle IIで改善が見込まれる



paper	tag手法	τ 崩壊	#BB events	fit variable	Reconstructed decay mode	$R(D^*)$ $\pm \text{stat} \pm \text{syst.}$	$R(D)$ $\pm \text{stat} \pm \text{syst.}$
Babar 2012	hadronic	$\tau \rightarrow e\nu\nu, \tau \rightarrow \mu\nu\nu$	471×10^6	$M_{\text{miss}}^2, p_{\ell}^*$	$B \rightarrow D^* \ell \nu, B \rightarrow D \ell \nu$	$0.332 \pm 0.024 \pm 0.018$	$0.440 \pm 0.058 \pm 0.042$
Belle^a 2015	hadronic	$\tau \rightarrow e\nu\nu, \tau \rightarrow \mu\nu\nu$	772×10^6	$M_{\text{miss}}^2, \text{MVA}$	$B \rightarrow D^* \ell \nu, B \rightarrow D \ell \nu$	$0.293 \pm 0.038 \pm 0.015$	$0.375 \pm 0.064 \pm 0.026$
Belle^b 2017	hadronic	$\tau \rightarrow \pi\nu, \tau \rightarrow \rho\nu$	772×10^6	$M_{\text{miss}}^2, E_{\text{ECL}}^{\text{extra}}$	$B \rightarrow D^* \ell \nu$	$0.270 \pm 0.035 \pm 0.028$	
Belle^c 2020	semileptonic	$\tau \rightarrow e\nu\nu, \tau \rightarrow \mu\nu\nu$	772×10^6	MVA, $E_{\text{ECL}}^{\text{extra}}$	$B \rightarrow D^* \ell \nu, B \rightarrow D \ell \nu$	$0.283 \pm 0.018 \pm 0.014$	$0.307 \pm 0.037 \pm 0.016$
Belle II 2023	hadronic	$\tau \rightarrow e\nu\nu, \tau \rightarrow \mu\nu\nu$	198×10^6	$M_{\text{miss}}^2, E_{\text{ECL}}^{\text{extra}}$	$B \rightarrow D^* \ell \nu$	$0.267 \pm 0.041 \pm 0.033$	

- p_{ℓ}^* : Bの静止系でのレプトン運動量

-Belle2015 MVA: カロリメータ残存エネルギー($E_{\text{ECL}}^{\text{extra}}$), $M_{\text{miss}}^2, q_2, p_{\ell}^*, \#\pi^0$ in ROE, $\cos\theta_{YD^*}$

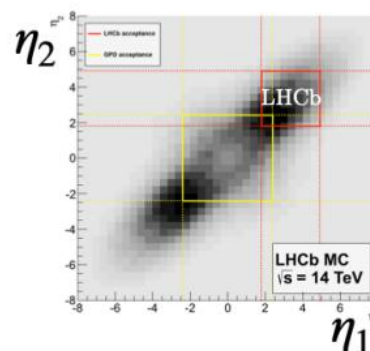
-Belle2020 MVA: M_{miss}^2 , カロリメータ再構成エネルギー, $\cos\theta_{B,D^*\ell}$

LHCb experiment

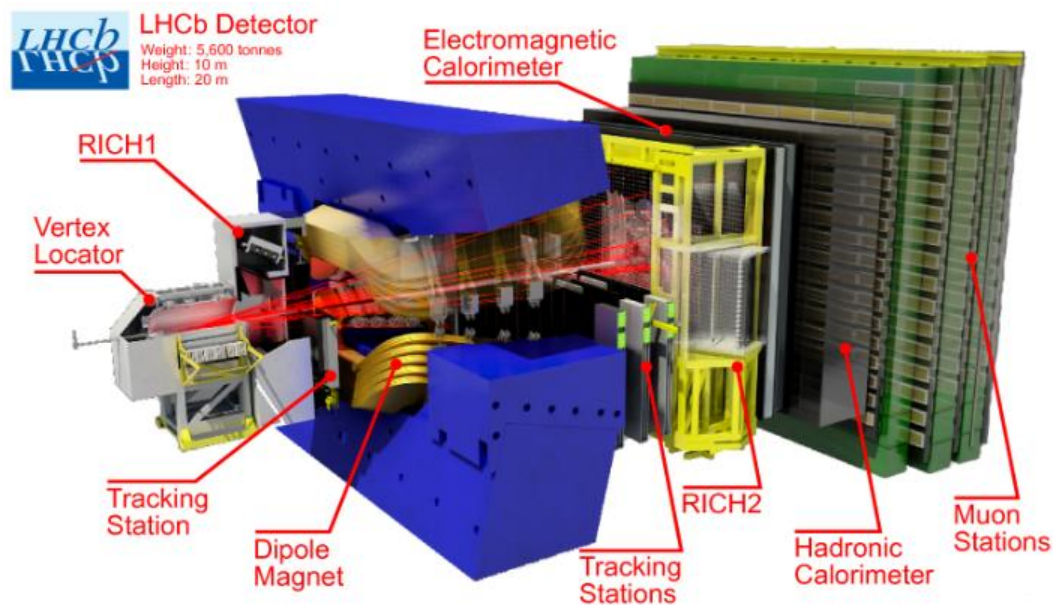
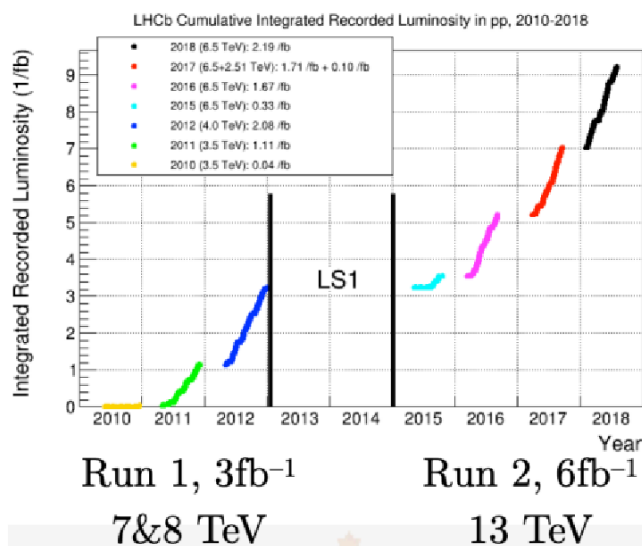
-LHCb: $b\bar{b}$ production with pp collision at 7,8,13 TeV

