

Dynamically integrated transport approach for high-energy nuclear collisions at high baryon density

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based on [Phys. Rev. C98, 024909 \(2018\) \[arXiv:1805.09024 \[nucl-th\]\]](#)

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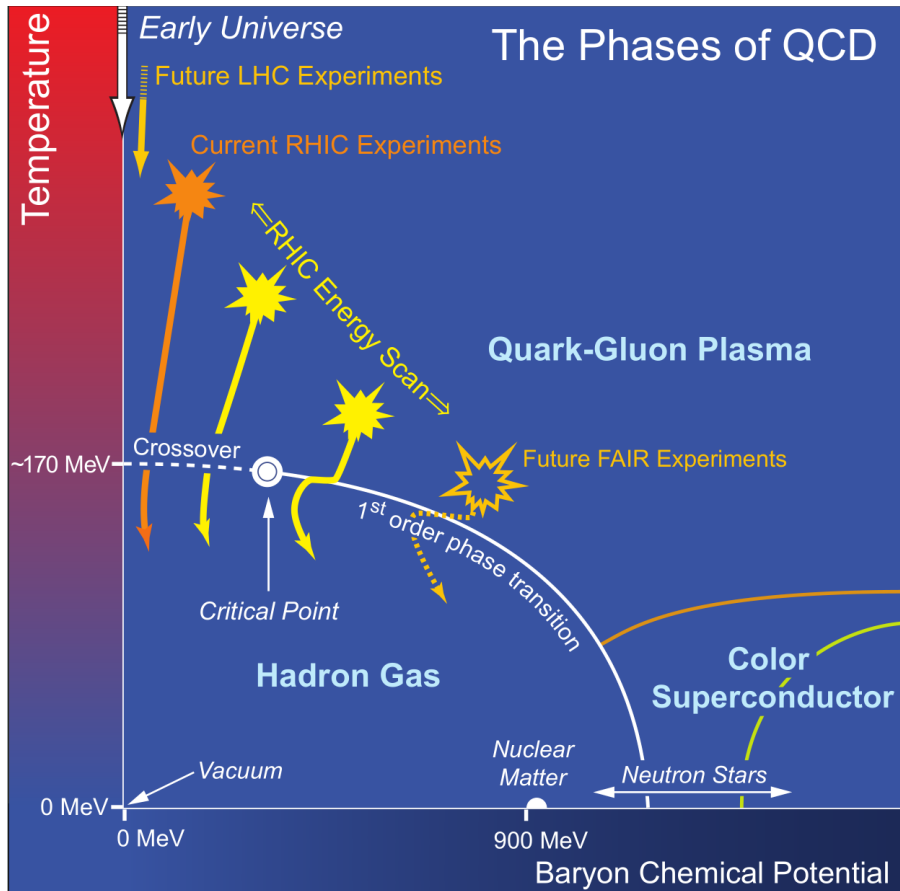
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Introduction

QCD critical point/ 1^{st} -order phase transition search



Beam energy scan for high-energy heavy-ion collisions

Search high-baryon density domain of phase diagram in RHIC, SPS, FAIR, NICA, J-PARC, etc.

Schematic phase diagram of QCD
[taken from the 2007 NSAC Long Range Plan]

MODEL

Dynamical modeling

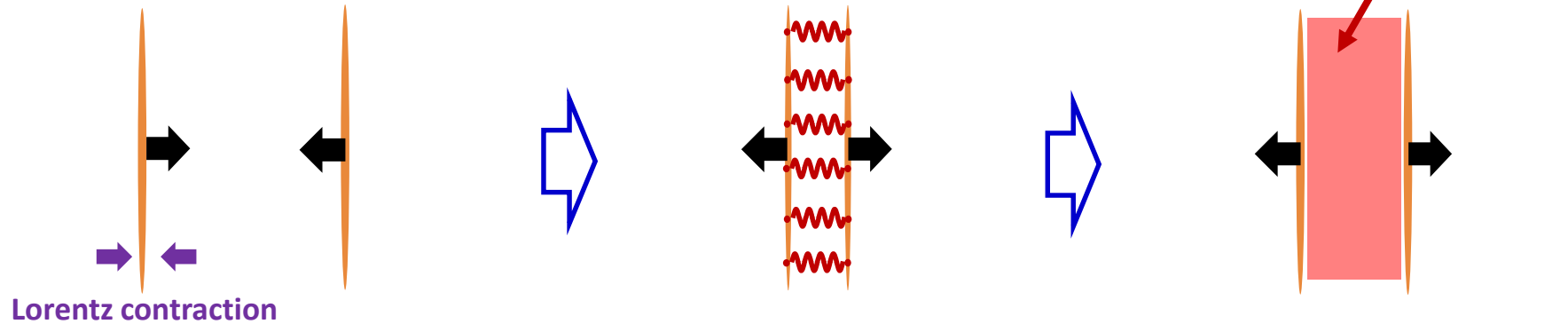
Transport models (such as *hydro model* and *microscopic transport model*)
needed to extract *physical information*
of created matter from *final hadron spectra*

Three important notions in lower energy collisions
(which are closely related to one another)

- **Dynamical initialization:**
hydrodynamics initialized via *source terms*
- **Dynamical core-corona separation:**
thermalized region (*core*) and other part (*corona*)
- **Dynamical integration:**
microscopic transport model and hydro
dynamically coupled to each other

