

# Theory of Charged Lepton Flavour Violation

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« Unlocking the Mysteries of Life, Matter and the Universe »

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\*Supported by NSF



# Outline

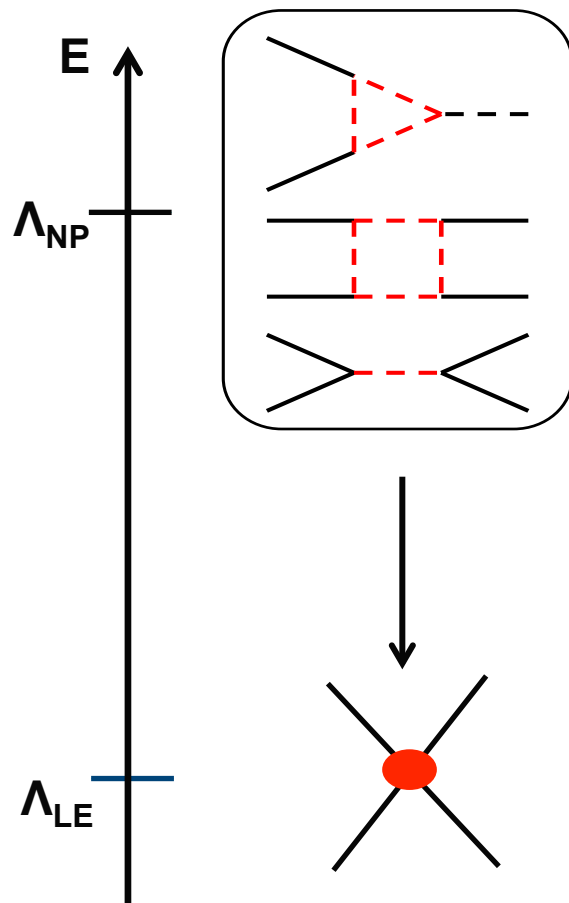
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1. Introduction and Motivation
2. Charged Lepton-Flavour Violation: Model discriminating power of muons and tau channels
3. Ex: Non-Standard LFV couplings of the Higgs boson
4. Conclusion and Outlook

# 1. Introduction and Motivation

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# 1.1 Why study charged leptons?



- In the quest of New Physics, can be sensitive to very high scale:

- Kaon physics:  $\frac{s\bar{d}s\bar{d}}{\Lambda^2} \Rightarrow \Lambda \gtrsim 10^5 \text{ TeV}$   
 $[\epsilon_K]$

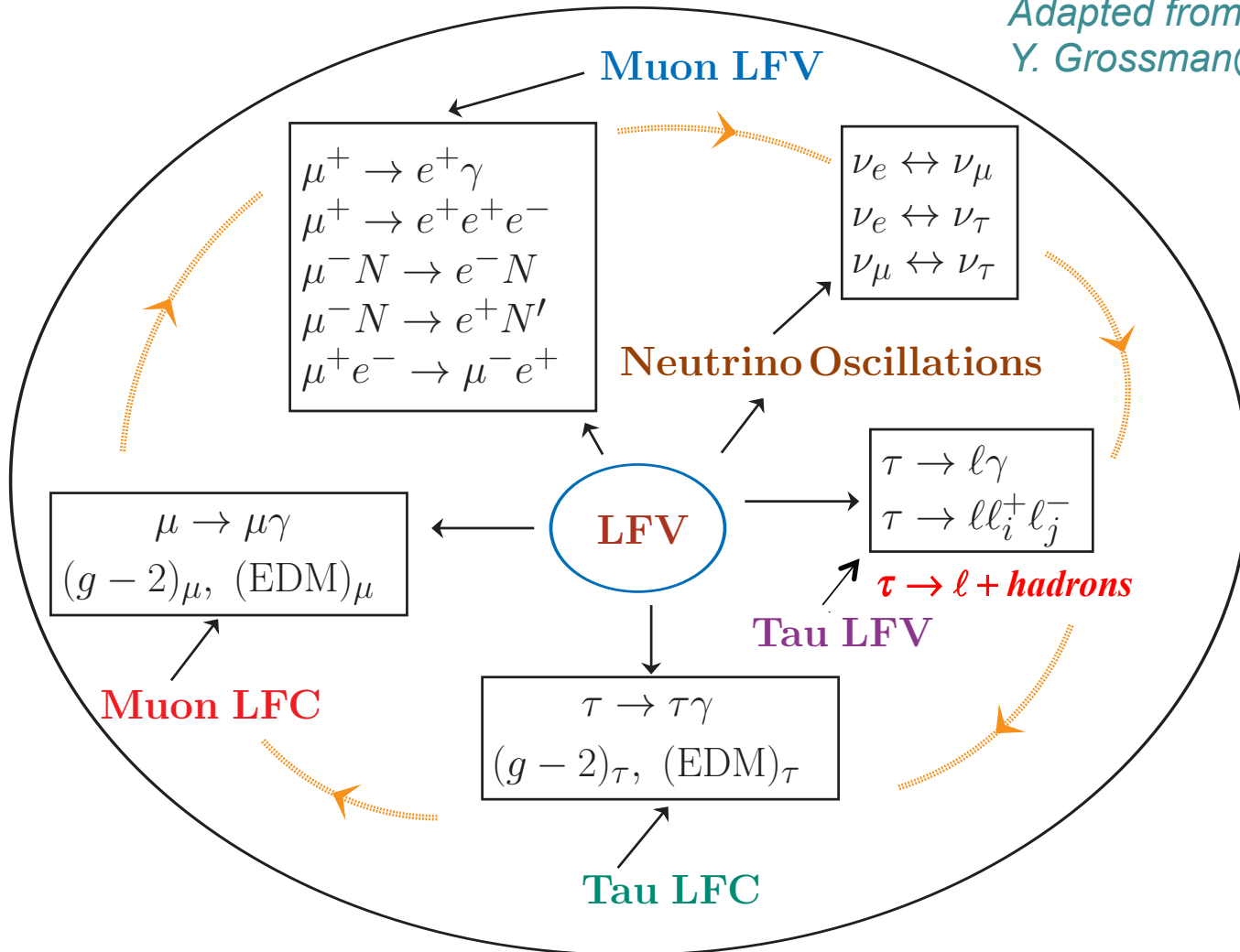
- Charged Leptons:  $\frac{\mu\bar{e}f\bar{f}}{\Lambda^2} \Rightarrow \Lambda \gtrsim 10^4 \text{ TeV}$   
 $[\mu \rightarrow e\gamma]$

- At low energy: lots of experiments e.g., *MEG*, *COMET*, *Mu2e*, *E-969*, *BaBar*, *Belle-II*, *BESIII*, *LHCb* ➡ huge improvements on measurements and bounds obtained and more expected
- In many cases no SM background: e.g., LFV, EDMs
- For some modes accurate calculations of hadronic uncertainties essential

➡ Charged leptons very important to look for *New Physics*!

## 1.2 The Program

Adapted from Talk by  
Y. Grossman@CLFV2013



## 2. Charged Lepton-Flavour Violation

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## 2.1 Introduction and Motivation

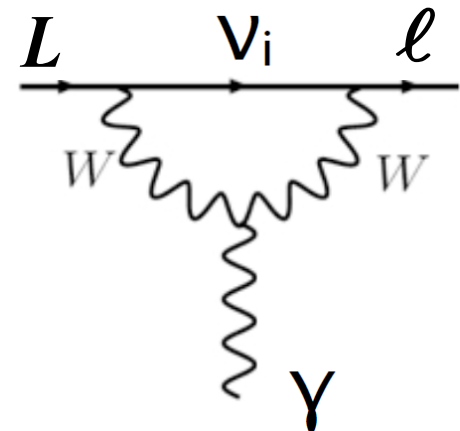
- Neutrino oscillations are the first evidence for lepton flavour violation
- How about in the charged lepton sector?
- In the *SM* with massive neutrinos effective CLFV vertices are tiny due to GIM suppression  $\Rightarrow$  *unobservably small rates!*

E.g.:  $\mu \rightarrow e \gamma$

$$Br(\mu \rightarrow e \gamma) = \frac{3\alpha}{32\pi} \left| \sum_{i=2,3} U_{\mu i}^* U_{ei} \frac{\Delta m_{1i}^2}{M_W^2} \right|^2 < 10^{-54}$$

*Petcov'77, Marciano & Sanda'77, Lee & St*

$$\left[ Br(\tau \rightarrow \mu \gamma) < 10^{-40} \right]$$



## 2.1 Introduction and Motivation

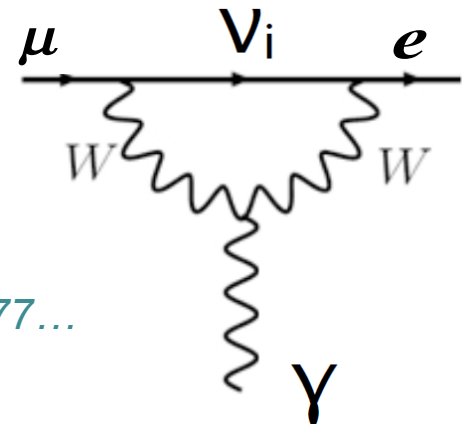
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*Petcov'77, Marciano & Sanda'77, Lee & Shrock'77...*