Forward spectrometer $2 < \eta < 5$

- large $b\bar{b}$ cross section: $\sim 200\mu\text{b}$
- large B momentum: $p_B \sim 80\text{GeV}$
- Run 1+2: $\sim 9\text{fb}^{-1}$ of pp collisions



arxiv.2105.12668, [ICHEP 2024](#)



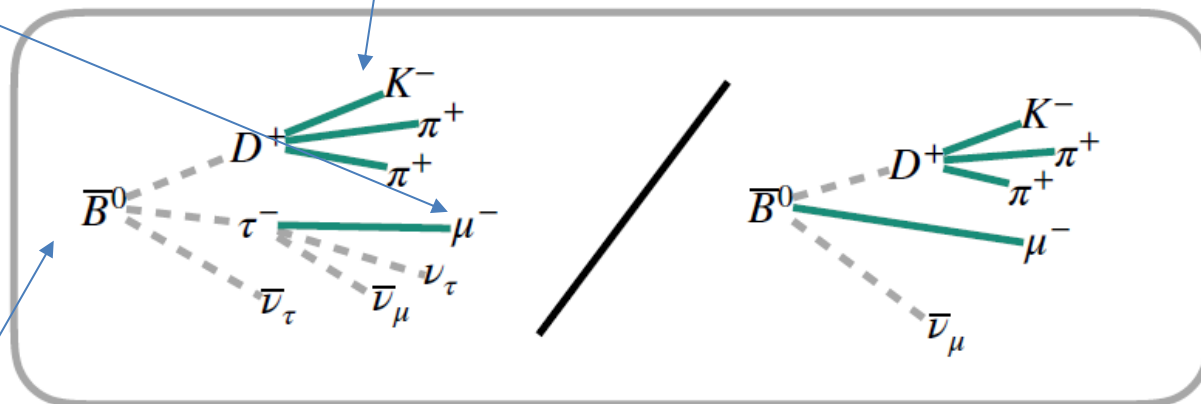
$R(D^*)$ 測定手法 @LHCb

-Reconstruct $B \rightarrow D^* \tau \nu_\tau$ $B \rightarrow D^* \ell \nu_\ell$

- leptonic τ decay and/or hadronic τ decay
- use $D^0 \rightarrow K\pi$ or $D^+ \rightarrow K\pi\pi$ (cleanest D decay) to reduce BG.
- use muon only (not electron)

[R\(D*\)cern seminar](#)

$R(D^+) =$



-Challenge: multiple neutrinos in final state

- No use of Btag. Estimate B momentum from visible particles approximately.
- Check remained particles to estimate background
- Major BG: $B \rightarrow D^{**} \ell \nu$, $B \rightarrow D^* D (\rightarrow \mu X) X$, combinatorial, misidentified, ..
- amount of BG is larger than Babar, Belle in general

-Cancel many systematics error by taking ratio of $B \rightarrow D^* \tau \nu$ and $B \rightarrow D^* \ell \nu$

B 再構成 @LHCb

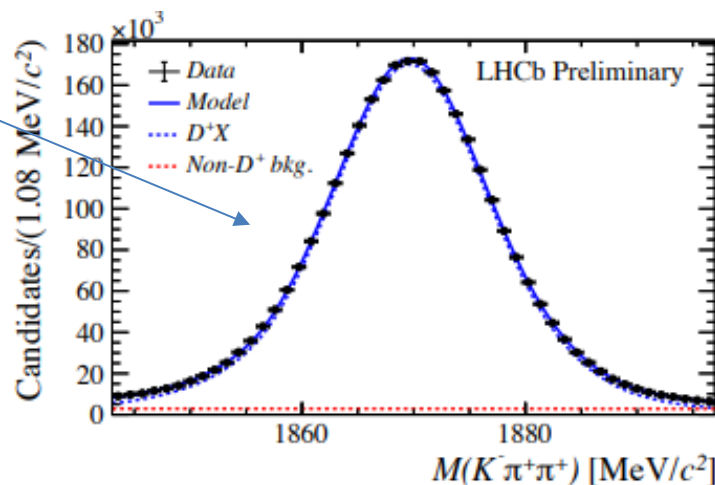
[ICHEP slide](#)

