

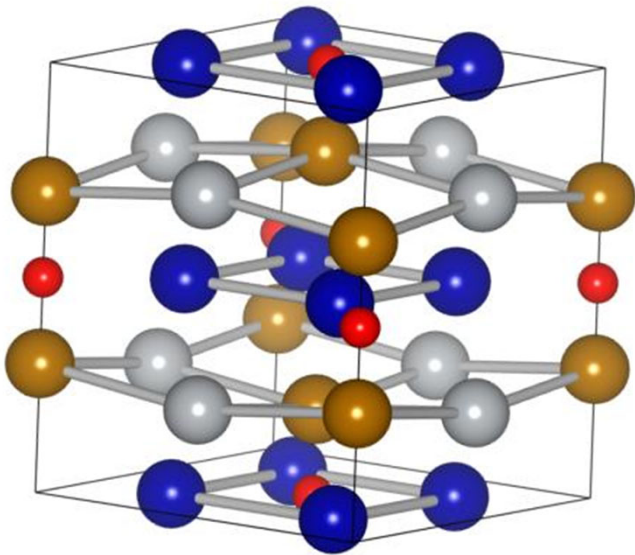
# Neutron Diffraction

--- Practical Technique of crystal and magnetic structure refinements by **powder diffraction**. ---

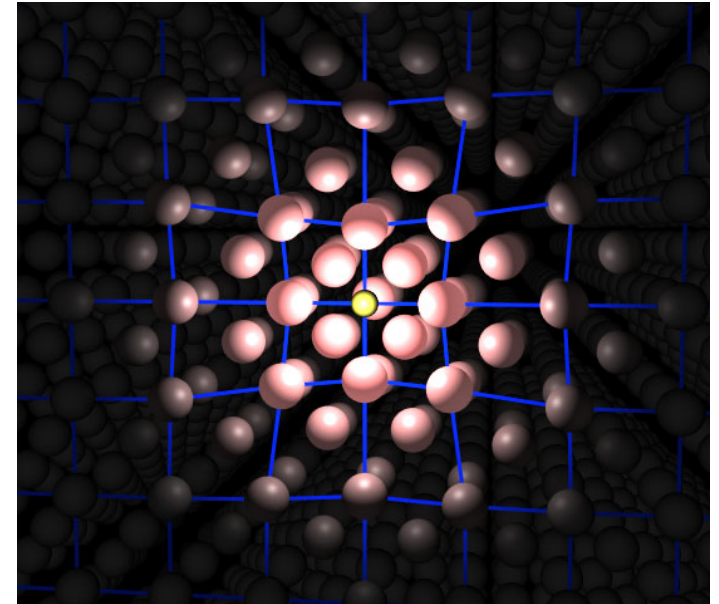
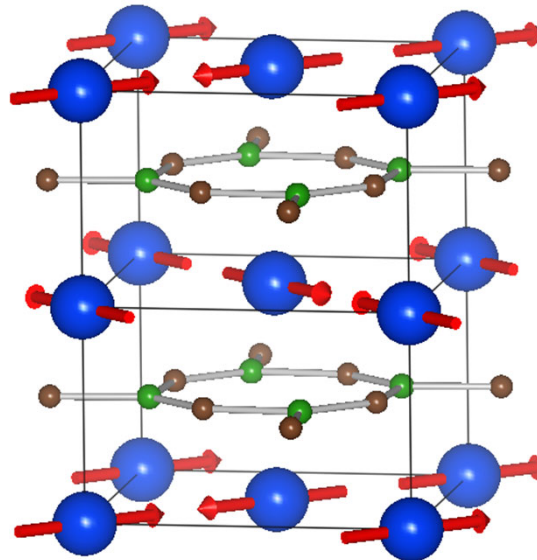
Prof. Kenji Ohoyama

Ibaraki Univ.

# About me



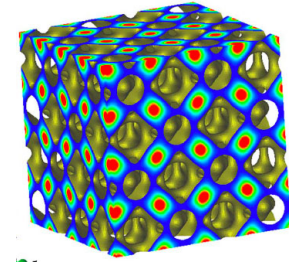
Structural Physics by neutron scattering.



Local structure around dopant by newly developed technique , neutron holography

# Advantages of Neutrons

Ion conductor  
Yashima et al. 2005



Light elements

Hydrogen Storage  
Li-Batteries  
Ion Conductors

Transmission

Radiography  
Stress

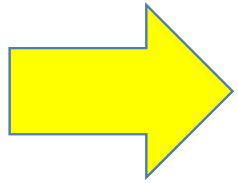
Magnetic Moment

Magnetic Structure  
Spin wave  
Magnetic Device

Energy-Wave length

Spin wave  
Phonon  
Interaction

# Contents



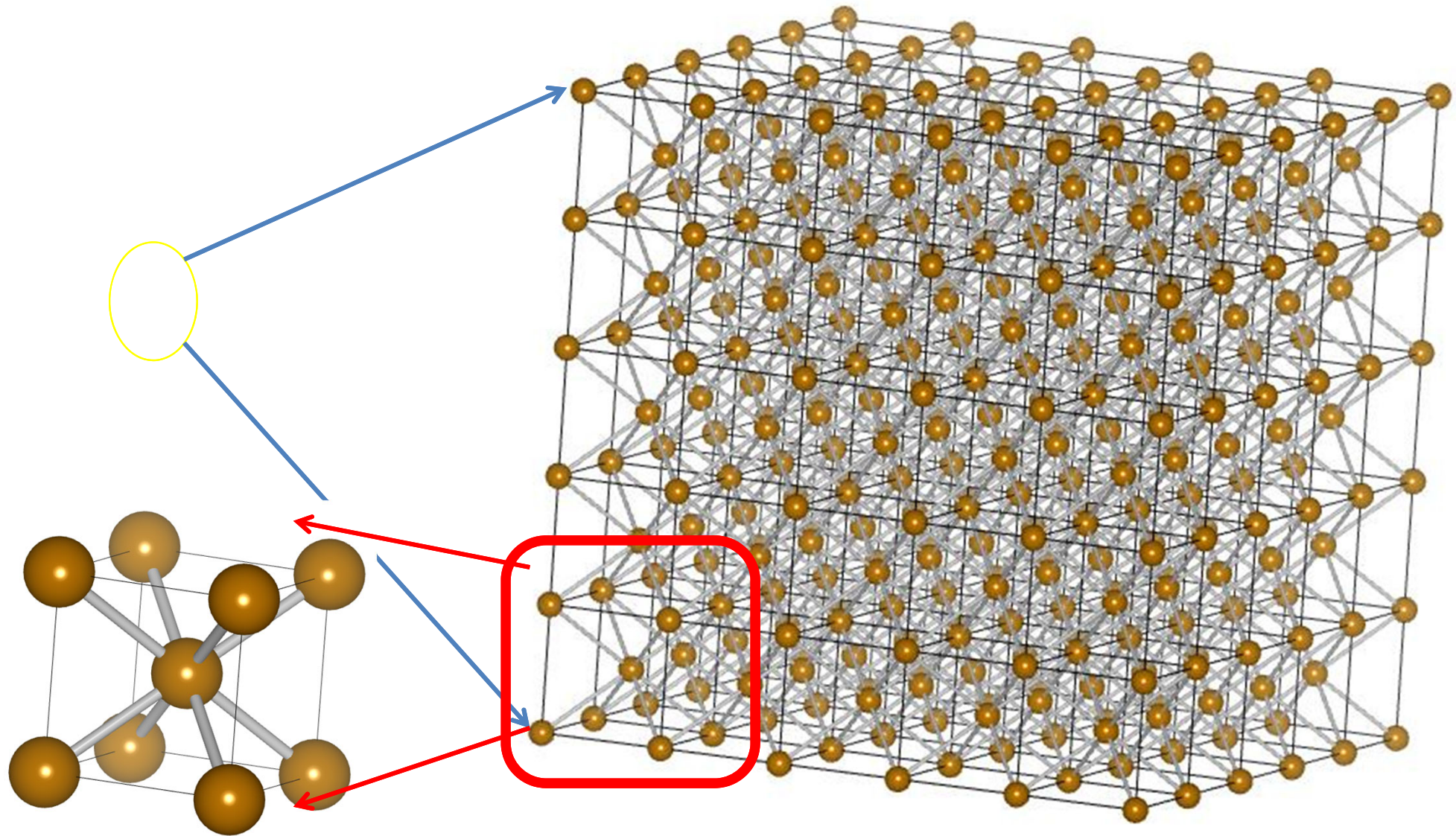
1: Why you have to know atomic structures?

2: Diffraction = Direct observation of Reciprocal Lattice

3: Crystal Structure Refinements

4: Magnetic Structure Refinements.

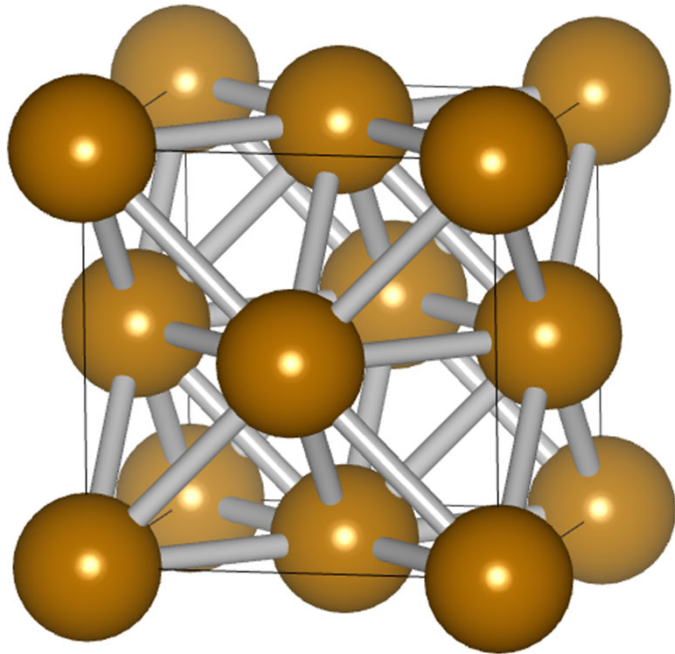
# Why you have to understand Crystal Structures?





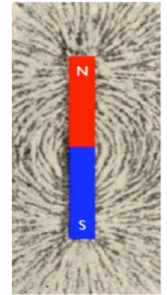
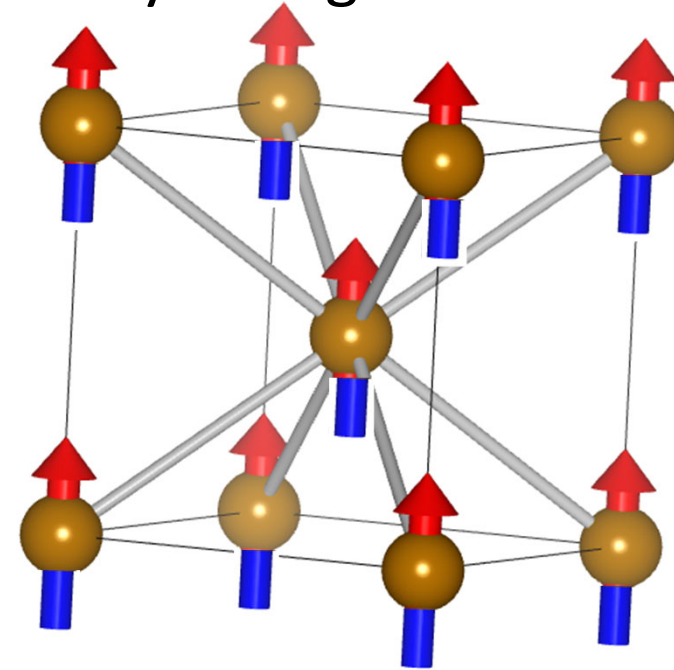
# Importance of Crystal Structure

Iron which is **NOT** attracted by a magnet.



Iron

Iron which is attracted by a magnet at RT.



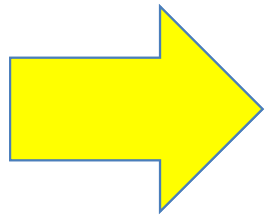
To understand **Macro**sopic properties, information on atomic structures is indispensable.

Probe = diffraction

X-ray, electron, and **NEUTRON**

# Contents

1: Why structures are important?



