

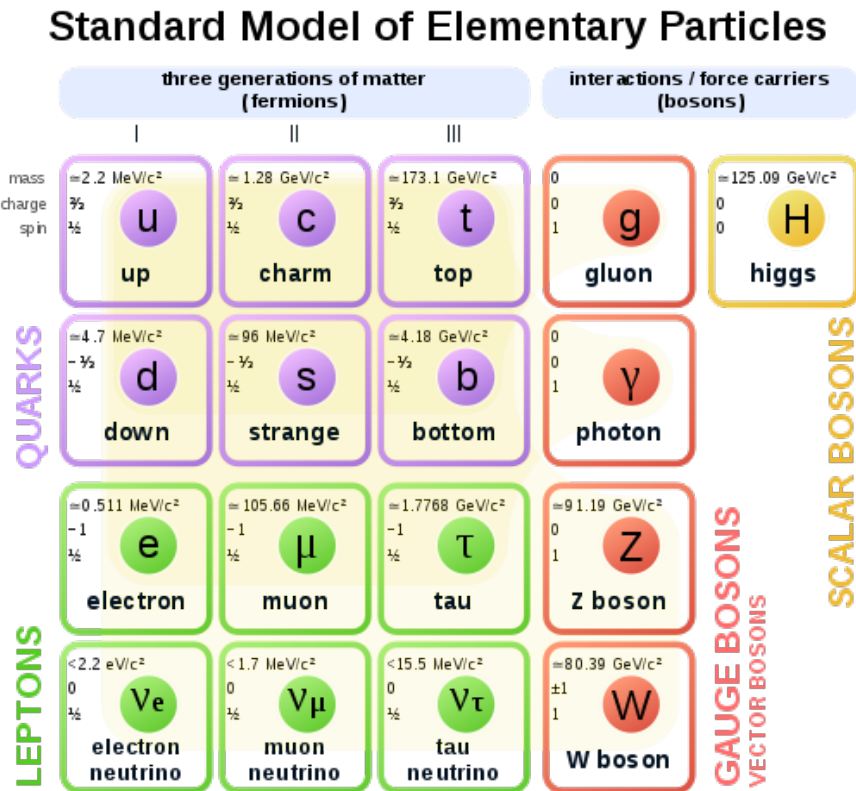
Extended Higgs sectors and CLFV

Takaaki Nomura (KIAS)



1. Introduction

The standard model (SM) of particle physics is successful



The only scalar boson in the SM

H: $SU(2)_L$ doublet
 $U(1)_Y$ charge $1/2$

The SM is based on gauge symmetry $SU(3)_c \times SU(2)_L \times U(1)_Y$

However there should be beyond the SM (BSM) physics

No reason we have only one scalar field around EW scale

1. Introduction

Some issues suggesting BSM physics

□ Non-zero neutrino mass

- ❖ We need a mechanism to generate neutrino mass
- ❖ Also smallness of the mass should be explained

□ Anomalous muon magnetic moment (muon g-2)

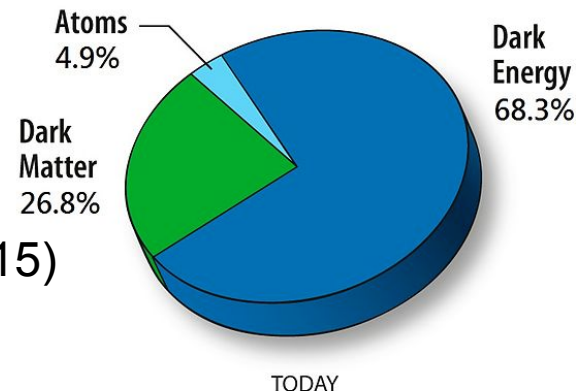
- ❖ Deviation from SM prediction

$$\Delta a_\mu = a_\mu^{\text{exp}} - a_\mu^{\text{SM}} = (28.8 \pm 8.0) \times 10^{-10}$$

□ Existence of dark matter in our Universe

- ❖ Observed relic density

➡ $\Omega_{DM} h^2 = 0.1188 \pm 0.0010$ Planck (2015)



1. Introduction

Some issues suggesting BSM physics

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- ❖ Also smallness of the mass should be explained

□ Anomalous muon magnetic moment (muon g-2)

- ❖ Deviation from SM prediction

$$\Delta a_\mu = a_\mu^{\text{exp}} - a_\mu^{\text{SM}} = (28.8 \pm 8.0) \times 10^{-10}$$

□ Existence of dark matter

It can be explained by extended Higgs sector

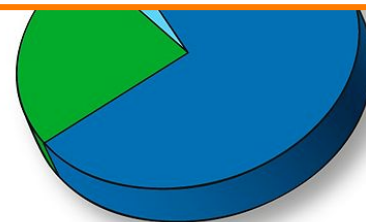


Connection to CLFV processes

- ❖ Observed relic density

➡ $\Omega_{DM} h^2 = 0.1188 \pm 0.0010$ Planck (2015)

Dark
Matter
26.8%



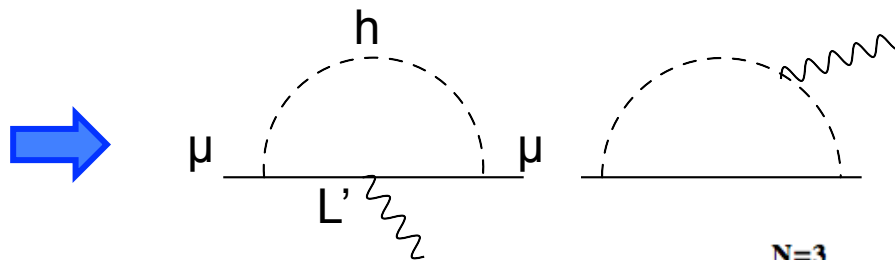
TODAY

Muon g-2 and extended Higgs sector

◆ New charged scalar + extra vector-like lepton

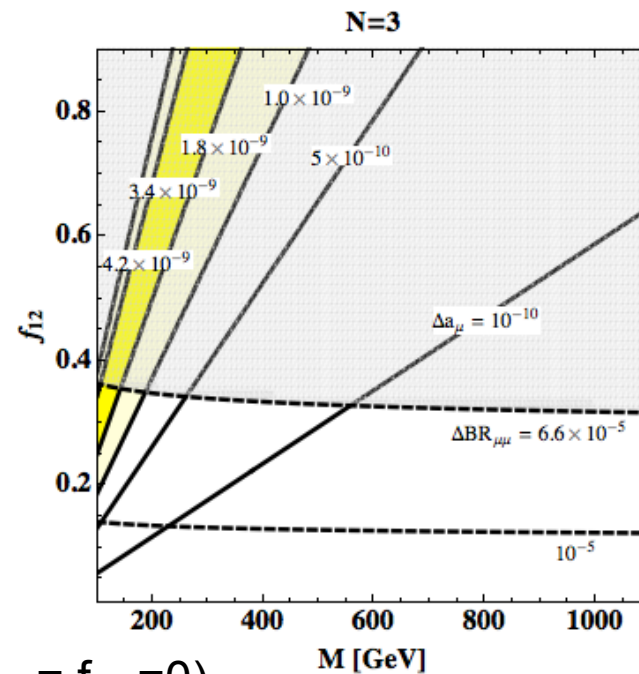
$$h^{+n} \text{ (n: electric charge)} \quad L' = (\psi^{-n}, \psi^{-n-1}) \quad (\text{Hypercharge } N = 2n+1)$$

$$-L_Y = f_{ia} \bar{L}_{L_i} L'_{R_a} h^n + h.c.$$



Sizable contribution to muon g-2 is possible

- ✓ L' mass around $\text{few} \times 100 \text{ GeV}$
- ✓ Constraint from $\Delta \text{BR}(Z \rightarrow \mu^+ \mu^-)$
- ✓ To avoid LFV tuning of f_{ja} is required

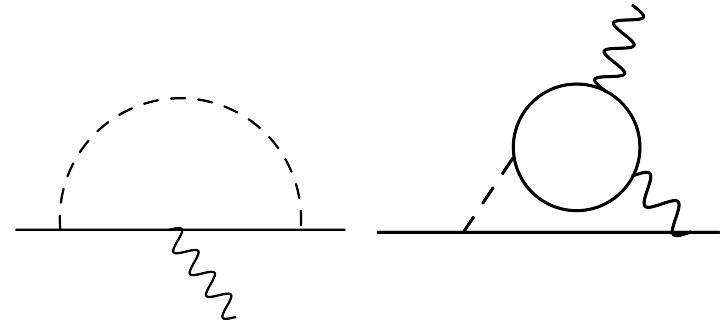

$$(f_{13} = f_{11} = 0)$$

1. Introduction

Muon g-2 and extended Higgs sector

◆ 2 Higgs doublet model (2HDM)

- ✓ New scalar boson contributions
- ✓ One- and two-loop contributions
- ✓ By Yukawa couplings :



$$-L_Y = \bar{Q}_L Y_u^1 u_R \Phi_1^c + \bar{Q}_L Y_u^2 u_R \Phi_2^c + \bar{Q}_L Y_d^1 d_R \Phi_1 + \bar{Q}_L Y_d^2 d_R \Phi_2 + \bar{L}_L Y_\ell^1 \ell_R \Phi_1 + \bar{L}_L Y_\ell^2 \ell_R \Phi_2$$

Ex) type-X 2HDM

Z_2 symmetry to suppress FCNC:

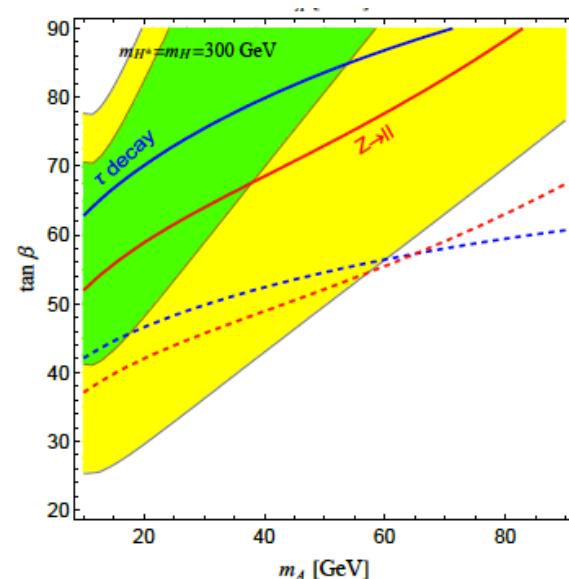
$$\Phi_2 \rightarrow -\Phi_2, \quad u_R \rightarrow -u_R, \quad d_R \rightarrow -d_R$$

$$-L_Y = \bar{Q}_L Y_u^2 u_R \Phi_2^c + \bar{Q}_L Y_d^2 d_R \Phi_2 + \bar{L}_L Y_\ell^1 \ell_R \Phi_1$$

❖ CLFV processes are induced without Z_2



It will be discussed in this talk



1. Introduction

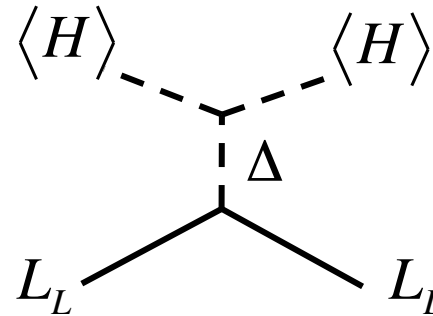
Neutrino mass and extended Higgs sector

◆ SM + Higgs triplet Δ

W.Konetschny, W.Kummer (1977) T. P. Chen, L. F. Li (1980)

J. Schechter, J. W. F. Valle (1980)

$$\Delta = \begin{pmatrix} \delta^+ / \sqrt{2} & \delta^{++} \\ (v_\Delta + \delta^0 + i\eta^0) / \sqrt{2} & -\delta^+ / \sqrt{2} \end{pmatrix}$$

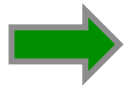


✓ Neutrino mass by VEV of triplet

✓ CLFVs are induced by the Yukawa interaction

$$\Rightarrow y_\Delta \bar{L}^c \Delta L \rightarrow \frac{y_\Delta v_\Delta}{\sqrt{2}} \bar{\nu}^c \nu$$

Doubly charged scalar from Higgs triplet



Specific signatures at the collider experiments

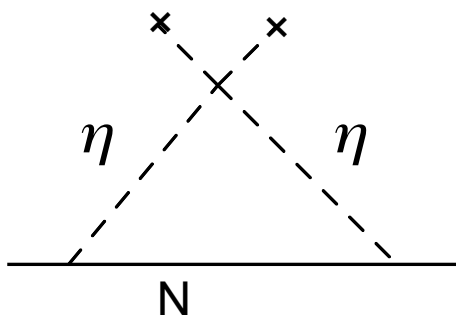
$$pp \rightarrow \delta^{++} \delta^{--} (\delta^{\pm\pm} \rightarrow \ell^\pm \ell^\pm, W^\pm W^\pm)$$

1. Introduction

Neutrino mass and extended Higgs sector

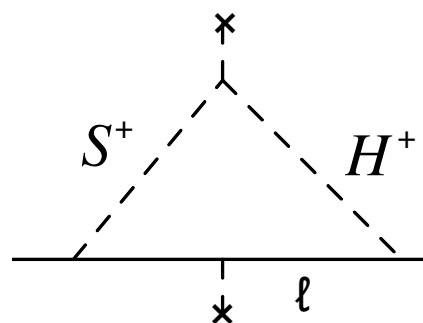
◆ SM + second Higgs doublet (+ some extra fields)

EX)



Scotogenic model (inert doublet η)

Ma (2006)

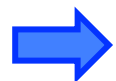


$\times$: VEV

Zee-model (charged scalar S^+)

Zee (1980)

Radiative neutrino mass case is interesting



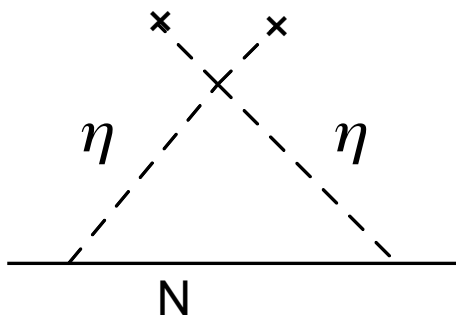
New particles could be around TeV scale

1. Introduction

Neutrino mass and extended Higgs sector

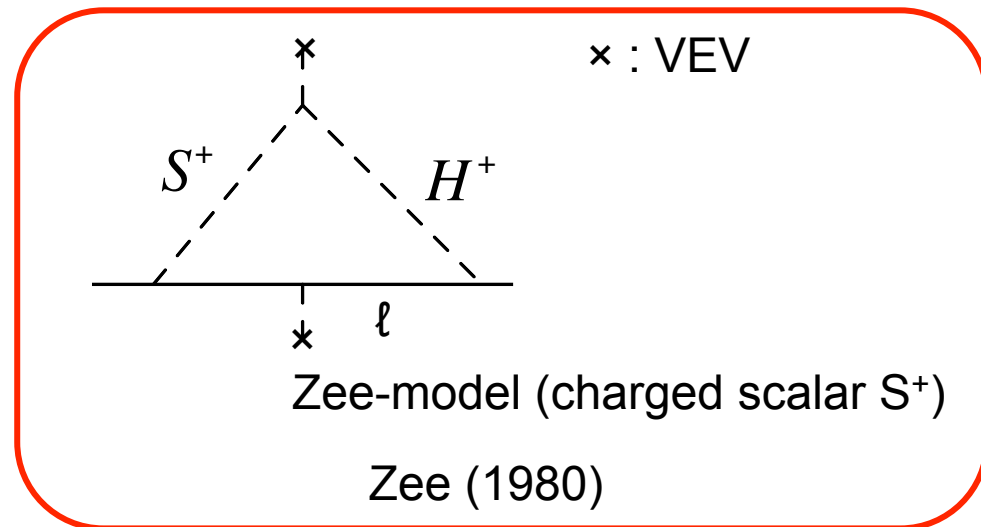
◆ SM + second Higgs doublet (+ some extra fields)

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Scotogenic model (inert doublet η)

Ma (2006)



Zee-model (charged scalar S^+)

Zee (1980)

Radiative neutrino mass case is interesting

➡ New particles could be around TeV scale

Zee-model: only Higgs sector is extended

➤ In this talk we discuss Zee-model with flavor dependent global $U(1)$

In this talk we will discuss

(1) General 2HDM explaining muon $g-2$ and CLFV

R. Benbrik, C. Chen, T.N. PRD 93 (2016)

(2) Zee-model with flavor symmetry
neutrino mass generation and related CLFV

T.N., K. Yagyu, arXiv:1905.11568

1. Introduction

2. Muon $g-2$ and CLFV in 2HDM

3. Zee-model with flavor symmetry

4. Summary and discussion

General two Higgs doublet model

⇒ **SM fermion contents + two Higgs doublet $\Phi_{1,2}$**

$$\Phi_i = \begin{pmatrix} \phi_i^+ & \frac{1}{\sqrt{2}}(v_i + \phi_i + i\eta_i) \end{pmatrix}$$

□ Yukawa interactions

$$\begin{aligned} -L_Y = & \bar{Q}_L Y_u^1 u_R \Phi_1^c + \bar{Q}_L Y_u^2 u_R \Phi_2^c + \bar{Q}_L Y_d^1 d_R \Phi_1 + \bar{Q}_L Y_d^2 d_R \Phi_2 \\ & + \bar{L}_L Y_\ell^1 \ell_R \Phi_1 + \bar{L}_L Y_\ell^2 \ell_R \Phi_2 \end{aligned}$$

□ Scalar potential

$$\begin{aligned} V(\Phi_1, \Phi_2) = & m_1^2 \Phi_1^\dagger \Phi_1 + m_2^2 \Phi_2^\dagger \Phi_2 - (m_{12}^2 \Phi_1^\dagger \Phi_2 + \text{h.c.}) + \frac{1}{2} \lambda_1 (\Phi_1^\dagger \Phi_1)^2 \\ & + \frac{1}{2} \lambda_2 (\Phi_2^\dagger \Phi_2)^2 + \lambda_3 (\Phi_1^\dagger \Phi_1) (\Phi_2^\dagger \Phi_2) + \lambda_4 (\Phi_1^\dagger \Phi_2) (\Phi_2^\dagger \Phi_1) \\ & + \left[\frac{\lambda_5}{2} (\Phi_1^\dagger \Phi_2)^2 + \left(\lambda_6 \Phi_1^\dagger \Phi_1 + \lambda_7 \Phi_2^\dagger \Phi_2 \right) \Phi_1^\dagger \Phi_2 + \text{h.c.} \right]. \end{aligned}$$

2. Muon g-2 and CLFV in 2HDM

Physical mass eigenstates for scalars

$$h = -s_\alpha \phi_1 + c_\alpha \phi_2,$$

$$H = c_\alpha \phi_1 + s_\alpha \phi_2,$$

$$H^\pm(A) = -s_\beta \phi_1^\pm(\eta_1) + c_\beta \phi_2^\pm(\eta_2)$$

$$\left[\begin{array}{l} c_\alpha(s_\alpha) = \cos \alpha(\sin \alpha) \\ c_\beta = \cos \beta = v_1 / v, \quad s_\beta = \sin \beta = v_2 / v \end{array} \right]$$