- $D \rightarrow K\pi\pi$ or $D \rightarrow K\pi$ を再構成
- vertexのBDTでB decayかどうか判断
- π^0/γ があればBDTで D^* と区別

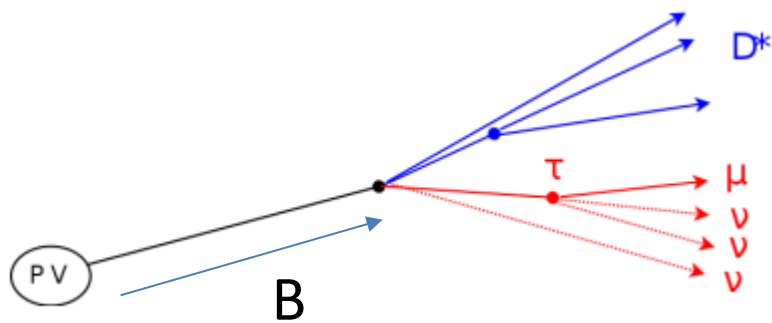
- D^* , μ でBを再構成. Bの運動量概算.

$$(p_B)_z = (m_B/m_{\text{reco}})(p_{\text{reco}})_z \quad (z: \text{ビーム軸})$$

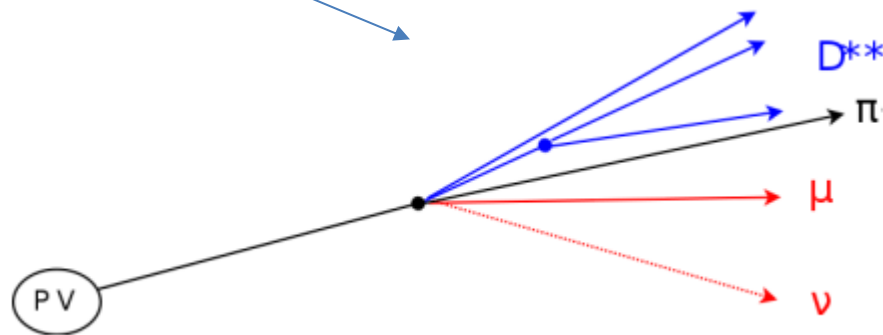
- 残った飛跡の本数で場合分け
(0本: 信号, 1本以上: バックグラウンド)