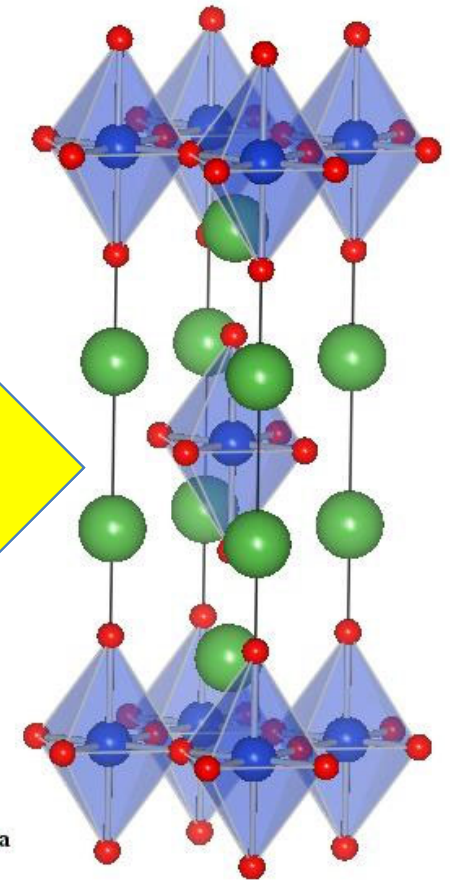
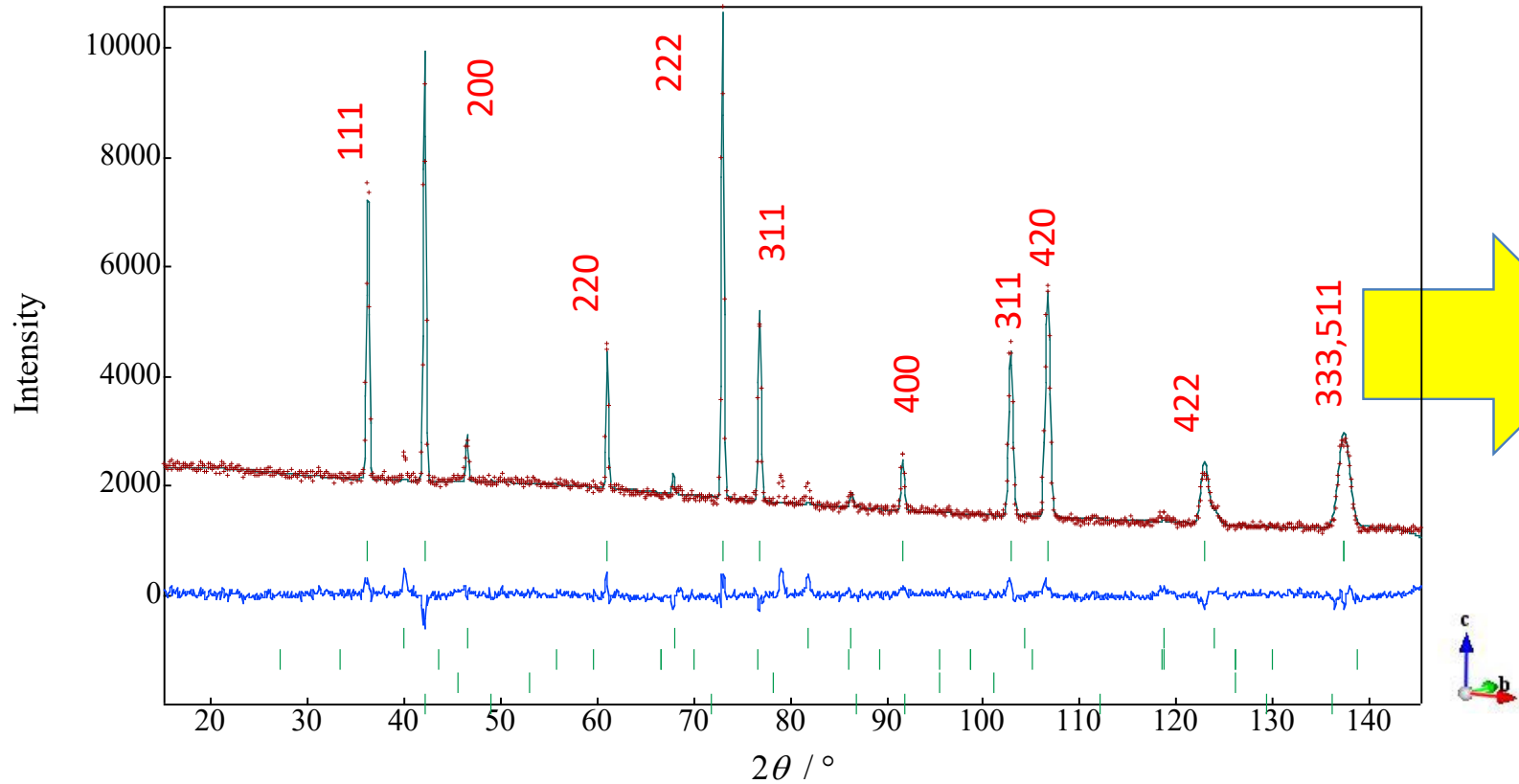
2: Diffraction = Direct Observation of Reciprocal Lattice

3: Crystal Structure Refinements

4: Magnetic Structure Refinements.

# Crystal Structure Refinement?

## Powder Diffraction Pattern



**Peak Position, Index** -> Lattice Parameter, Unit Cell,  
Space Group

**Peak Intensity** -> Atomic Position, occupancy, vibration



# Intensity of Bragg Peaks

Completely the same as X-ray diffraction

f: atomic scattering factor

↑ for X-ray

Integrated Intensity of a Bragg

$$\left( \frac{d\sigma}{d\Omega} \right)_{hkl} = c \left| \sum_i b_i \exp(2\pi i(\vec{r}_i \cdot \vec{K})) \right|^2$$

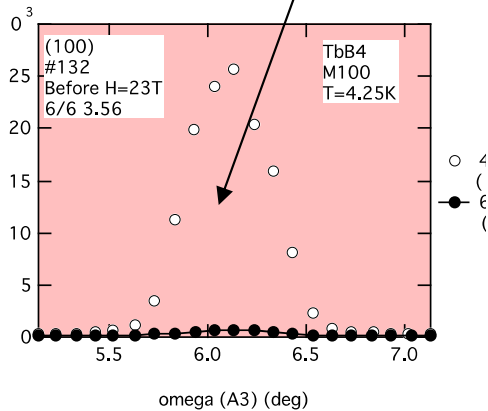
↓  
 $b_i$ : scattering length

$\vec{r}_i = (x_i, y_i, z_i)$  Position of i-th atom in the unit cell

$\vec{K} = (h, k, l)$  Scattering vector or Index

$$= c_{hkl} \left| \sum_i b_i \exp(2\pi i(x_i h + y_i k + z_i l)) \right|^2$$

Structure Factor



# Reciprocal Lattice is “Real”

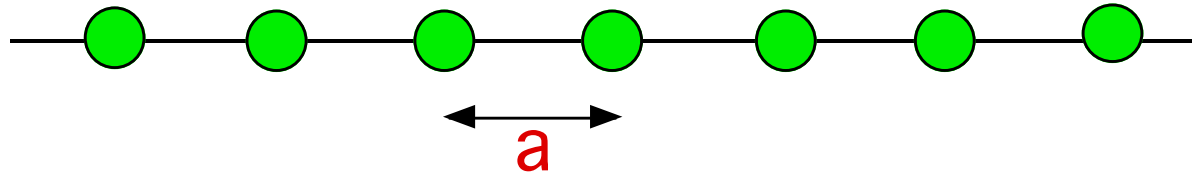
You can see it.

$\text{CaO}_7 \text{Al}_2\text{O}_3$  Oikawa et al. 2014

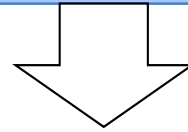
Bragg reflection = Reciprocal lattice point



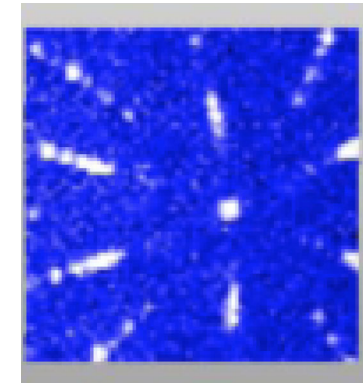
# Reciprocal Space (Lattice) is



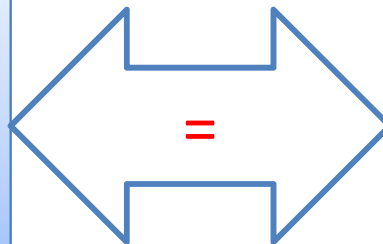
Space which indicates Spatial periodicity of materials with points



$1/a$  or  $2\pi/a$



Bragg peaks at a  
reciprocal space.  
=Reciprocal Lattice

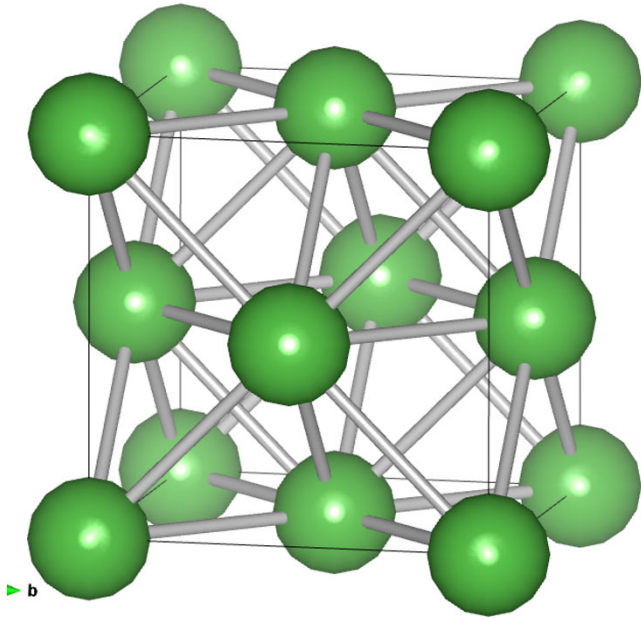


The sample has THE  
periodicity

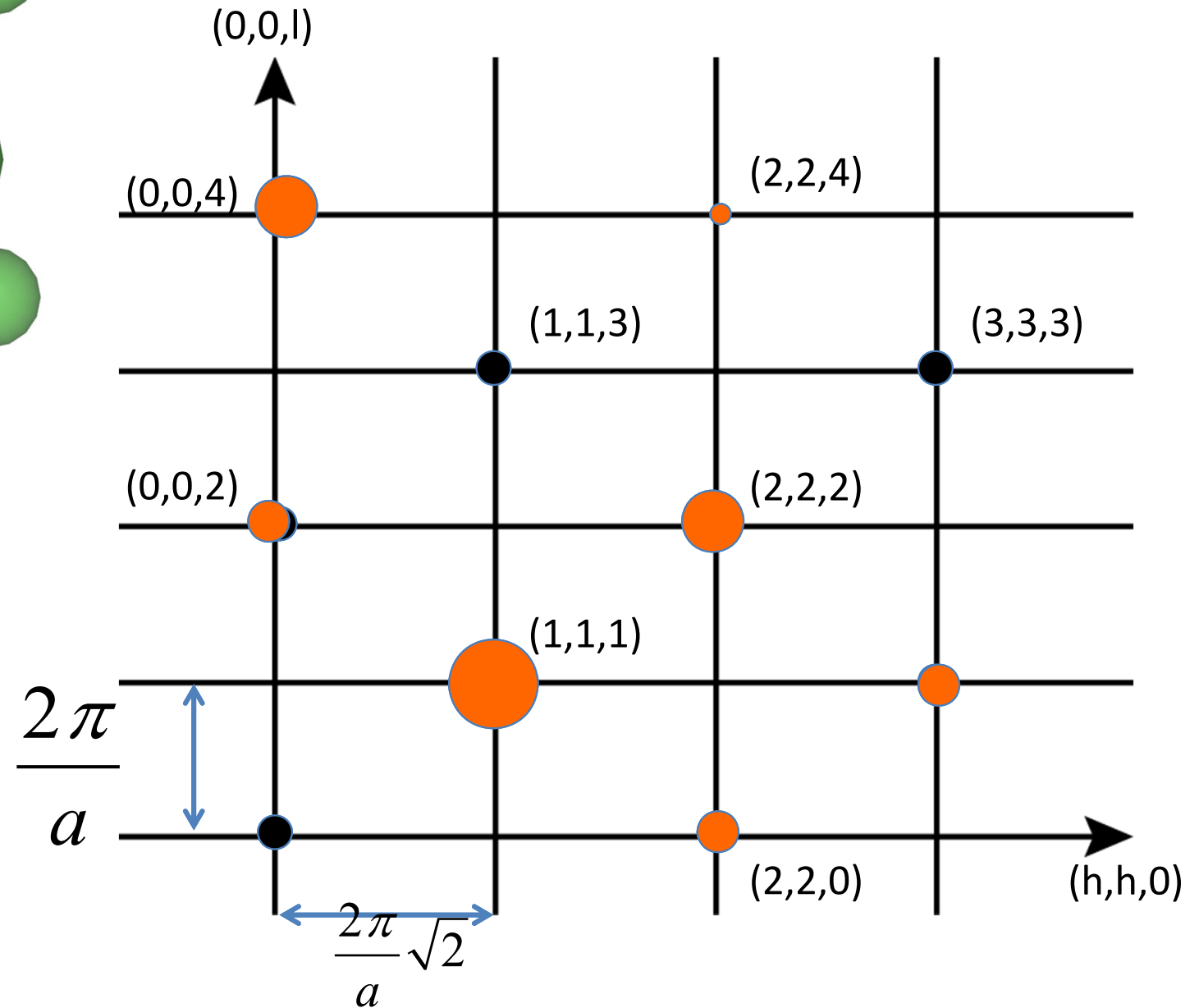
Atom, Nucleus  
Magnetic moment,  
Vacancy

# Reciprocal Lattice of FCC

= Positions of Bragg Peaks



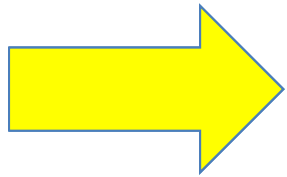
Reflection rule  
All even / all odd



# Contents

1: Why structures are important?

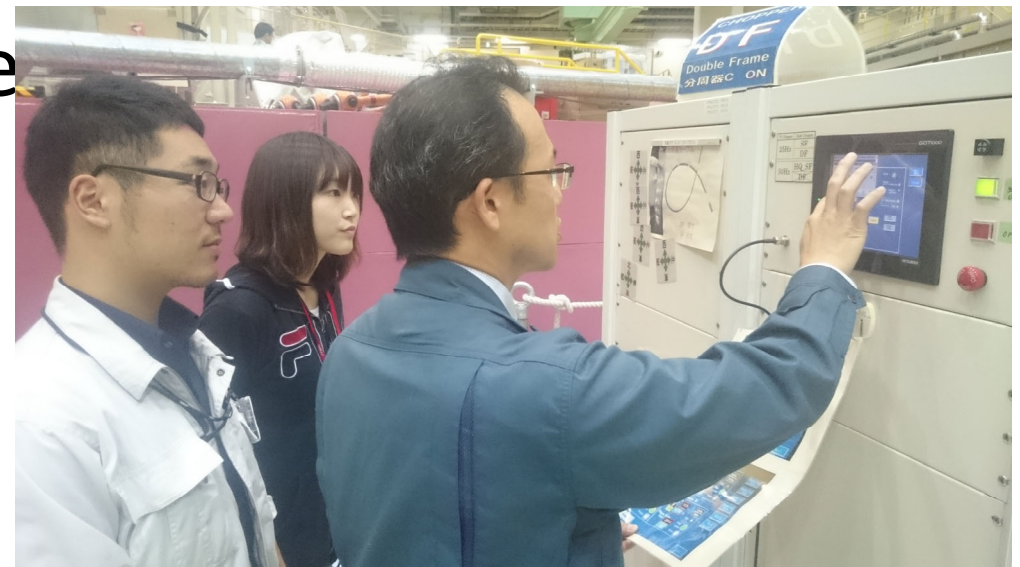
2: Diffraction = Direct Observation of Reciprocal Lattice



3: Crystal Structure Refinements

Practical Process for refinement of a Hydride

4: Magnetic Structure



# Hydride in Society

HP of Orimo Lab of IMR < Tohoku Univ

Compact Hydrogen Storage

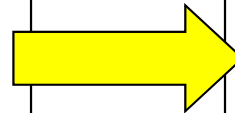
Properties can be changed  
by Hydrogen

Storage Materials

Liquid H<sub>2</sub>  
(-250° C)

High P H<sub>2</sub> Gas  
(200 atm)