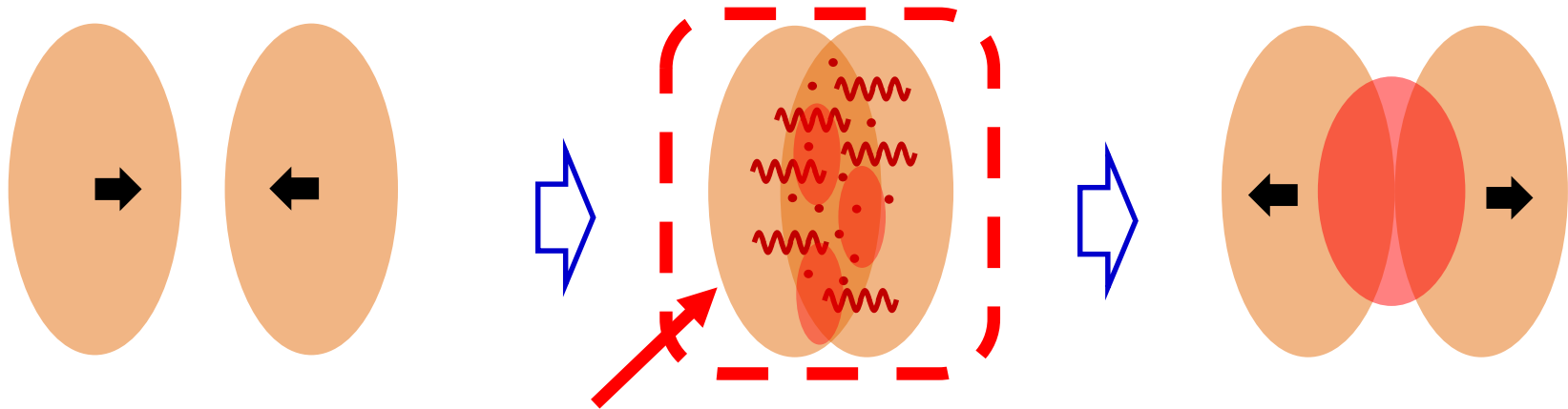
Dynamical initialization

High-energy collisions at RHIC/LHC



Lower-energy collisions

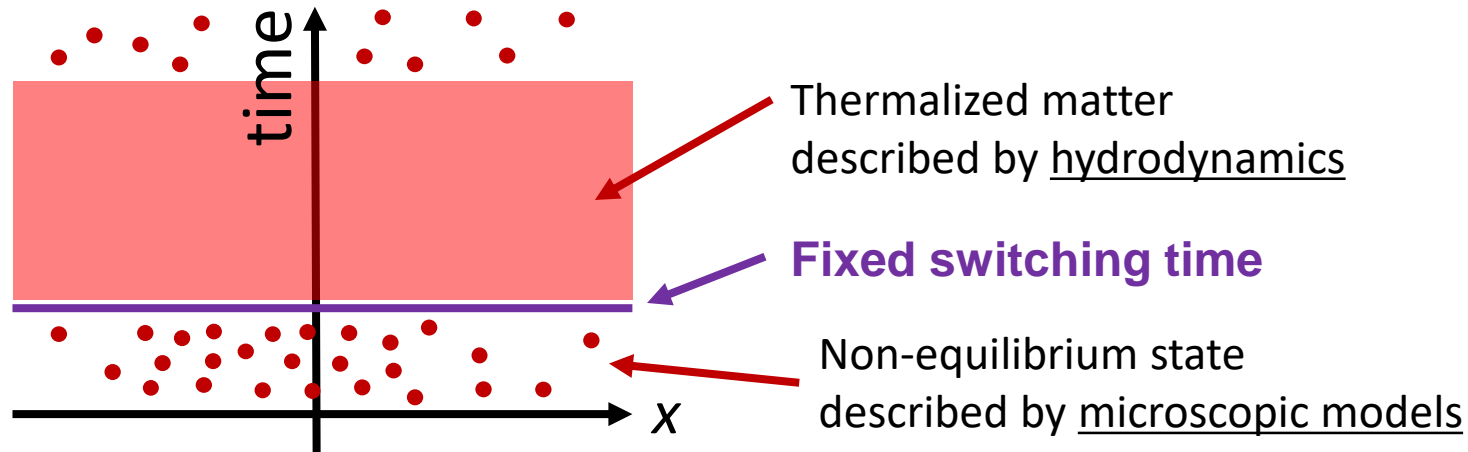
detailed description required



dynamical description of this non-equilibrium process
= Dynamical initialization

Dynamical core-corona separation

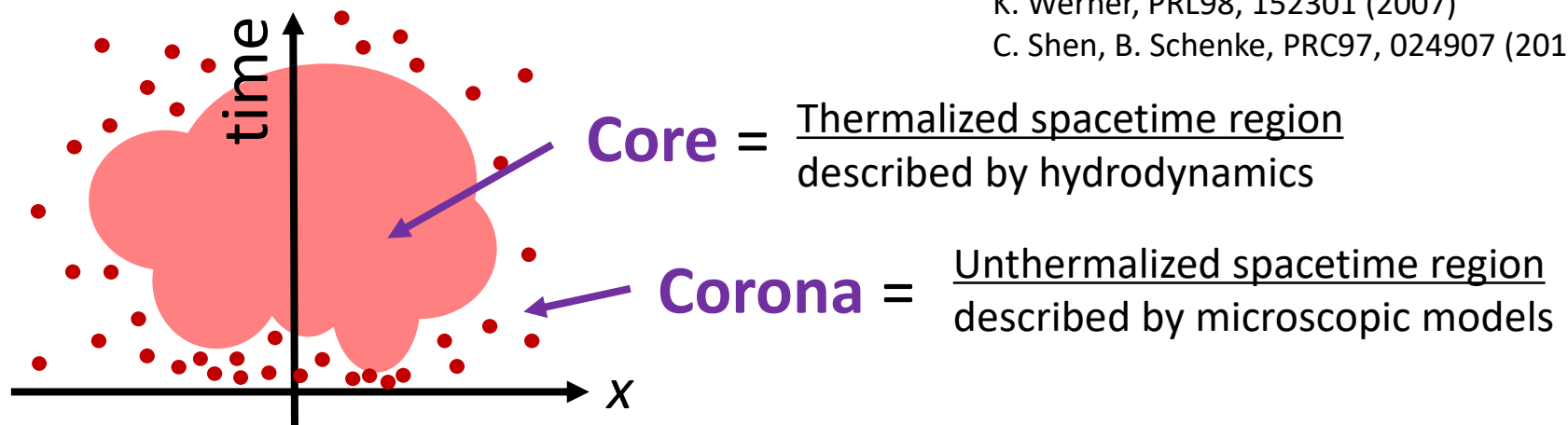
Fixed-time conversion to hydro



Core-corona separation in **space** and **time**

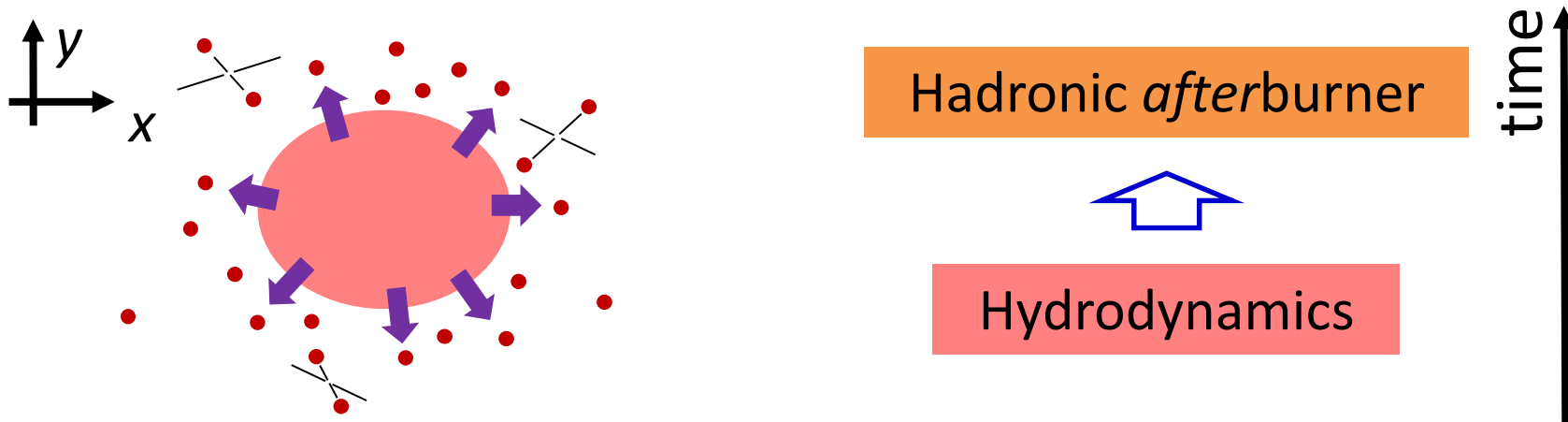
K. Werner, PRL98, 152301 (2007)