$$\bar{B}^0 \rightarrow D^{*+} \tau^- \bar{\nu}_\tau$$



バックグラウンド

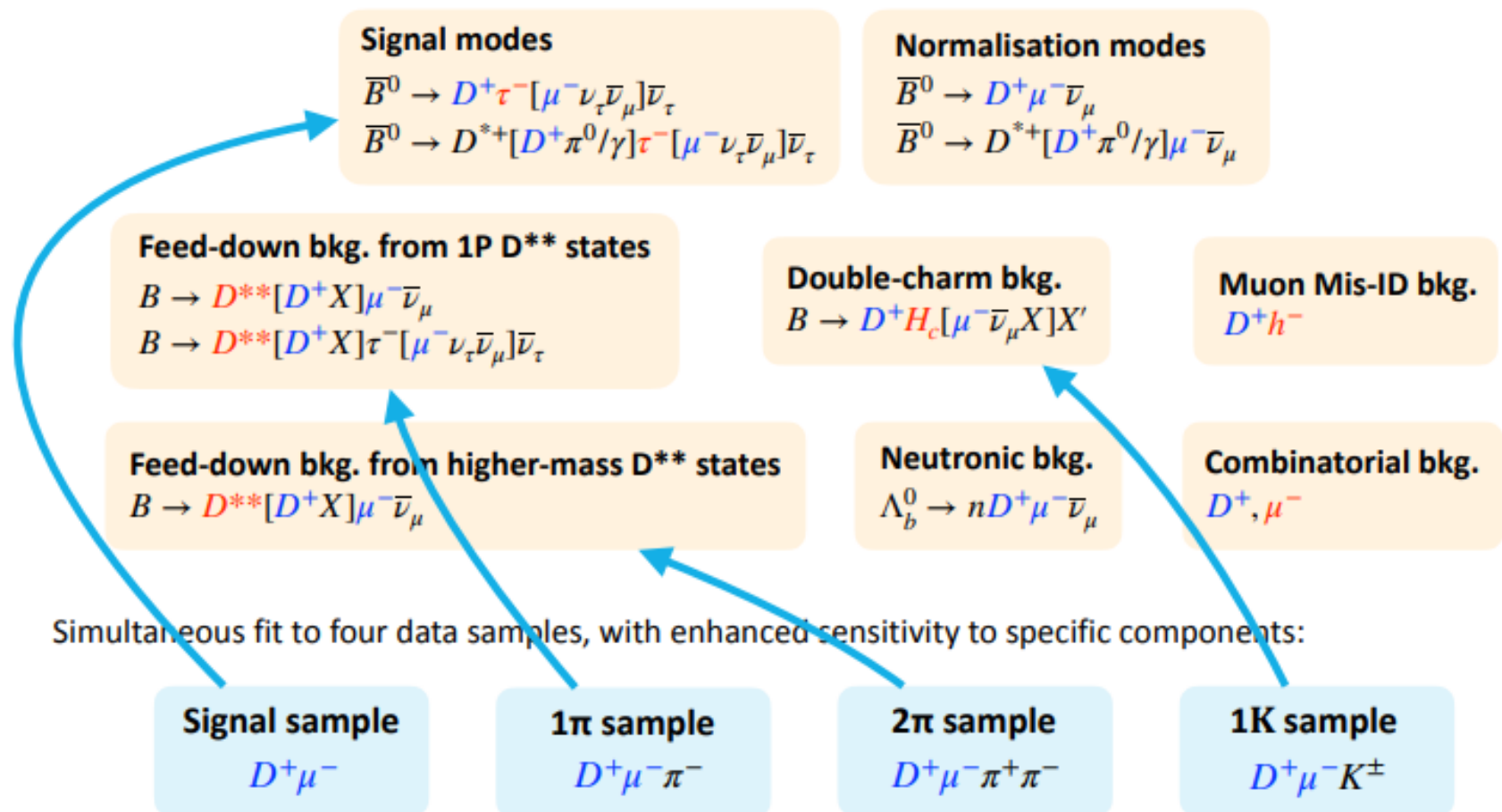


R(D(*)) fit @LHCb

[ICHEP slide](#)

-(M_{miss}^2 , E_μ^* (Bの静止系での μ エネルギー), $q^2=(p_B-p_D)^2$)で3次元フィット

-残飛跡数=1本, 2本のサンプルも同時フィットしてバックグラウンド見積



R(D(*)) result @LHCb

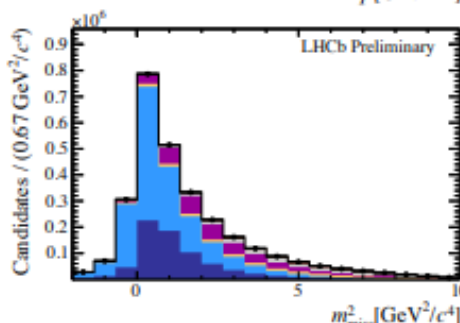
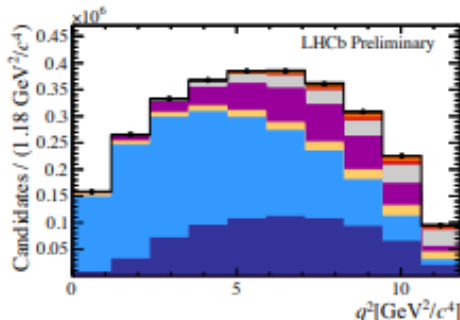
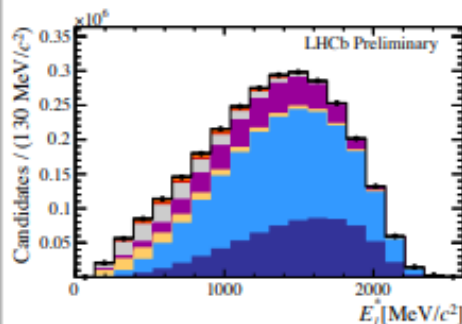
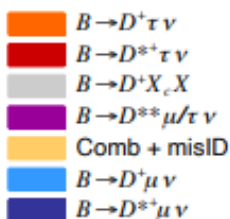
[ICHEP slide](#)

-(M_{miss}^2 , E_μ^* (Bの静止系での μ エネルギー), $q^2=(p_B-p_D)^2$)で3次元フィット

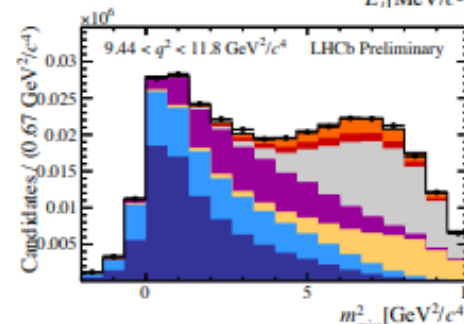
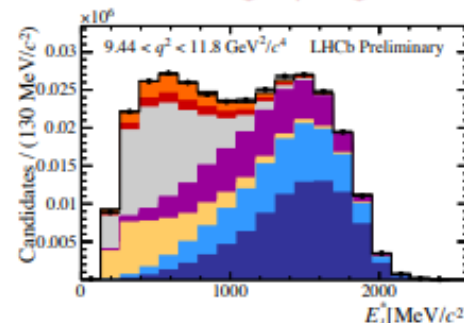
LHCb-PAPER-2024-007

