

# LHCb anomaly and B physics in flavored $Z'$ models with flavored Higgs doublets

Yoshihiro SHIGEKAMI (Nagoya U.)

with P. Ko (KIAS), Y. Omura (Nagoya U., KMI), C. Yu (Korea U.)

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# Introduction

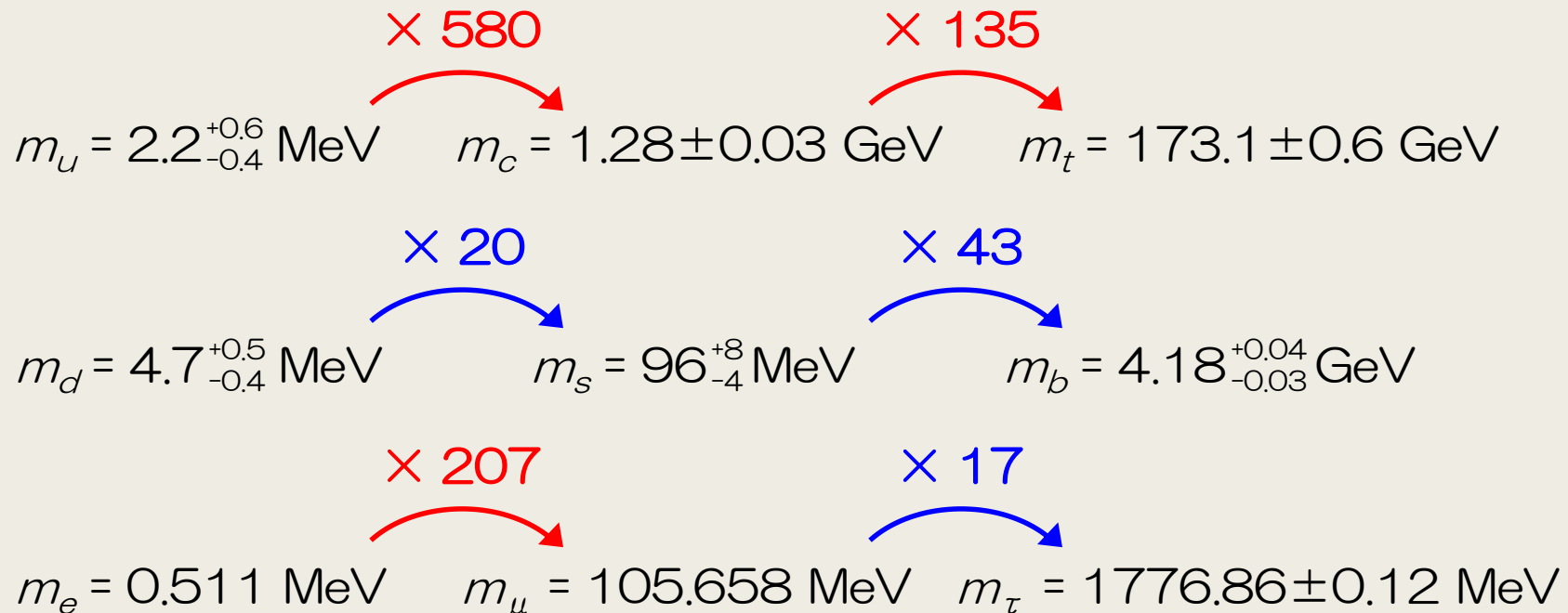
- The SM can explain almost all the exp. data
- However, there are some problems
  - fermion mass hierarchy
  - charge quantization
  - dark matter
  - ...
- These are hints of physics beyond the SM

# Introduction

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- However, there are some problems
  - fermion mass hierarchy ←
  - charge quantization
  - dark matter
  - ...
- These are hints of physics beyond the SM

# Introduction

- Fermion mass hierarchy



from PDG

- How obtain these hierarchy?