C. Shen, B. Schenke, PRC97, 024907 (2018)

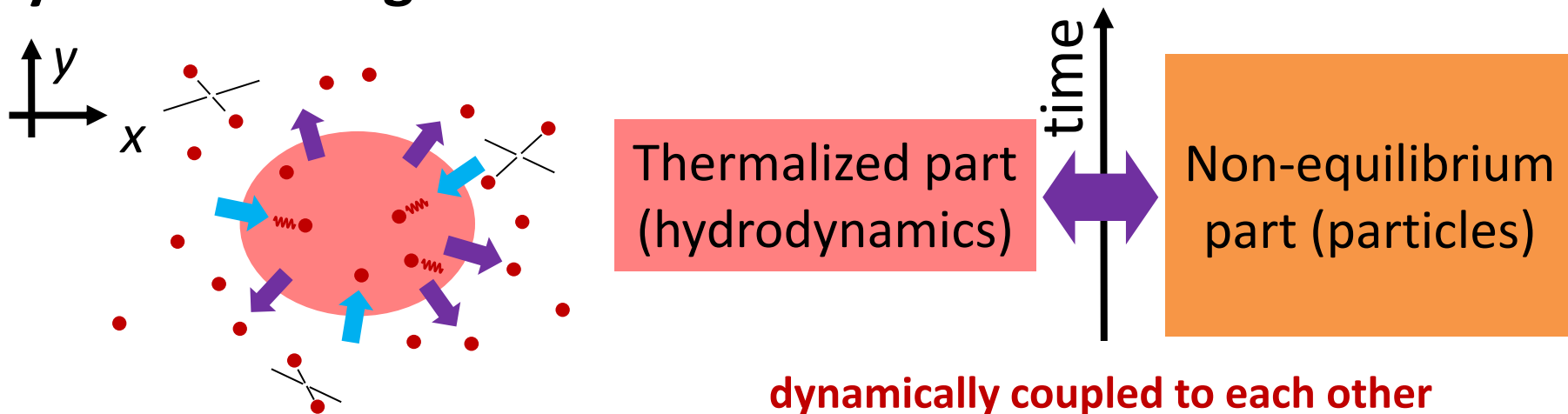


Dynamical integration

Conventional integration of hydro & cascades



Dynamical integration



JAM+hydro model (JAM 1.9)

JAM cascade

Binary collisions of particles

String excitation:
same scheme with HIJING

String fragmentation:
PYTHIA6 Lund model

Resonance decays

Core

$$e > e_f$$



Decay
Fragmentation

$$e_f = 0.5\text{--}1.0 \text{ GeV/fm}^3$$

$$e < e_p$$



Cooper-Frye
formula

$$e_p = 0.5 \text{ GeV/fm}^3$$

Ideal hydrodynamics with source terms

$$\partial_\mu T_f^{\mu\nu} = J^\nu \quad \text{Energy momentum}$$

$$\partial_\mu N_f^\mu = \rho \quad \text{Baryon currents}$$

HLLC scheme
with modified MC limiter

var Leer, J. Comput. Phys. 32, 101 (1979)

K. Okamoto, C. Nonaka, Eur. Phys. J. C77, 383 (2017)

EOS-Q: Sollfrank, Huovinen, Kataja, Ruuskanen,
Prakash, Venugopalan, PRC55, 392 (1997)
Kolb, Sollfrank, Heinz, PLB459, 667 (1999),
PRC62, 054909 (2000)

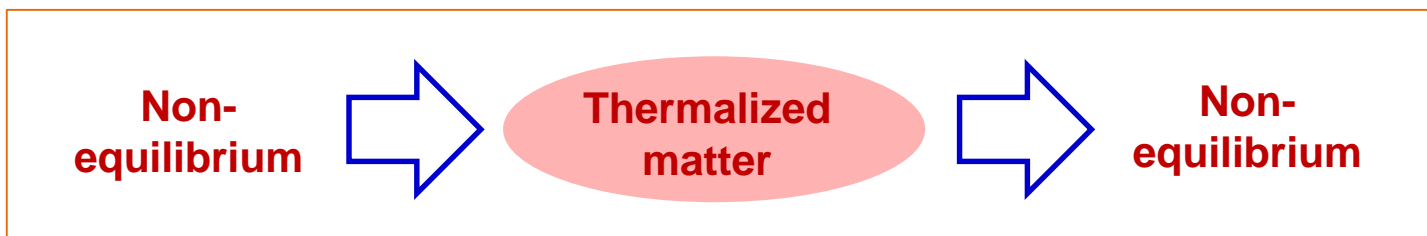
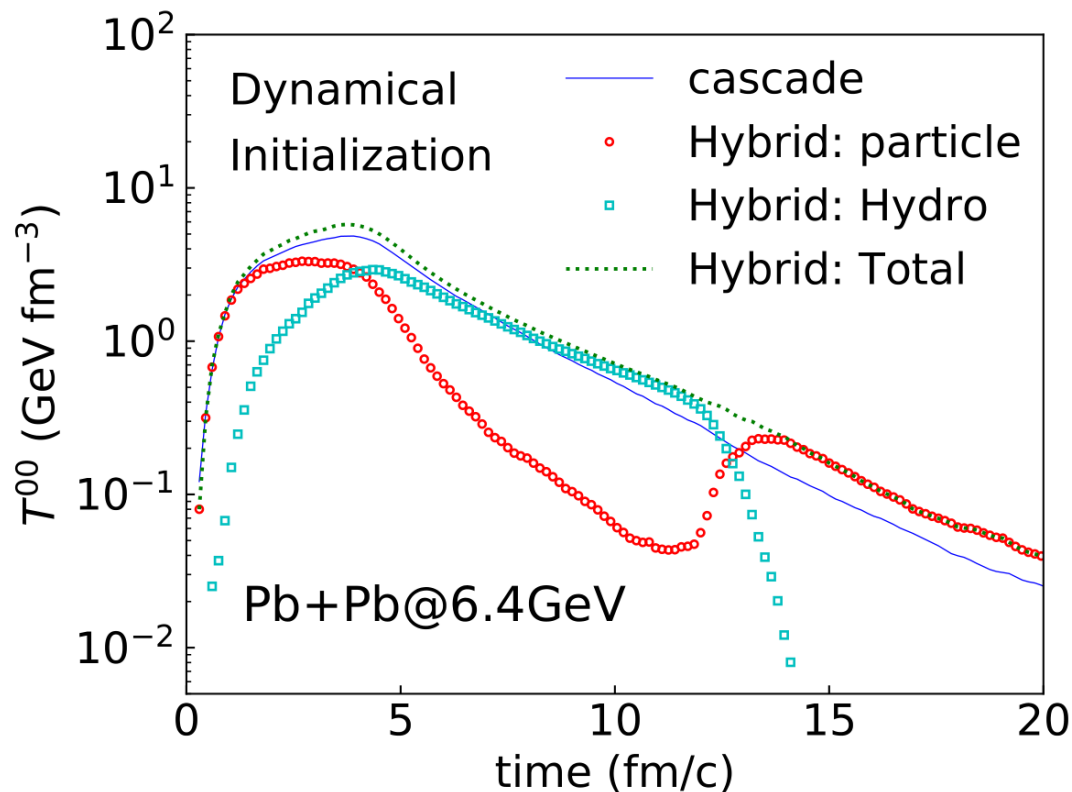
phenomenological EoS with
1st order phase transition