SM fermion masses

$$M_f = \frac{v}{\sqrt{2}} (Y_f^1 \cos \beta + Y_f^2 \sin \beta) \quad \longrightarrow \quad m_f = U_L^f M_f (U_R^f)^\dagger$$

$$f_{L,R} \rightarrow (U_{L,R}^f)^\dagger f_{L,R}$$

Leptonic Yukawa couplings in mass basis

$$(y_h^\ell)_{ij} = -\frac{s_\alpha}{c_\beta} \frac{m_i}{v} \delta_{ij} + \frac{c_{\beta\alpha}}{c_\beta} X_{ij}^\ell,$$

$$(y_H^\ell)_{ij} = \frac{c_\alpha}{c_\beta} \frac{m_i}{v} \delta_{ij} - \frac{s_{\beta\alpha}}{c_\beta} X_{ij}^\ell,$$

$$(y_A^\ell)_{ij} = -\tan \beta \frac{m_i}{v} \delta_{ij} + \frac{X_{ij}^\ell}{c_\beta},$$

$$\left[\begin{array}{l} X^u = U_L^u \frac{Y_u^1}{\sqrt{2}} (U_R^u)^\dagger \\ X^d = U_L^d \frac{Y_d^2}{\sqrt{2}} (U_R^d)^\dagger \\ X^\ell = U_L^\ell \frac{Y_\ell^2}{\sqrt{2}} (U_R^\ell)^\dagger \end{array} \right]$$

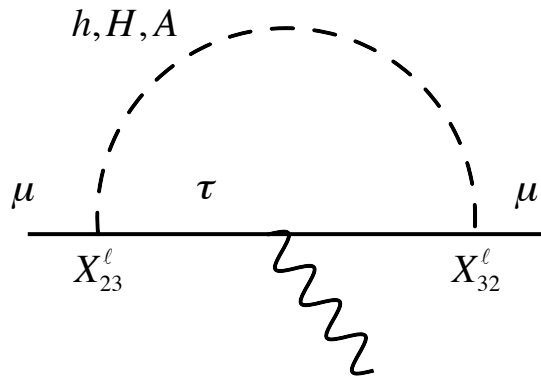
Flavor changing Yukawa interactions (neural scalar)

$$\begin{aligned} -L_Y \supset & \bar{\ell}_L \left[-\frac{s_\alpha}{v c_\beta} m_\ell + \frac{c_{\beta\alpha}}{c_\beta} X^\ell \right] \ell_R h + \bar{\ell}_L \left[\frac{c_\alpha}{v c_\beta} m_\ell - \frac{s_{\beta\alpha}}{c_\beta} X^\ell \right] \ell_R H \\ & + \bar{\ell}_L \left[-\frac{t_\beta}{v} m_\ell + \frac{1}{c_\beta} X^\ell \right] \ell_R A + h.c. \end{aligned}$$

- 
- ✓ CLFV processes are induced by these interactions
 - ✓ Muon g-2 can be enhanced by LFV coupling

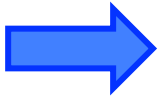
2. Muon g-2 and CLFV in 2HDM

Flavor changing couplings and muon g-2



- ✓ Enhancement by tau lepton mass
- ✓ Positive contribution from H loop

$$\Delta a_\mu \approx \frac{m_\mu m_\tau X_{23}^\ell X_{32}^\ell}{8\pi^2 c_\beta^2} Z_\phi$$



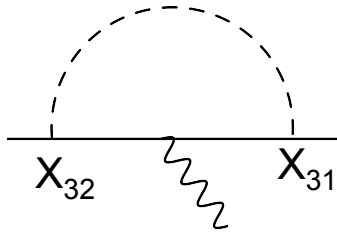
$$Z_\phi = \frac{c_{\beta\alpha}^2 \left(\ln \left(\frac{m_h^2}{m_\tau^2} \right) - \frac{3}{2} \right)}{m_h^2} + \frac{s_{\beta\alpha}^2 \left(\ln \left(\frac{m_H^2}{m_\tau^2} \right) - \frac{3}{2} \right)}{m_H^2} - \frac{\ln \left(\frac{m_A^2}{m_\tau^2} \right) - \frac{3}{2}}{m_A^2}$$

- Sizable muon g-2 at one-loop level can be obtained
- The flavor changing couplings contribute to LFV process

2. Muon g-2 and CLFV in 2HDM

CLFV decays via Yukawa couplings

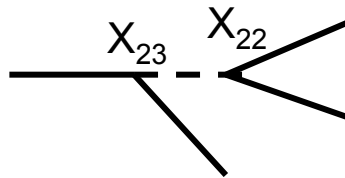
□ $\mu \rightarrow e \gamma$ process



$$\frac{BR(\mu \rightarrow e \gamma)}{BR(\mu \rightarrow e \bar{\nu}_e \nu_\mu)} = \frac{3\alpha_e}{4\pi G_F^2} (|C_L|^2 + |C_R|^2)$$

$$\left(\begin{aligned} C_{L(R)} &= C_{L(R)}^\phi + C_{L(R)}^{H^\pm}, \\ C_L^\phi &= \frac{X_{32}^\ell X_{13}^\ell}{2c_\beta^2} \frac{m_\tau}{m_\mu} Z_\phi, \\ C_L^{H^\pm} &= -\frac{1}{12m_{H^\pm}^2} \left(\frac{2X_{23}^\ell X_{13}^\ell}{c_\beta^2} \right), \end{aligned} \right)$$

□ $\tau \rightarrow 3\mu$ process

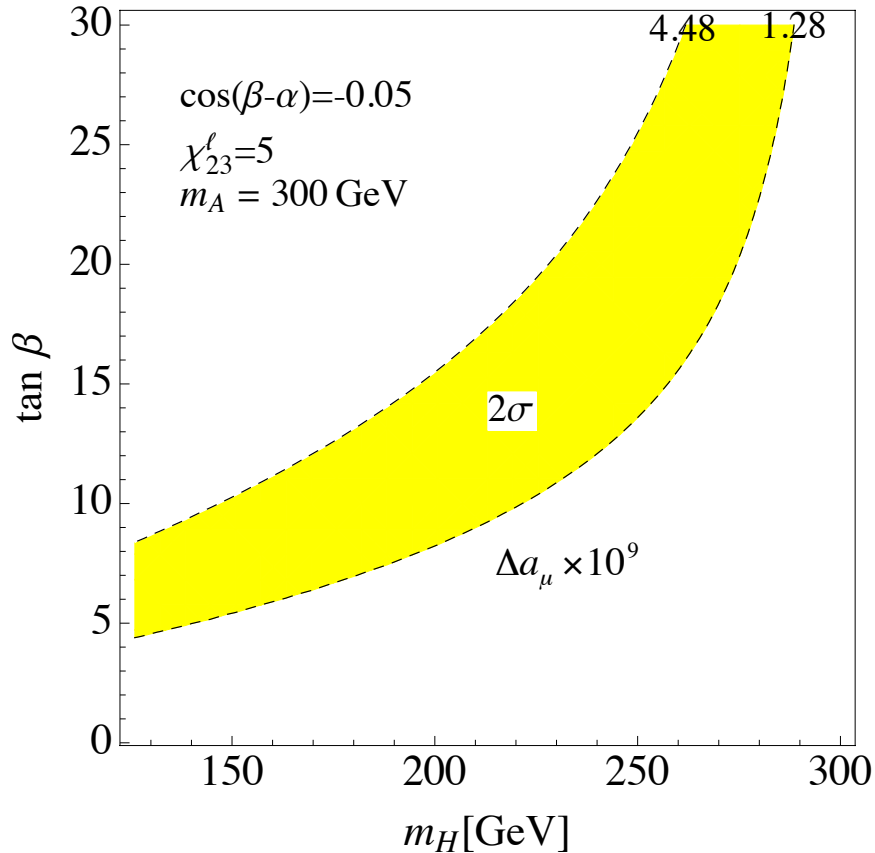


$$BR(\tau \rightarrow 3\mu) = \frac{\tau_\tau m_\tau^5}{3 \cdot 2^9 \pi^3} \frac{|X_{23}^\ell|^2}{c_\beta^2} \left[\left| \frac{c_{\beta\alpha} y_{h22}^\ell}{m_h^2} - \frac{s_{\beta\alpha} y_{H22}^\ell}{m_H^2} \right|^2 + \left| \frac{y_{A22}^\ell}{m_A^2} \right|^2 \right]$$

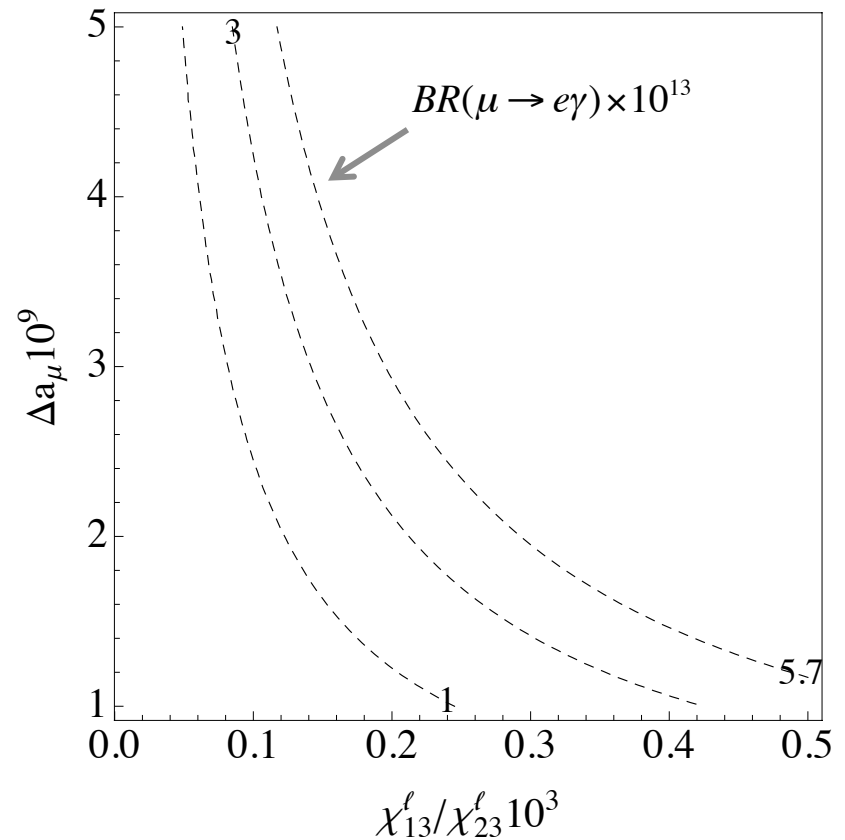
Here we apply ansatz: $X_{ij}^\ell = \frac{\sqrt{m_i m_j}}{v} \chi_{ij}^\ell$