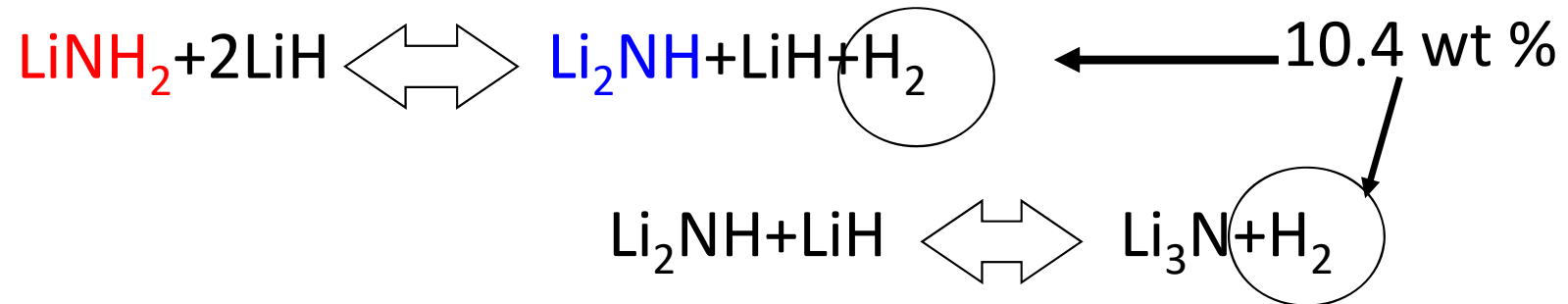
Accurate information on crystal  
structure of Hydrogen is  
important



Advantage of neutrons

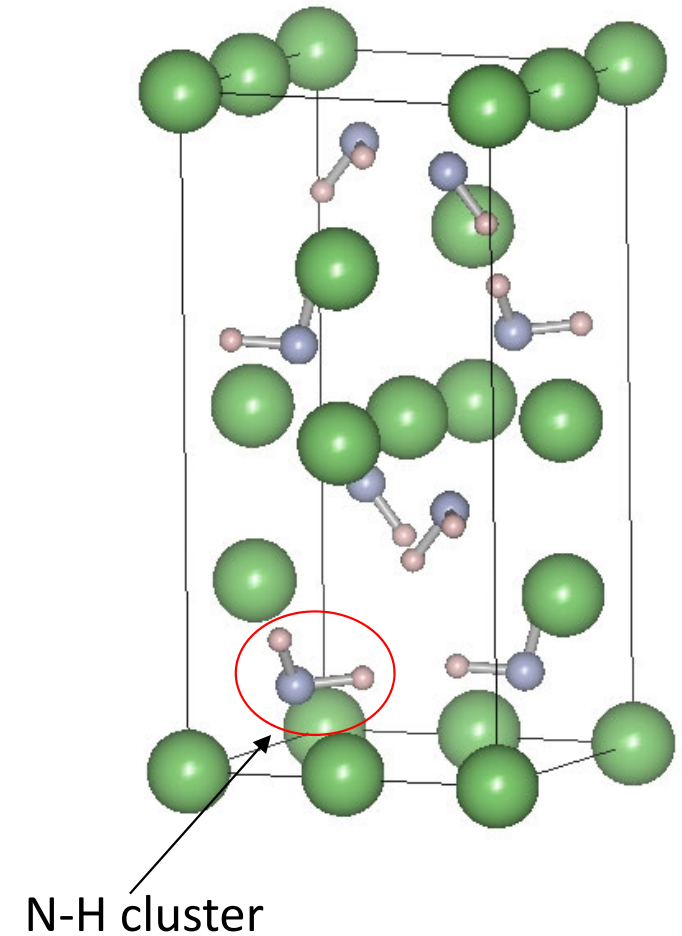
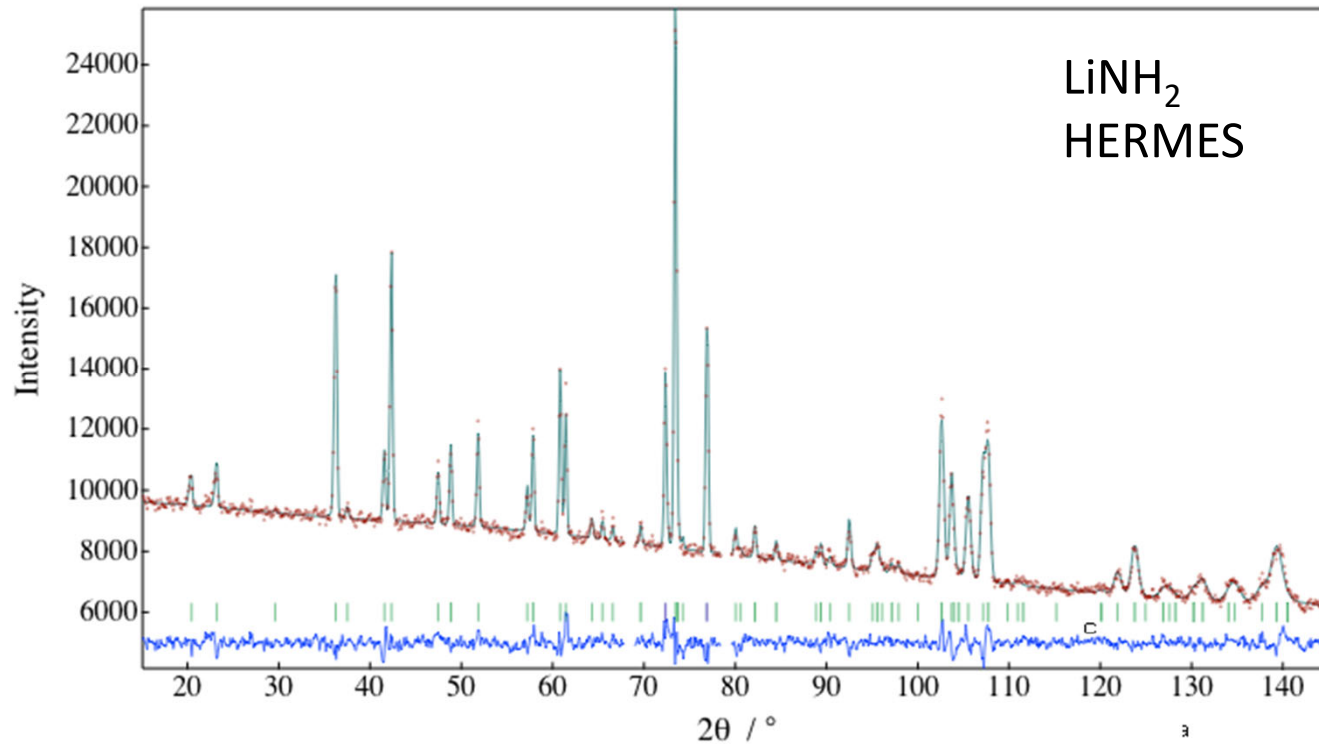


# Li-N-H compounds



# Crystal Structure of $\text{LiNH}_2$

## Rietveld Analysis



$\text{LiNH}_2$

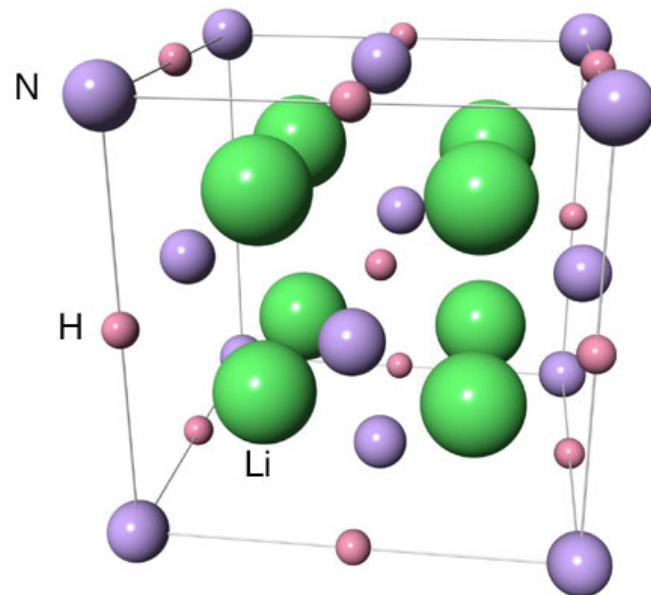
N-H Distance  $\sim \text{NH}_3$

H. Jacob and R. Juza, Z. Anorg. Allg. Chem. 391 (1972) 271 .



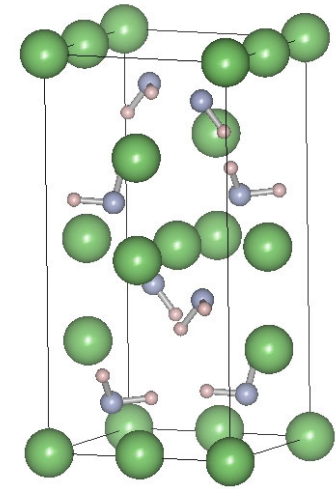
# On the other hand, $\text{Li}_2\text{NH}$ ?

The structure in a Database



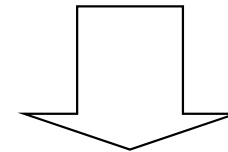
Fm-3m  
A=5.05Å

Powder Diffraction File, 6-0417.



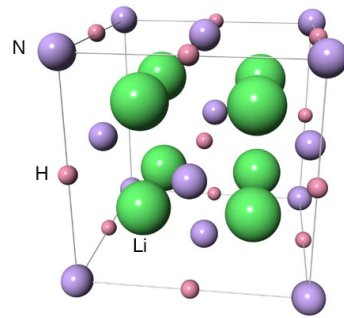
Completely different from  $\text{LiNH}_2$

- 1) N-H  $\sim 2.5\text{\AA}$  (1.03Å for  $\text{LiNH}_2$ )
- 2) No N-H cluster

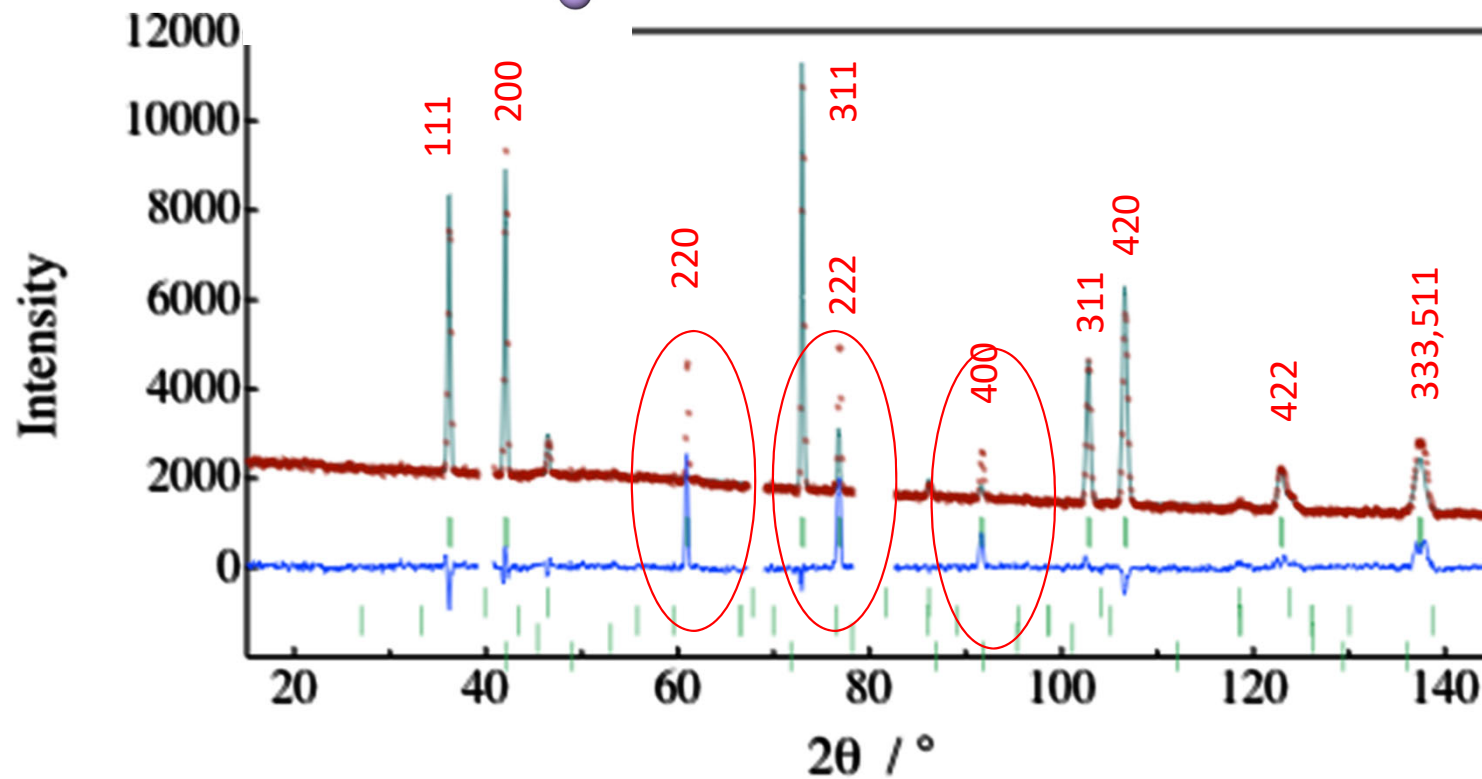


The structure may be wrong?

# Li<sub>2</sub>NH: ND pattern



← This is wrong!



→ FCC

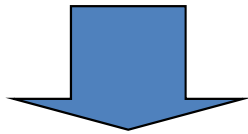


# What is the structure of $\text{Li}_2\text{NH}$ ?

Basic Conditions

1: FCC ( $a \sim 5.05 \text{ \AA}$ )

2: 4 molecule in a unit cell. ( $Z=4$ )



There are only 5 Space Groups allowed.

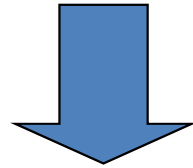
$F23$ ,  $Fm-3$ ,  $F432$ ,  $F-43m$ ,  $Fm-3m$

You can check the all the 5 space groups.