Results

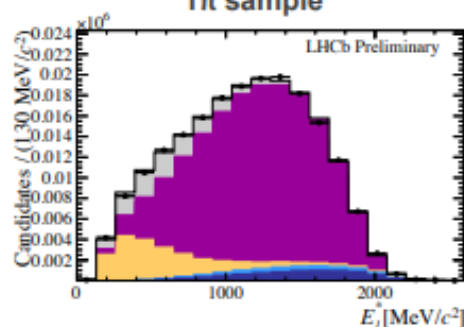
Signal sample



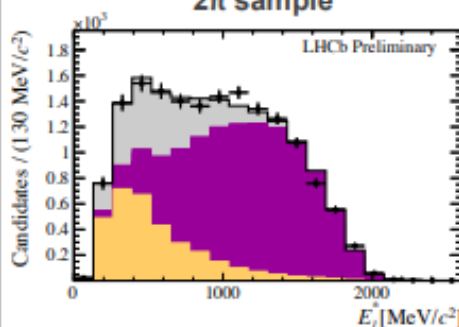
Zoom in high q^2 region



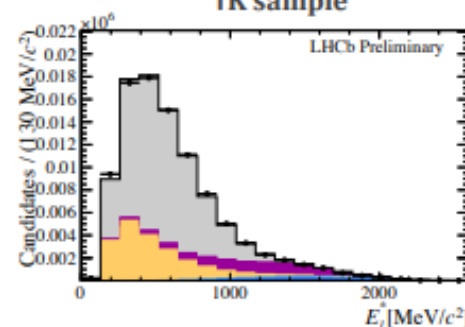
1 π sample



2 π sample



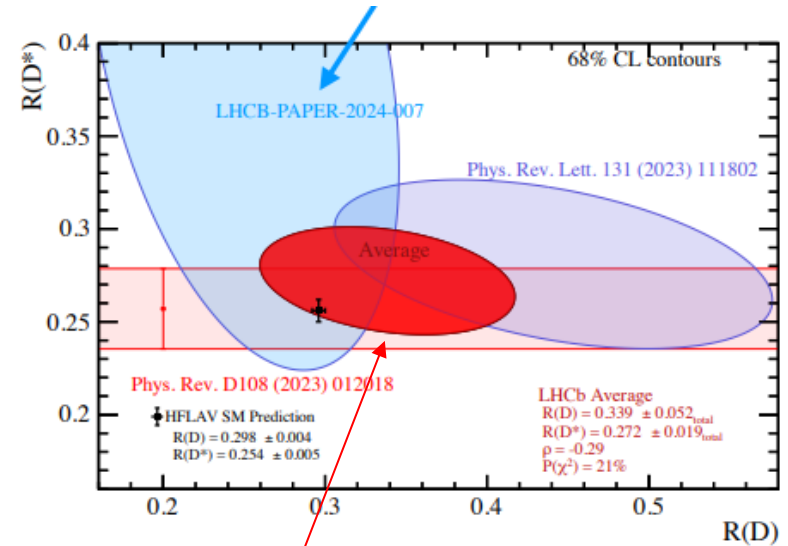
1K sample



R(D(*)) 結果 @LHCb

- LHCbから3つの測定 ($R(J/\psi)$, $R(\Lambda_c^+)$ も)
- D^0 or D^+ , τ の崩壊モード, fit変数が異なる
- LHCb^bは $B \rightarrow D^* \pi \pi \pi$ との比をとって誤差削減.

- どの測定も系統誤差が支配的
- BG, MC stat., form factor. 今後は？



- LHCb の結果のみだと、SMと68%CLでコンシステント

paper	D崩壊	τ 崩壊	dataset	fit variable	$R(D^*)$ $\pm \text{stat} \pm \text{syst.}$	$R(D)$ $\pm \text{stat} \pm \text{syst.}$
LHCb^a 2023	$D^0 \rightarrow K\pi$	$\tau \rightarrow \mu \nu \nu$	RUN1 3fb ⁻¹	$M_{\text{miss}}^2, E^*_\ell, q^2$	$0.281 \pm 0.018 \pm 0.024$	$0.441 \pm 0.060 \pm 0.066$
LHCb^b 2023	$D^0 \rightarrow K\pi$	$\tau \rightarrow \pi \pi \pi (\pi^0) \nu$	RUN1 3fb ⁻¹	M_{miss}^2 , tau decay time, BDT	$0.247 \pm 0.015 \pm 0.015 \pm 0.012$	--
LHCb^c 2024	$D^+ \rightarrow K \pi \pi$	$\tau \rightarrow \mu \nu \nu$	RUN2 2fb ⁻¹	$M_{\text{miss}}^2, E^*_\ell, q^2$	$0.402 \pm 0.081 \pm 0.085$	$0.249 \pm 0.043 \pm 0.047$

external BR

-LHCb^b 2023 BDT: neutral particles around 3π to identify BG from 3π system from D_s^+ decays

Inclusive measurement of $R(X)$ @ Belle II

-The first measurement of $R(X) = \frac{\mathcal{B}(B \rightarrow X\tau\nu_\tau)}{\mathcal{B}(B \rightarrow X\ell\nu_\ell)}$ at B factory, 189fb^{-1}