# Introduction

## ■ We consider $U(1)'$ extended model

flavored  $Z'$  model

P. Ko, Y. Omura, YS, C. Yu, PRD **95**, 115040 (2017)

- ✓ all fermions have **flavor dependent charges**
- ✓ new Higgs doublets for Yukawa couplings

→ can explain SM fermion mass hierarchy

## ■ New particles

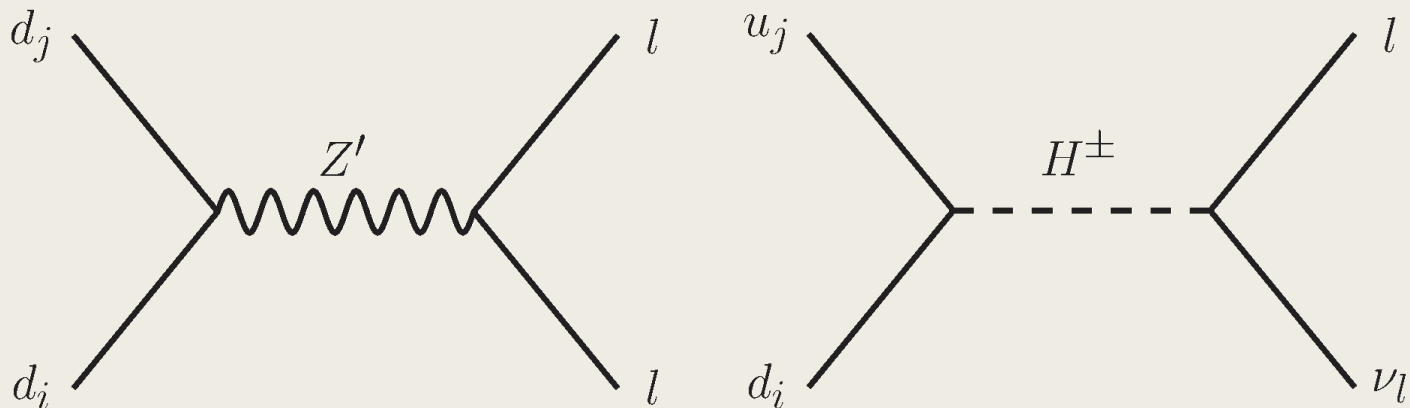
- new gauge boson,  $Z'$  ( $\leftarrow U(1)'$  gauge sym.)
- physical modes in Higgs doublets

$$H^1 = \begin{pmatrix} H_1^+ \\ H_1^0 \end{pmatrix}, \quad H^2 = \begin{pmatrix} H_2^+ \\ H_2^0 \end{pmatrix}, \quad \dots$$

→ many physical modes (e.g. charged Higgs, ...)

# Introduction

- These particles cause FCNC processes
  - U(1)' charges are **flavor dependent**
  - tree level processes



⇒ Affect flavor physics

# Introduction

## ■ We focus on B physics

- $b \rightarrow sll$  ( $R(K)$ ) R. Aaij *et al.* [LHCb Collab.], PRL **113**, 151601 (2014).

- $\Delta M_{B_s}$

- $B \rightarrow X_s \gamma$  

- $R(D)$ ,  $R(D^*)$

Experiment	$R(D)$	$R(D^*)$
Belle	$0.375 \pm 0.064 \pm 0.026$ [15]	$0.302 \pm 0.03 \pm 0.011$ [16]
BABAR	$0.440 \pm 0.058 \pm 0.042$ [13, 14]	$0.332 \pm 0.024 \pm 0.018$ [13, 14]
LHCb		$0.336 \pm 0.027 \pm 0.030$ [99]
HFAG	$0.397 \pm 0.040 \pm 0.028$ [93]	$0.316 \pm 0.016 \pm 0.010$ [93]
SM prediction	$0.300 \pm 0.008$ [100–103]	$0.252 \pm 0.003$ [104]

[13,14] J.P. Lees *et al.* [BaBar Collab.], PRL **109**, 101802 (2012); PRD **88**, 072012 (2013).

[15] M. Huschle *et al.* [Belle Collab.], PRD **92**, 072014 (2015).