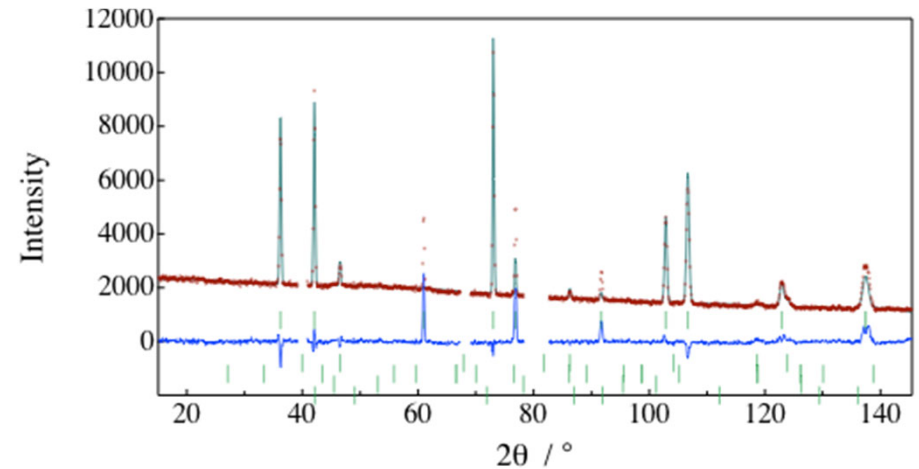
However,

However,

The 5 Space Groups never give good models which can represent the data.

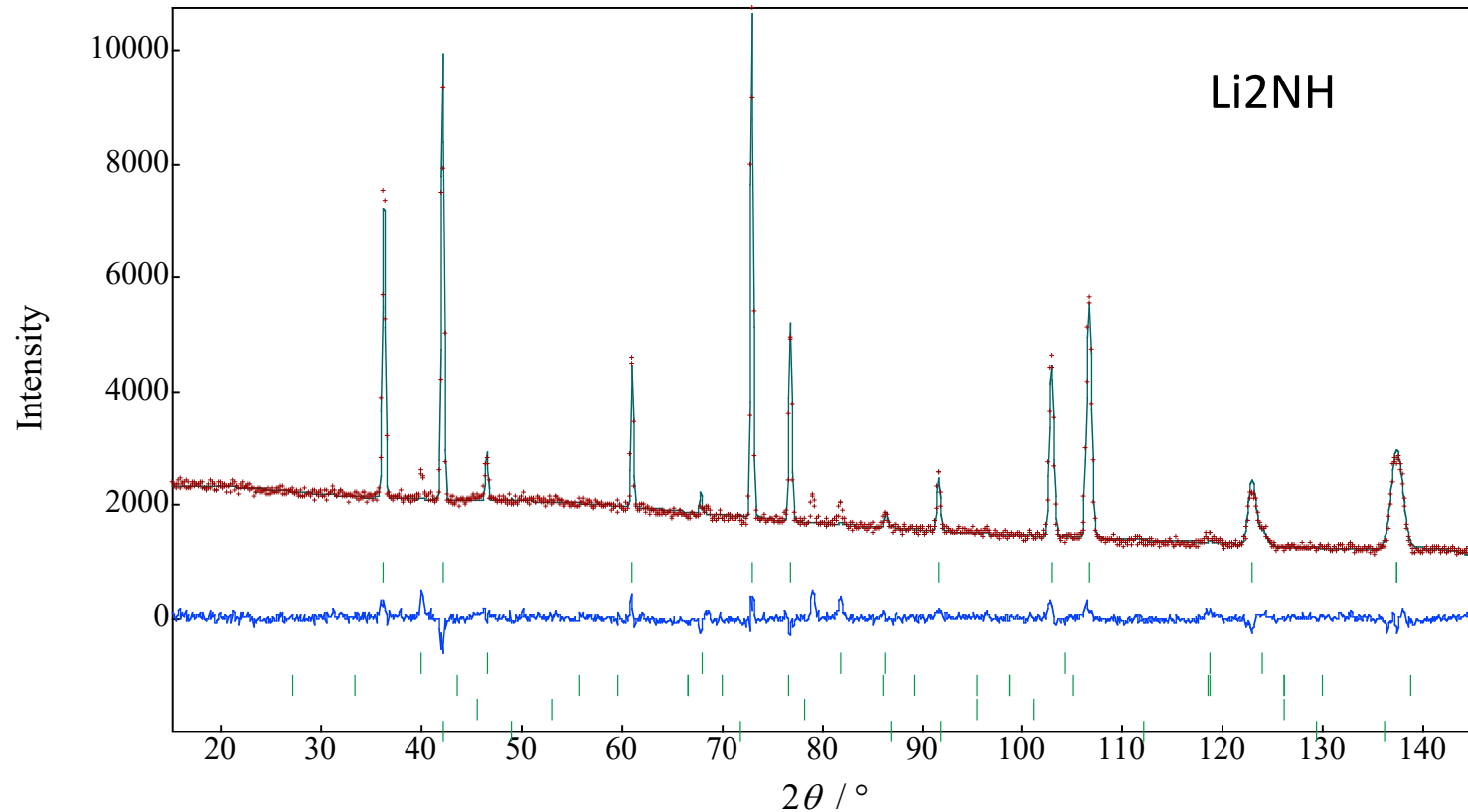
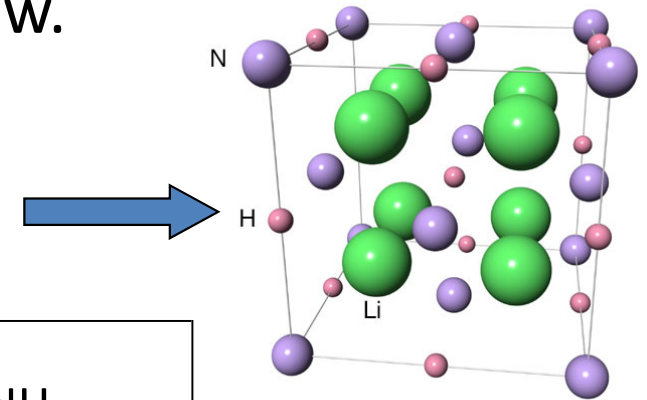


There is no space group for  $\text{Li}_2\text{NH}$ ????



If you believe that the hydrogen site is fully occupied.

Model : Occupation of Hydrogen is extremely low.



It represents the data!

But, the occupation of H is only 3% ! !

# Partially Occupied Model

Basic COndition

1: FCC ( $a \sim 5.05 \text{ \AA}$ )

2: 4 molecule in a unit cell. ( $Z=4$ )

+

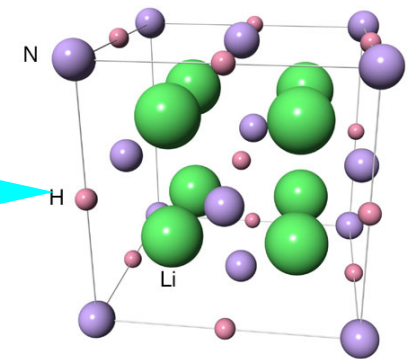
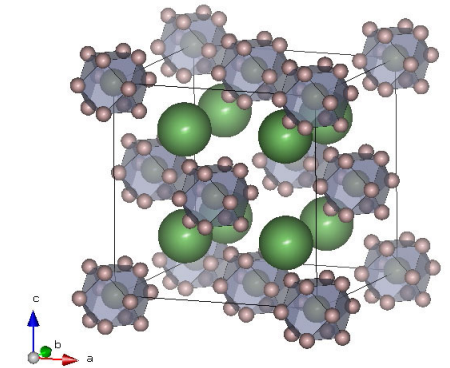
Hydrogen locates at a lower symmetry site.

Occupation of H must be  $4/m$  ( $m$ : multiplicity)

# Low symmetry Site

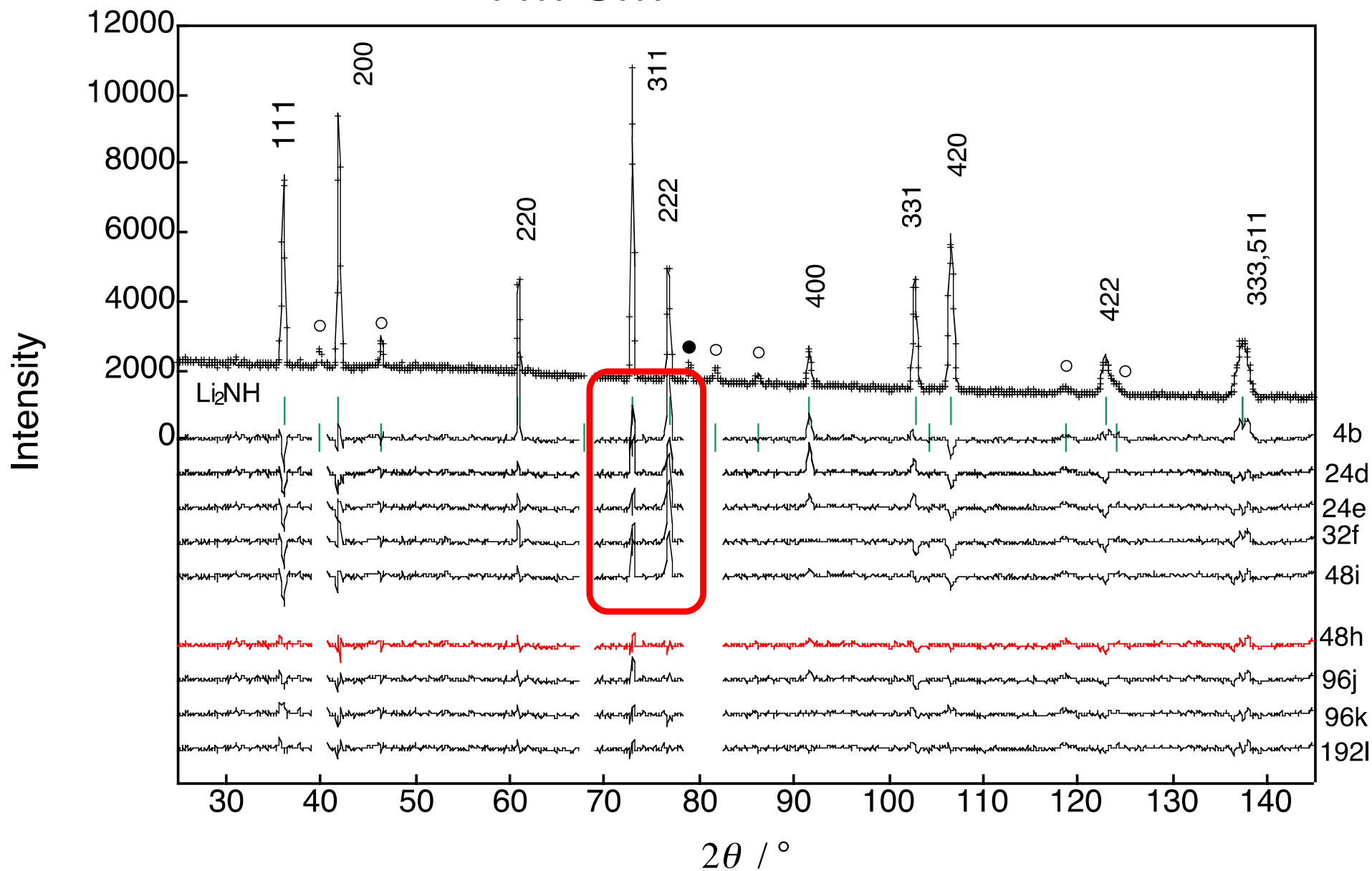
SP : Fm-3m

Site	Position of H	No. of H
192l	$(x,y,z)$	192
96k	$(x,x,z)$	96
96j	$(0,y,z)$	96
48i	$(1/2,y,y)$	48
48h	$(0,y,y)$	48
32f	$(x,x,x)$	32
24e	$(x,0,0)$	24
24d		24
8c	Li	
4b	$(1/2,1/2,1/2)$	4
2a	N	