2. Muon g-2 and CLFV in 2HDM

Muon g-2



Muon g-2 and $\text{BR}(\mu \rightarrow e\gamma)$



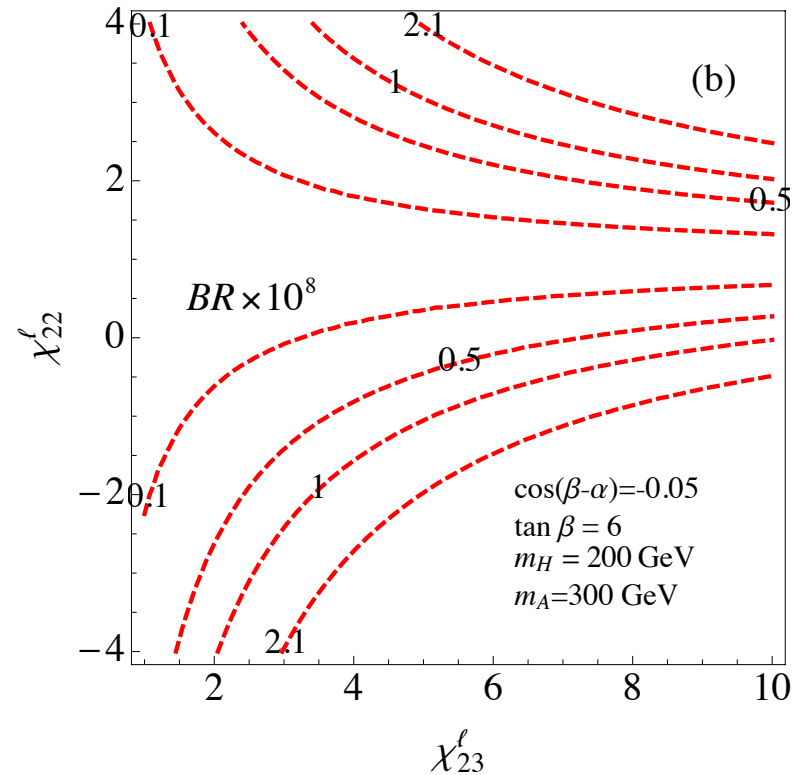
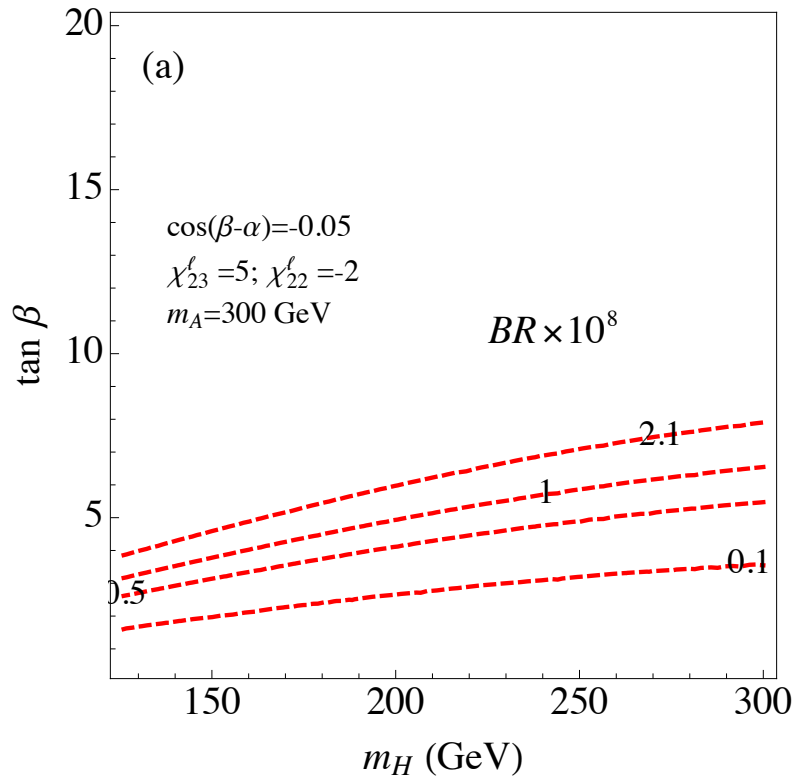
$$\text{BR}(\mu \rightarrow e\gamma) < 4.2 \times 10^{-13}$$

MEG (2016)

- ✓ Muon g-2 can be explained for $m_H < m_A$
- ✓ Coupling χ_{13} is strongly constrained by $\mu \rightarrow e\gamma$

2. Muon g-2 and CLFV in 2HDM

$BR(\tau \rightarrow 3\mu)$



✓ Sizable BR for $\tau \rightarrow 3\mu$

✓ More parameter region can be tested in future

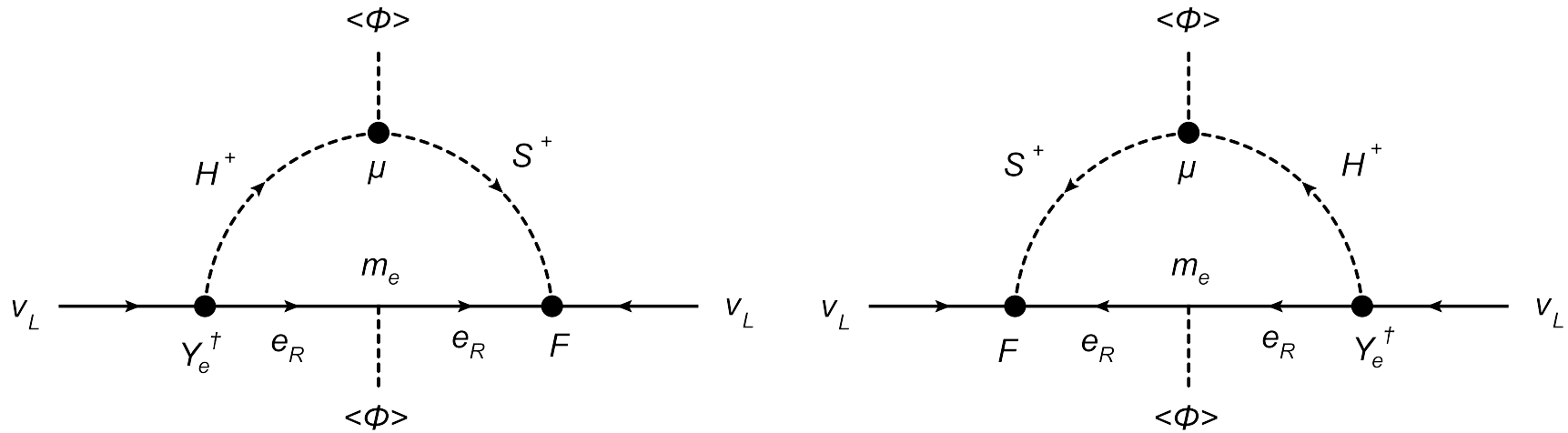
$$BR(\tau \rightarrow \mu\mu\mu) < 2.1 \times 10^{-8}$$

Belle (2010)

- 1. Introduction**
- 2. Muon $g-2$ and CLFV in 2HDM**
- 3. Zee-model with flavor symmetry**
- 4. Summary and discussion**

3. Zee-model with flavor symmetry

Original Zee-model for neutrino mass



One-loop mass generation

Realized by SM + second Higgs doublet + charged scalar

Softly-broken Z_2 symmetry is assigned to forbid FCNC: $\Phi_2 \rightarrow -\Phi_2$

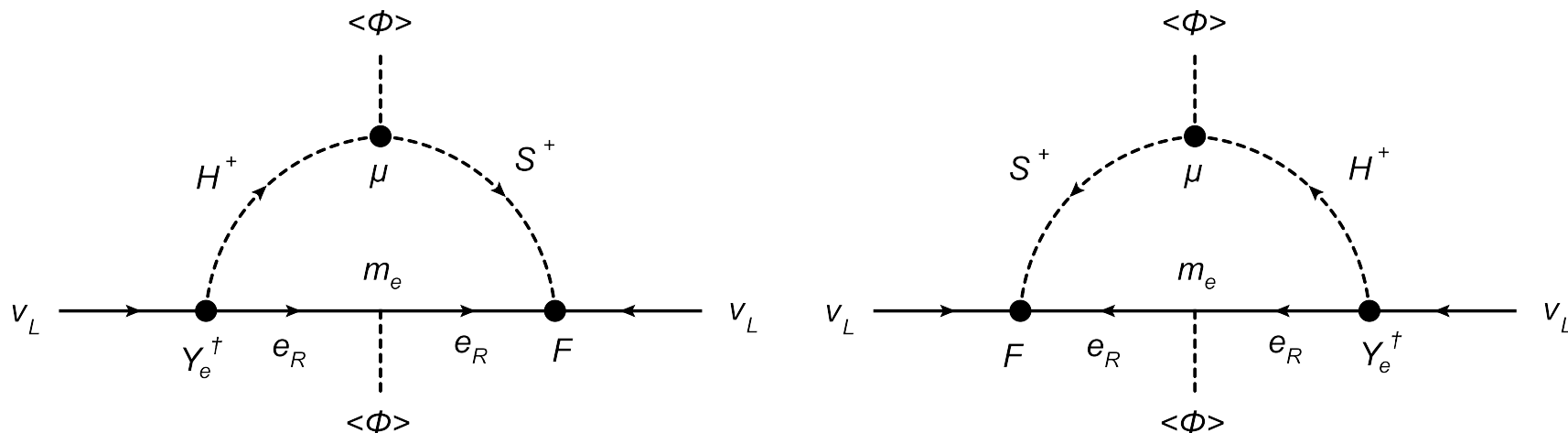
	Q_L^i	u_R^i	d_R^i	L_L^i	ℓ_R^i	Φ_1	Φ_2	S^+
$SU(3)_c$	3	3	3	1	1	1	1	1
$SU(2)_L$	2	1	1	2	1	2	2	1
$U(1)_Y$	1/6	2/3	-1/3	-1/2	-1	1/2	1/2	1

$$L \supset F_{ij} \bar{L}_L^{ic} L_L^j S^+ + \frac{\sqrt{2} m_\ell}{v} \cot \beta \bar{\nu}_L e_R H^+ + \mu \left[\Phi_1^T (i\sigma_2) \Phi_2 (S^+)^* + h.c. \right]$$