[16] A. Abdesselam *et al.* [Belle Collab.], arXiv:1603.06711 [hep-ex].

[93] Y. Amhis *et al.* [Heavy Flavor Averaging Group (HFAG)], arXiv:1412.7515 [hep-ex].

[99] R. Aaij *et al.* [LHCb Collab.], PRL **115**, 111803 (2015).

[100] J.F. Kamenik and F. Mescia, PRD **78** 014003 (2008).

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[102] J.A. Bailey *et al.* [MILC Collab.], PRD **92** 034506 (2015).

[103] H. Na *et al.* [HPQCD Collab.], PRD **92**, 054510 (2015).

[104] S. Fajfer, J.F. Kamenik, and I. Nisandzic, PRD **85**, 094025 (2012).

## ■ Can our model explain these obs.?



Model



# Flavored Z' Model

## ■ Charge assignment

P. Ko, Y. Omura, YS, C. Yu, PRD **95**, 115040 (2017)

New gauge sym.

Fields	spin	SU(3) <sub>c</sub>	SU(2) <sub>L</sub>	U(1) <sub>Y</sub>	U(1)'
$\hat{Q}_L^a$	1/2	<b>3</b>	<b>2</b>	1/6	0
$\hat{Q}_L^3$	1/2	<b>3</b>	<b>2</b>	1/6	1
$\hat{u}_R^a$	1/2	<b>3</b>	<b>1</b>	2/3	$q_a$
$\hat{u}_R^3$	1/2	<b>3</b>	<b>1</b>	2/3	$1 + q_3$
$\hat{d}_R^i$	1/2	<b>3</b>	<b>1</b>	-1/3	$-q_1$
$\hat{L}^1$	1/2	<b>1</b>	<b>2</b>	-1/2	0
$\hat{L}^A$	1/2	<b>1</b>	<b>2</b>	-1/2	$q_e$
$\hat{e}_R^1$	1/2	<b>1</b>	<b>1</b>	-1	$-q_1$
$\hat{e}_R^A$	1/2	<b>1</b>	<b>1</b>	-1	$q_e - q_2$
$H^i$	0	<b>1</b>	<b>2</b>	1/2	$q_i$
$\Phi$	0	<b>1</b>	<b>1</b>	0	$q_\Phi$

$a = 1, 2; A = 2, 3; i = 1, 2, 3$

✓ In this work,  $(q_1, q_2, q_3, q_\Phi) = (0, 1, 3, -1)$

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$\hat{L}^1$	1/2	<b>1</b>	<b>2</b>	-1/2	0
$\hat{L}^A$	1/2	<b>1</b>	<b>2</b>	-1/2	$q_e$
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$\Phi$	0	<b>1</b>	<b>1</b>	0	$q_\Phi$

New gauge sym.

3 Higgs doublets

New SM singlet scalar

$a = 1, 2; A = 2, 3; i = 1, 2, 3$

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# Flavored $Z'$ Model

- Scalar potential (renormalizable level)

$$V_H = m_{H_i}^2 |H_i|^2 + m_\Phi^2 |\Phi|^2 + \lambda_{H_i}^{ij} |H_i|^2 |H_j|^2 + \lambda_{H\Phi}^i |H_i|^2 |\Phi|^2 + \lambda_\Phi |\Phi|^4 \\ - A_1 H_1^\dagger H_2 \Phi - A_2 H_2^\dagger H_3 \Phi^2 + \text{H.c.}$$

- Integrate  $H_1$  out :  $H_1 \rightarrow \frac{A_1}{m_{H_1}^2} \Phi H_2$

# Flavored Z' Model

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- Integrate  $H_1$  out :  $H_1 \rightarrow \frac{A_1}{m_{H_1}^2} \Phi H_2$

$$\text{Higgs VEVs} \quad \langle H_2^0 \rangle = \frac{v}{\sqrt{2}} \cos \beta, \quad \langle H_3^0 \rangle = \frac{v}{\sqrt{2}} \sin \beta, \quad \langle \Phi \rangle = \frac{v_\Phi}{\sqrt{2}}$$