## Fm-3m



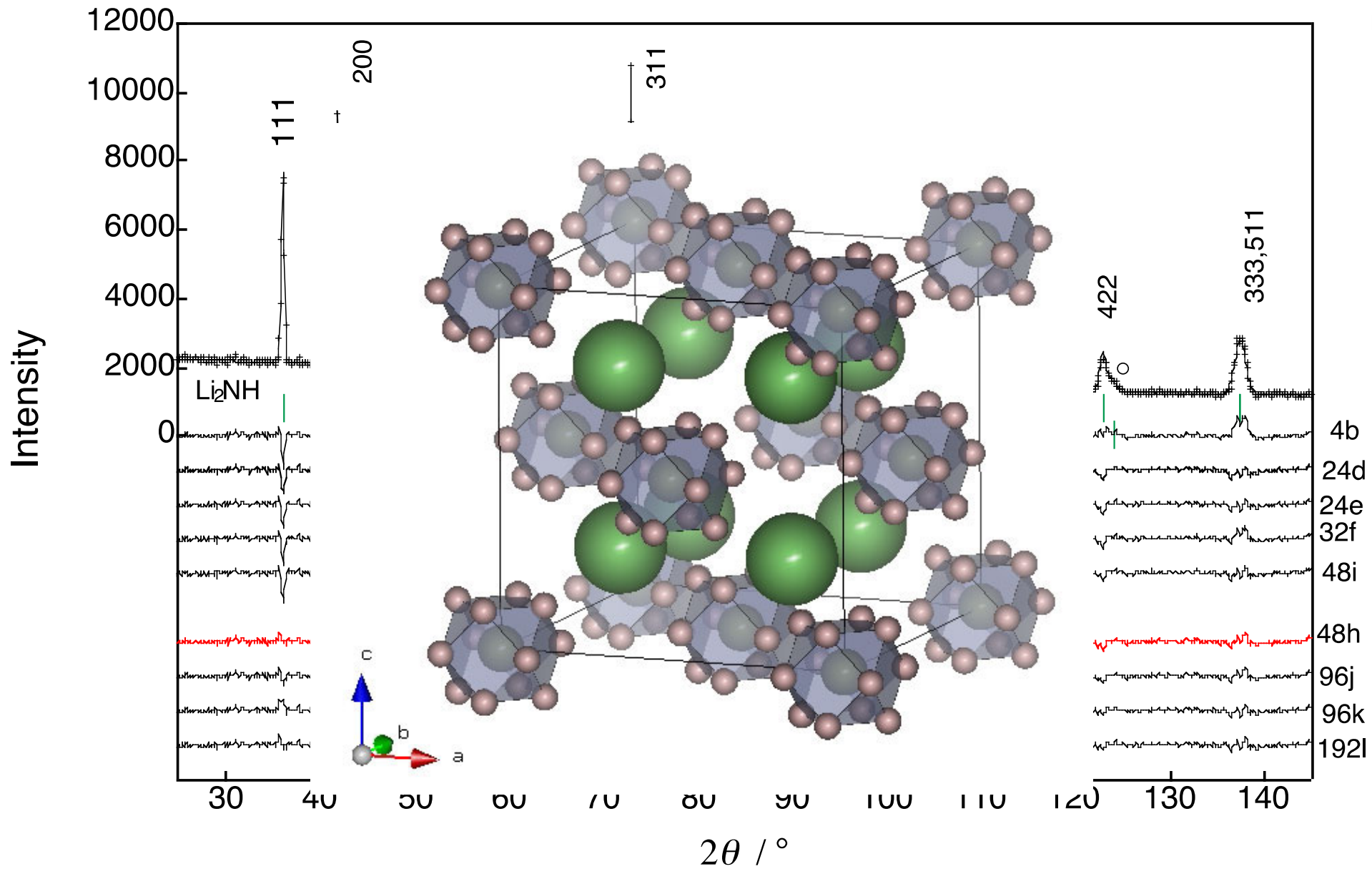
Fm-3m 48h model is the best

Occupancy:  $g = 8.7(5)\%$   $\sim 4/48 = 1/12$





## Fm-3m



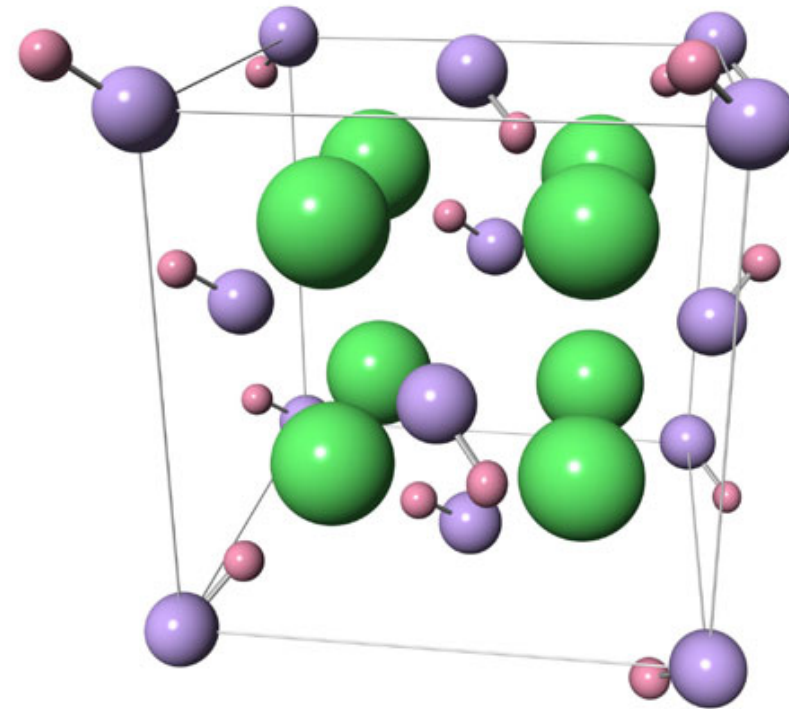
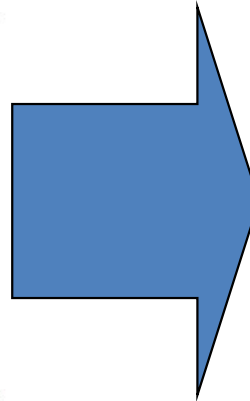
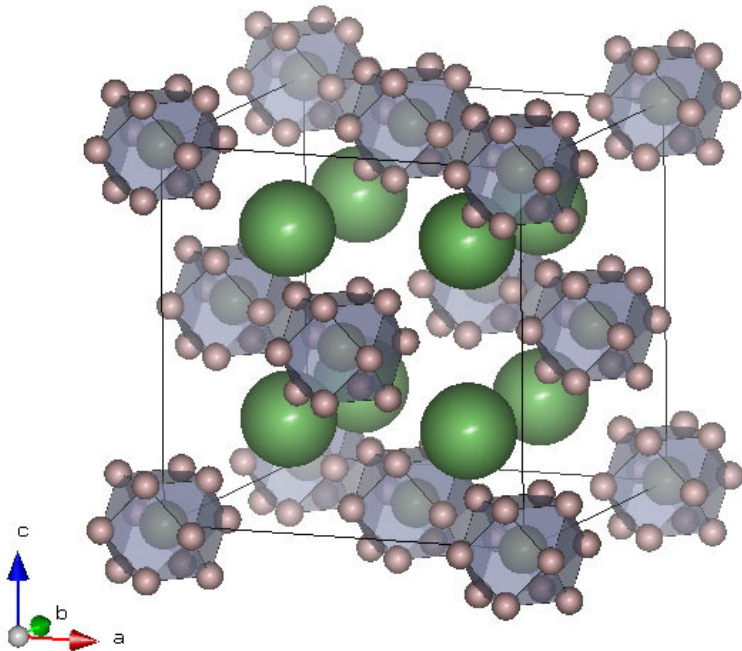
Fm-3m 48h model is the best

Occupancy:  $g = 8.7(5)\%$   $\sim 4/48 = 1/12$

# Li<sub>2</sub>NH : Average and Local structure

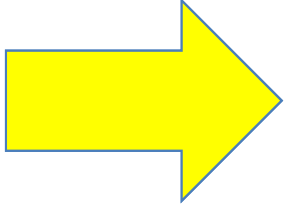
Only One H around a N

Fm-3m  
g=8.3%



Local Structure

# Contents

- 1: Why structures are important?
- 2: Diffraction = Direct Observation of Reciprocal Lattice
- 3: Crystal Structure Refinements
-  4: Magnetic Structure Refinements.



# Magnetic Structure

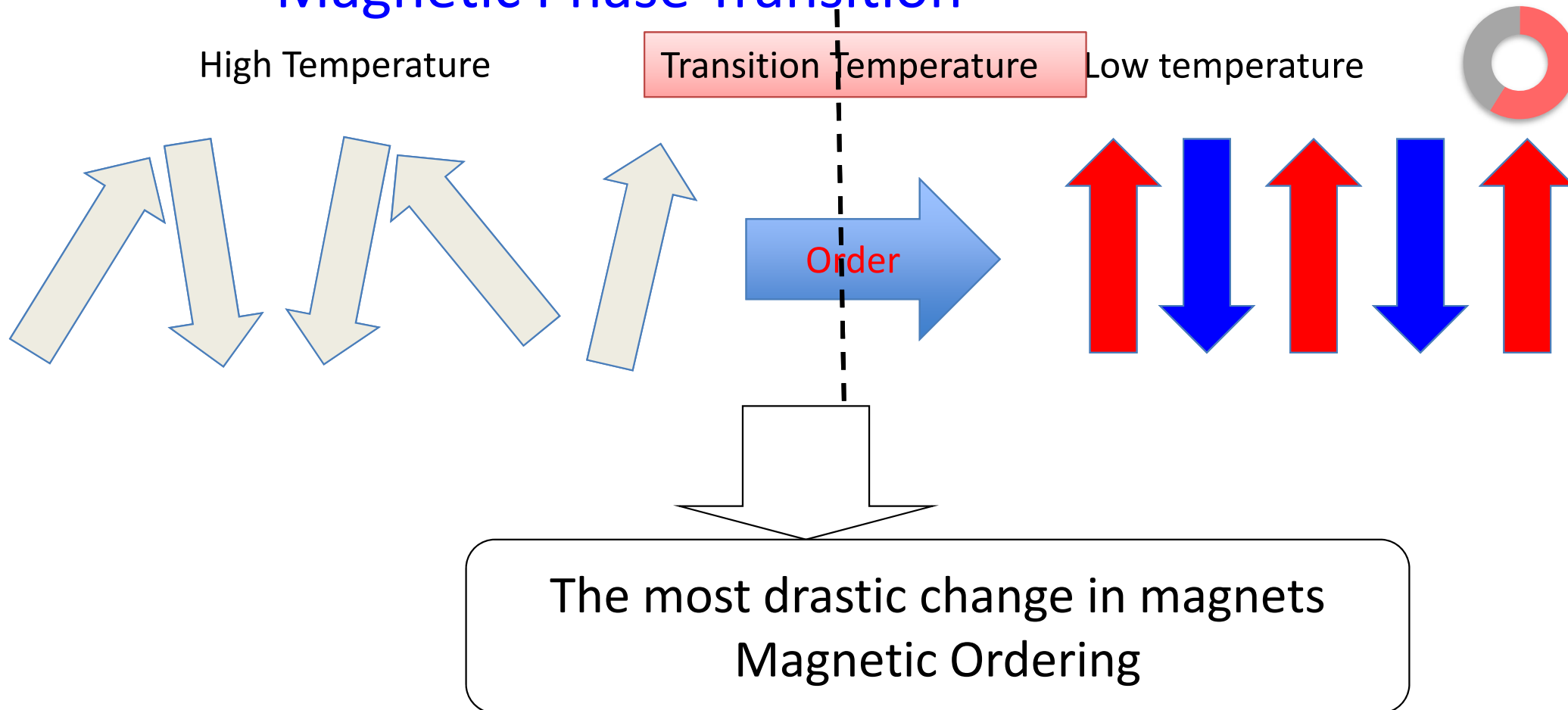
Why you have to understand magnetic structure?

How it can be observed by Neutron

Magnetic structure refinement



# Magnetic Phase Transition

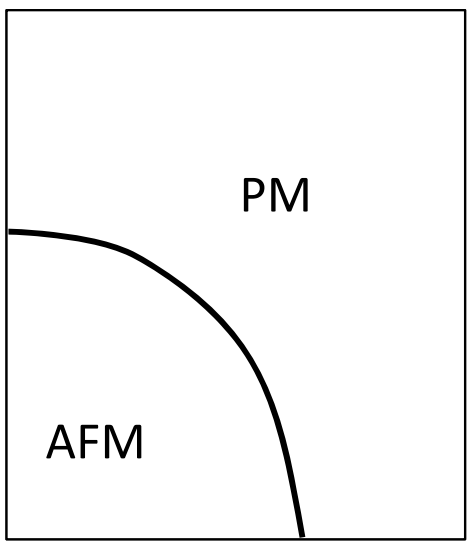
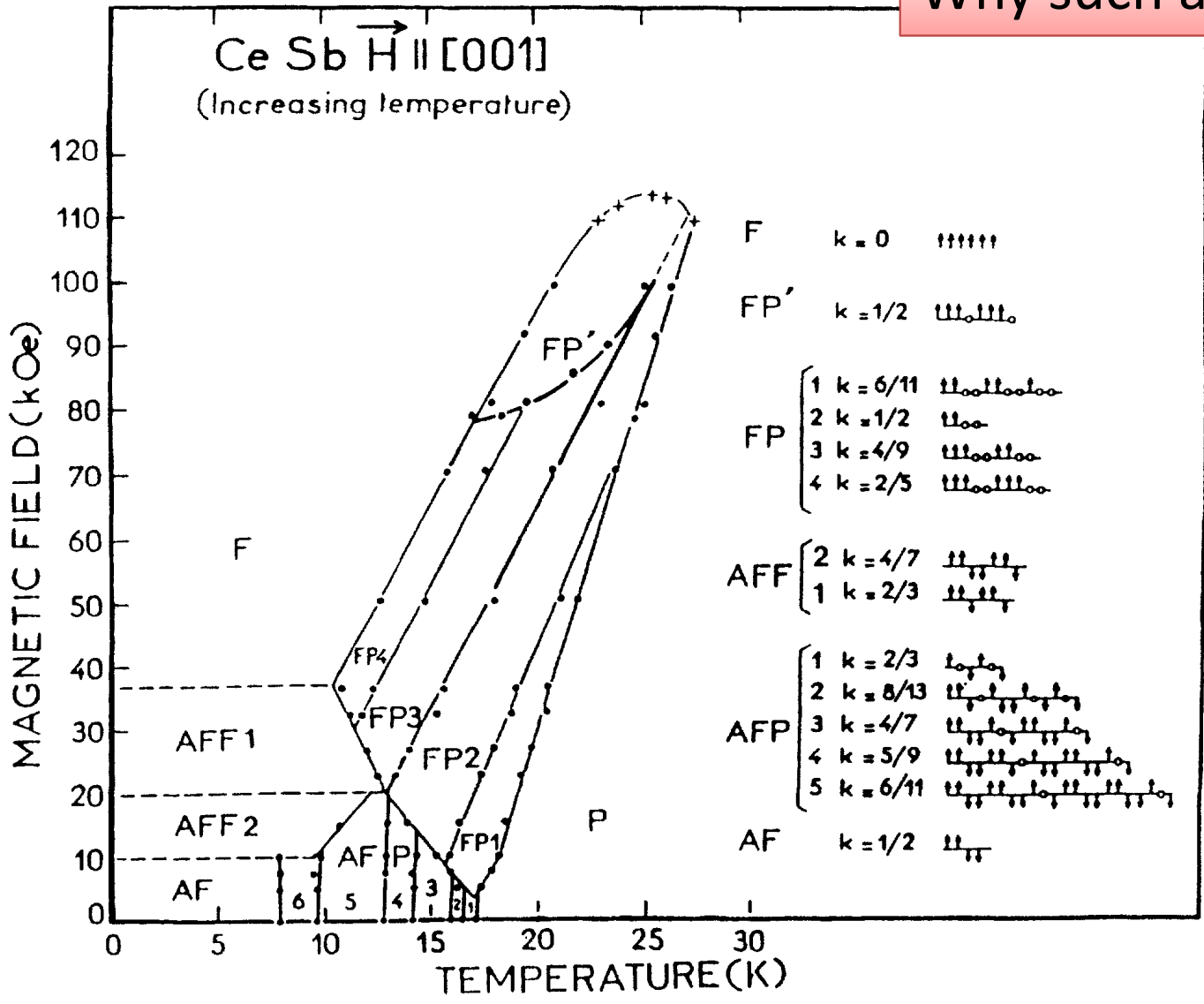


Purpose of Magnetic Physics is understanding of interactions.