$$B^{1/4} = 235 \text{ GeV/fm}^3$$

$$V(\rho_B) = K\rho_B \text{ in hadron phase}$$

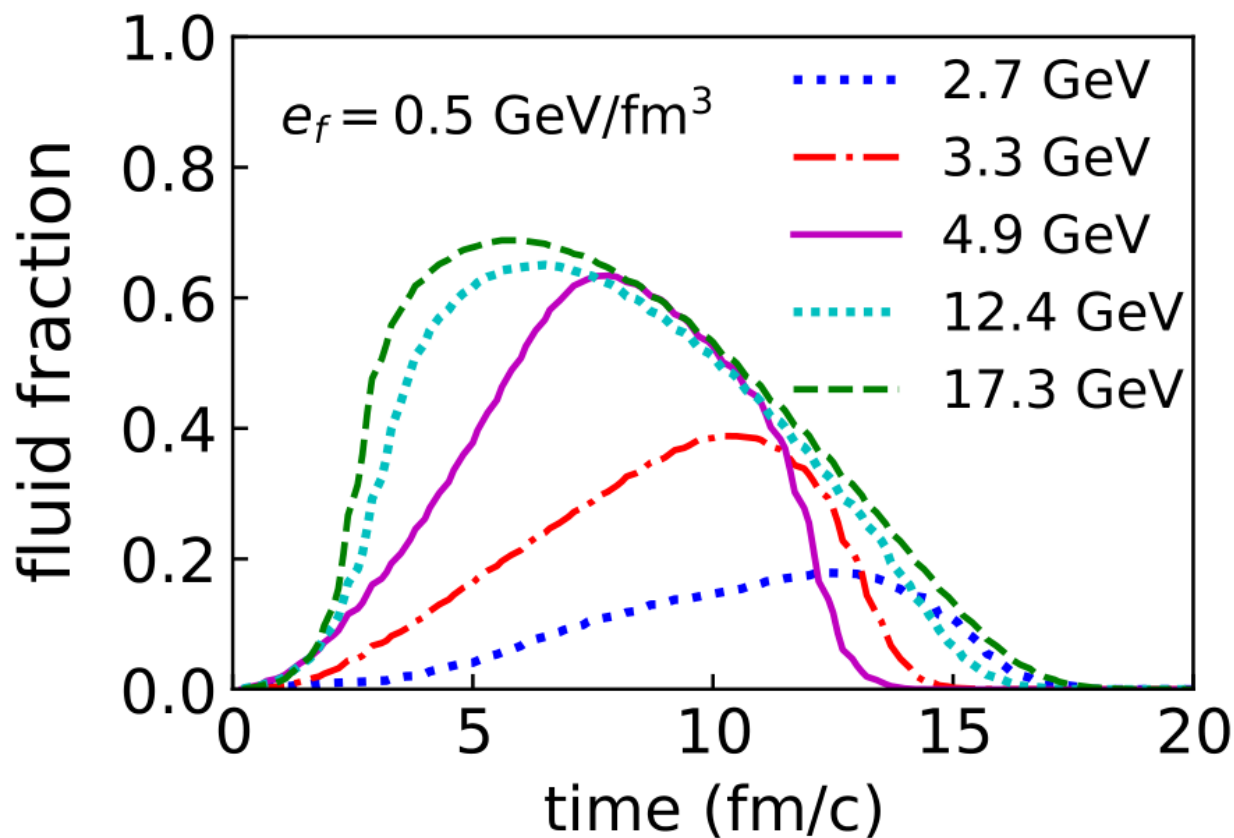
RESULTS

Evolution of particles/hydro energies

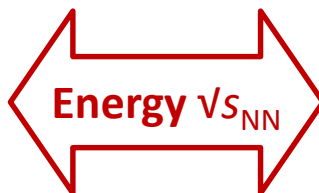


Slower expansion compared to JAM cascade w/o hydro

Fluid fraction of different energies



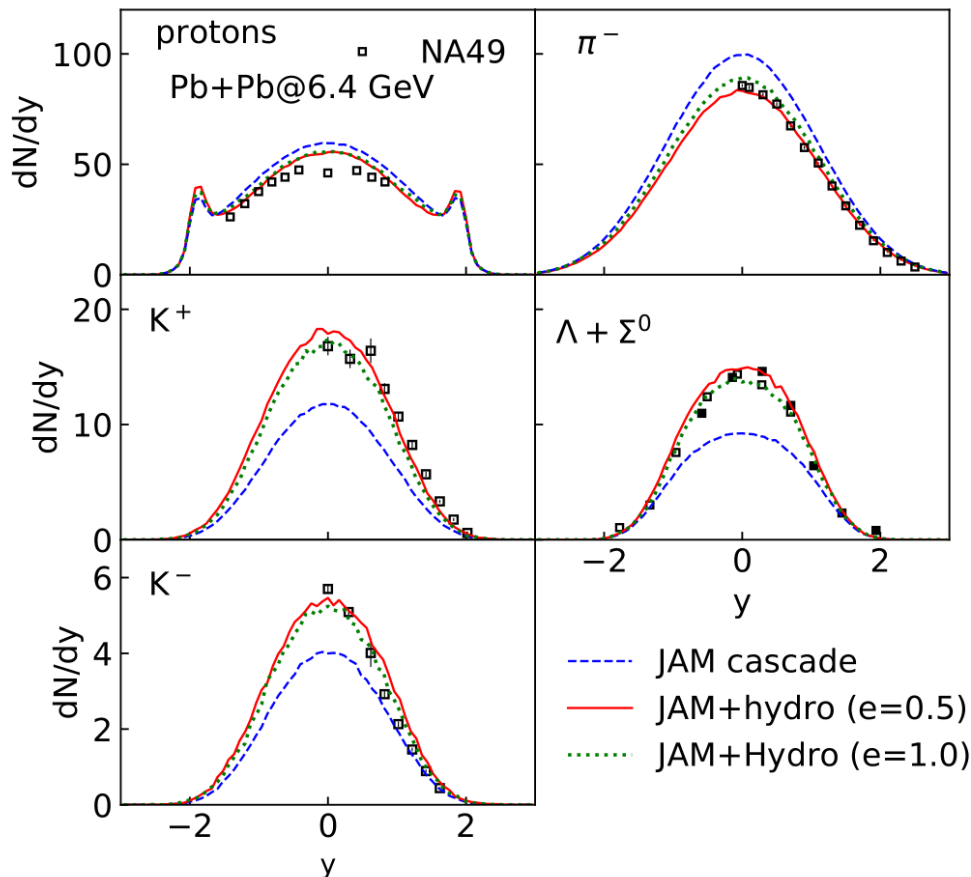
Lower energies
Particle fraction large



Higher energies
Fluid fraction large
→ fixed-time init