-inclusive: complementary to exclusive analyses of $R(D^*)$

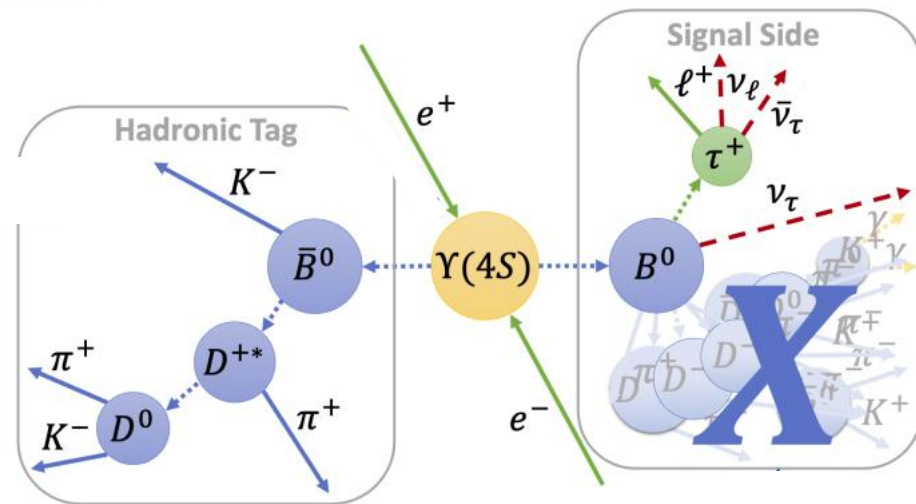
-one of unique and high-profile goals of BelleII

-Reconstruct $B \rightarrow X\tau\nu_\tau, B \rightarrow X\ell\nu_\ell$

- B_{tag} : Hadronic tag

- B_{sig} : Leptonic τ decays of $\tau \rightarrow e\bar{\nu}_e\nu_\tau / \mu\bar{\nu}_\mu\nu_\tau$
 $e(\mu)$ momentum^{lab} $> 0.5(0.7)$ GeV

Any other particles in final state (X)



-Challenge: large BG and modeling of many decay channels

-correct understanding of PDF shapes and background yields:

PDF shapes are calibrated in side-band by using X mass distribution

R(X) signal extraction

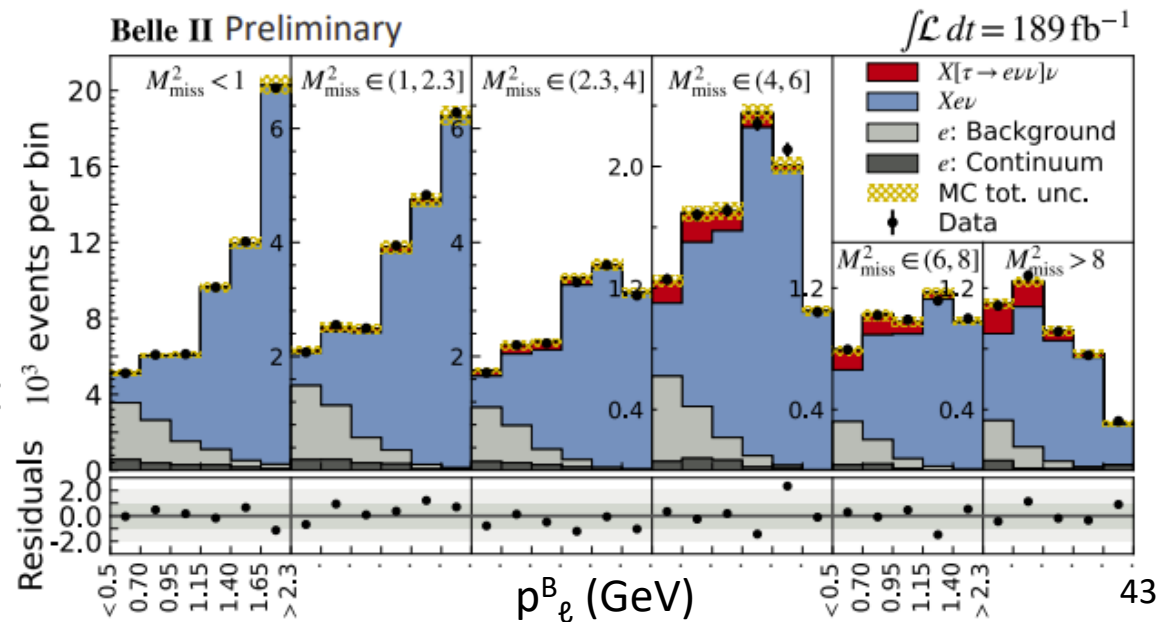
-Two-dimensional binned likelihood is used to extract $N_{B \rightarrow X\tau\nu}$, $N_{B \rightarrow X\ell\nu}$

- p_{ℓ}^B : lepton momentum in B rest frame
- M_{miss}^2 : missing mass of un-detected particles

-Templates for fitting

- $X\tau\nu$, $X\ell\nu$
- Continuum with off-resonant data constraint
- Background from fake and secondaries leptons

-Post fit distributions show good data/MC agreement, including BG dominant bin:



R(X) Result

-The first results of $R(X) = \frac{\mathcal{B}(B \rightarrow X\tau\nu_\tau)}{\mathcal{B}(B \rightarrow X\ell\nu_\ell)}$ at B factory:

[PRL 132,211804\(2024\)](#)

$$R(X_{\tau/\ell}) = 0.228 \pm 0.016(\text{stat.}) \pm 0.036(\text{syst.})$$

$$\text{-e only: } R(X_{\tau/\mu}) = 0.232 \pm 0.020(\text{stat.}) \pm 0.037(\text{syst.})$$