$$\left[ Br(\tau \rightarrow \mu\gamma) < 10^{-40} \right]$$



- Extremely *clean probe of beyond SM physics*



## 2.1 Introduction and Motivation

- In New Physics scenarios CLFV can reach observable levels in several channels

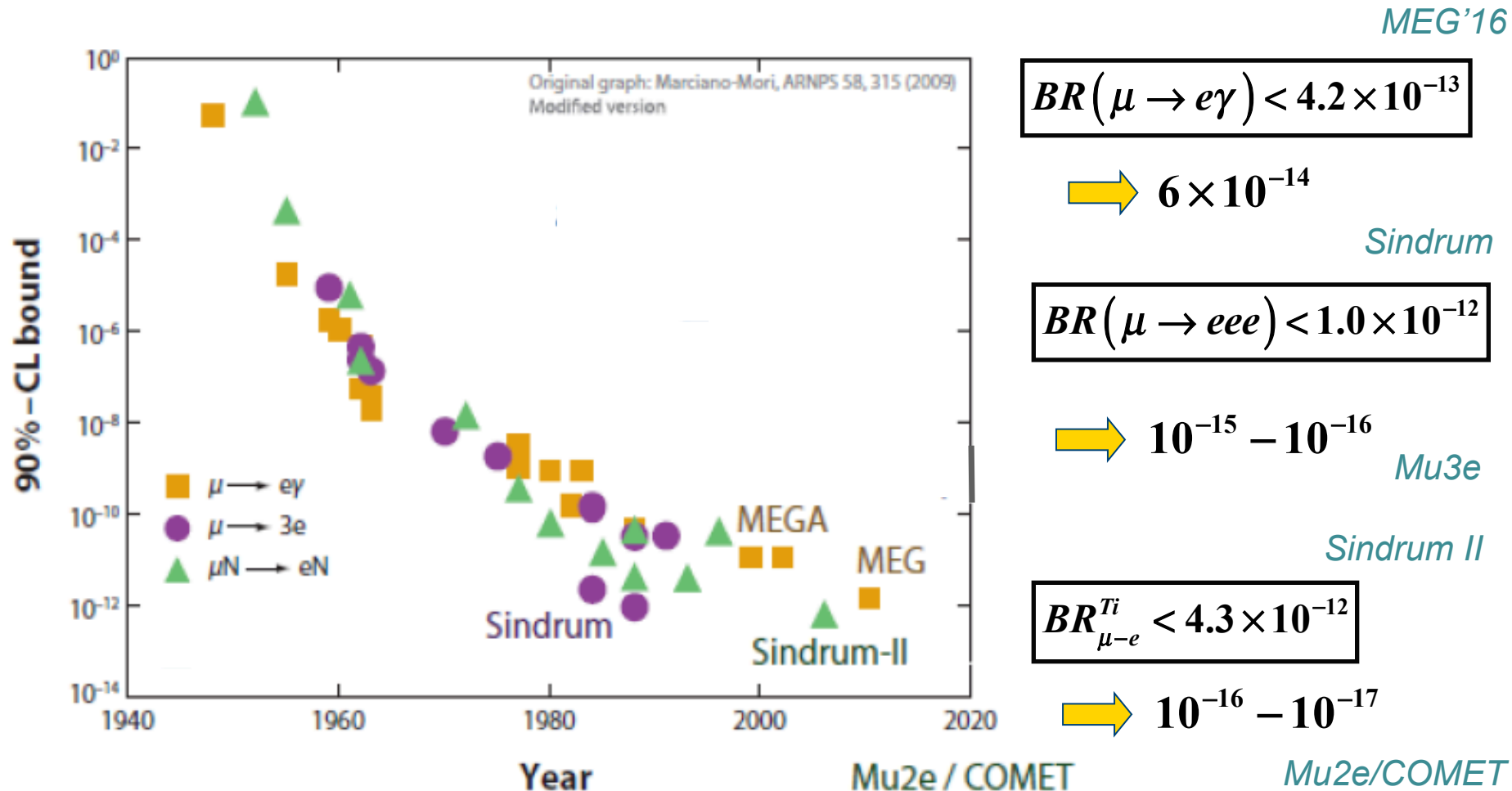
*Talk by D. Hitlin @ CLFV2013*

		$\tau \rightarrow \mu\gamma \quad \tau \rightarrow \ell\ell\ell$	
SM + $\nu$ mixing	Lee, Shrock, PRD 16 (1977) 1444 Cheng, Li, PRD 45 (1980) 1908	Undetectable	
SUSY Higgs	Dedes, Ellis, Raidal, PLB 549 (2002) 159 Brignole, Rossi, PLB 566 (2003) 517	$10^{-10}$	$10^{-7}$
SM + heavy Maj $\nu_R$	Cvetič, Dib, Kim, Kim, PRD 66 (2002) 034008	$10^{-9}$	$10^{-10}$
Non-universal $Z'$	Yue, Zhang, Liu, PLB 547 (2002) 252	$10^{-9}$	$10^{-8}$
SUSY SO(10)	Masiero, Vempati, Vives, NPB 649 (2003) 189 Fukuyama, Kikuchi, Okada, PRD 68 (2003) 033012	$10^{-8}$	$10^{-10}$
mSUGRA + Seesaw	Ellis, Gomez, Leontaris, Lola, Nanopoulos, EPJ C14 (2002) 319 Ellis, Hisano, Raidal, Shimizu, PRD 66 (2002) 115013	$10^{-7}$	$10^{-9}$

- But the sensitivity of particular modes to CLFV couplings is model dependent
- Comparison in muonic and tauonic channels of branching ratios, conversion rates and spectra is model-diagnostic

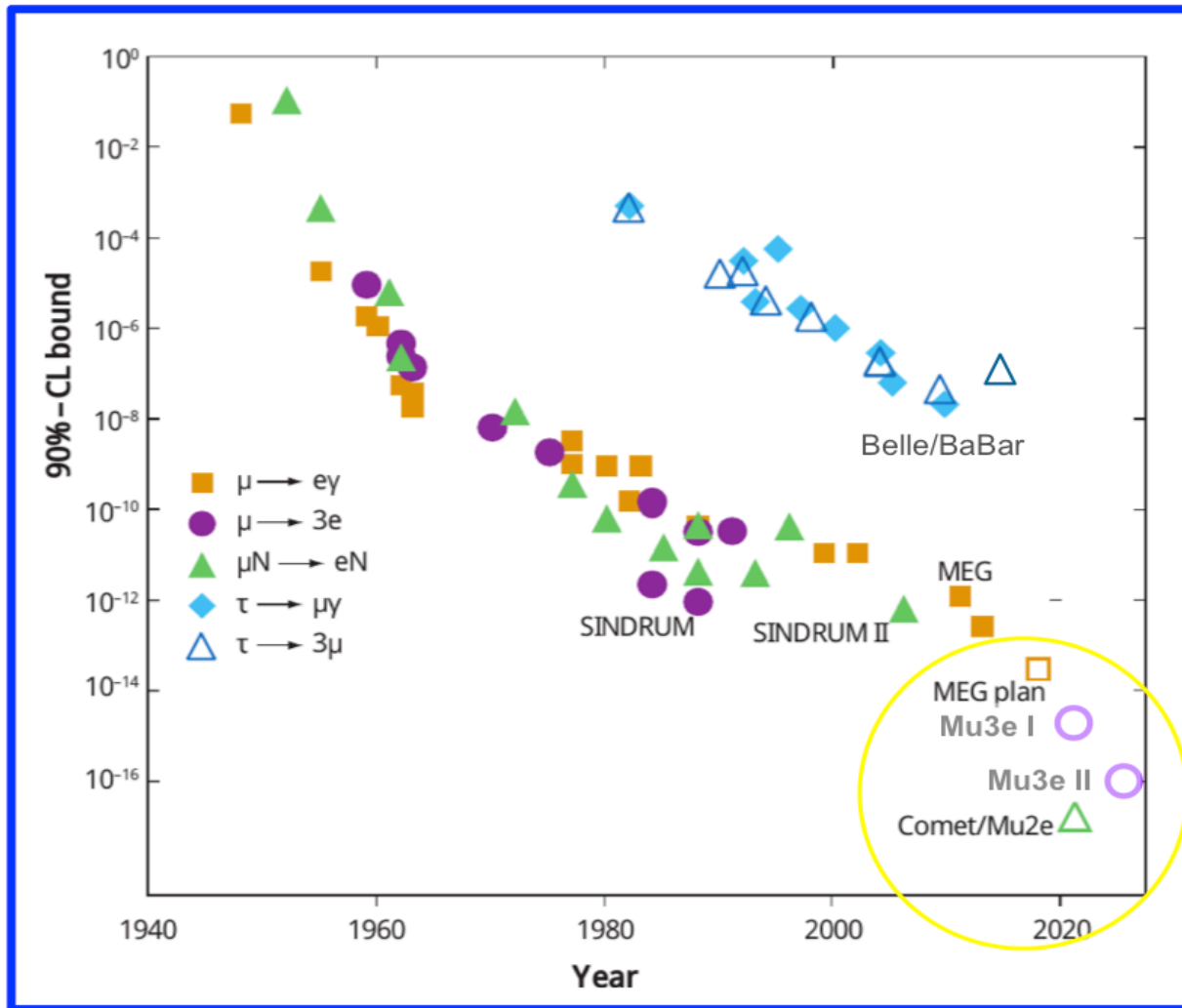
## 2.2 CLFV processes: muon decays

- Several processes:  $\mu \rightarrow e\gamma$ ,  $\mu \rightarrow e\bar{e}e$ ,  $\mu(A, Z) \rightarrow e(A, Z)$



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MEG'16

$$BR(\mu \rightarrow e\gamma) < 4.2 \times 10^{-13}$$

$$\Rightarrow 6 \times 10^{-14}$$

Sindrum

$$BR(\mu \rightarrow eee) < 1.0 \times 10^{-12}$$

$$\Rightarrow 10^{-15} - 10^{-16}$$

Mu3e

Sindrum II

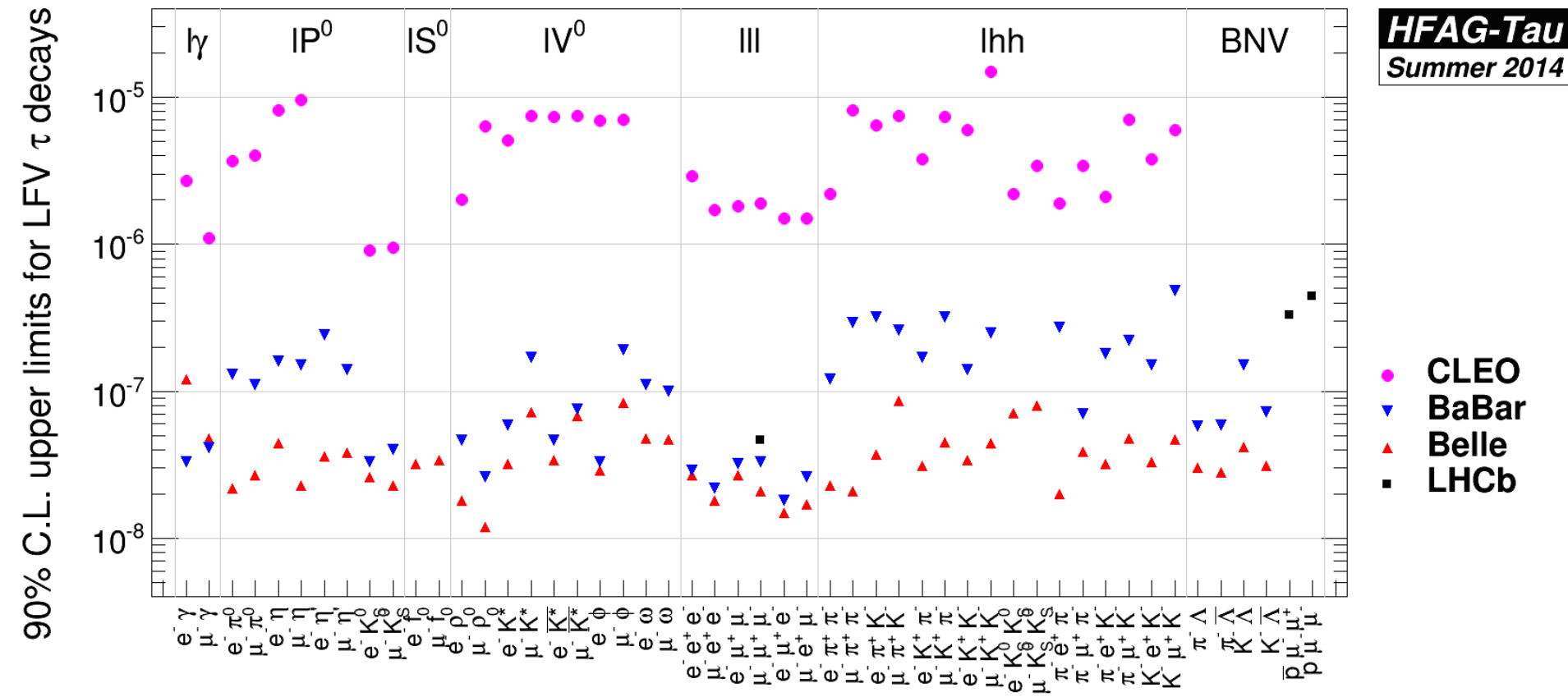
$$BR_{\mu-e}^{Ti} < 4.3 \times 10^{-12}$$

$$\Rightarrow 10^{-16} - 10^{-17}$$

Mu2e/COMET

## 2.2 CLFV processes: tau decays

- Several processes:  $\tau \rightarrow \ell \gamma$ ,  $\tau \rightarrow \ell_\alpha \bar{\ell}_\beta \ell_\beta$ ,  $\tau \rightarrow \ell Y$   $\leftarrow P, S, V, P\bar{P}, \dots$