dN/dy for $p/\pi/K/\Lambda+\Sigma^0$

Pb+Pb 6.4 GeV Central 0-7%



data: NA49, J. Phys. G 34, S951 (2007);
 NA49, PRC77, 024903 (2008); NA49,
 PRC78, 034918 (2008)

Compared to JAM cascade w/o hydro...

Protons almost the same
 = Similar stopping power

Note: leading hadrons not converted into hydro

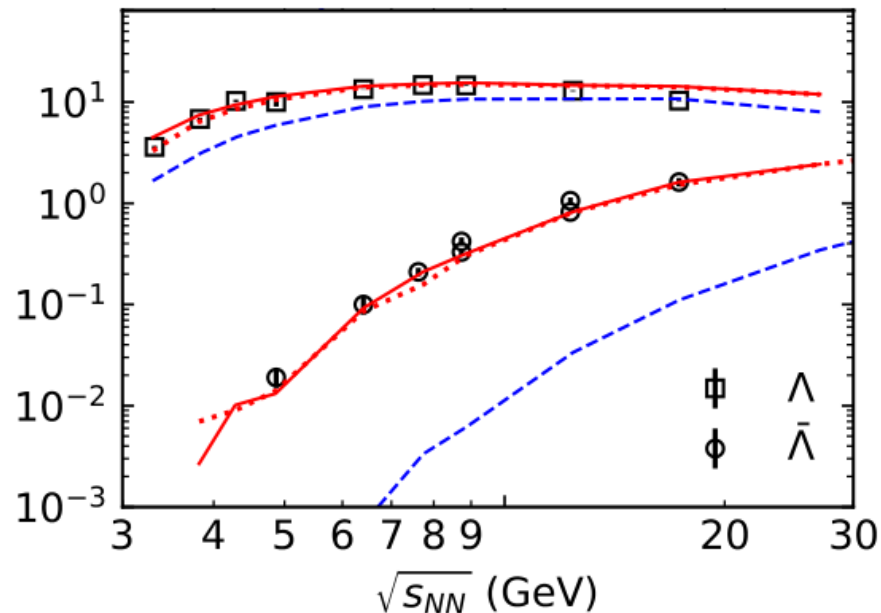
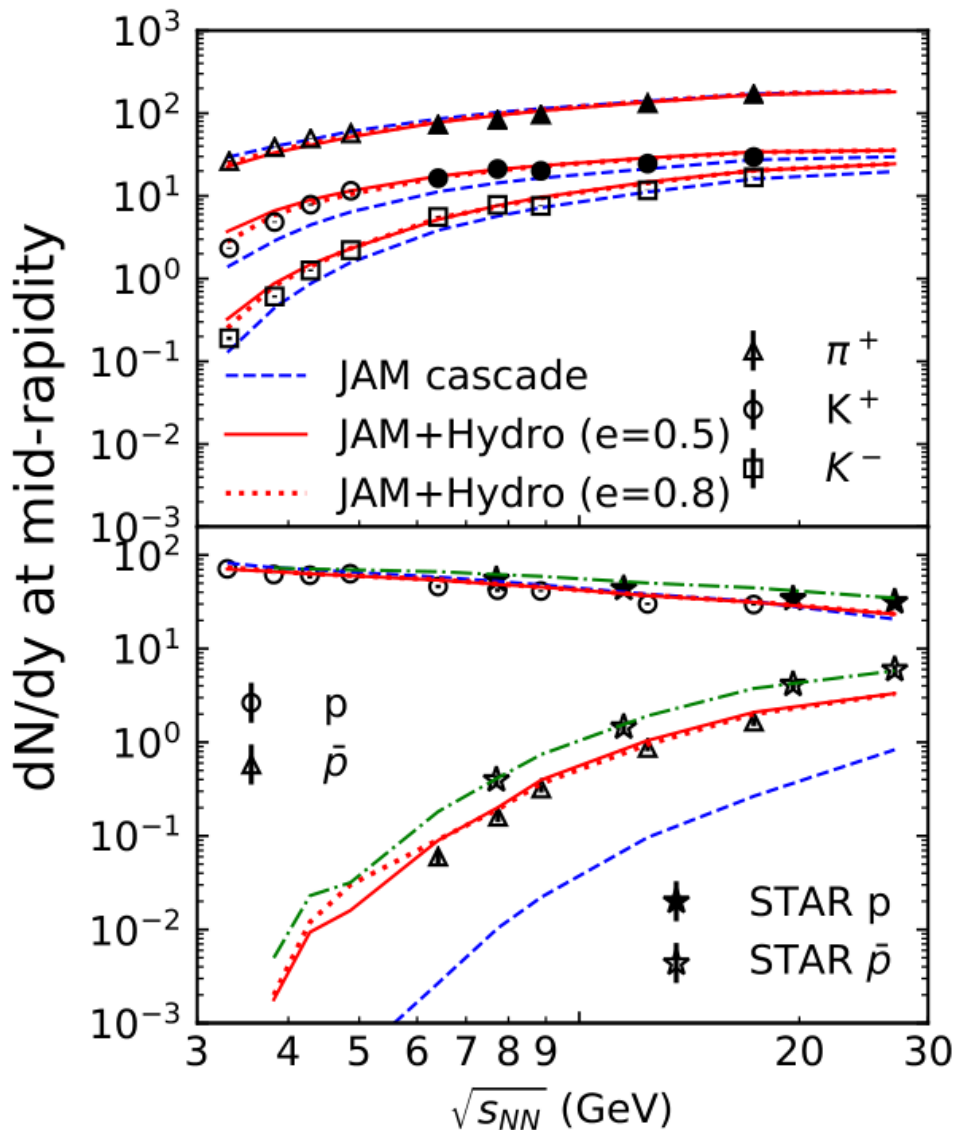
Decrease of pions,
 Increase of strange hadrons
 = Strangeness enhancement