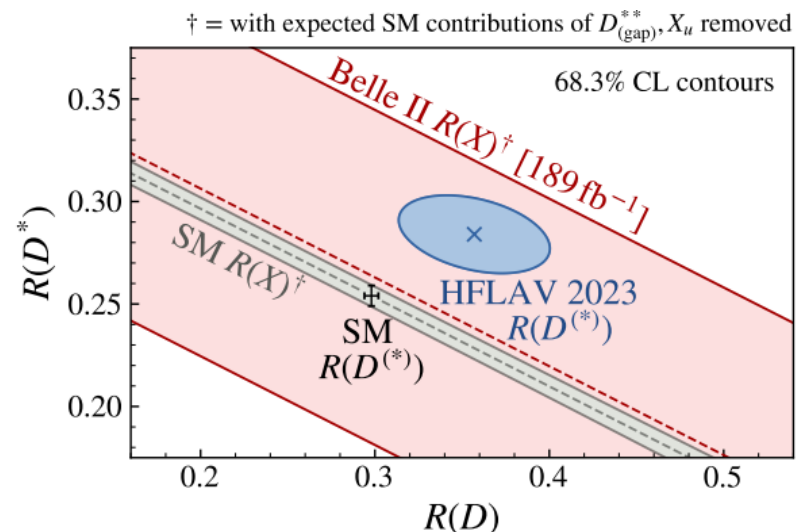
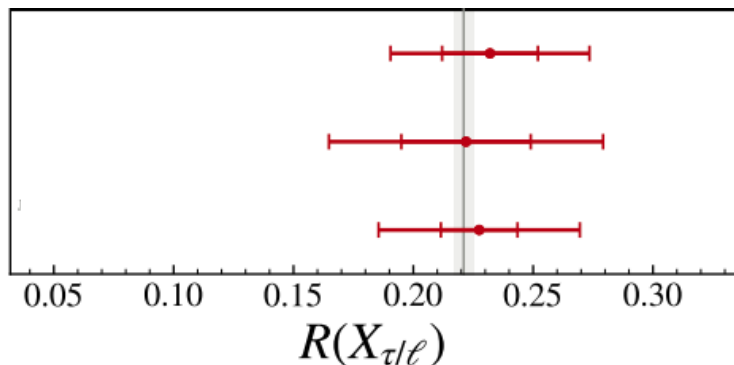
$$\text{-}\mu \text{ only: } R(X_{\tau/e}) = 0.228 \pm 0.027(\text{stat.}) \pm 0.050(\text{syst.})$$

Major systematics: MC statistics, PDF shape, BR of $B \rightarrow D^{**}\ell\nu$

-Consistent with SM prediction and $R(D^{(*)})$ measurements

SM prediction

J. High Energy Phys. 11, 7 (2022)



B→D*τν τ偏極度測定 @Belle II

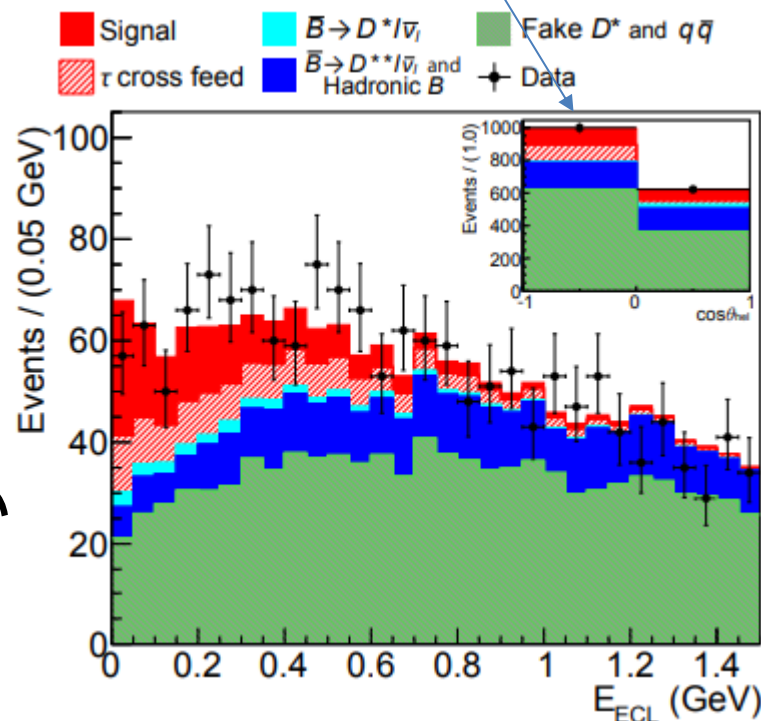
-[Belle^b 2017](#) で $R(D^*)$ と $P_\tau(D^*)$ を測定

- 測定手順は $R(D^*)$ と同様
- ただし $\cos\theta_{\text{hel}}$ の正負(forward, backward)にビンを分けて同時フィット

-測定結果:

$$R(D^*) = 0.270 \pm 0.035(\text{stat.})^{+0.028}_{-0.025}(\text{syst.})$$
$$P_\tau(D^*) = -0.38 \pm 0.51(\text{stat.})^{+0.21}_{-0.16}(\text{syst.}).$$