→ For fermion mass hierarchy,

$$\text{large } \tan \beta \text{ \& small } \epsilon \equiv \frac{A_1}{m_{H_1}^2} \langle \Phi \rangle$$

# Flavored Z' Model

Fields	spin	SU(3) <sub>c</sub>	SU(2) <sub>L</sub>	U(1) <sub>Y</sub>	U(1)'
$\hat{Q}_L^a$	1/2	<b>3</b>	<b>2</b>	1/6	0
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$H^i$	0	<b>1</b>	<b>2</b>	1/2	$q_i$
$\Phi$	0	<b>1</b>	<b>1</b>	0	$q_\Phi$

## ■ Yukawa terms

$$\begin{aligned}
 V_Y = & y_{1a}^u \overline{\hat{Q}_L^1} \widetilde{H}^a \hat{u}_R^a + y_{2a}^u \overline{\hat{Q}_L^2} \widetilde{H}^a \hat{u}_R^a + y_{33}^u \overline{\hat{Q}_L^3} \widetilde{H}^3 \hat{u}_R^3 + y_{32}^u \overline{\hat{Q}_L^3} \widetilde{H}^1 \hat{u}_R^2 \\
 & + y_{ai}^d \overline{\hat{Q}_L^a} H^1 \hat{d}_R^i + y_{3i}^d \overline{\hat{Q}_L^3} H^2 \hat{d}_R^i \\
 & + y_{11}^e \overline{\hat{L}^1} H^1 \hat{e}_R^1 + y_{AB}^e \overline{\hat{L}^A} H^2 \hat{e}_R^B + \text{H.c.}
 \end{aligned}$$

$a = 1, 2; A = 2, 3; i = 1, 2, 3$

## ■ Fermion Yukawa couplings

$$(Y_{ij}^u) = \begin{pmatrix} y_{11}^u \epsilon & y_{12}^u & 0 \\ y_{21}^u \epsilon & y_{22}^u & 0 \\ 0 & y_{32}^u \epsilon & y_{33}^u \end{pmatrix} \begin{pmatrix} \cos \beta \\ \cos \beta \\ \sin \beta \end{pmatrix}, \quad \epsilon \equiv \frac{A_1}{m_{H_1}^2} \langle \Phi \rangle \sim 0.01$$

$$(Y_{ij}^d) = \cos \beta \begin{pmatrix} \epsilon & & \\ & \epsilon & \\ & & 1 \end{pmatrix} \begin{pmatrix} y_{11}^d & y_{12}^d & y_{13}^d \\ y_{21}^d & y_{22}^d & y_{23}^d \\ y_{31}^d & y_{32}^d & y_{33}^d \end{pmatrix}, \quad (Y_{ij}^e) = \cos \beta \begin{pmatrix} \epsilon & & \\ & 1 & \\ & & 1 \end{pmatrix} \begin{pmatrix} y_{11}^e & 0 & 0 \\ 0 & y_{22}^e & y_{23}^e \\ 0 & y_{32}^e & y_{33}^e \end{pmatrix}$$

$$\Rightarrow m_s/m_b = \mathcal{O}(\epsilon), \quad m_e/m_\mu = \mathcal{O}(\epsilon)$$

# Flavored Z' Model

## ■ Fermion masses

$$(Y_{ij}^u) = \begin{pmatrix} y_{11}^u \epsilon & y_{12}^u & 0 \\ y_{21}^u \epsilon & y_{22}^u & 0 \\ 0 & y_{32}^u \epsilon & y_{33}^u \end{pmatrix} \begin{pmatrix} \cos \beta & & \\ & \cos \beta & \\ & & \sin \beta \end{pmatrix},$$