← chemical equilibration

← conversion to hydro

Results insensitive to
 $e_f = 0.5--1.0 \text{ GeV}/\text{fm}^3$

dN/dy vs $\sqrt{s_{NN}}$

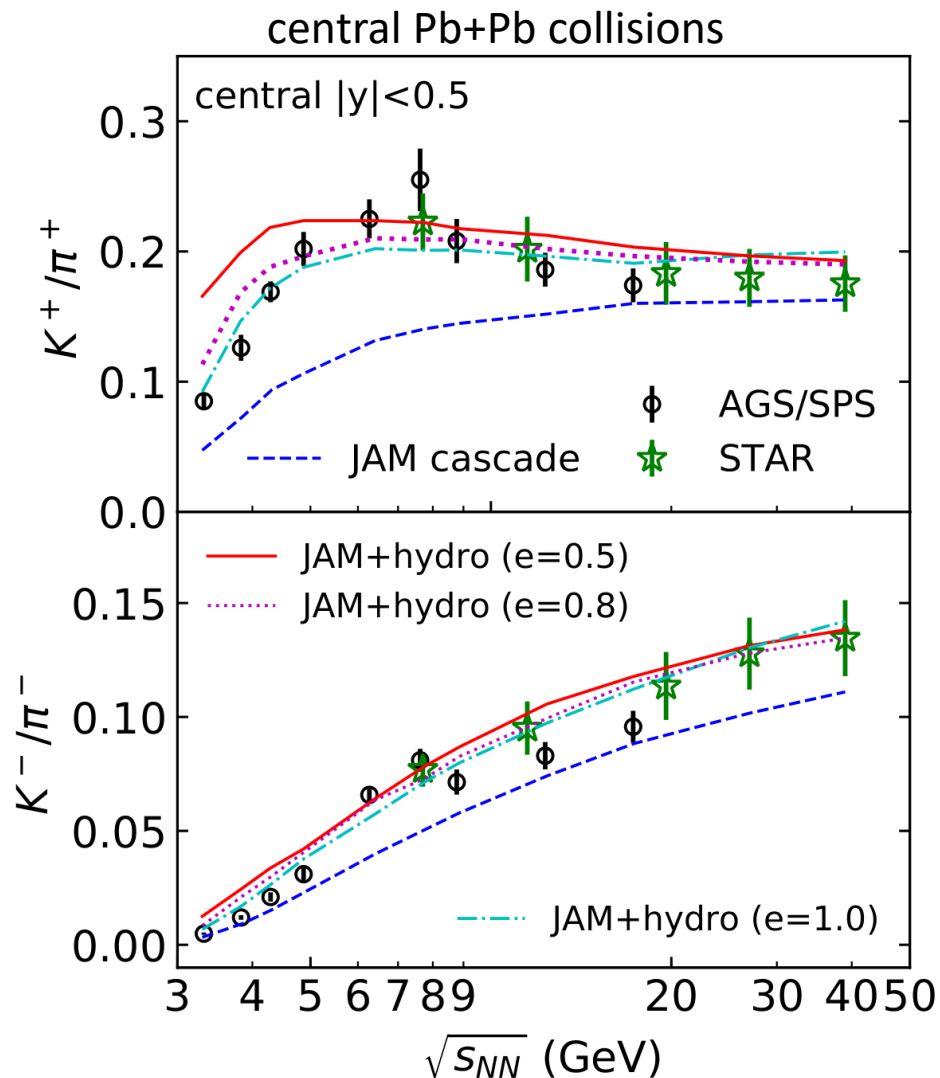


Central Pb+Pb collisions

data: E866 and E917, PLB476, 1 (2000); Blume, Markert, PPNP66, 834 (2011); E802, PRC57, R466 (1998); E895, PRL88, 102301 (2002)

Reproduce
 dN/dy energy dependence
 for π , K , ρ , ρ^{bar} , Λ , Λ^{bar}

K / π ratio vs $\sqrt{s_{NN}}$



data from NA49, PRC66, 054902 (2002); NA49, PRC77, 024903 (2008); STAR, PRC96, 044904 (2017)

Consistent
with experimental “horn”

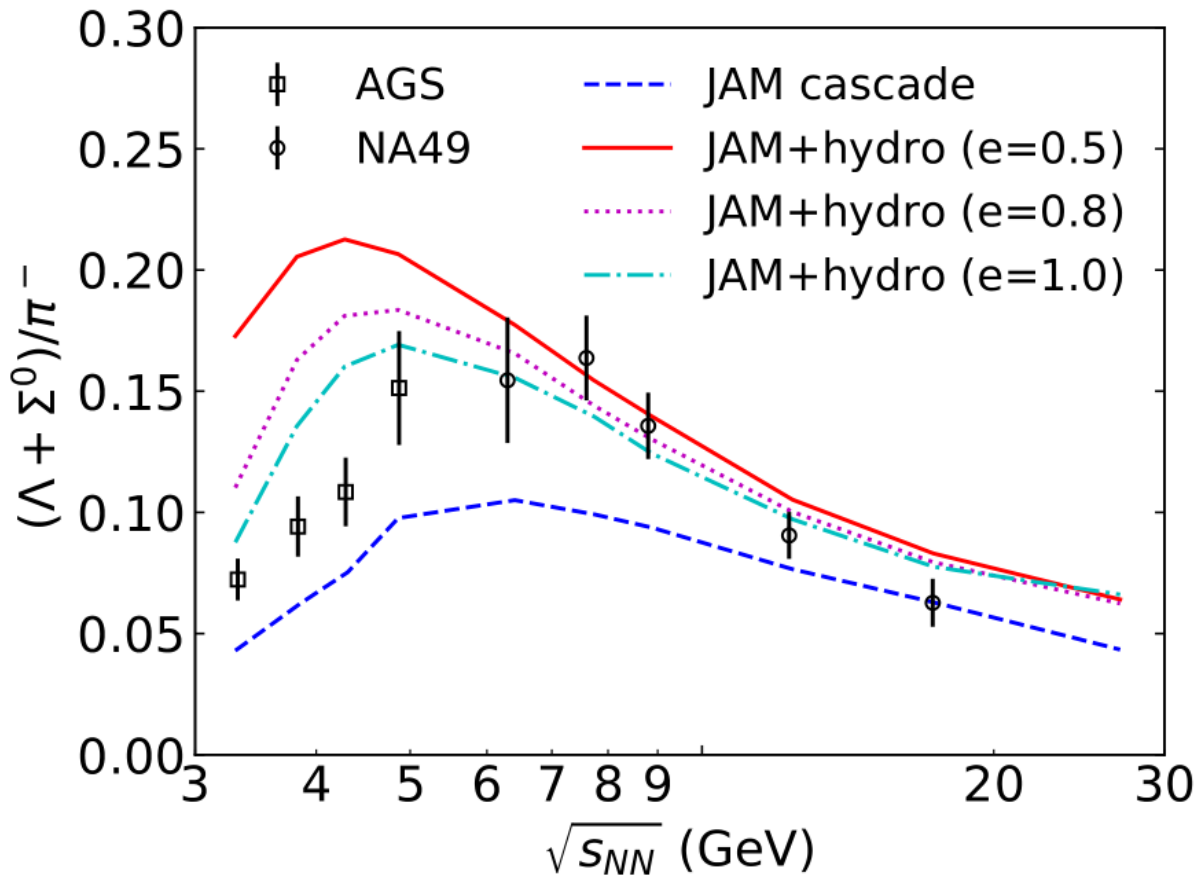
At lower energies:

Sensitive to e_f . Higher e_f
than $e_p = 0.5 \text{ GeV}/\text{fm}^3$
is favored

At higher energies:

Less sensitive to e_f

$(\Lambda + \Sigma^0) / \pi^-$ ratio vs $\sqrt{s_{NN}}$



central Pb+Pb collisions

data: NA49, PRL93, 022302
(2004); STAR, PRC83, 024901
(2011)

Describes data well at higher energies.
Overestimates at lower energies.

SUMMARY

Summary/Outlook

JAM + hydro hybrid model [Phys. Rev. C98, 024909 \(2018\) \[arXiv:1805.09024 \[nucl-th\]\]](#)

- Dynamical initialization/core-corona sep./integration
- Reproduce various experimental data
 - Rapidity distribution for $p/\pi/K/\Lambda+\Sigma^0$,
 - dN/dy vs $\sqrt{s_{NN}}$ for $\pi/K/p/p^{\text{bar}}/\Lambda/\Lambda^{\text{bar}}$,
 - K/π , $(\Lambda+\Sigma^0)/\pi$ ratio vs $\sqrt{s_{NN}}$, etc.

Outlook

- Various observables and centrality dependence: multistrange particles, dv_1/dy , v_2 , etc.
- Sensitivity to EoS, viscous effects
- Full particle-fluid interaction: energy deposition of particles traveling through the medium

BACKUP

Particles to Fluid

- Absorption of particles into fluid

Source terms for hydrodynamics

$$J^\mu(\mathbf{r}) = \frac{1}{\Delta t} \sum_i p_i^\mu(t) G(\mathbf{r} - \mathbf{r}_i(t)),$$

$$\rho(\mathbf{r}) = \frac{1}{\Delta t} \sum_i B_i G(\mathbf{r} - \mathbf{r}_i(t)),$$

Lorentz-contracted deposition profile

$$G(\mathbf{r}) = \frac{\gamma}{(2\pi\sigma^2)^{3/2}} \exp\left(-\frac{\mathbf{r}^2 + (\mathbf{r} \cdot \mathbf{u})^2}{2\sigma^2}\right),$$

Fluid to particles

- Sample particles by Cooper-Frye formula

Positive contribution of Cooper-Frye formula

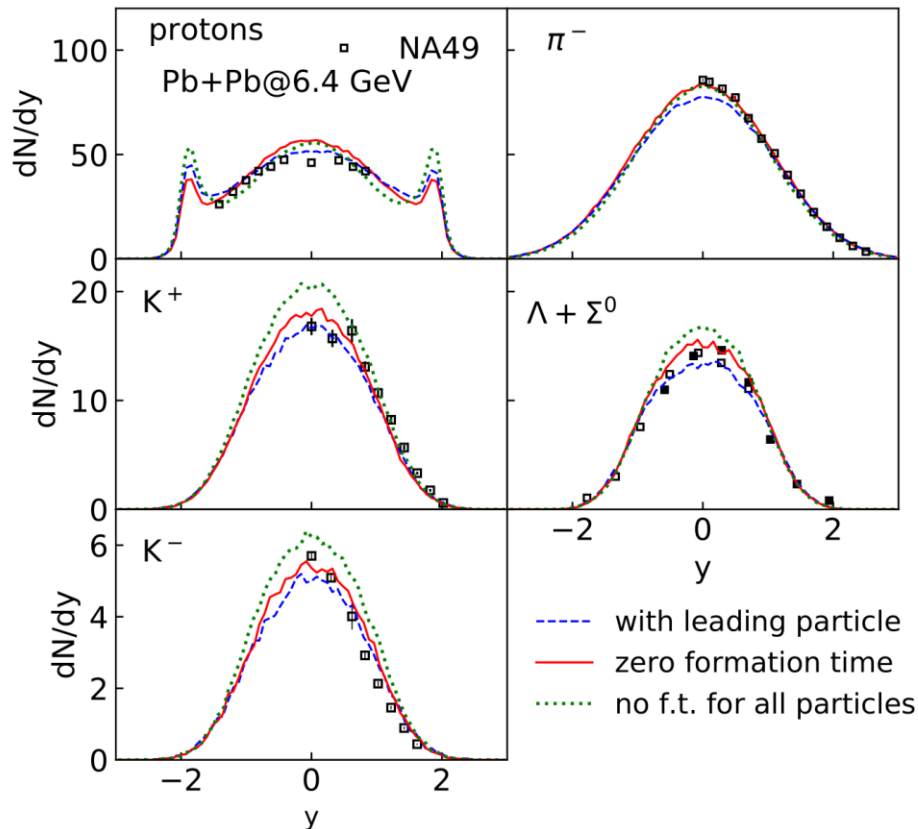
$$\Delta N_i = \frac{g_i}{(2\pi)^3} \int \frac{d^3 p}{E} \frac{[\Delta\sigma \cdot p]_+}{\exp[(p \cdot u - \mu_i)/T] \pm 1},$$