Zee (1980)

3. Zee-model with flavor symmetry

Original Zee-model for neutrino mass



One-loop mass generation

Realized by SM + second Higgs doublet + charged scalar

Softly broken Z_2 symmetry is assigned to forbid FCNC: $\Phi_2 \rightarrow -\Phi_2$

⇒ Current neutrino oscillation data can not be fitted

- ✓ We relax Z_2 symmetry to get more general structure of couplings
- ✓ To avoid FCNC in quark sector, we introduce global $U(1)$ symmetry

3. Zee-model with flavor symmetry

Zee-model with global U(1) symmetry

□ We assign global U(1) charge for leptons and scalars

	Q_L^i	u_R^i	d_R^i	L_L^i	ℓ_R^i	Φ_1	Φ_2	S^+
$SU(3)_c$	3	3	3	1	1	1	1	1
$SU(2)_L$	2	1	1	2	1	2	2	1
$U(1)_Y$	1/6	2/3	-1/3	-1/2	-1	1/2	1/2	1
$U(1)'$	0	0	0	q_L^i	q_R^i	q	0	q_S

Particle contents are the same as the original Zee-model

← **Lepton flavor dependent**

◆ Yukawa interactions

$$-L_Y = \left(\tilde{Y}_u\right)_{ij} \bar{Q}_L^i \Phi_2^c u_R^j + \left(\tilde{Y}_d\right)_{ij} \bar{Q}_L^i \Phi_2 d_R^j + \left(\tilde{Y}_\ell^1\right)_{ij} \bar{L}_L^i \Phi_1 \ell_R^j + \left(\tilde{Y}_\ell^2\right)_{ij} \bar{L}_L^i \Phi_2 \ell_R^j + \tilde{F}_{ij} \bar{L}_L^{ci} (i\sigma_2) L_L^j S^+ + h.c.$$

◆ Relevant term for neutrino mass generation in Higgs potential

$$V \supset \mu \left[\Phi_1^T (i\sigma_2) \Phi_2 (S^+)^* + h.c. \right]$$

3. Zee-model with flavor symmetry

Structure of Yukawa coupling with global U(1)

➤ **Class I :** $q_R = (0, 0, -q)$, $q_L = q_S = 0$

➡
$$\tilde{Y}_\ell^1 = \begin{pmatrix} 0 & 0 & \times \\ 0 & 0 & \times \\ 0 & 0 & \times \end{pmatrix}, \quad \tilde{Y}_\ell^2 = \begin{pmatrix} \times & \times & 0 \\ \times & \times & 0 \\ \times & \times & 0 \end{pmatrix}, \quad \tilde{F} = \begin{pmatrix} 0 & \times & \times \\ & 0 & \times \\ & & 0 \end{pmatrix},$$

➤ **Class II :** $q_R = 0$, $q_L = (0, 0, q)$, $q_S = -q$

➡
$$\tilde{Y}_\ell^1 = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ \times & \times & \times \end{pmatrix}, \quad \tilde{Y}_\ell^2 = \begin{pmatrix} \times & \times & \times \\ \times & \times & \times \\ 0 & 0 & 0 \end{pmatrix}, \quad \tilde{F} = \begin{pmatrix} 0 & 0 & \times \\ & 0 & \times \\ & & 0 \end{pmatrix}$$

➤ **Class III :** $q_R = (0, 0, q)$, $q_L = (0, 0, -2q)$, $q_S = q$

➡
$$\tilde{Y}_\ell^1 = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & \times \end{pmatrix}, \quad \tilde{Y}_\ell^2 = \begin{pmatrix} \times & \times & 0 \\ \times & \times & 0 \\ 0 & 0 & 0 \end{pmatrix}, \quad \tilde{F} = \begin{pmatrix} 0 & 0 & \times \\ & 0 & \times \\ & & 0 \end{pmatrix}$$

3. Zee-model with flavor symmetry

Structure of Yukawa coupling with global U(1)

➤ **Class I :** $q_R = (0, 0, -q)$, $q_L = q_S = 0$

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$$\tilde{Y}_\ell^1 = \begin{pmatrix} 0 & 0 & \times \\ 0 & 0 & \times \\ 0 & 0 & \times \end{pmatrix}, \quad \tilde{Y}_\ell^2 = \begin{pmatrix} \times & \times & 0 \\ \times & \times & 0 \\ \times & \times & 0 \end{pmatrix}, \quad \tilde{F} = \begin{pmatrix} 0 & \times & \times \\ & 0 & \times \\ & & 0 \end{pmatrix},$$

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$$\tilde{Y}_\ell^1 = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & \times \end{pmatrix}, \quad \tilde{Y}_\ell^2 = \begin{pmatrix} \times & \times & 0 \\ \times & \times & 0 \\ 0 & 0 & 0 \end{pmatrix}, \quad \tilde{F} = \begin{pmatrix} 0 & 0 & \times \\ & 0 & \times \\ & & 0 \end{pmatrix}$$

3. Zee-model with flavor symmetry

Charged lepton mass and relevant couplings

Charged lepton mass: $M_\ell = \frac{v}{\sqrt{2}} (c_\beta \tilde{Y}_\ell^1 + s_\beta \tilde{Y}_\ell^2)$

$$\ell_{L,R} \rightarrow U_{L,R} \ell_{L,R}$$

$$U_L^\dagger M_\ell U_R = (m_e, m_\mu, m_\tau)$$

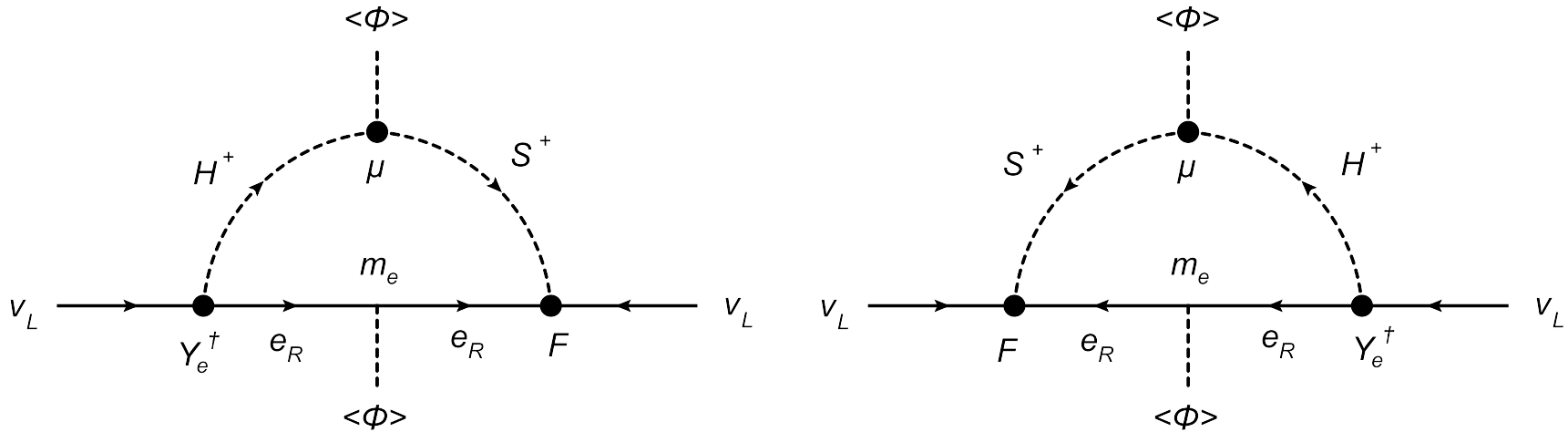
Couplings in charged lepton mass basis

$$-L_Y \supset \begin{pmatrix} \bar{\nu}_L & \bar{\ell}_L \end{pmatrix} \left[\frac{\sqrt{2}}{v} \begin{pmatrix} M_\ell U_R G^+ \\ m_\ell \Phi^0 \end{pmatrix} + \begin{pmatrix} Y_\ell H^+ \\ Y_\ell^0 \Phi'^0 \end{pmatrix} \right] \ell_R - 2F \bar{\nu}^c \ell_R S^+ + h.c.$$

$$\left(\begin{array}{l} Y_\ell^0 = U_L^\dagger \tilde{Y}_\ell U_R, \quad Y_e = \tilde{Y}_\ell U_R, \quad (\tilde{Y}_\ell = -s_\beta \tilde{Y}_\ell^1 + c_\beta \tilde{Y}_\ell^2) \\ F = \tilde{F} U_R \end{array} \right)$$