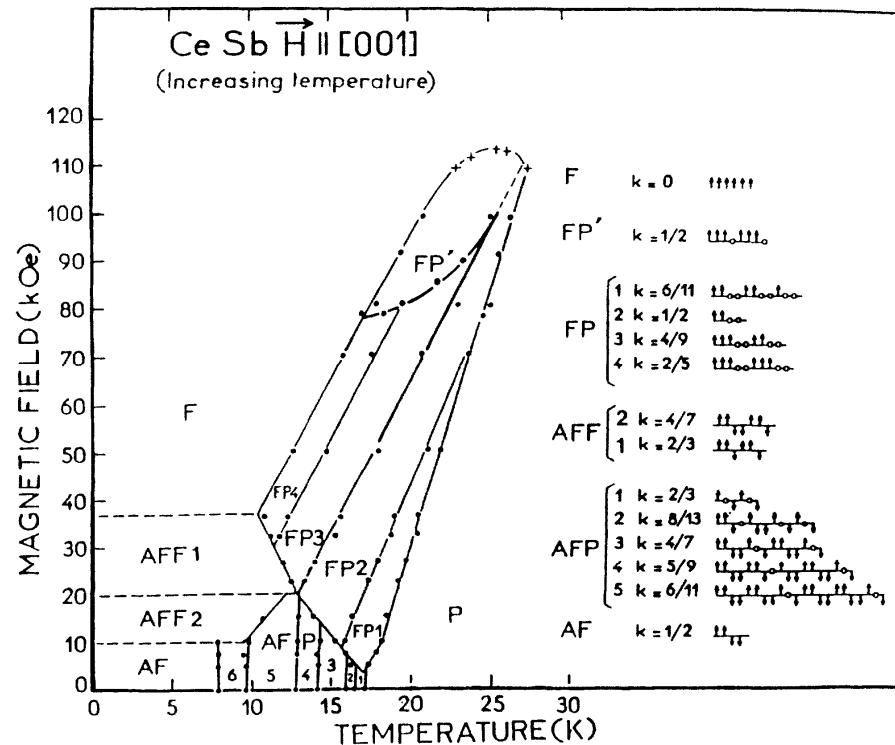
Information on magnetic structures is indispensable.

# H-T phase diagram: Develis Stairs :CeSb

Why such a complicated one?

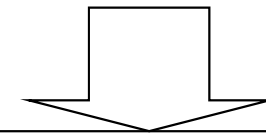


# Why you have to know magnetic structures?



It is not a purpose.

But, to understand the phase diagrams, magnetic structures (spin alignments) are indispensable.

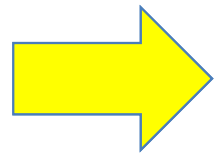


What is the origin which stabilize the spin in magnets?

T. Chattopadhyay et al. Phys Rev. B 49, 15096 (1994)

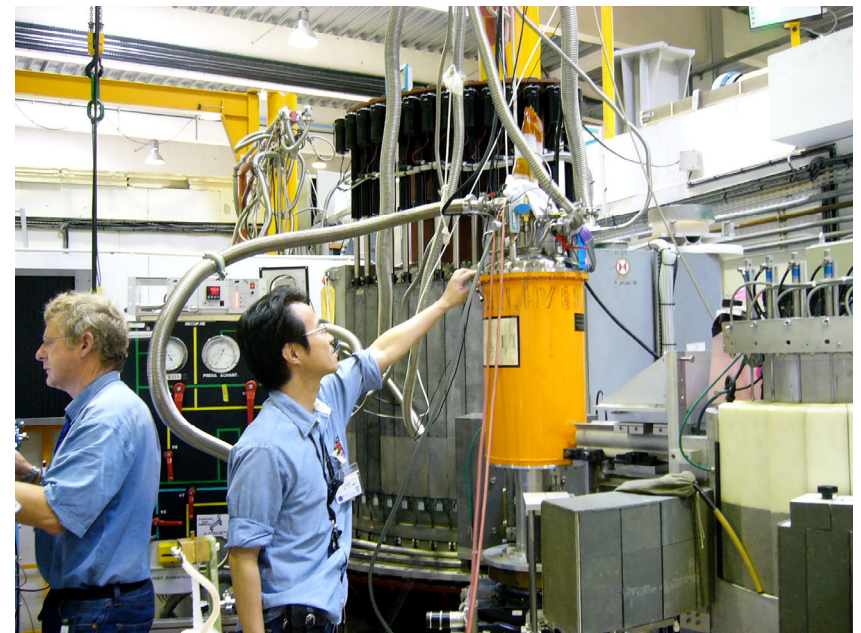
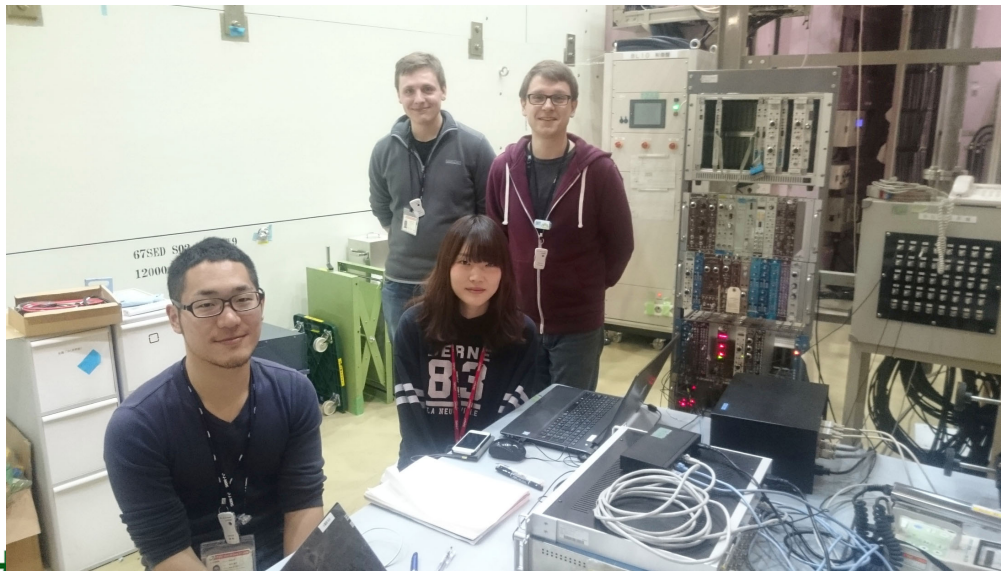
# Magnetic Structure

Why you have to understand magnetic structures?



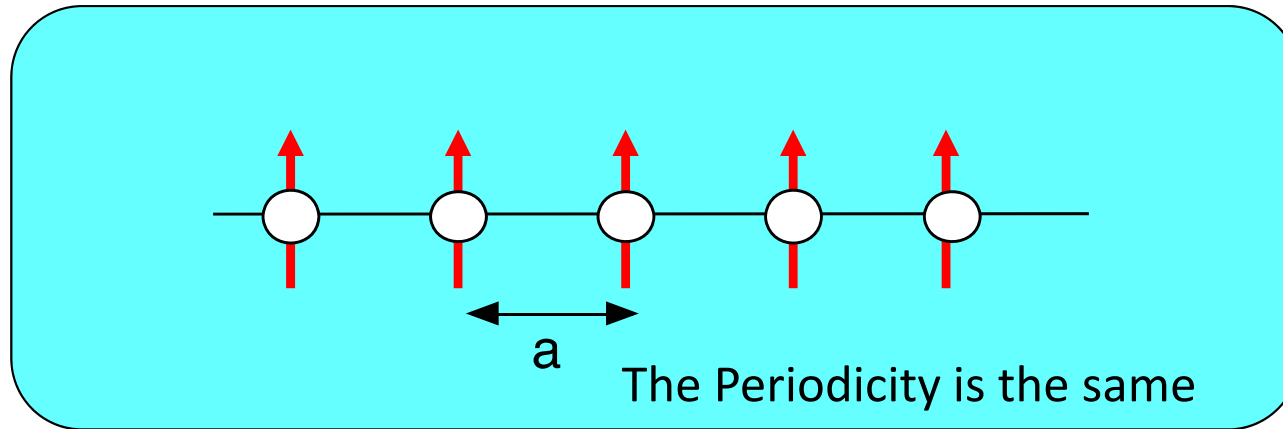
How you can observe it by Neutron

Magnetic structure refinement

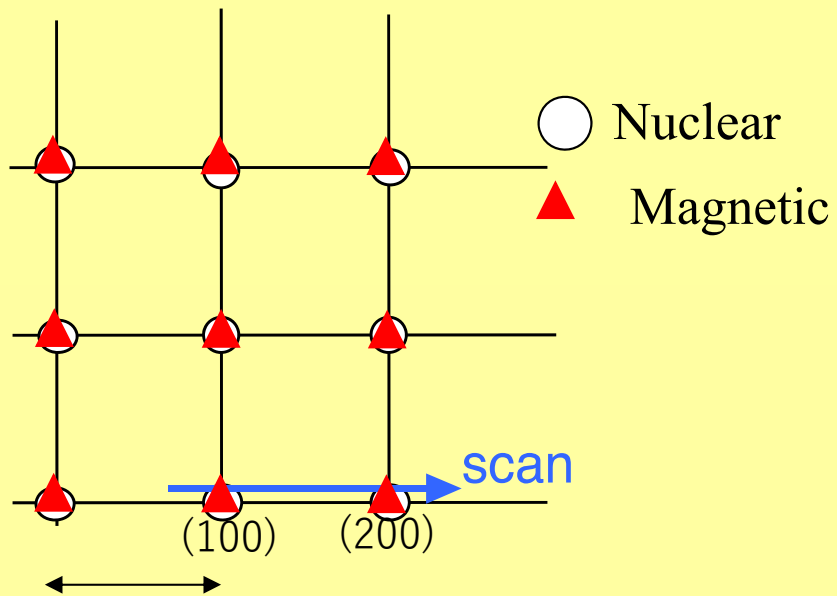




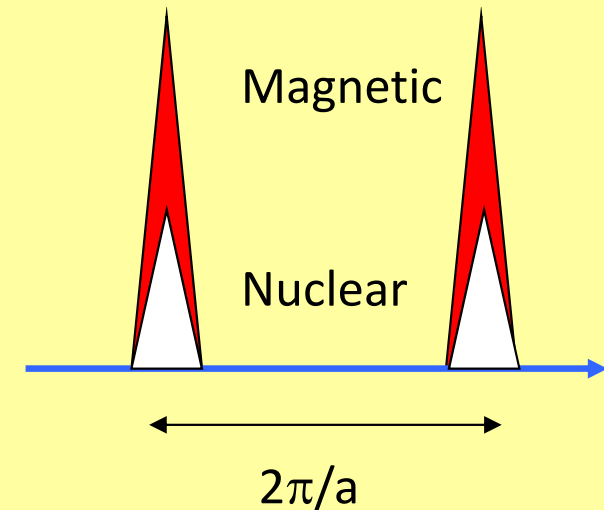
# Observation by ND : Ferromagnet



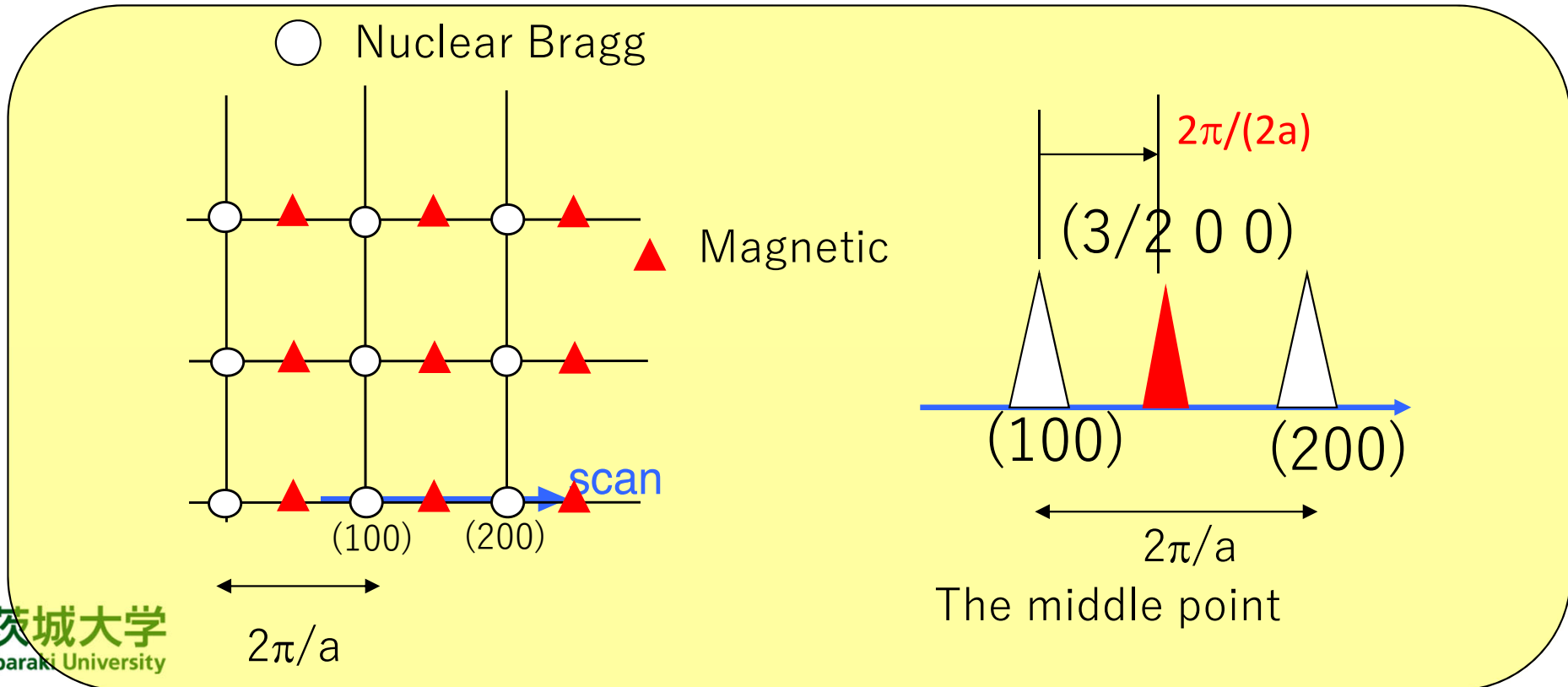
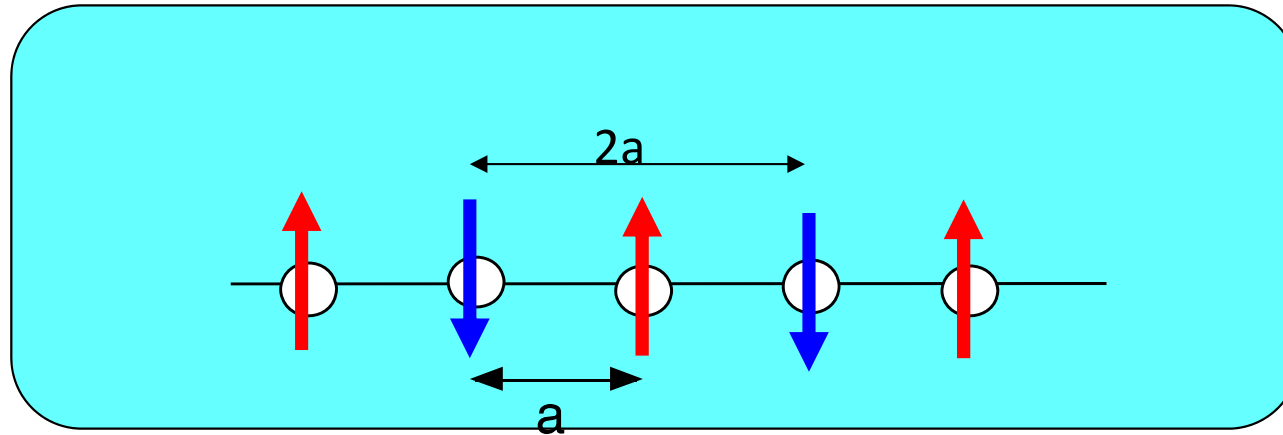
Reciprocal Lattice)