SM prediction: $P_\tau(D^*) = -0.497 \pm 0.013$
と誤差の範囲で一致. ただし誤差は大きい



$B \rightarrow D^* \tau \nu$ D^* 偏極度測定 @Belle

-Belleでの 772×10^6 BB pairを使った微分崩壊分岐比の解析

-統計を重視するため(?), 解析手法がこれまでに述べた解析と異なる

- $\tau \rightarrow \ell \nu \nu$, $\pi \nu$ 両方使用

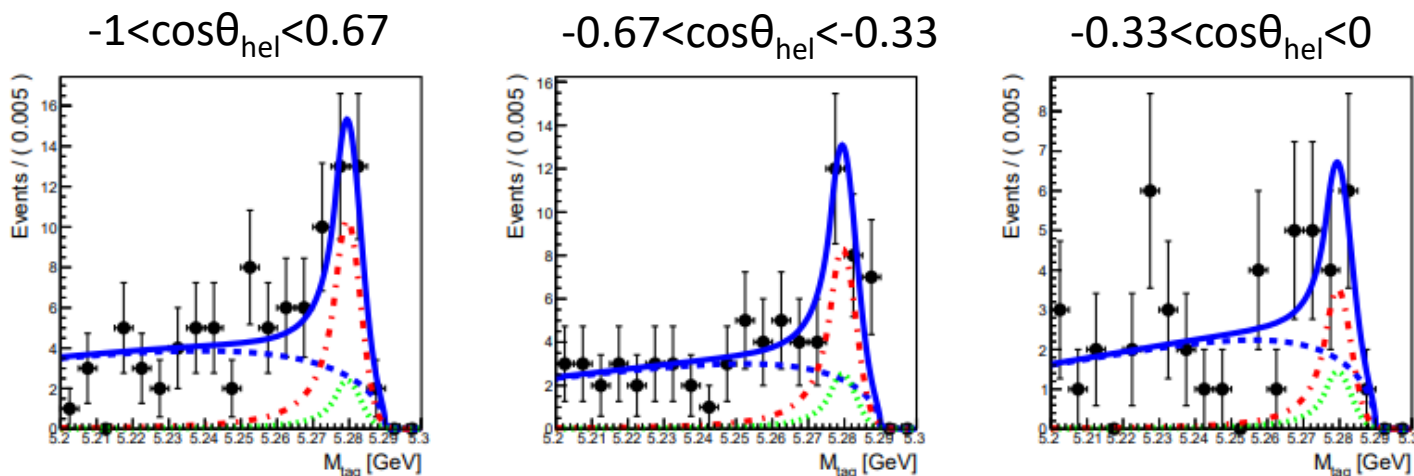
- B_{tag} の再構成をカットベースで緩く行う $\rightarrow$ 統計増

- $B \rightarrow D^* \tau \nu$ をカットベースでエンハンス ($X_{\text{miss}} = (E_{\text{miss}} - |p_{D^*} + p_{\tau}|) / \sqrt{(E_{\text{beam}}^2 - m_B^2)}$)

- B_{tag} の質量を $\cos\theta$ ごとにフィットして微分断面積を算出

arxiv.1903.03102

$B \rightarrow D^* \tau \nu$ ($D^* \rightarrow \pi D$, $D \rightarrow K \pi$, $\tau \rightarrow e \nu \nu$)の例



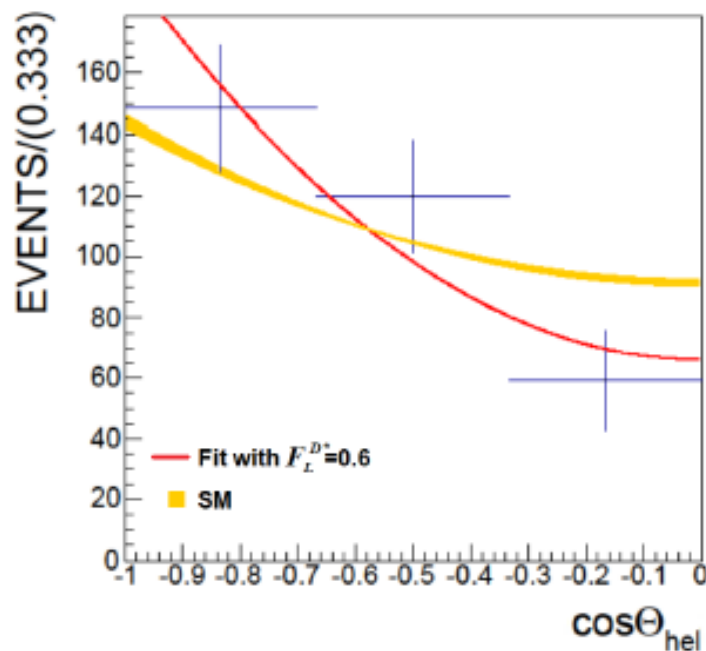
$B \rightarrow D^* \tau \nu$ D^* 偏極度測定 @Belle

-Belleでの 772×10^6 BB pairを使った微分崩壊分岐比の解析

-微分崩壊分岐比より $F_L^{D^*}$ をfit:

$$F_L^{D^*} = 0.60 \pm 0.08(\text{stat.}) \pm 0.04(\text{sys.})$$

SM model: $F_L^{D^*} = 0.441 \pm 0.06, 0.457 \pm 0.010$ など. $\sim 1.7\sigma$ で一致.



arxiv.1903.03102