3. Zee-model with flavor symmetry

Neutrino mass generation at one loop level

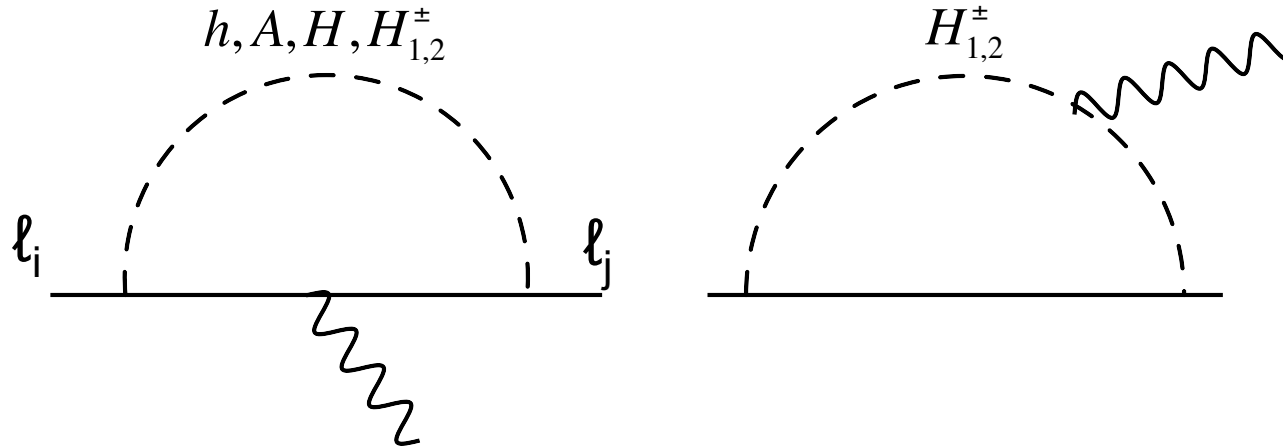


$$M_{\nu}^{ij} = \frac{1}{16\pi^2} \frac{\sqrt{2}v\mu}{m_{H_2^\pm}^2 - m_{H_1^\pm}^2} \ln\left(\frac{m_{H_2^\pm}^2}{m_{H_1^\pm}^2}\right) \left(F m_\ell Y_\ell^\dagger\right) + (i \leftrightarrow j)$$

✓ Two charged scalar mass eigenstate : $H_1^\pm, H_2^\pm$

3. Zee-model with flavor symmetry

□ LFV decay of charged lepton $\ell_i \rightarrow \ell_j \gamma$



$$\frac{BR(\ell_i \rightarrow \ell_j \gamma)}{BR(\ell_i \rightarrow \ell_j \nu_i \bar{\nu}_j)} \approx \frac{48\pi^3 \alpha_{em}}{G_F^2 m_{\ell_i}^2} \left(\left| \sum_{\phi} (a_R^{\phi})_{ij} \right|^2 + \left| \sum_{\phi} (a_L^{\phi})_{ij} \right|^2 \right) \quad \phi = h, H, A, H_1^{\pm}$$

$\left[a_{L,R}^{\phi} : \text{Amplitude estimated from diagrams and given by Yukawa couplings} \right]$

3. Zee-model with flavor symmetry

Numerical analysis

Searching for Yukawa couplings with mixing $U_{L,R}$ satisfying:

- Charged lepton mass
- Neutrino mass matrix which can fit neutrino oscillation data



Calculate BRs for CLFV processes by allowed parameters

- Imposing constraint on $\ell_i \rightarrow \ell_j \gamma$:

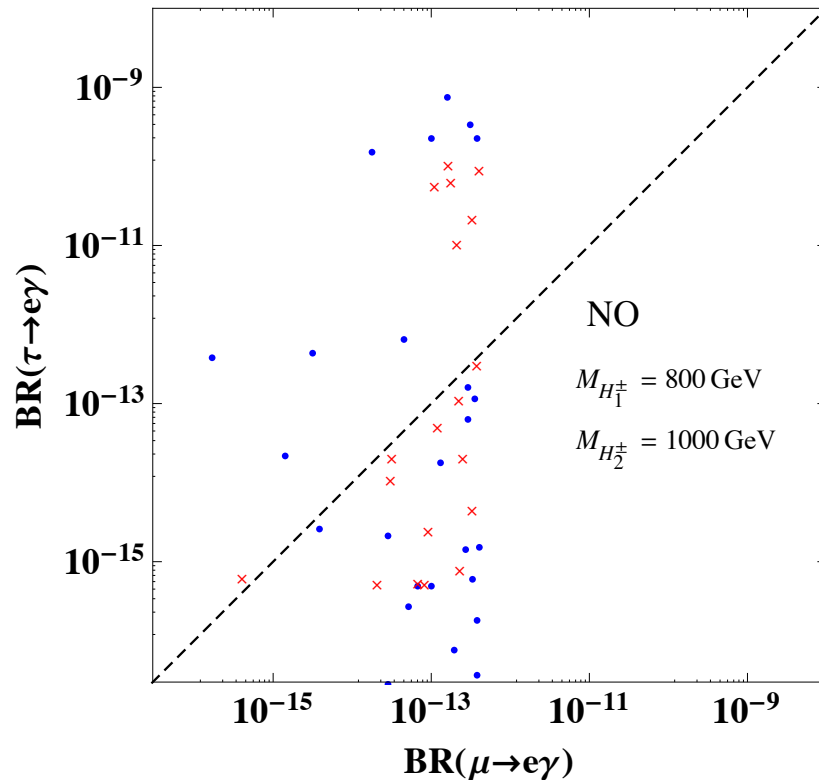
$$\text{BR}(\mu \rightarrow e \gamma) < 4.2 \times 10^{-13}, \quad \text{BR}(\tau \rightarrow e \gamma) < 3.3 \times 10^{-8}, \quad \text{BR}(\tau \rightarrow \mu \gamma) < 4.4 \times 10^{-8},$$

- Prediction for LFV decay of heavy Higgs H

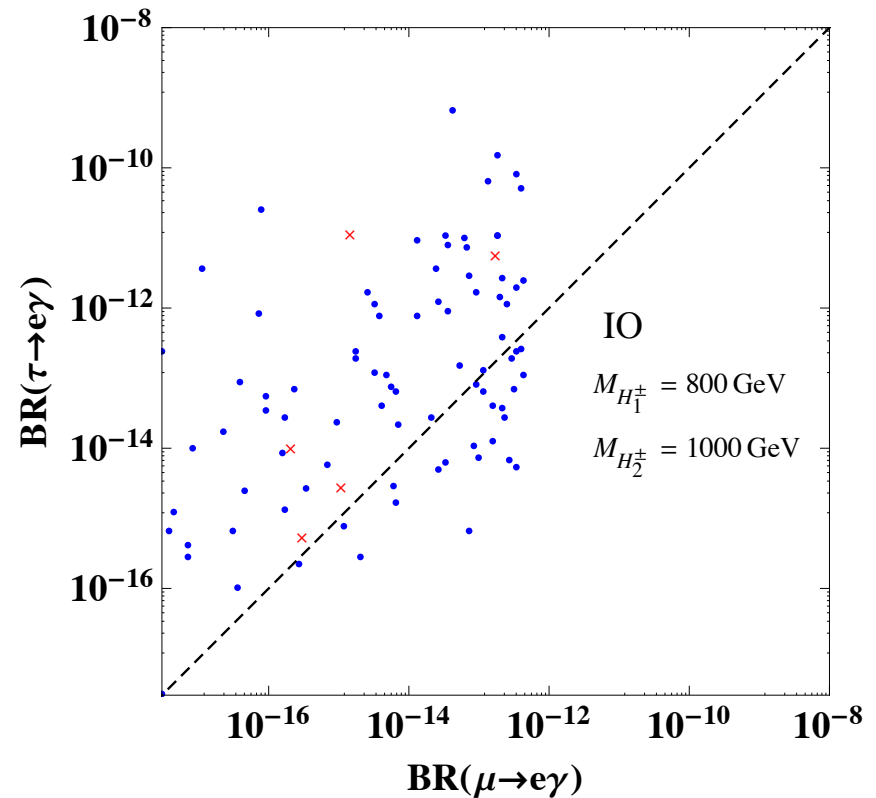
3. Zee-model with flavor symmetry

◆ Correlation between BR of $\mu \rightarrow e\gamma$ and $\tau \rightarrow e\gamma$

Normal ordering



Inverted ordering



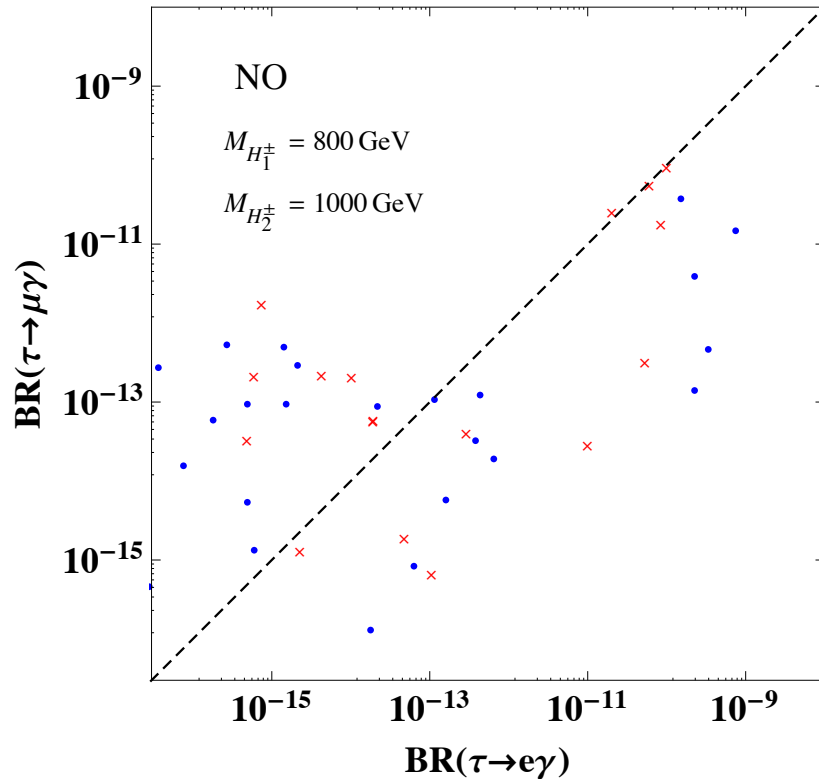
Blue dot : $1 < \tan\beta < 10$, Red cross : $10 < \tan\beta < 30$