Measurements



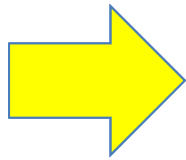
# Observation by ND : Antierromagnet



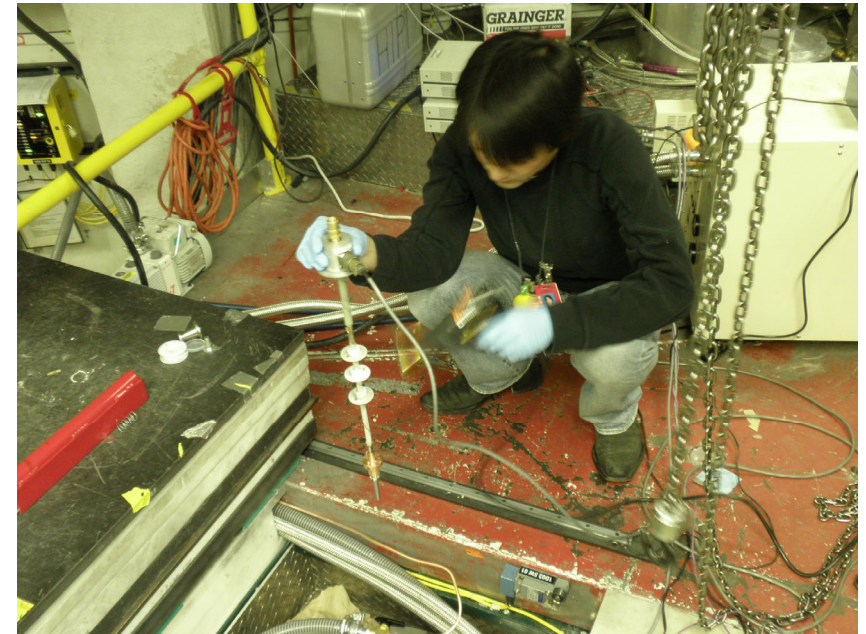
# Magnetic Structure

Why you have to understand magnetic structures?

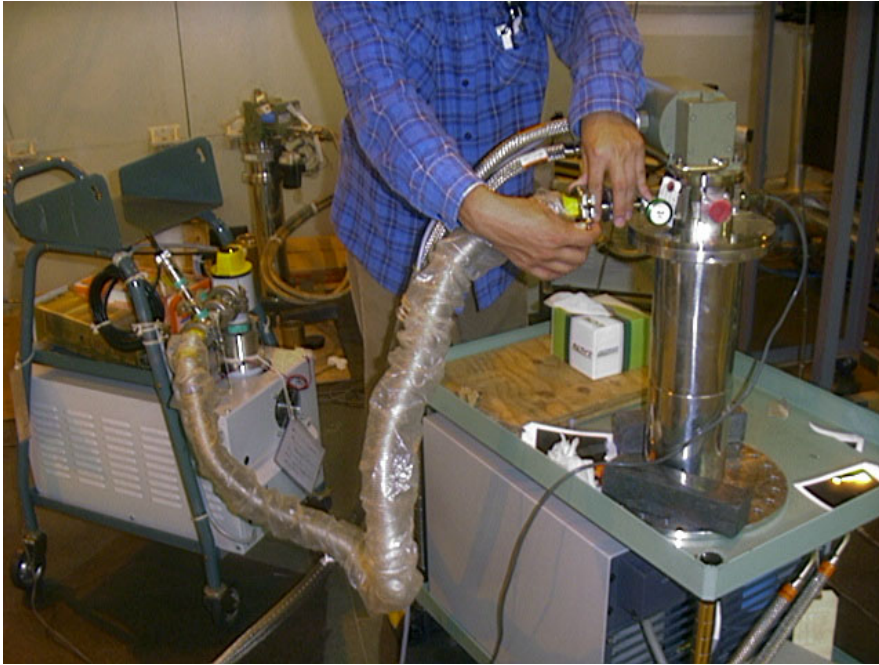
How you can observe it by Neutron



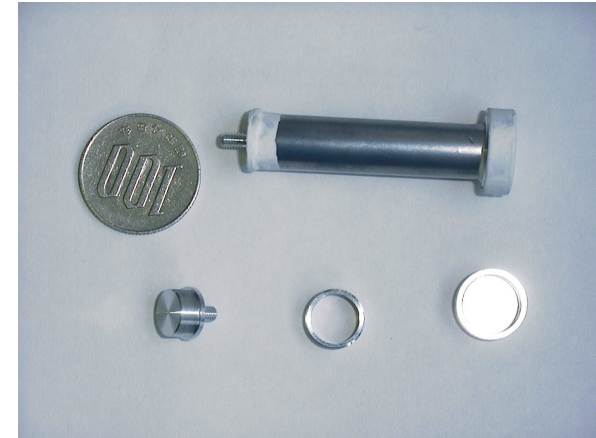
Magnetic Structure Refinement for Rare earth Compounds



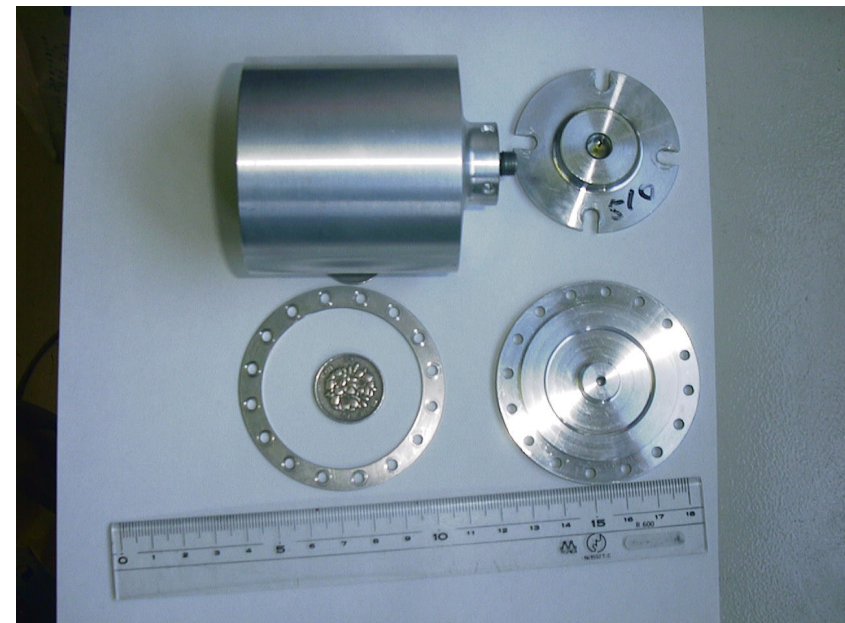
# Experiments



Cryostat (10K~300K)



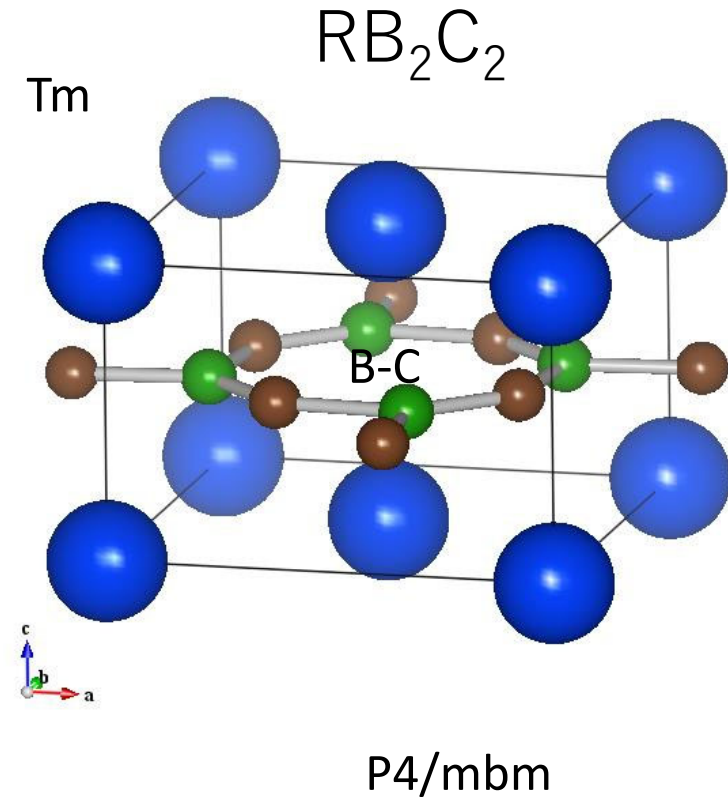
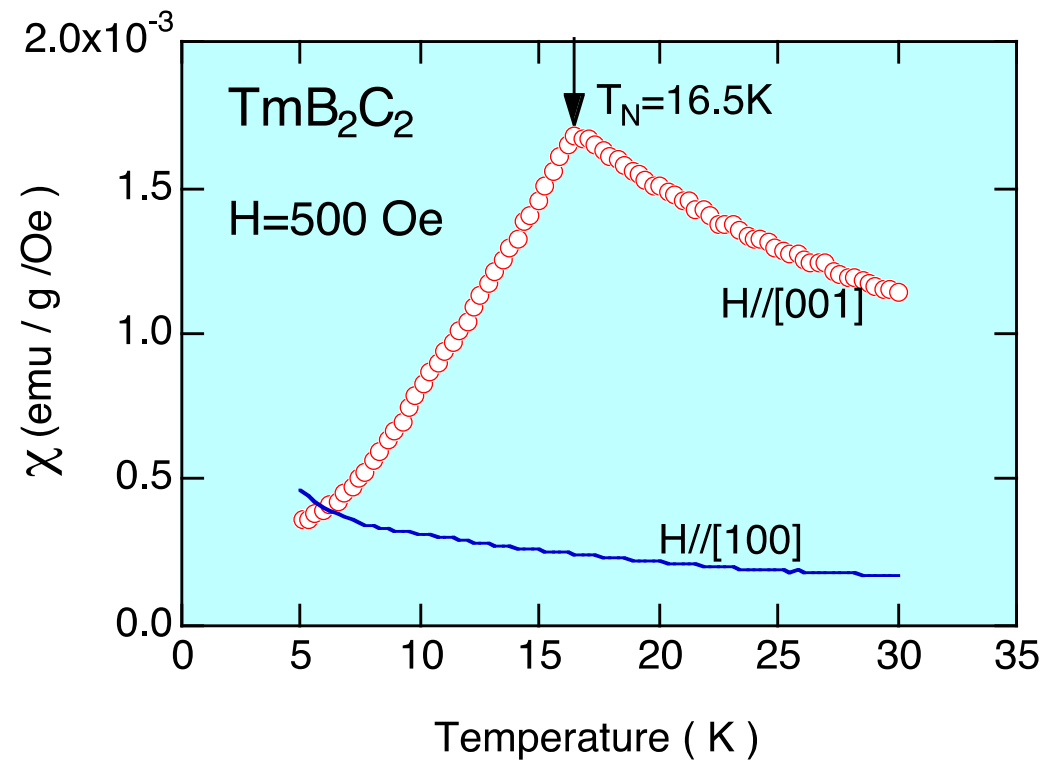
Vanadium Cell