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$$\Rightarrow \frac{v}{\sqrt{2}} Y^I = (U_L^I)^\dagger \text{diag}(m_1^I, m_2^I, m_3^I) U_R^I \quad (I = u, d, e)$$

each elements:

$$|(U_L^d)_{33}| \simeq 1, |(U_L^d)_{23}| = \mathcal{O}(\epsilon), |(U_L^d)_{13}| = \mathcal{O}(\epsilon)$$

&

$$|(U_R^u)_{33}| \simeq 1, |(U_R^u)_{23}| = \mathcal{O}(\epsilon), |(U_R^u)_{13}| \gg |(U_R^u)_{13}|.$$

→ Important for flavor physics

# Flavored Z' Model

- Yukawa couplings with charged Higgs

$$-\mathcal{L}_{Y_{\pm}} = (Y_{\pm}^u)_{ij} H^- \bar{d}_L^i u_R^j + (Y_{\pm}^d)_{ij} H^+ \bar{u}_L^i d_R^j + (Y_{\pm}^e)_{ij} H^+ \bar{\nu}_L^i e_R^j + \text{H.c.}$$

$$\begin{cases} (Y_{\pm}^u)_{ij} = -\frac{m_u^k \sqrt{2}}{v} (V_{\text{CKM}})_{ki}^* G_{kj} \\ (Y_{\pm}^d)_{ij} = -(V_{\text{CKM}})_{ij} \frac{m_d^j \sqrt{2}}{v} \tan \beta \end{cases}$$

$$G_{ij} = \left( U_R^u \begin{pmatrix} -\tan \beta & & \\ & -\tan \beta & \\ & & \frac{1}{\tan \beta} \end{pmatrix} U_R^{u\dagger} \right)_{ij}$$

$$= -\tan \beta \delta_{ij} + \left( \tan \beta + \frac{1}{\tan \beta} \right) (G_R^u)_{ij}$$

$$(G_R^u)_{ij} \equiv (U_R^u)_{i3} (U_R^u)_{j3}^*$$

# Flavored Z' Model

- Yukawa couplings with charged Higgs

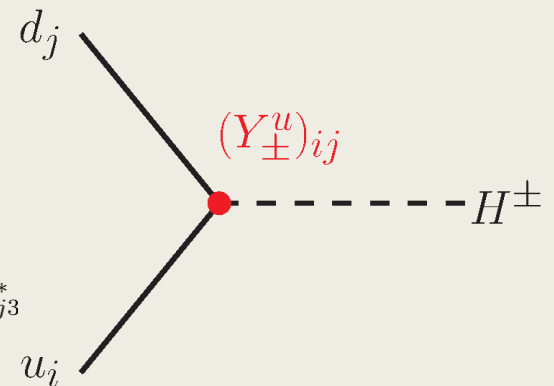
$$-\mathcal{L}_{Y_{\pm}} = (Y_{\pm}^u)_{ij} H^- \bar{d}_L^i u_R^j + (Y_{\pm}^d)_{ij} H^+ \bar{u}_L^i d_R^j + (Y_{\pm}^e)_{ij} H^+ \bar{\nu}_L^i e_R^j + \text{H.c.}$$

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Flavor-violating  $(G_R^u)_{ij} \equiv (U_R^u)_{i3} (U_R^u)_{j3}^*$





# Flavored Z' Model

## ■ Z' couplings

interaction basis

$$(q_1, q_2, q_3, q_\Phi) = (0, 1, 3, -1)$$

$$\begin{aligned} \mathcal{L}_{Z'} = & g' \hat{Z}'_\mu \left( \overline{\hat{Q}}_L^3 \gamma^\mu \hat{Q}_L^3 + q_1 \overline{\hat{u}}_R^1 \gamma^\mu \hat{u}_R^1 + (1 + q_1) \overline{\hat{u}}_R^2 \gamma^\mu \hat{u}_R^2 + (1 + q_3) \overline{\hat{u}}_R^3 \gamma^\mu \hat{u}_R^3 \right) \\ & + g' \hat{Z}'_\mu \left( q_e \overline{\hat{L}}^A \gamma^\mu \hat{L}^A - q_1 \overline{\hat{d}}_R^i \gamma^\mu \hat{d}_R^i - q_1 \overline{\hat{e}}_R^1 \gamma^\mu \hat{e}_R^1 + (q_e - q_2) \overline{\hat{e}}_R^A \gamma^\mu \hat{e}_R^A \right) \end{aligned}$$