$$[\dots]_+ = \theta(\dots) |\dots|$$

Effective baryon chemical potential consistent with EoS

$$\mu_B^{\text{eff}} = \mu_B - V(\rho_B) = \mu_B - K\rho_B$$

Backup: dN/dy comparisons



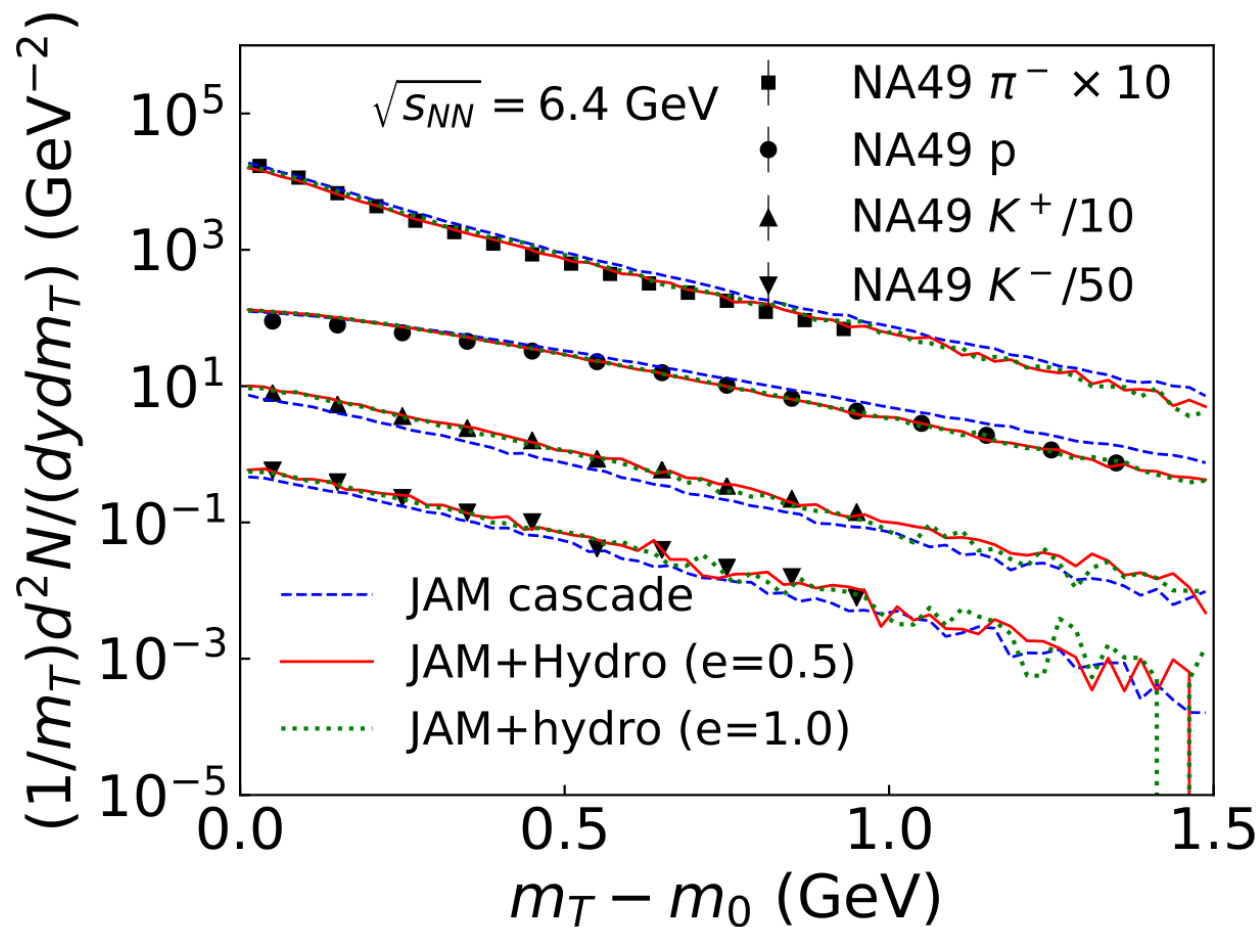
Blue: Stopping power decreased by conversion of leading particles to hydro

Red: effects of formation time negligible

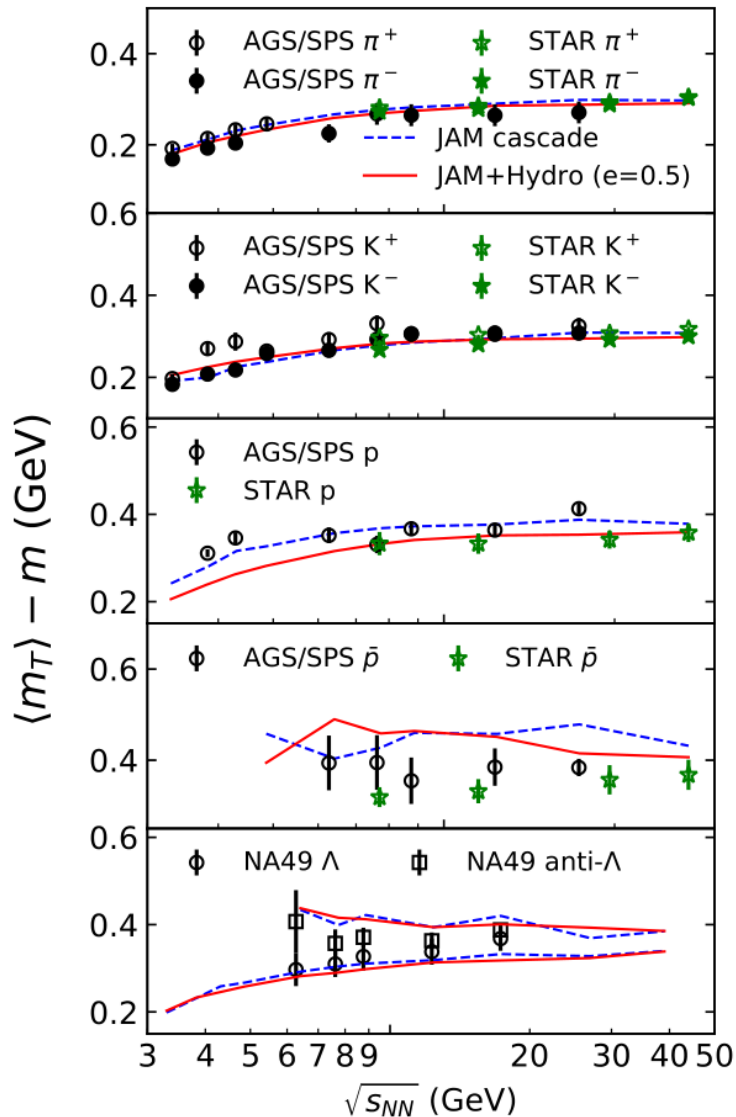
Green: overshoots strange hadron production with everything converted to hydro (equiv. to one-fluid model)

Backup: m_T distributions

Pb+Pb 6.4 GeV Central 0-5%



Backup: $\langle m_T \rangle$ excitation function



proton: decreased by hydrodynamics

others: unaffected by hydrodynamics

Backup: Comparison to UrQMD+hydro

Compared to UrQMD+hydro core-corona model
J. Steinheimer and M. Bleicher, PRC84, 024905 (2011)