✓ Normal ordering case tends to give larger $\text{BR}(\mu \rightarrow e\gamma)$

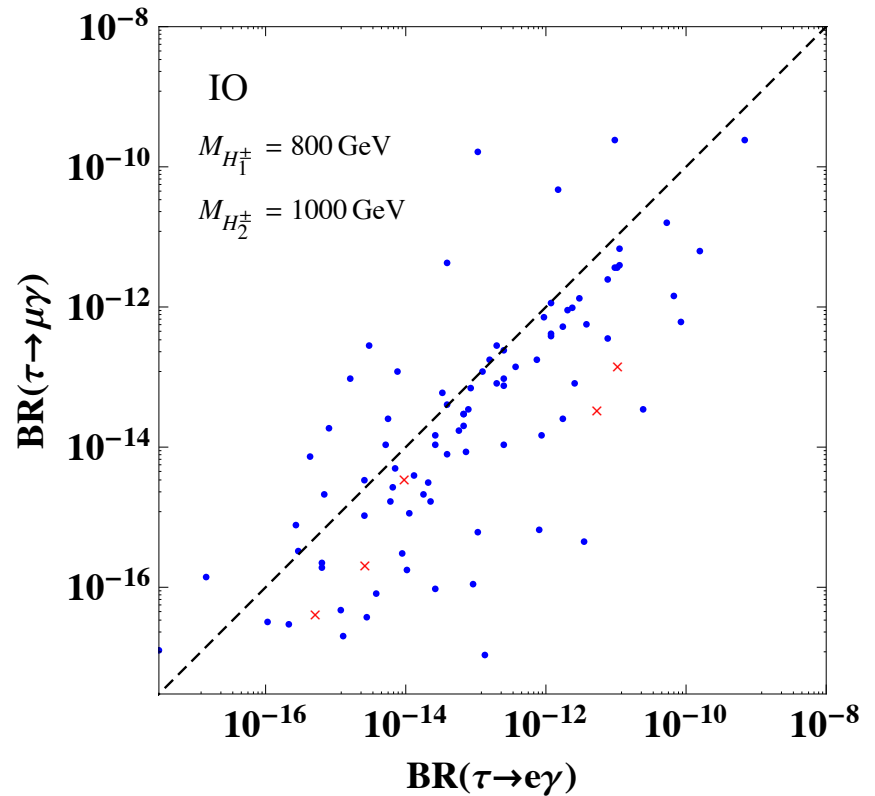
3. Zee-model with flavor symmetry

◆ Correlation between BR of $\tau \rightarrow e\gamma$ and $\tau \rightarrow \mu\gamma$

Normal ordering



Inverted ordering

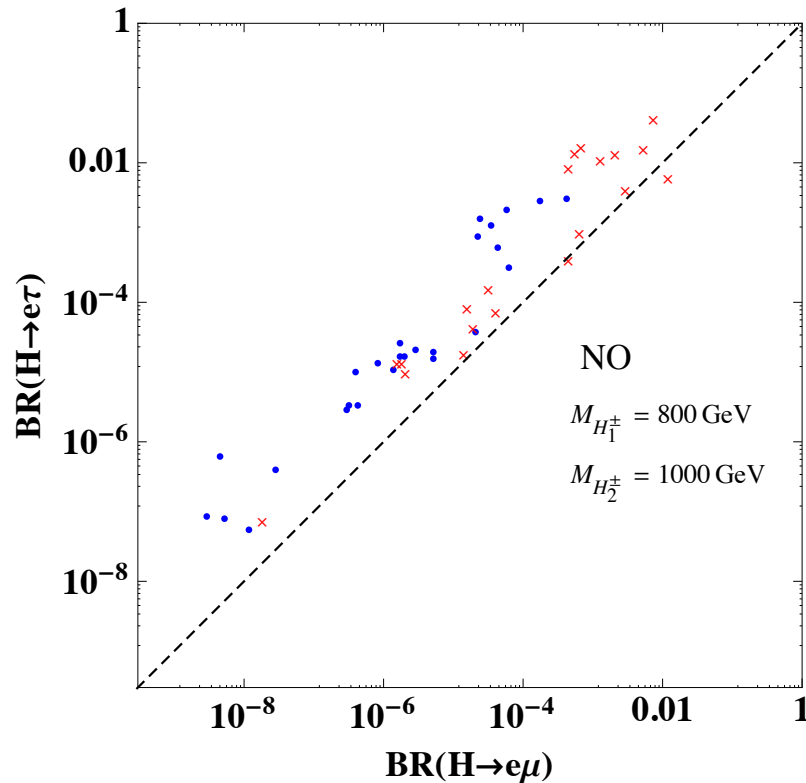


✓ BRs are more correlated for inverted ordering case

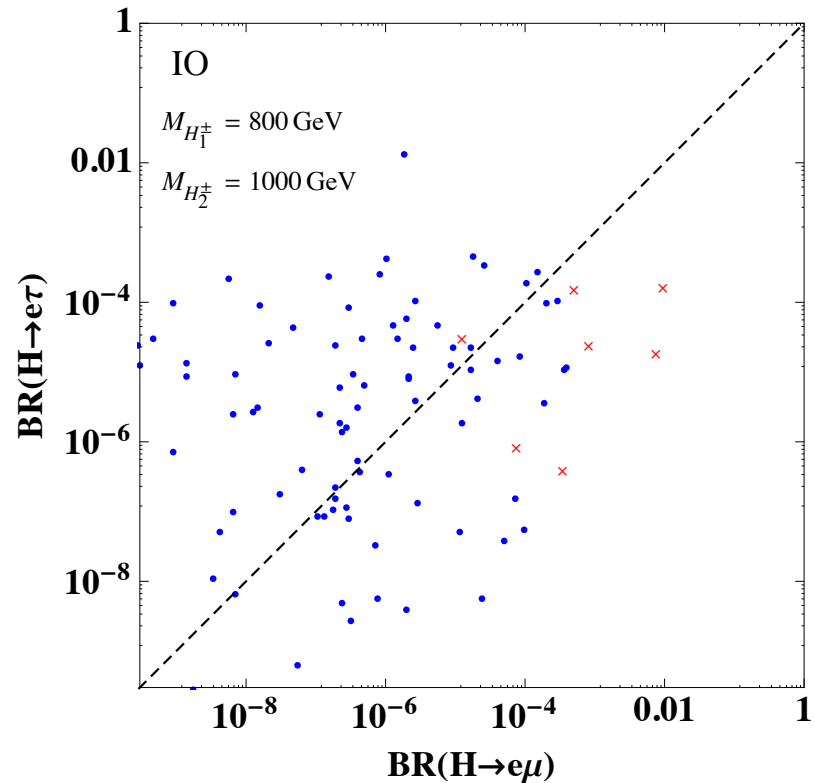
3. Zee-model with flavor symmetry

◆ Correlation between BR of $H \rightarrow e\mu$ and $H \rightarrow e\tau$

Normal ordering



Inverted ordering

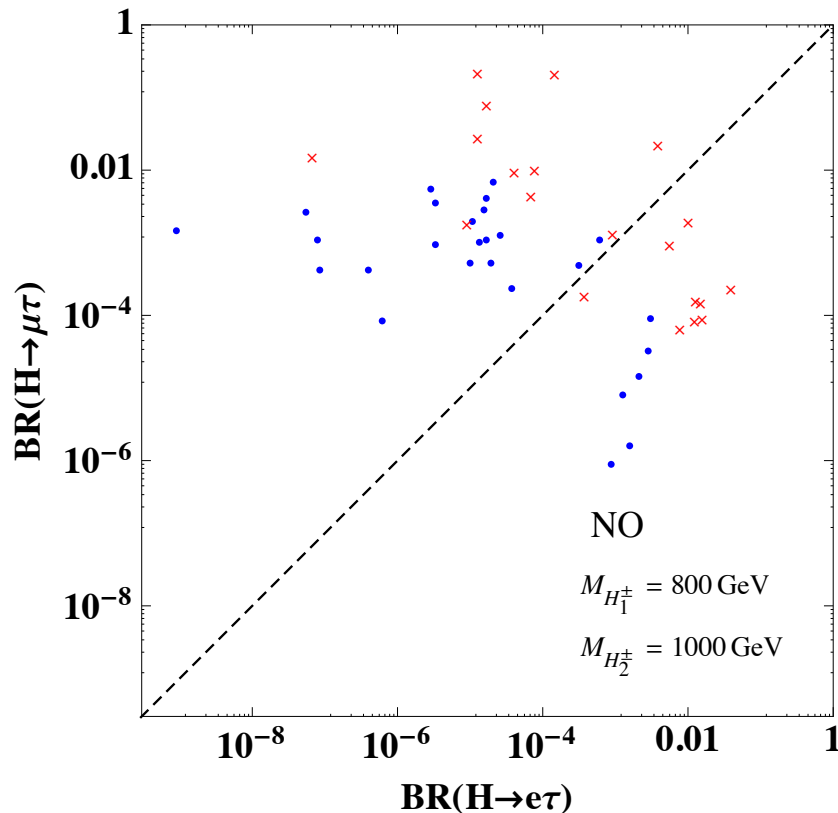


- ✓ Correlation in normal ordering case
- ✓ Inverted ordering case is less correlated