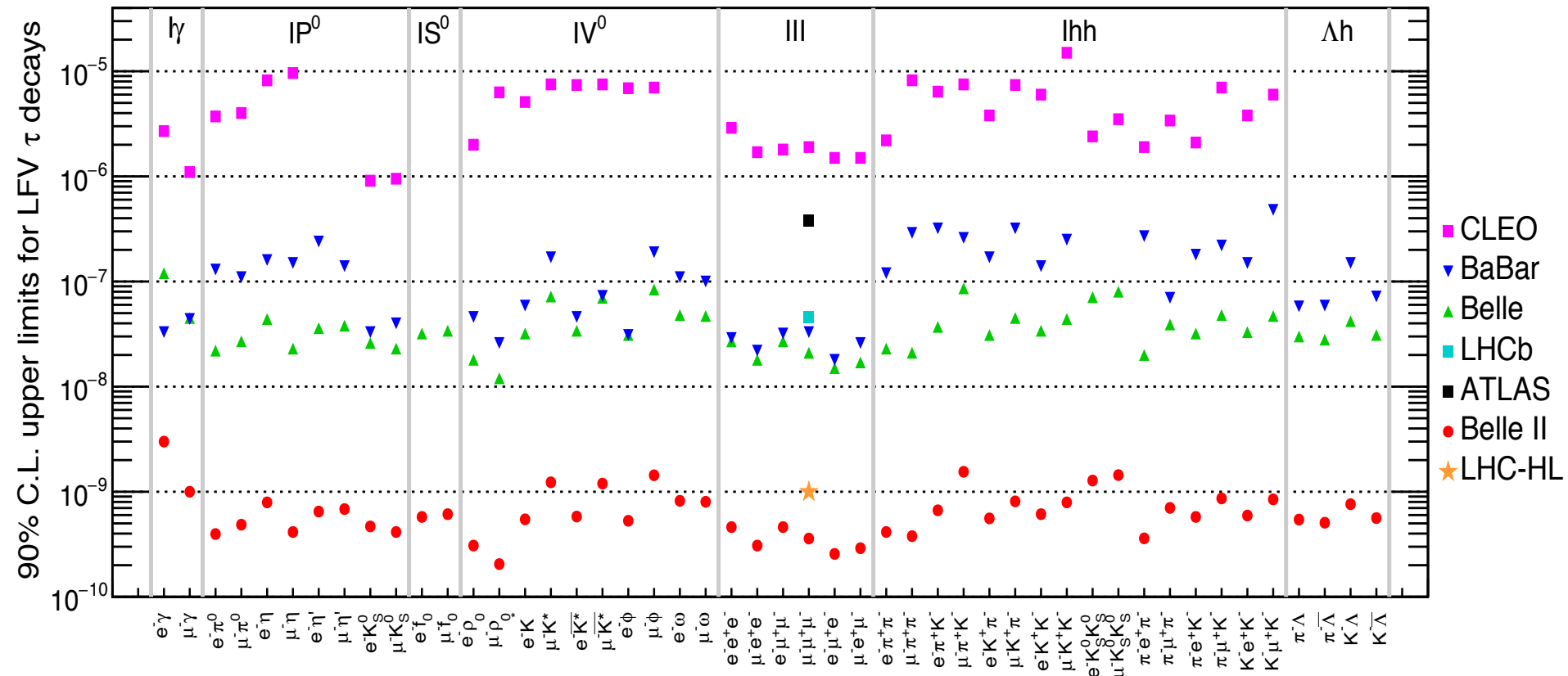
- 48 LFV modes studied at Belle and BaBar

## 2.2 CLFV processes: tau decays

Belle II Physics Book'18

HL-LHC&HE-LHC'18

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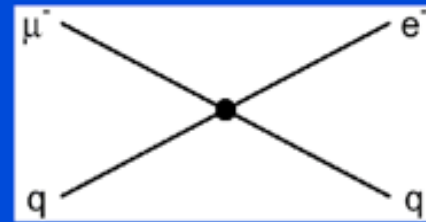
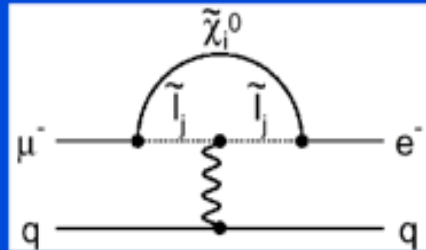


- Expected sensitivity  $10^{-9}$  or better at *LHCb*, *Belle II*, *HL-LHC*?

# A multitude of models...

## Supersymmetry

Predictions at  $10^{-15}$

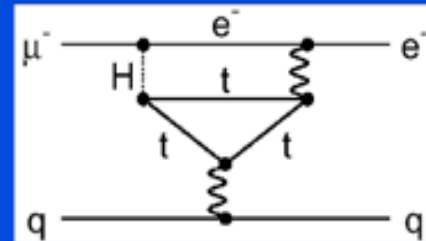
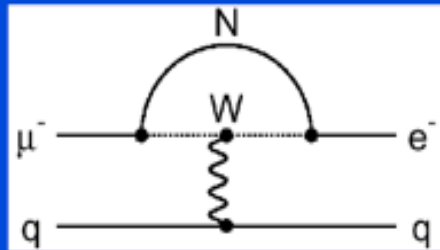


## Compositeness

$$\Lambda_c = 3000 \text{ TeV}$$

## Heavy Neutrinos

$$|U_{\mu N}^* U_{eN}|^2 = 8 \times 10^{-13}$$

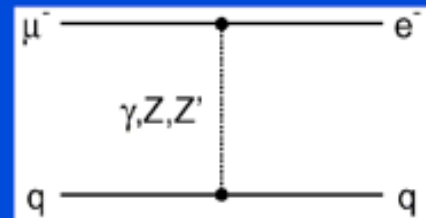
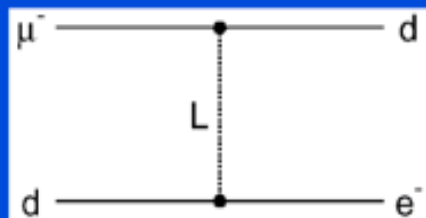


## Second Higgs doublet

$$g_{H_{\mu e}} = 10^{-4} \times g_{H_{\mu\mu}}$$

## Leptoquarks

$$M_L = 3000 \sqrt{\lambda_{\mu d} \lambda_{e d}} \text{ TeV}/c^2$$



## Heavy $Z'$ , Anomalous $Z$ coupling

$$M_{Z'} = 3000 \text{ TeV}/c^2$$

$$B(Z \rightarrow \mu e) < 10^{-17}$$

After W. Marciano

## 2.3 Effective Field Theory approach

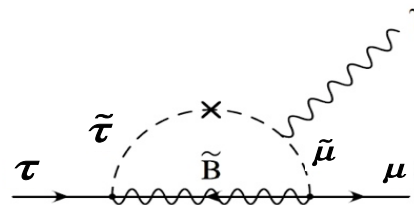
$$\mathcal{L} = \mathcal{L}_{SM} + \frac{C^{(5)}}{\Lambda} \mathcal{O}^{(5)} + \sum_i \frac{C_i^{(6)}}{\Lambda^2} \mathcal{O}_i^{(6)} + \dots$$

- Build all  $D > 5$  LFV operators:

➤ Dipole:

$$\mathcal{L}_{eff}^D \supset -\frac{C_D}{\Lambda^2} m_\tau \bar{\mu} \sigma^{\mu\nu} P_{L,R} \tau F_{\mu\nu}$$

e.g.



See e.g.

*Black, Han, He, Sher'02*

*Brignole & Rossi'04*

*Dassinger, Feldmann, Mannel, Turczyk'07*

*Matsuzaki & Sanda'08*

*Giffels et al.'08*

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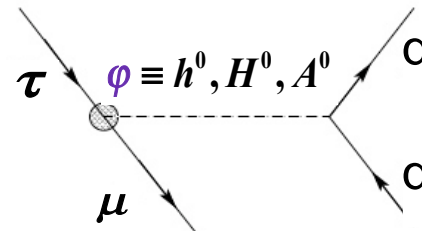
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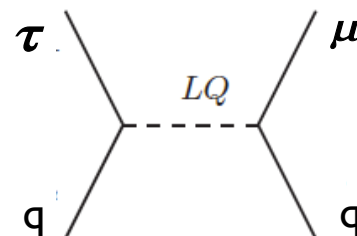
- Lepton-quark (Scalar, Pseudo-scalar, Vector, Axial-vector):

$$\mathcal{L}_{eff}^{S,V} \supset -\frac{C_{S,V}}{\Lambda^2} m_\tau m_q G_F \bar{\mu} \Gamma P_{L,R} \tau \bar{q} \Gamma q$$

e.g.



$$\Gamma \equiv 1$$



$$\Gamma \equiv \gamma^\mu$$



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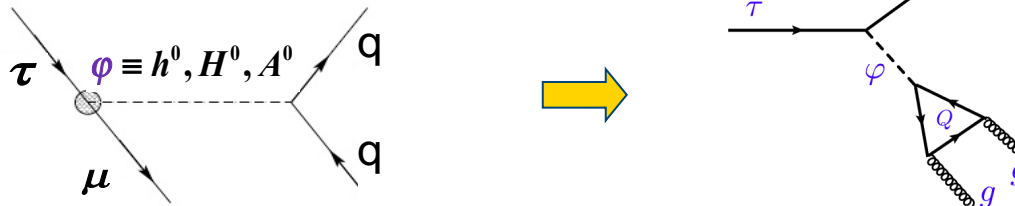
- Lepton-quark (Scalar, Pseudo-scalar, Vector, Axial-vector):

$$\mathcal{L}_{eff}^S \supset -\frac{C_{S,V}}{\Lambda^2} m_\tau m_q G_F \bar{\mu} \Gamma P_{L,R} \tau \bar{q} \Gamma q$$

- Integrating out heavy quarks generates *gluonic operator*

$$\frac{1}{\Lambda^2} \bar{\mu} P_{L,R} \tau Q \bar{Q} \rightarrow \mathcal{L}_{eff}^G \supset -\frac{C_G}{\Lambda^2} m_\tau G_F \bar{\mu} P_{L,R} \tau G_{\mu\nu}^a G_a^{\mu\nu}$$

Importance of this operator emphasized in *Petrov & Zhuridov'14*



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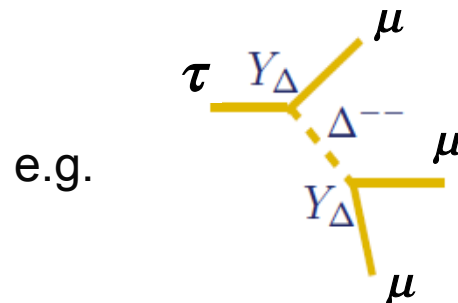
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- 4 leptons (Scalar, Pseudo-scalar, Vector, Axial-vector):

$$\mathcal{L}_{eff}^{4\ell} \supset -\frac{C_{S,V}^{4\ell}}{\Lambda^2} \bar{\mu} \Gamma P_{L,R} \tau \bar{\mu} \Gamma P_{L,R} \mu$$

$$\Gamma \equiv 1, \gamma^\mu$$



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- Lepton-gluon (Scalar, Pseudo-scalar):

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$$\Gamma \equiv 1, \gamma^\mu$$

- Each UV model generates a *specific pattern* of them

## 2.4 Model discriminating power of muon processes

- Summary table:

Cirigliano@Beauty2014

	$\mu \rightarrow 3e$	$\mu \rightarrow e\gamma$	$\mu \rightarrow e$ conversion
$O_{S,V}^{4\ell}$	✓	—	—
$O_D$	✓	✓	✓
$O_V^q$	—	—	✓
$O_S^q$	—	—	✓

- The notion of “*best probe*” (process with largest decay rate) is *model dependent*
- If observed, compare rate of processes  
➡ key handle on *relative strength* between operators and hence on the *underlying mechanism*

## 2.4 Model discriminating power of muon processes

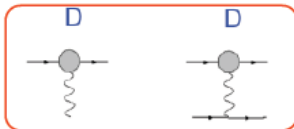
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$O_V^q$	—	—	✓
$O_S^q$	—	—	✓

- $\mu \rightarrow e\gamma$  vs.  $\mu \rightarrow 3e$   $\Rightarrow$  relative strength between *dipole* and *4L* operators

$$\frac{\Gamma_{\mu \rightarrow 3e}}{\Gamma_{\mu \rightarrow e\gamma}} = \frac{\alpha}{4\pi} I_{\text{PS}} \left( 1 + \sum_i \frac{c_i^{(\text{contact})}}{c^{(\text{dipole})}} \right)$$