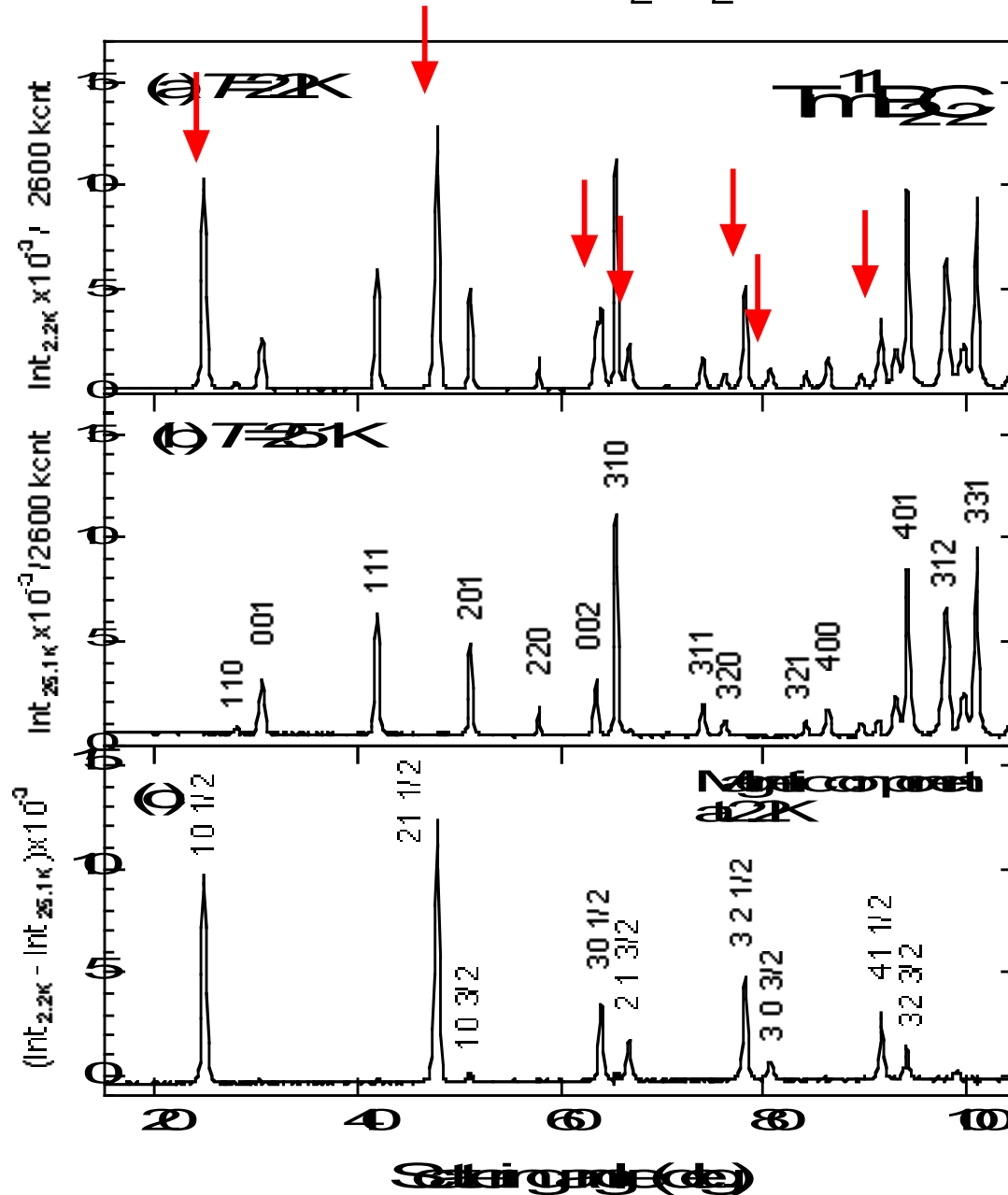


Al Cell

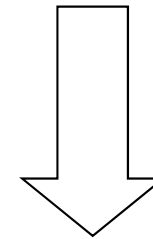


# TmB<sub>2</sub>C<sub>2</sub>



ND of  $\text{TmB}_2\text{C}_2$ 

Nuclear	Magnetic
000	1 0 1/2
110	2 1 1/2
001	1 0 3/2
200	3 0 1/2
111	2 1 3/2



$$k=(1,0,1/2)$$

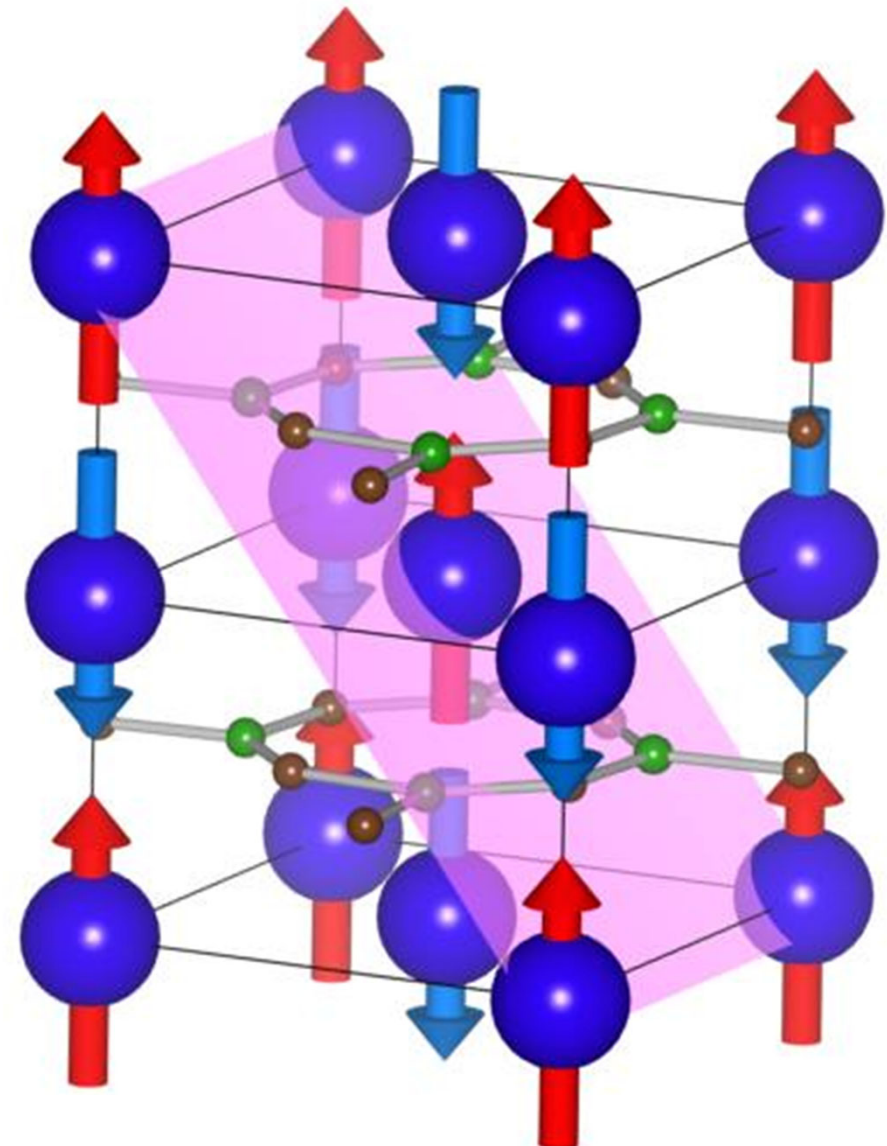
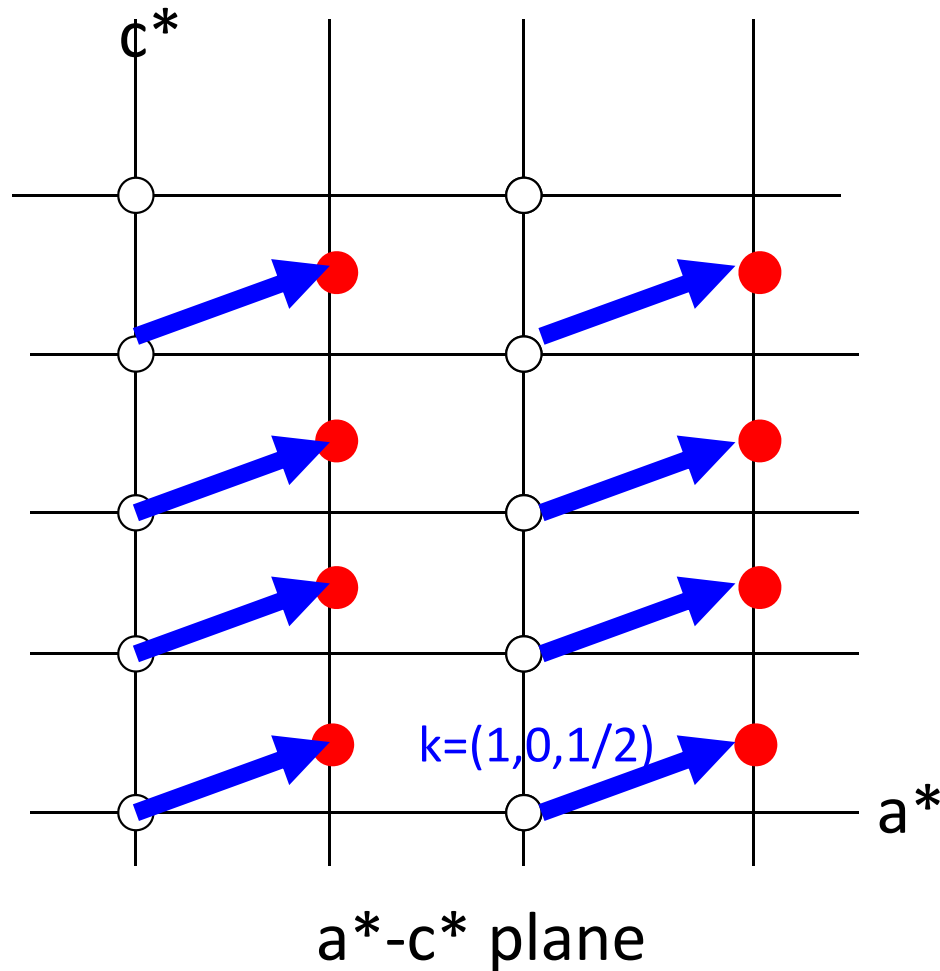
# In the Reciprocal Lattice

- Nuclear
- Magnetic

$$k=(1,0,1/2)$$

a-axis 1unit  $\rightarrow$  1 Rotation

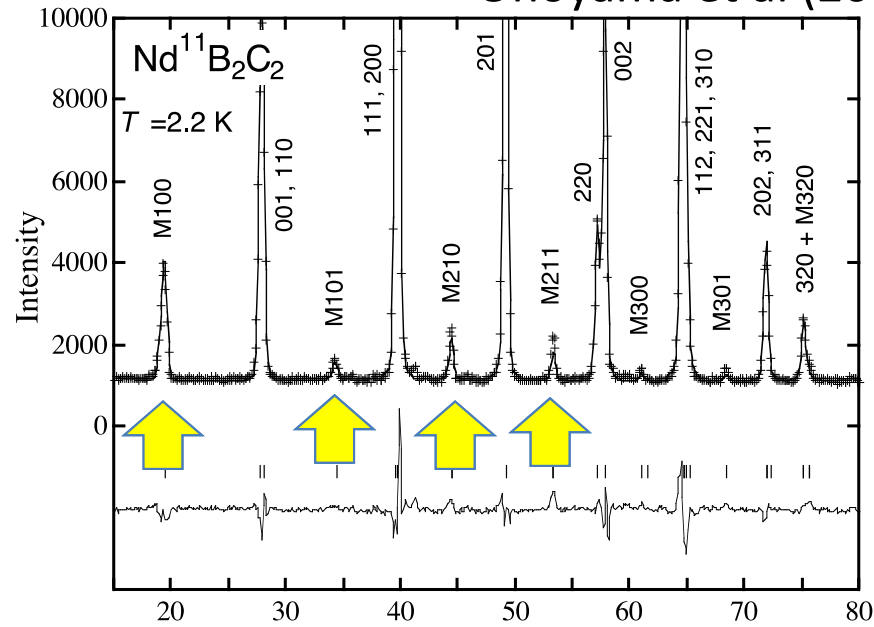
C-axis 2unit  $\rightarrow$  1 Rotation



# Rietveld Analysis

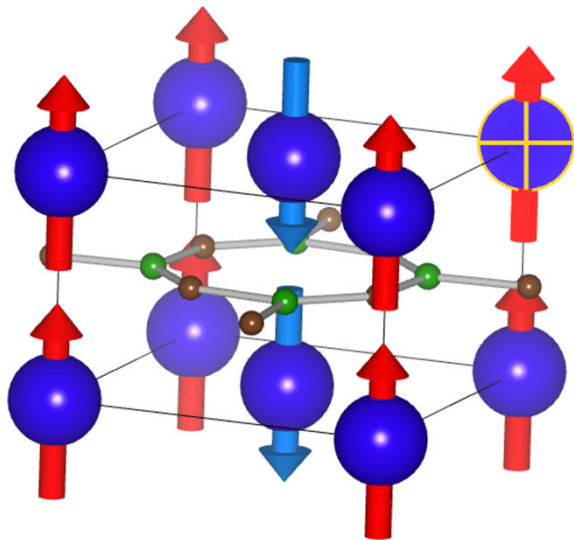
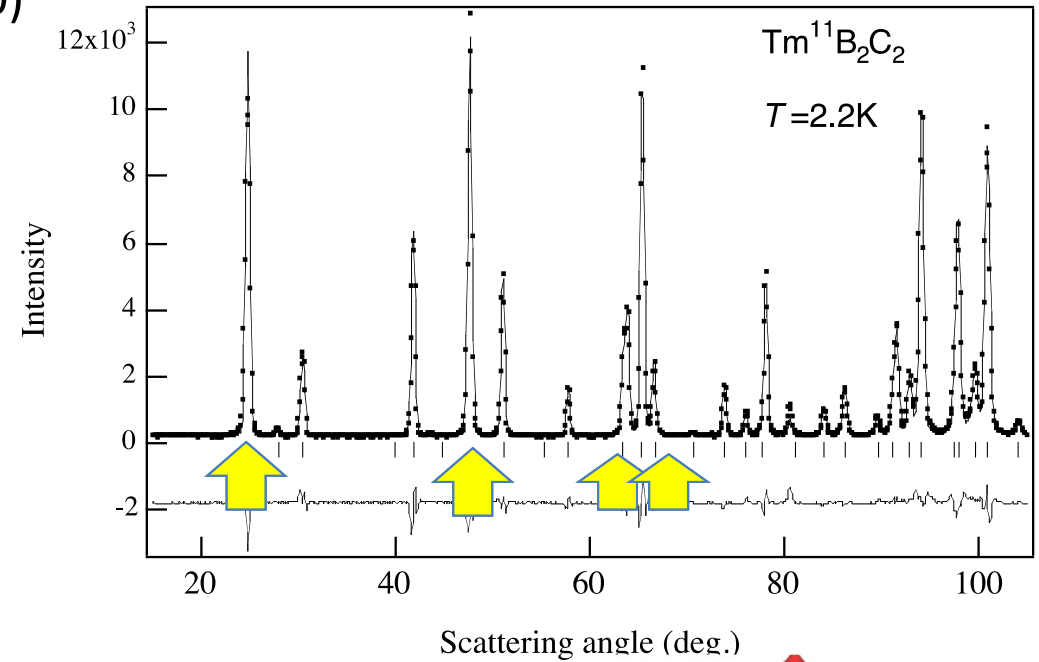
## NdB<sub>2</sub>C<sub>2</sub>

Ohoyama et al (2000)

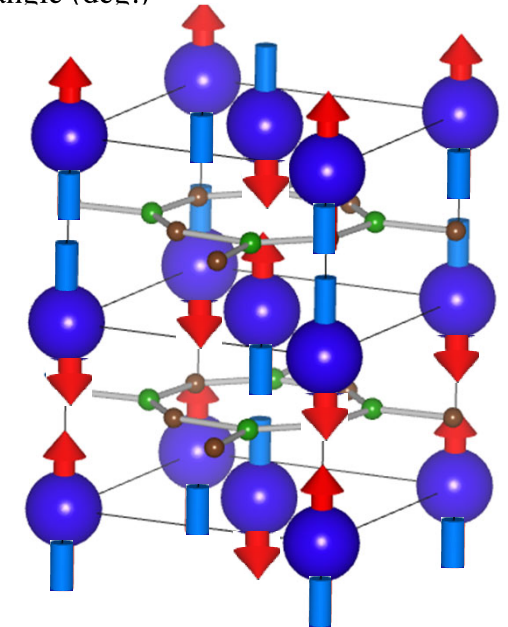


## TmB<sub>2</sub>C<sub>2</sub>

Ohoyama et al (2002)



By simultaneous analysis of nuclear and magnetic Bragg peaks, one can obtain direction and amplitude of magnetic moments.





# Summary

- Neutron Diffraction experiments provide information on detailed structures of materials with light elements such as Hydrogen, Oxygen.
- Neutron also can determine magnetic structures in magnets.

Diffraction is the method to observe the reciprocal lattice:  
For structure refinement , information on the reciprocal lattice is quite rich and useful.