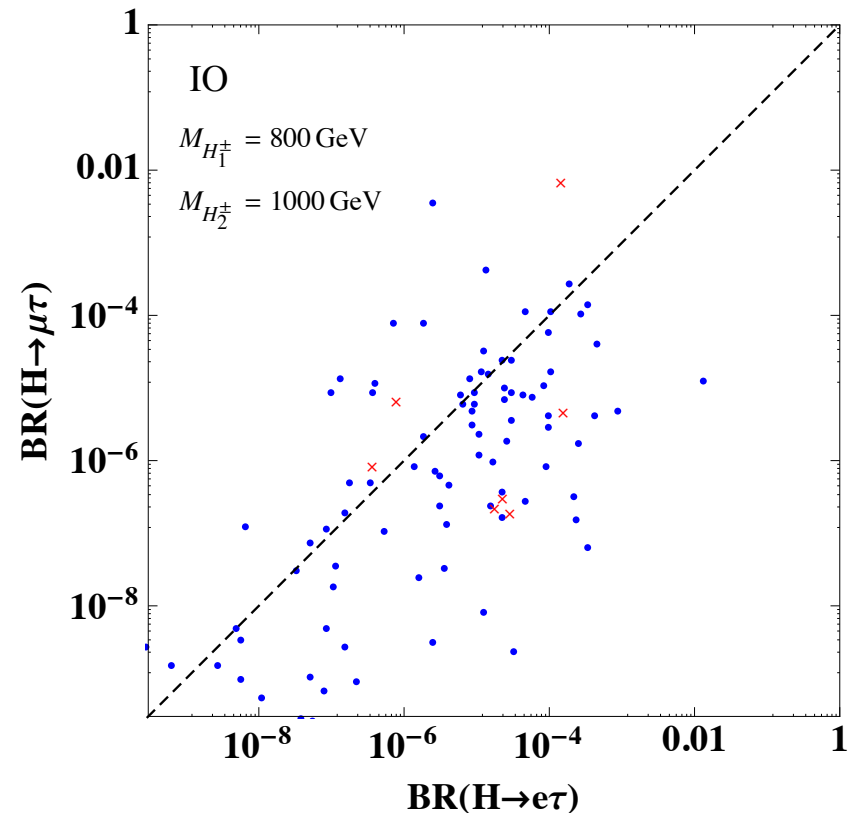
3. Zee-model with flavor symmetry

◆ Correlation between BR of $H \rightarrow e\tau$ and $H \rightarrow \mu\tau$

Normal ordering



Inverted ordering



- ✓ BRs are more correlated for inverted ordering case
- ✓ These LFV H decay could be searched for at the LHC

Summary and discussion

- ❑ Extended Higgs sector is attractive BSM candidate
- ❑ New Yukawa couplings with extra scalar give CLFV
 - In particular CLFV would be related to muon $g-2$ and/or neutrino mass
- ❑ We discussed models with CLFV
 - Muon $g-2$ explained by 2HDM and related CLFV
 - Zee-model with flavor symmetry connecting neutrino mass and CLFV

Thanks for listening !

All Yukawa interactions in general 2HDM

$$\begin{aligned}
 -\mathcal{L}_Y^h &= \bar{u}_L \left[\frac{c_\alpha}{vs_\beta} \mathbf{m}_u - \frac{c_{\beta\alpha}}{s_\beta} \mathbf{X}^u \right] u_R h + \bar{d}_L \left[-\frac{s_\alpha}{vc_\beta} \mathbf{m}_d + \frac{c_{\beta\alpha}}{c_\beta} \mathbf{X}^d \right] d_R h \\
 &+ \bar{\ell}_L \left[-\frac{s_\alpha}{vc_\beta} \mathbf{m}_\ell + \frac{c_{\beta\alpha}}{c_\beta} \mathbf{X}^\ell \right] \ell_R h + h.c. ,
 \end{aligned}$$

$$\begin{aligned}
 -\mathcal{L}_Y^{H,A} &= \bar{u}_L \left[\frac{s_\alpha}{vs_\beta} \mathbf{m}_u + \frac{s_{\beta\alpha}}{s_\beta} \mathbf{X}^u \right] u_R H + \bar{d}_L \left[\frac{c_\alpha}{vc_\beta} \mathbf{m}_d - \frac{s_{\beta\alpha}}{c_\beta} \mathbf{X}^d \right] d_R H \\
 &+ \bar{\ell}_L \left[\frac{c_\alpha}{vc_\beta} \mathbf{m}_\ell - \frac{s_{\beta\alpha}}{c_\beta} \mathbf{X}^\ell \right] \ell_R H + i\bar{u}_L \left[-\frac{\cot \beta}{v} \mathbf{m}_u + \frac{\mathbf{X}^u}{s_\beta} \right] u_R A \\
 &+ i\bar{d}_L \left[-\frac{\tan \beta}{v} \mathbf{m}_d + \frac{\mathbf{X}^d}{c_\beta} \right] d_R A + i\bar{\ell}_L \left[-\frac{\tan \beta}{v} \mathbf{m}_\ell + \frac{\mathbf{X}^\ell}{c_\beta} \right] \ell_R A + h.c.
 \end{aligned}$$

$$\begin{aligned}
 -\mathcal{L}_Y^{H^\pm} &= \sqrt{2}\bar{d}_L V_{CKM}^\dagger \left[-\frac{\cot \beta}{v} \mathbf{m}_u + \frac{\mathbf{X}^u}{s_\beta} \right] u_R H^- \\
 &+ \sqrt{2}\bar{u}_L V_{CKM} \left[-\frac{\tan \beta}{v} \mathbf{m}_d + \frac{\mathbf{X}^d}{c_\beta} \right] d_R H^+ \\
 &+ \sqrt{2}\bar{\nu}_L V_{PMNS} \left[-\frac{\tan \beta}{v} \mathbf{m}_\ell + \frac{\mathbf{X}^\ell}{c_\beta} \right] \ell_R H^+ + h.c. ,
 \end{aligned}$$

CLFV amplitudes in Zee-model

$$(a_R^{H_1^\pm})_{ij} = \frac{1}{16\pi^2} \sum_{k=1}^3 \left[(Y_\ell)_{kj}^* (Y_\ell)_{ki} c_\chi^2 F_1(m_{\ell_i}, m_{\ell_j}, m_{H_1^\pm}) - F_{kj}^* F_{ki} s_\chi^2 F_2(m_{\ell_i}, m_{\ell_j}, m_{H_2^\pm}) \right], \quad (C1)$$

$$(a_L^{H_1^\pm})_{ij} = \frac{1}{16\pi^2} \sum_{k=1}^3 \left[(Y_\ell)_{kj}^* (Y_\ell)_{ki} c_\chi^2 F_2(m_{\ell_i}, m_{\ell_j}, m_{H_1^\pm}) - F_{kj}^* F_{ki} s_\chi^2 F_1(m_{\ell_i}, m_{\ell_j}, m_{H_2^\pm}) \right], \quad (C2)$$

$$(a_R^{H_2^\pm})_{ij} = (a_R^{H_1^\pm})_{ij} \Big|_{c_\chi^2 \leftrightarrow s_\chi^2}, \quad (a_L^{H_2^\pm})_{ij} = (a_L^{H_1^\pm})_{ij} \Big|_{c_\chi^2 \leftrightarrow s_\chi^2}. \quad (C3)$$

$$F_{1[2]}(m_1, m_2, m_3) = \int [dX] \frac{xzm_2[xy m_1]}{(x^2 - x)m_1^2 + xz(m_1^2 - m_2^2) + (y + z)m_3^2},$$

$$(a_R^\varphi)_{ij} = \frac{1}{8\pi^2} \sum_{k=1}^3 \int [dX] \frac{xym_{\ell_i} f_\varphi^{jk} f_\varphi^{ki} + xzm_{\ell_j} g_\varphi^{jk} g_\varphi^{ki} + (1-x)m_{\ell_k} f_\varphi^{jk} g_\varphi^{ki}}{-x(1-x)m_{\ell_i}^2 - xz(m_{\ell_j}^2 - m_{\ell_i}^2) + (z+y)m_{\ell_k}^2 + xm_\varphi^2},$$

$$(a_L^\varphi)_{ij} = \frac{1}{8\pi^2} \sum_{k=1}^3 \int [dX] \frac{xzm_{\ell_i} f_\varphi^{jk} f_\varphi^{ki} + xym_{\ell_j} g_\varphi^{jk} g_\varphi^{ki} + (1-x)m_{\ell_k} g_\varphi^{jk} f_\varphi^{ki}}{-x(1-x)m_{\ell_i}^2 - xz(m_{\ell_j}^2 - m_{\ell_i}^2) + (z+y)m_{\ell_k}^2 + xm_\varphi^2},$$

$$f_h^{ij} = \frac{\sqrt{2}m_{\ell_i}}{v} s_{\beta-\alpha} \delta_{ij} + \frac{1}{\sqrt{2}} (Y_\ell^0)_{ji}^* c_{\beta-\alpha}, \quad g_h^{ij} = \frac{\sqrt{2}m_{\ell_i}}{v} s_{\beta-\alpha} \delta_{ij} + \frac{1}{\sqrt{2}} (Y_\ell^0)_{ij} c_{\beta-\alpha}$$

$$f_H^{ij} = \frac{\sqrt{2}m_{\ell_i}}{v} c_{\beta-\alpha} \delta_{ij} - \frac{1}{\sqrt{2}} (Y_\ell^0)_{ji}^* s_{\beta-\alpha}, \quad g_H^{ij} = \frac{\sqrt{2}m_{\ell_i}}{v} c_{\beta-\alpha} \delta_{ij} - \frac{1}{\sqrt{2}} (Y_\ell^0)_{ij} s_{\beta-\alpha}$$

$$f_A^{ij} = -\frac{i}{\sqrt{2}} (Y_\ell^0)_{ji}^* c_{\beta-\alpha}, \quad g_A^{ij} = \frac{i}{\sqrt{2}} (Y_\ell^0)_{ij} c_{\beta-\alpha}.$$