$6 \times 10^{-3}$



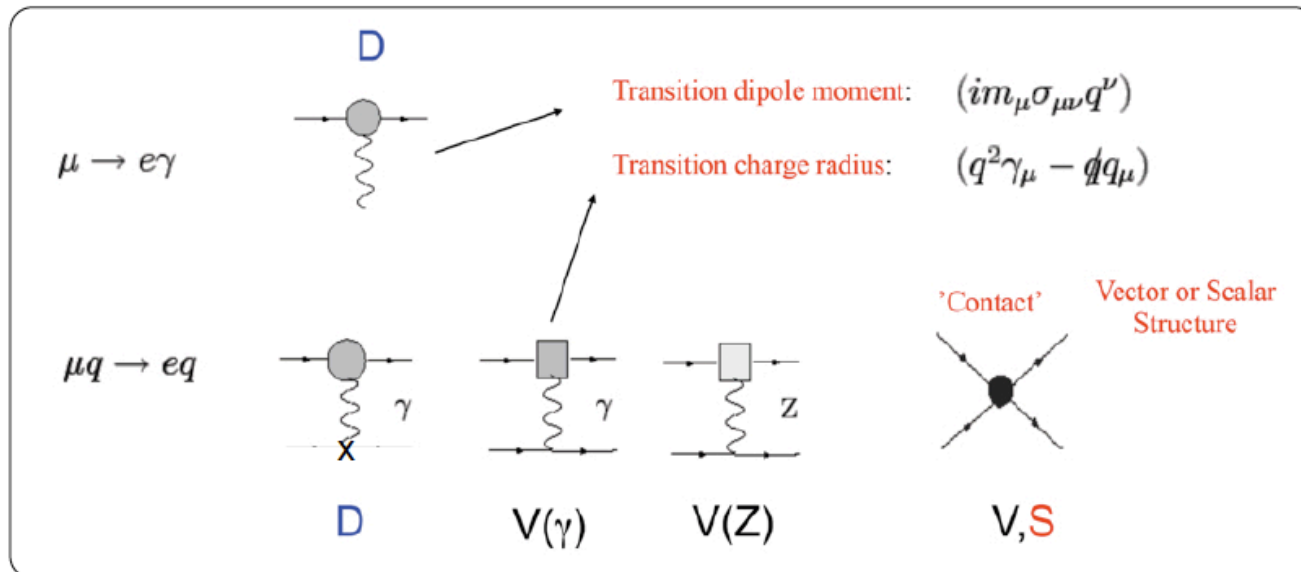
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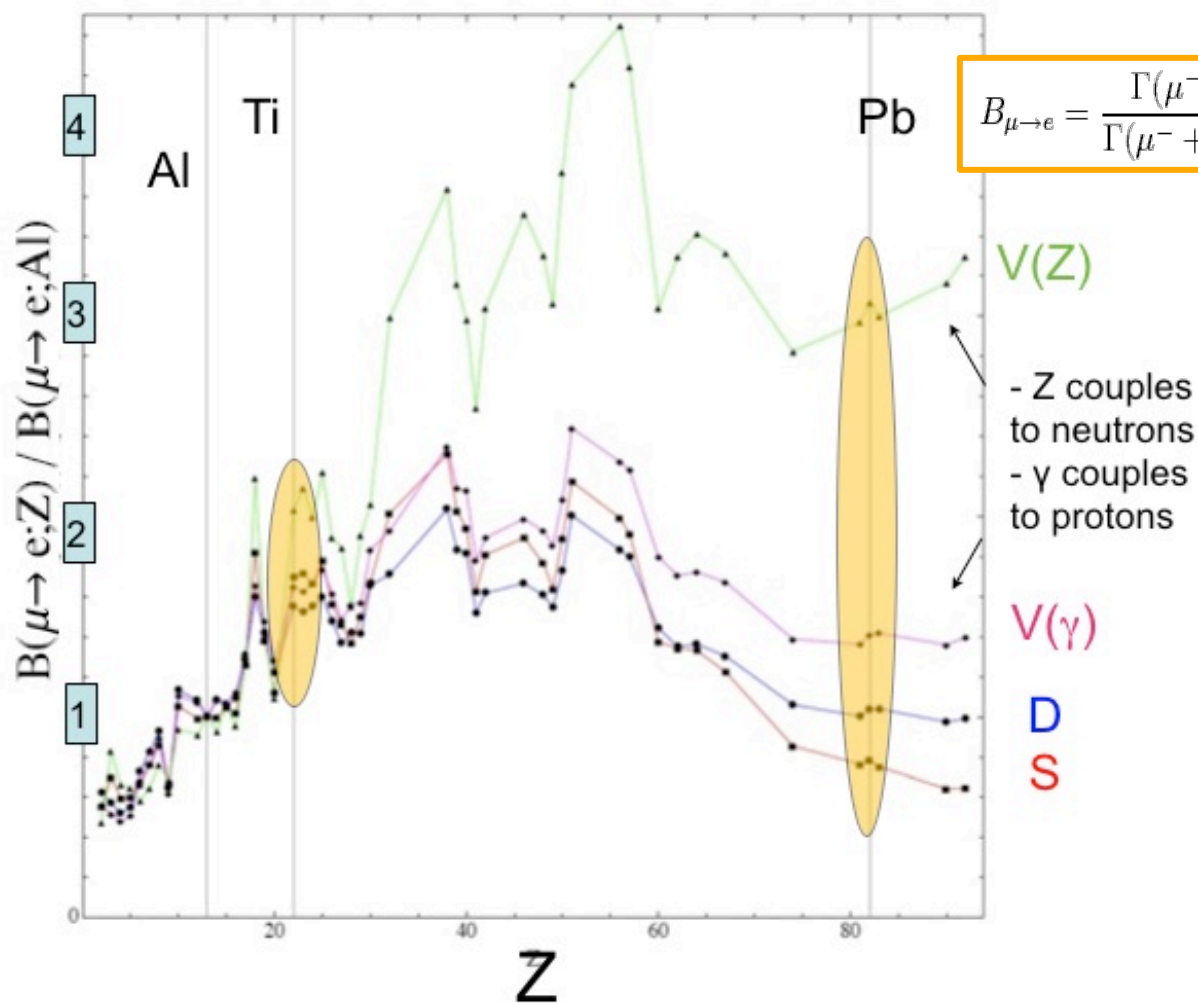
- $\mu \rightarrow e\gamma$  vs.  $\mu \rightarrow e$  conversion  $\Rightarrow$  relative strength between *dipole* and *quark* operators



# BR for $\mu \rightarrow e$ conversion

- For  $\mu \rightarrow e$  conversion, target dependence of the amplitude is different for V,D or S models

*Cirigliano, Kitano, Okada, Tuzon'09*



$$B_{\mu \rightarrow e} = \frac{\Gamma(\mu^- + (Z, A) \rightarrow e^- + (Z, A))}{\Gamma(\mu^- + (Z, A) \rightarrow \nu_\mu + (Z-1, A))}$$

## 2.5 Model discriminating power of Tau processes

- Summary table:

*Celis, Cirigliano, E.P.'14*

	$\tau \rightarrow 3\mu$	$\tau \rightarrow \mu\gamma$	$\tau \rightarrow \mu\pi^+\pi^-$	$\tau \rightarrow \mu K\bar{K}$	$\tau \rightarrow \mu\pi$	$\tau \rightarrow \mu\eta^{(\prime)}$
$O_{S,V}^{4\ell}$	✓	—	—	—	—	—
$O_D$	✓	✓	✓	✓	—	—
$O_V^q$	—	—	✓ (I=1)	✓ (I=0,1)	—	—
$O_S^q$	—	—	✓ (I=0)	✓ (I=0,1)	—	—
$O_{GG}$	—	—	✓	✓	—	—
$O_A^q$	—	—	—	—	✓ (I=1)	✓ (I=0)
$O_P^q$	—	—	—	—	✓ (I=1)	✓ (I=0)
$O_{G\tilde{G}}$	—	—	—	—	—	✓

- In addition to leptonic and radiative decays, *hadronic decays* are very important → sensitive to large number of operators!
- But need reliable determinations of the hadronic part:  
*form factors* and *decay constants* (e.g.  $f_\eta, f_{\eta'}$ )



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$O_{S,V}^{4\ell}$	✓	—	—	—	—	—
$O_D$	✓	✓	✓	✓	—	—
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$O_S^q$	—	—	✓ (I=0)	✓ (I=0,1)	—	—
$O_{GG}$	—	—	✓	✓	—	—
$O_A^q$	—	—	—	—	✓ (I=1)	✓ (I=0)
$O_P^q$	—	—	—	—	✓ (I=1)	✓ (I=0)
$O_{G\tilde{G}}$	—	—	—	—	—	✓

- Form factors for  $\tau \rightarrow \mu(e)\pi\pi$  determined using *dispersive techniques*

- Hadronic part:

*Donoghue, Gasser, Leutwyler'90*

*Moussallam'99*

*Daub et al'13*

*Celis, Cirigliano, E.P.'14*

$$H_\mu = \langle \pi\pi | (V_\mu - A_\mu) e^{iL_{QCD}} | 0 \rangle = (\text{Lorentz struct.})_\mu^i F_i(s)$$

with

$$s = (p_{\pi^+} + p_{\pi^-})^2$$

- 2-channel unitarity condition is solved with  
I=0 S-wave  $\pi\pi$  and  $KK$  scattering data as input

$$n = \pi\pi, K\bar{K}$$

$$\text{Im}F_n(s) = \sum_{m=1}^2 T_{nm}^*(s) \sigma_m(s) F_m(s)$$

## 2.5 Model discriminating power of Tau processes

*Celis, Cirigliano, E.P.'14*

- Two handles:

➤ Branching ratios:  $R_{F,M} \equiv \frac{\Gamma(\tau \rightarrow F)}{\Gamma(\tau \rightarrow F_M)}$  with  $F_M$  dominant LFV mode for model M

- Spectra for > 2 bodies in the final state:

$$\frac{dBR(\tau \rightarrow \mu\pi^+\pi^-)}{d\sqrt{s}} \quad \text{and} \quad dR_{\pi^+\pi^-} \equiv \frac{1}{\Gamma(\tau \rightarrow \mu\gamma)} \frac{d\Gamma(\tau \rightarrow \mu\pi^+\pi^-)}{d\sqrt{s}}$$

## 2.6 Model discriminating of BRs

- Studies in specific models

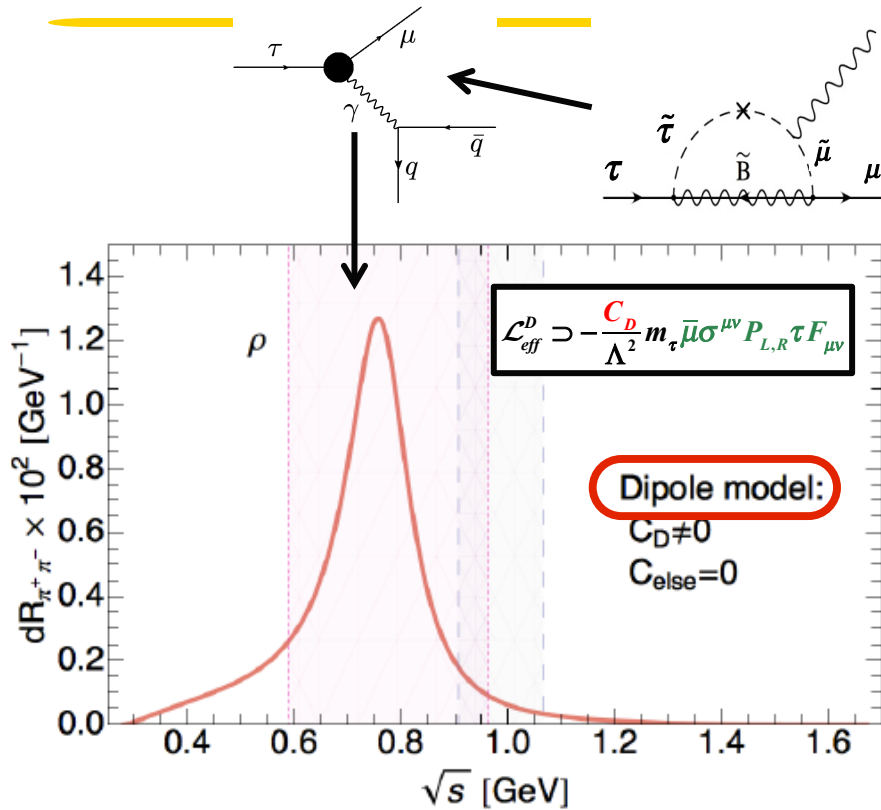
*Buras et al.'10*

ratio	LHT	MSSM (dipole)	MSSM (Higgs)	SM4
$\frac{\text{Br}(\mu^- \rightarrow e^- e^+ e^-)}{\text{Br}(\mu \rightarrow e \gamma)}$	0.02...1	$\sim 6 \cdot 10^{-3}$	$\sim 6 \cdot 10^{-3}$	0.06...2.2
$\frac{\text{Br}(\tau^- \rightarrow e^- e^+ e^-)}{\text{Br}(\tau \rightarrow e \gamma)}$	0.04...0.4	$\sim 1 \cdot 10^{-2}$	$\sim 1 \cdot 10^{-2}$	0.07...2.2
$\frac{\text{Br}(\tau^- \rightarrow \mu^- \mu^+ \mu^-)}{\text{Br}(\tau \rightarrow \mu \gamma)}$	0.04...0.4	$\sim 2 \cdot 10^{-3}$	0.06...0.1	0.06...2.2
$\frac{\text{Br}(\tau^- \rightarrow e^- \mu^+ \mu^-)}{\text{Br}(\tau \rightarrow e \gamma)}$	0.04...0.3	$\sim 2 \cdot 10^{-3}$	0.02...0.04	0.03...1.3
$\frac{\text{Br}(\tau^- \rightarrow \mu^- e^+ e^-)}{\text{Br}(\tau \rightarrow \mu \gamma)}$	0.04...0.3	$\sim 1 \cdot 10^{-2}$	$\sim 1 \cdot 10^{-2}$	0.04...1.4
$\frac{\text{Br}(\tau^- \rightarrow e^- e^+ e^-)}{\text{Br}(\tau^- \rightarrow e^- \mu^+ \mu^-)}$	0.8...2	$\sim 5$	0.3...0.5	1.5...2.3
$\frac{\text{Br}(\tau^- \rightarrow \mu^- \mu^+ \mu^-)}{\text{Br}(\tau^- \rightarrow \mu^- e^+ e^-)}$	0.7...1.6	$\sim 0.2$	5...10	1.4...1.7
$\frac{\text{R}(\mu \text{Ti} \rightarrow e \text{Ti})}{\text{Br}(\mu \rightarrow e \gamma)}$	$10^{-3} \dots 10^2$	$\sim 5 \cdot 10^{-3}$	0.08...0.15	$10^{-12} \dots 26$