$$\Downarrow \quad \frac{v}{\sqrt{2}} Y^I = (U_L^I)^\dagger \text{diag}(m_1^I, m_2^I, m_3^I) U_R^I \quad (I = u, d, e)$$

mass basis

$$\begin{aligned} \mathcal{L}_{Z'} = & g' \hat{Z}'_\mu \left\{ (g_L^u)_{ij} \overline{u}_L^i \gamma^\mu u_L^j + (g_L^d)_{ij} \overline{d}_L^i \gamma^\mu d_L^j + (g_R^u)_{ij} \overline{u}_R^i \gamma^\mu u_R^j - q_1 \overline{d}_R^i \gamma^\mu d_R^i \right\} \\ & + g' \hat{Z}'_\mu \left\{ q_e (\overline{\mu}_L \gamma^\mu \mu_L + \overline{\tau}_L \gamma^\mu \tau_L) + (g_L^\nu)_{ij} \overline{\nu}_L^i \gamma^\mu \nu_L^j - q_1 \overline{e}_R^1 \gamma^\mu e_R^1 + (q_e - q_2) \overline{e}_R^A \gamma^\mu e_R^A \right\} \end{aligned}$$

# Flavored Z' Model

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Flavor-violating couplings

# Flavored Z' Model

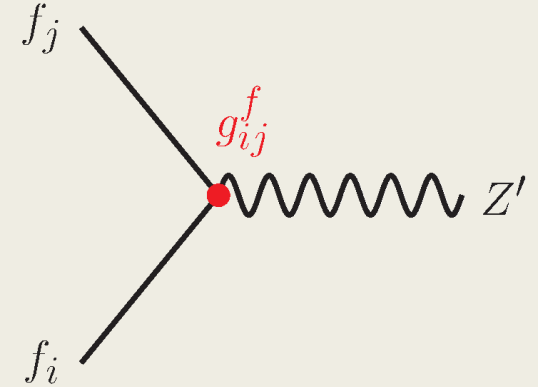
## ■ Z' couplings

$$(g_L^d)_{ij} = (U_L^d)_{i3}(U_L^d)_{j3}^*,$$

$$(g_L^u)_{ij} = (U_L^u)_{i3}(U_L^u)_{j3}^* = (V_{\text{CKM}})_{ik}(g_L^d)_{kk'}(V_{\text{CKM}})_{jk'}^*,$$

$$(g_R^u)_{ij} = (U_R^u)_{ik}q_k(U_R^u)_{jk}^*,$$

$$(g_L^\nu)_{ij} = q_e^k \left\{ (U_L^\nu)_{ik}(U_L^\nu)_{jk}^* \right\} = q_e \left\{ \delta_{ij} - (V_{\text{PMNS}}^\dagger)_{i3}(V_{\text{PMNS}}^\dagger)_{j3}^* \right\}.$$



$$\frac{v}{\sqrt{2}}Y^I = (U_L^I)^\dagger \text{diag}(m_1^I, m_2^I, m_3^I)U_R^I \quad (I = u, d, e)$$

## ■ The size of each $g_{ij}$

$$|(U_L^d)_{33}| \simeq 1, |(U_L^d)_{23}| = \mathcal{O}(\epsilon), |(U_L^d)_{13}| = \mathcal{O}(\epsilon)$$

$$|(U_R^u)_{33}| \simeq 1, |(U_R^u)_{23}| = \mathcal{O}(\epsilon), |(U_R^u)_{13}| \gg |(U_R^u)_{23}|.$$

$$(g_L^d)_{sb} = \mathcal{O}(\epsilon), (g_L^d)_{db} = \mathcal{O}(\epsilon), (g_L^d)_{sd} = \mathcal{O}(\epsilon^2),$$