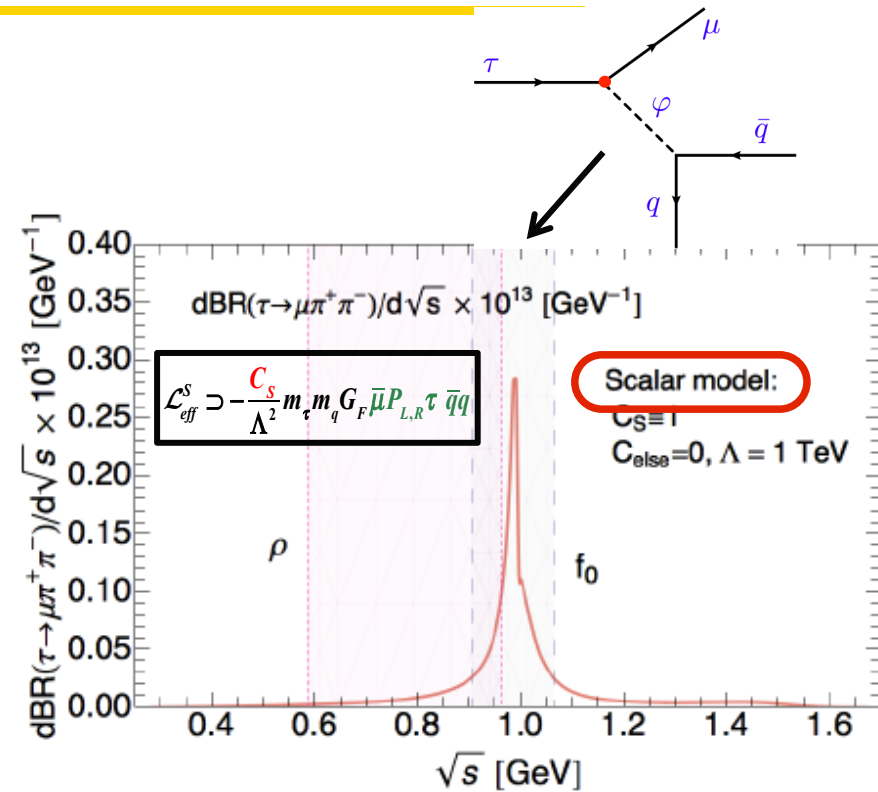
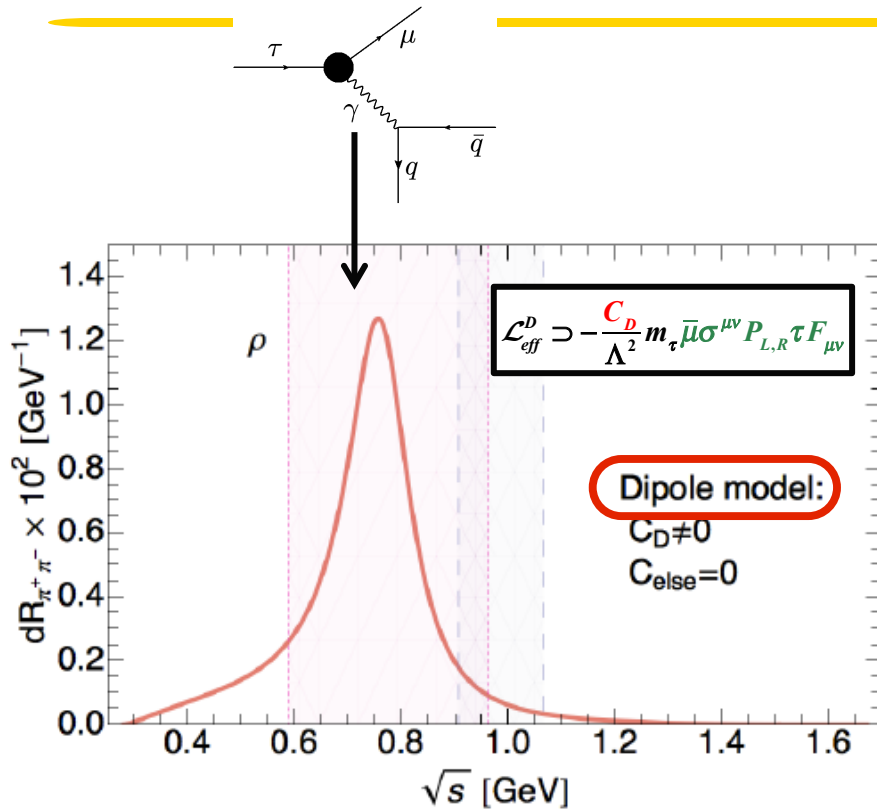
 Disentangle the *underlying dynamics* of NP

## 2.7 Discriminating power of $\tau \rightarrow \mu(e)\pi\pi$ decays

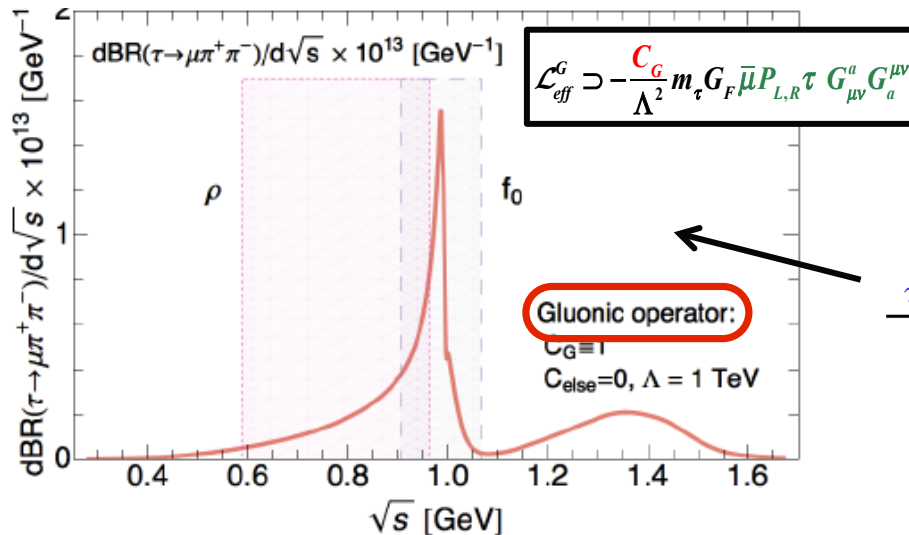
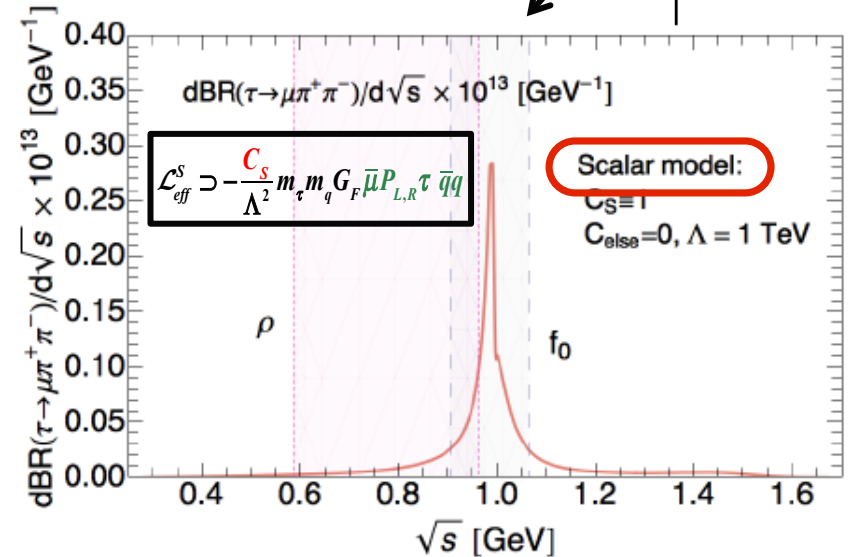
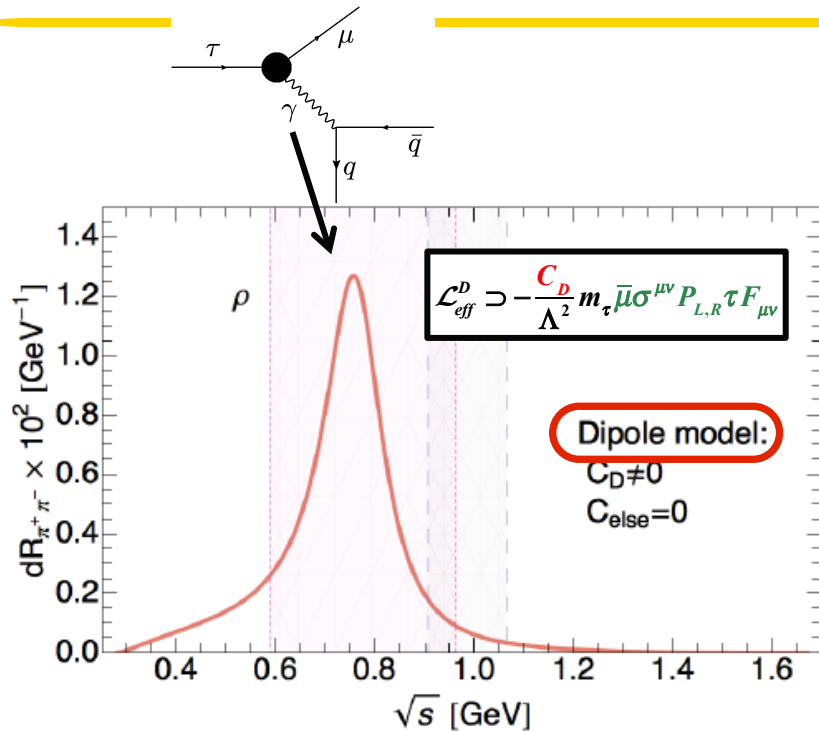
*Celis, Cirigliano, E.P.'14*



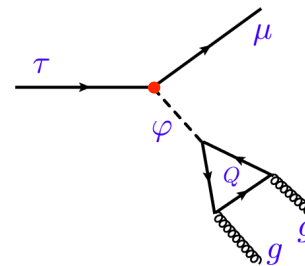
## 2.7 Discriminating power of $\tau \rightarrow \mu(e)\pi\pi$ decays



## 2.7 Discriminating power of $\tau \rightarrow \mu(e)\pi\pi$ decays



Different distributions according to the **operator!**



### 3. Ex: Charged Lepton-Flavour Violation and Higgs Physics

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### 3.1 Non standard LFV Higgs coupling

- $$\Delta\mathcal{L}_Y = -\frac{\lambda_{ij}}{\Lambda^2} (\bar{f}_L^i f_R^j H) H^\dagger H \quad \Rightarrow \quad -Y_{ij} (\bar{f}_L^i f_R^j) h$$

In the SM:  $Y_{ij}^{h_{SM}} = \frac{m_i}{v} \delta_{ij}$

Goudelis, Lebedev, Park'11  
 Davidson, Grenier'10  
 Harnik, Kopp, Zupan'12  
 Blankenburg, Ellis, Isidori'12  
 McKeen, Pospelov, Ritz'12  
 Arhrib, Cheng, Kong'12

$$\mathcal{L}_Y = -m_i \bar{f}_L^i f_R^i - h \left( Y_{e\mu} \bar{e}_L \mu_R + Y_{e\tau} \bar{e}_L \tau_R + Y_{\mu\tau} \bar{\mu}_L \tau_R \right) + \dots$$

- Arise in several models *Cheng, Sher'97, Goudelis, Lebedev, Park'11*  
*Davidson, Grenier'10*

*Cheng, Sher'97*

- Order of magnitude expected  $\Rightarrow$  No tuning:  $|Y_{\tau\mu} Y_{\mu\tau}| \lesssim \frac{m_\mu m_\tau}{v^2}$

- In concrete models, in general further parametrically suppressed



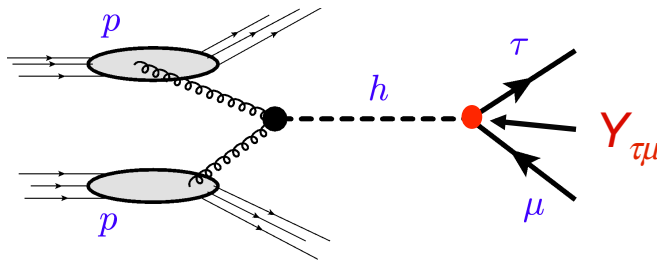
# 3.1 Non standard LFV Higgs coupling

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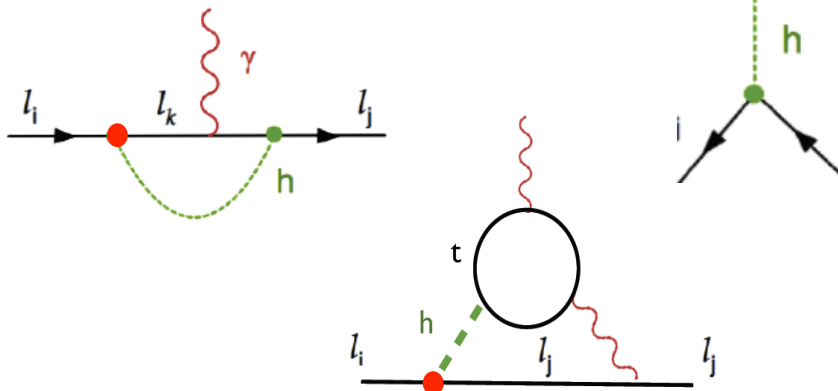
- High energy : LHC

In the SM:  $Y_{ij}^{h_{SM}} = \frac{m_i}{v} \delta_{ij}$



Hadronic part treated with perturbative QCD

- Low energy : D, S operators



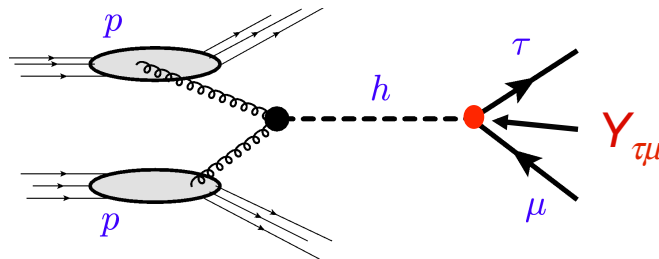
# 3.1 Non standard LFV Higgs coupling

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- High energy : LHC

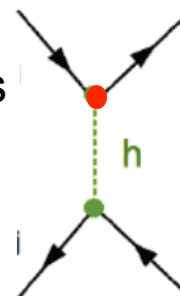
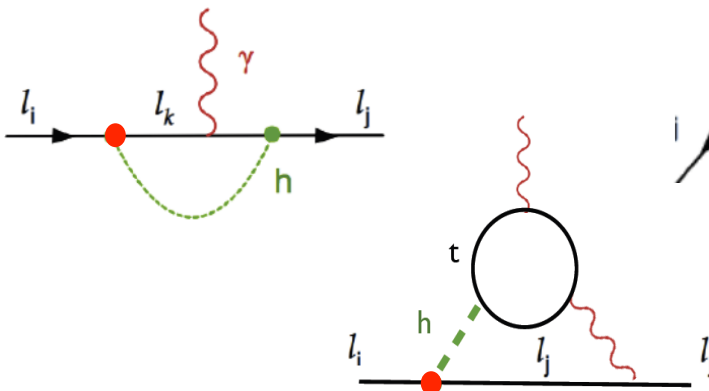
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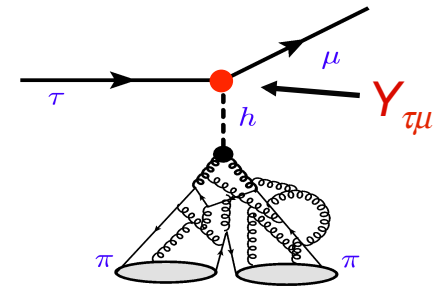
Hadronic part treated with perturbative QCD

Reverse the process

- Low energy : D, S, G operators



+

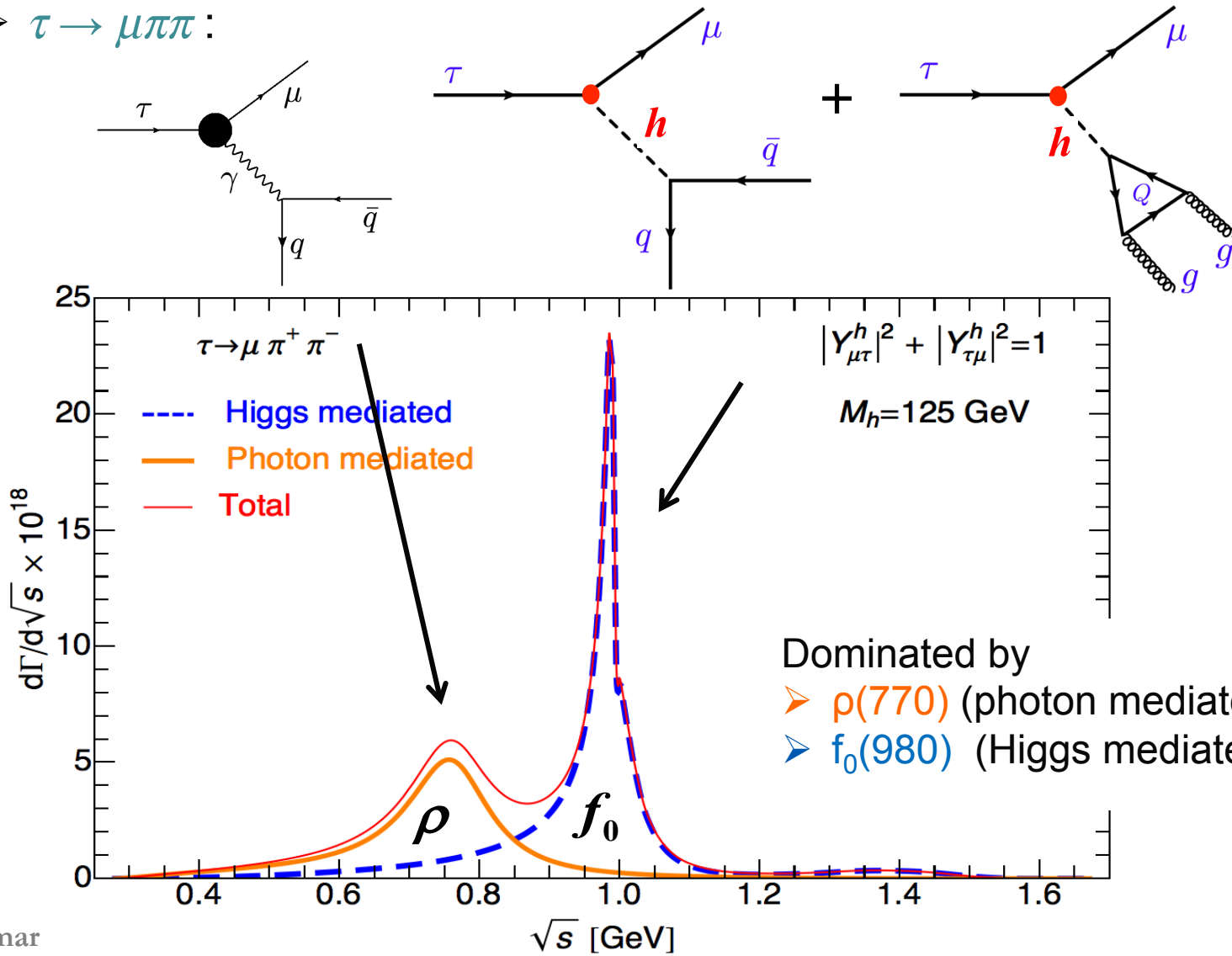


Hadronic part treated with non-perturbative QCD

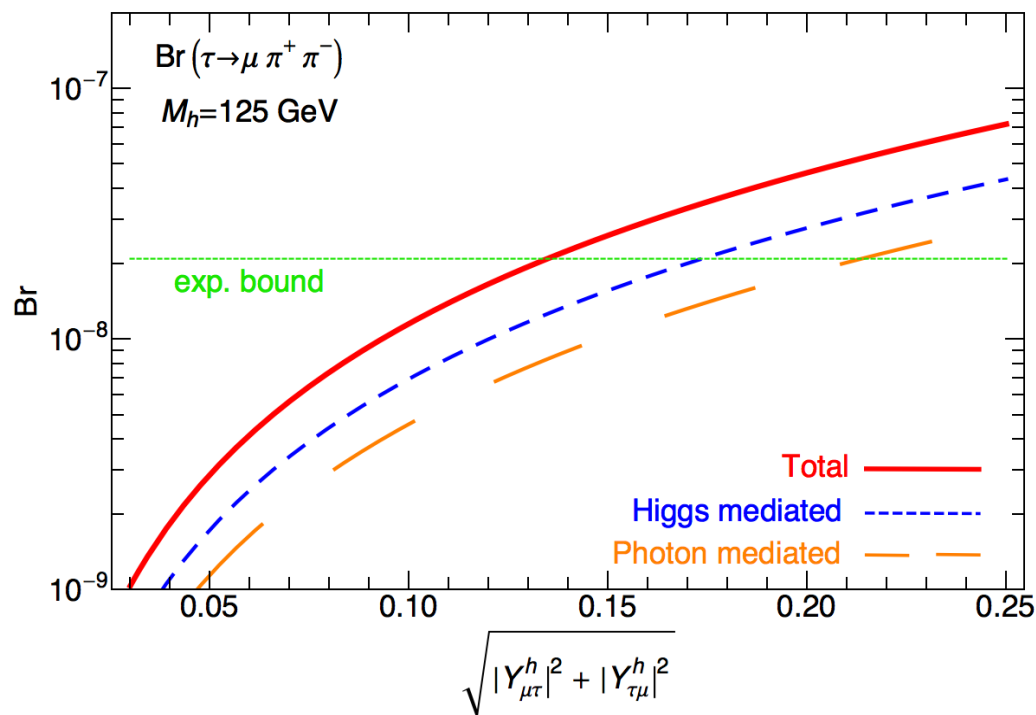
## 3.2 Constraints in the $\tau\mu$ sector

- At low energy

➤  $\tau \rightarrow \mu \pi \pi$ :



## 3.2 Constraints in the $\tau\mu$ sector



Bound:

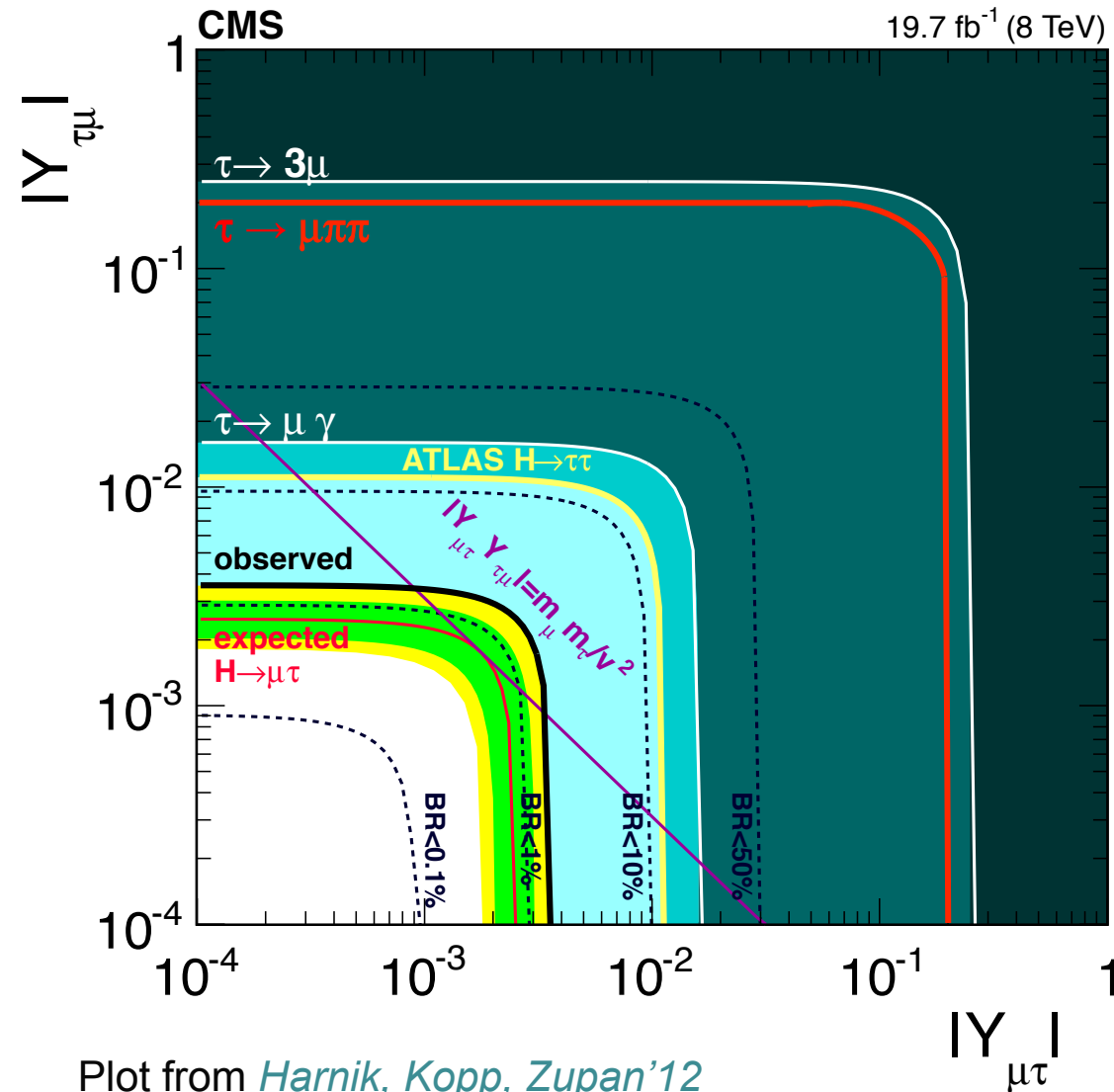
$$\sqrt{|Y_{\mu\tau}^h|^2 + |Y_{\tau\mu}^h|^2} \leq 0.13$$

Process	(BR $\times 10^8$ ) 90% CL	$\sqrt{ Y_{\mu\tau}^h ^2 +  Y_{\tau\mu}^h ^2}$	Operator(s)
$\tau \rightarrow \mu \gamma$	< 4.4 [88]	< 0.016	Dipole
$\tau \rightarrow \mu \mu \mu$	< 2.1 [89]	< 0.24	Dipole
$\tau \rightarrow \mu \pi^+ \pi^-$	< 2.1 [86]	< 0.13	Scalar, Gluon, Dipole
$\tau \rightarrow \mu \rho$	< 1.2 [85]	< 0.13	Scalar, Gluon, Dipole
$\tau \rightarrow \mu \pi^0 \pi^0$	< $1.4 \times 10^3$ [87]	< 6.3	Scalar, Gluon

Less stringent  
but more robust  
handle on LFV  
Higgs couplings

?

## 3.2 Constraints in the $\tau\mu$ sector



- Constraints from LE:
  - $\tau \rightarrow \mu\gamma$ : best constraints but loop level
    - sensitive to UV completion of the theory
  - $\tau \rightarrow \mu\pi\pi$ : tree level diagrams
    - robust handle on LFV
- Constraints from HE:
  - LHC** wins for  $\tau\mu$ !
- Opposite situation for  $\mu e$ !
- For LFV Higgs and nothing else: LHC bound



$$BR(\tau \rightarrow \mu\gamma) < 2.2 \times 10^{-9}$$

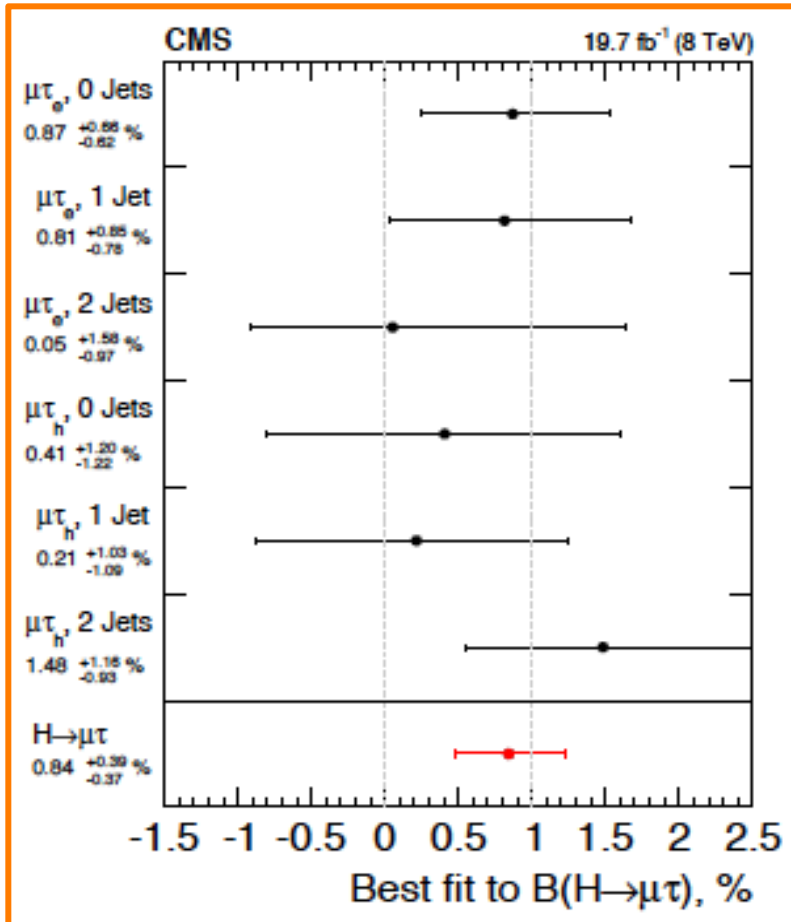
$$BR(\tau \rightarrow \mu\pi\pi) < 1.5 \times 10^{-11}$$

### 3.3 Hint of New Physics in $h \rightarrow \tau\mu$ ?

$$BR(h \rightarrow \tau\mu) = (0.84^{+0.39}_{-0.37})\%$$

@2.4 $\sigma$

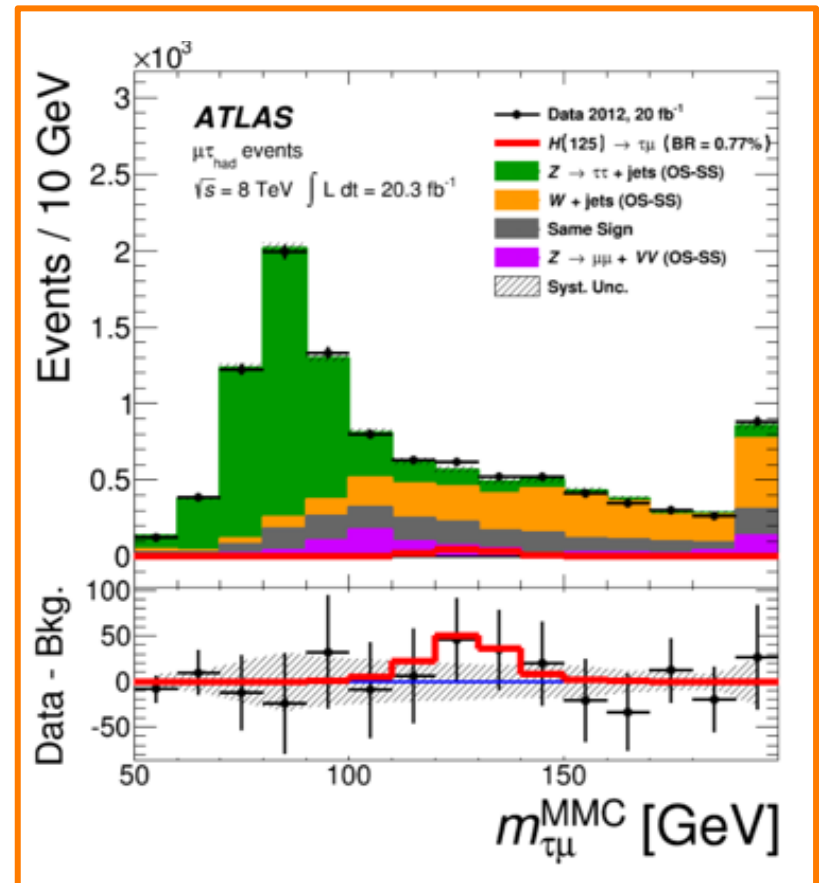
CMS'15

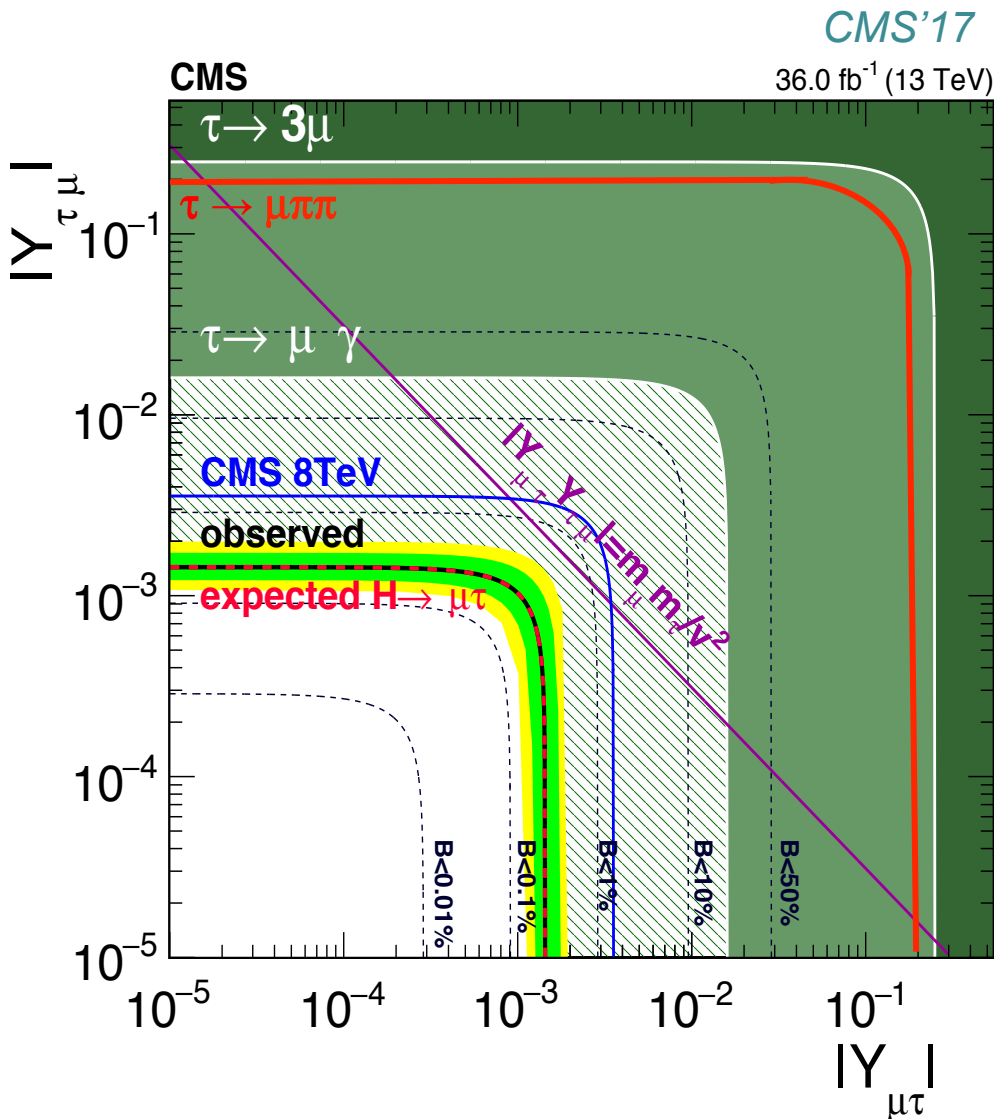


$$BR(h \rightarrow \tau\mu) = (0.53 \pm 0.51)\%$$

@1 $\sigma$

ATLAS'15



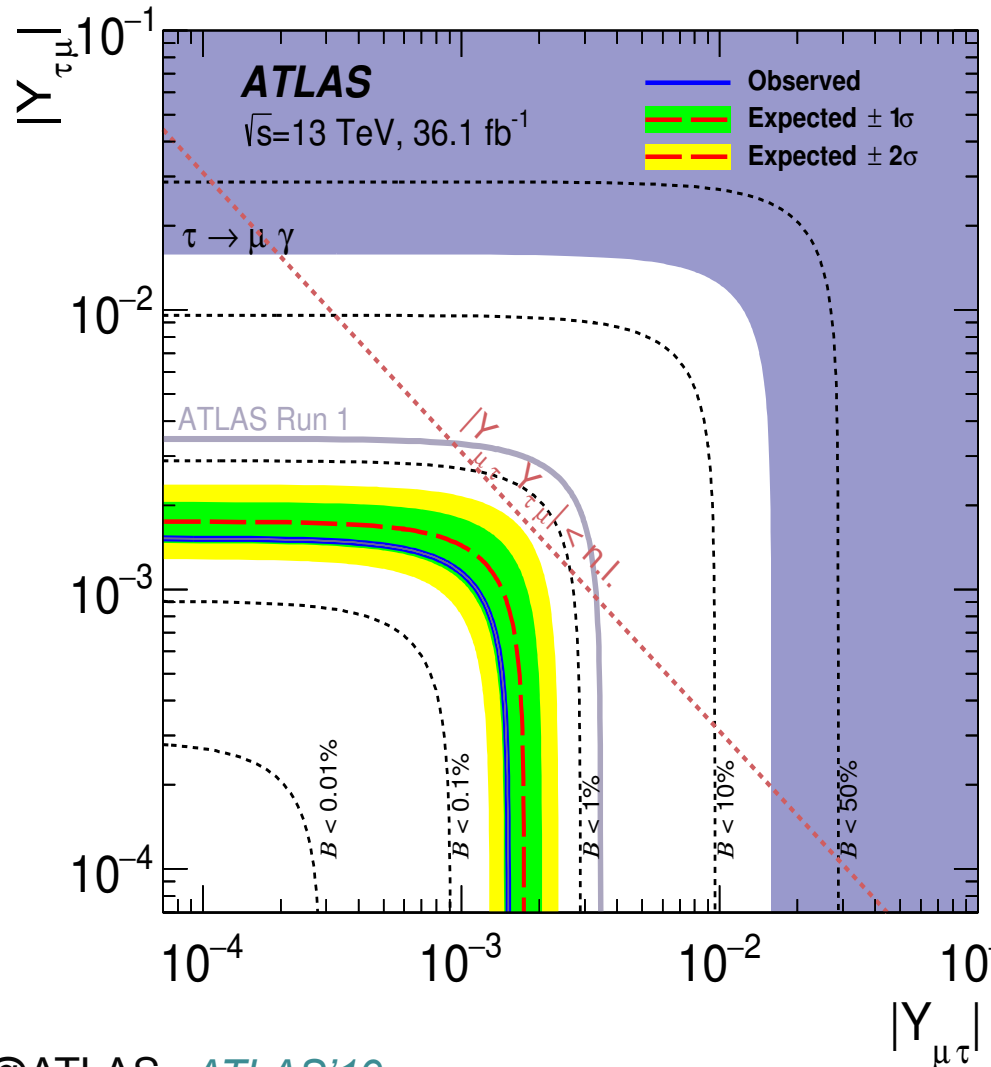
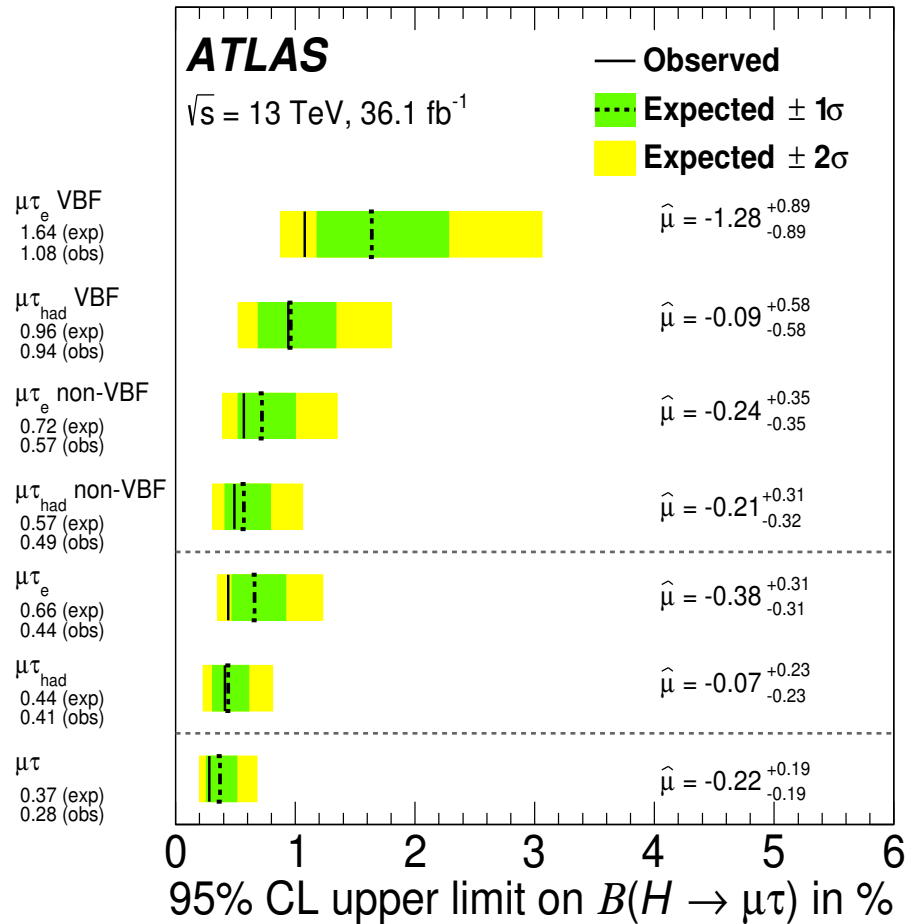


$$BR(h \rightarrow \tau\mu) = (0.25 \pm 0.25)\%$$

CMS'17

### 3.3 Hint of New Physics in $h \rightarrow \tau\mu$ ?

ATLAS'19



$$BR(h \rightarrow \tau\mu) \leq 0.28\%$$

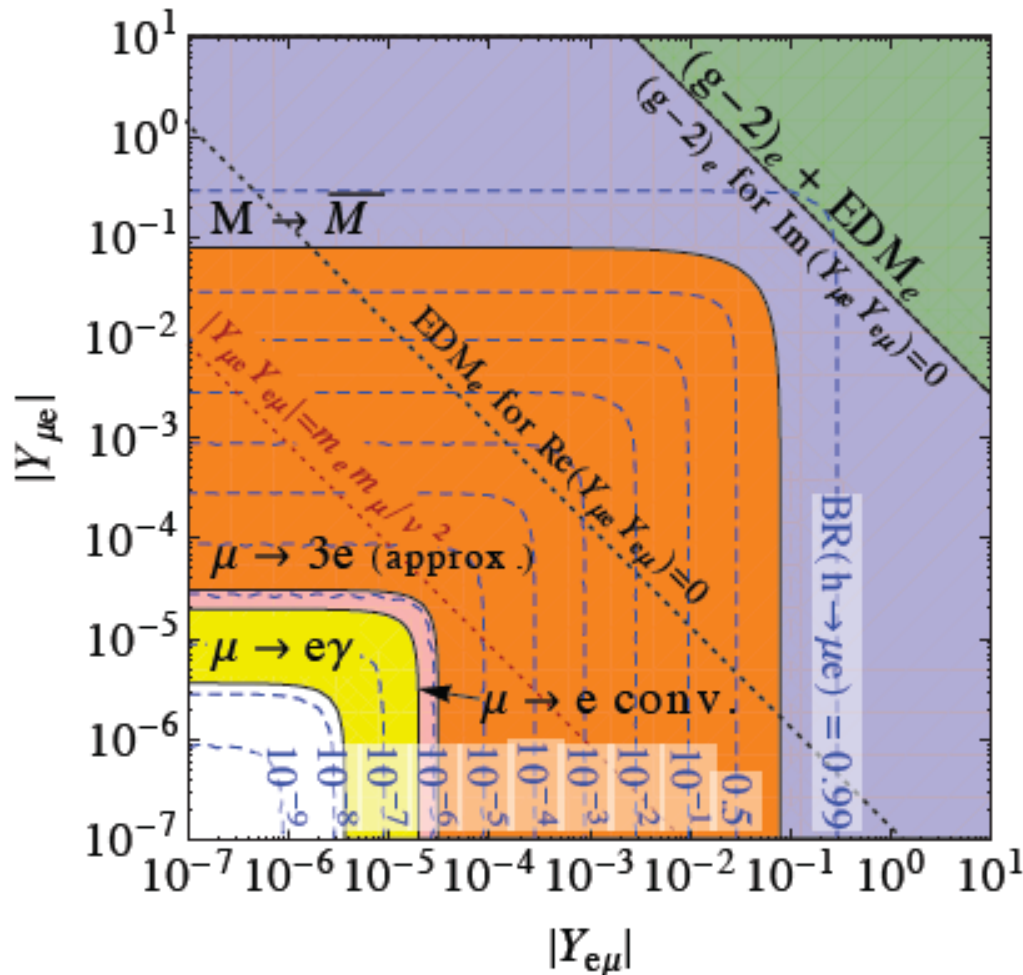
13 TeV@ATLAS ATLAS'19



## 3.4 Constraints in the $\mu e$ sector

- Constraints from Higgs decay (LHC) vs. low energy LFV and LFC observables

*Harnik, Kopp, Zupan'12*



- Best constraints coming from *low energy*:  $\mu \rightarrow e \gamma$

*MEG'13*

$$BR(\mu \rightarrow e \gamma) < 5.7 \cdot 10^{-13}$$





$$BR(h \rightarrow \mu e) < 10^{-7}$$

## 4. Conclusion and Outlook

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# Summary

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- Direct searches for new physics at the TeV-scale at LHC by ATLAS and CMS  energy frontier
- Probing new physics orders of magnitude beyond that scale and helping to decipher possible TeV-scale new physics requires to work hard on the *intensity* and *precision frontiers*
- *Charged leptons* offer an important spectrum of possibilities:
  - LFV measurements have SM-free signal
  - Current experiments and mature proposals promise orders of magnitude sensitivity improvements
  - In addition to leptonic and radiative decays  hadronic decays important, e.g.  $\tau \rightarrow \mu(e)\pi\pi$ ,  $\mu N \rightarrow eN$
  - New physics models usually strongly correlate these sectors

# Summary

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- Direct searches for new physics at the TeV-scale at LHC by ATLAS and CMS  energy frontier
- Probing new physics orders of magnitude beyond that scale and helping to decipher possible TeV-scale new physics requires to work hard on the *intensity* and *precision frontiers*
- *Charged leptons* offer an important spectrum of possibilities:
  - We show how CLFV decays offer an excellent model discriminating tools giving indications on
    - the *mediator* (operator structure)
    - the *source of flavour breaking* (comparison  $\tau\mu$  vs.  $\tau e$  vs.  $\mu e$ )
- Interplay low energy and collider physics: LFV of the Higgs boson
- Several experimental programs:  
*MEG, Mu3e, COMET, Mu2e, Belle II, BESIII, LHCb, LHC-HL*