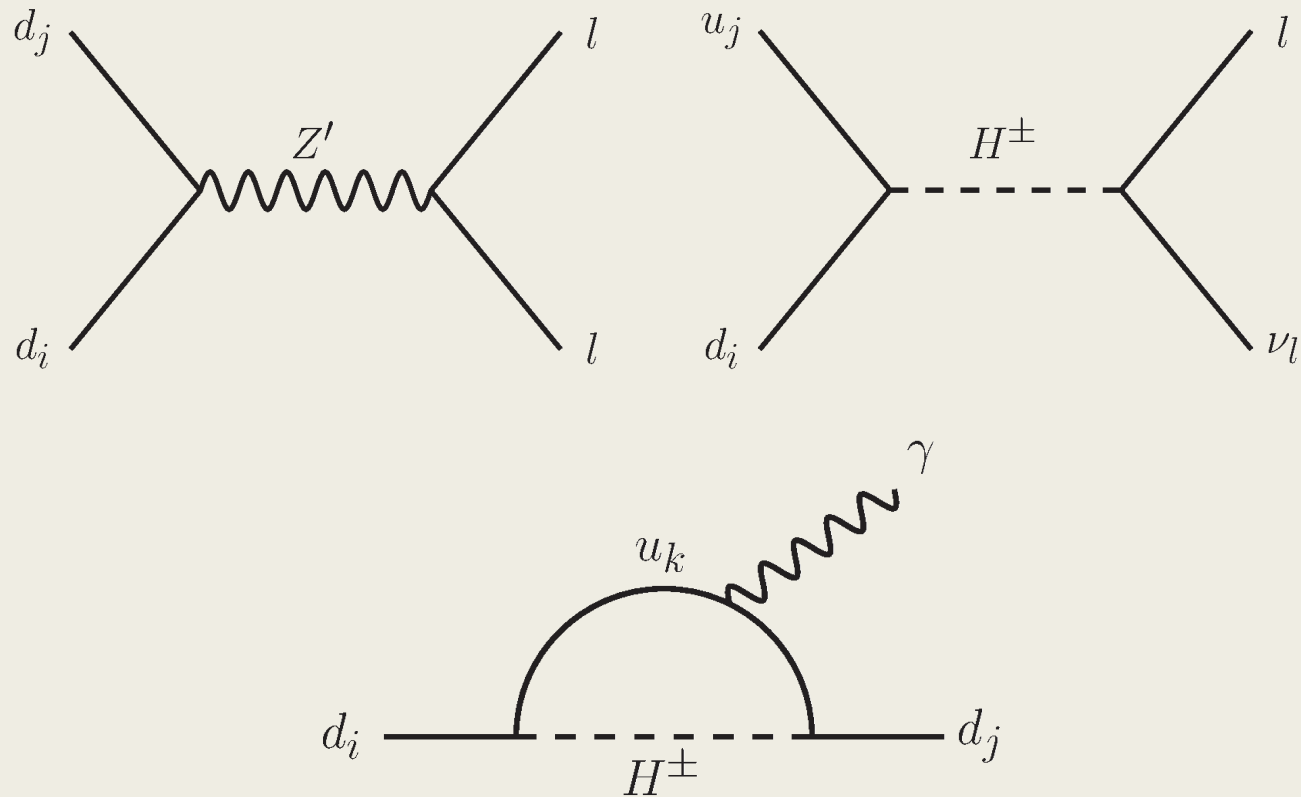
$$(g_L^u)_{ij} \simeq (g_L^d)_{ij}, (g_R^u)_{ct} = q_3 \times \mathcal{O}(\epsilon), |(g_R^u)_{ct}| \gg |(g_R^u)_{ut}|, |(g_R^u)_{uc}|.$$

The image features two large, thick black L-shaped brackets. One is positioned in the top-left corner, and the other is in the bottom-right corner, framing the central text. The text "Flavor Physics" is centered between these brackets.

# Flavor Physics

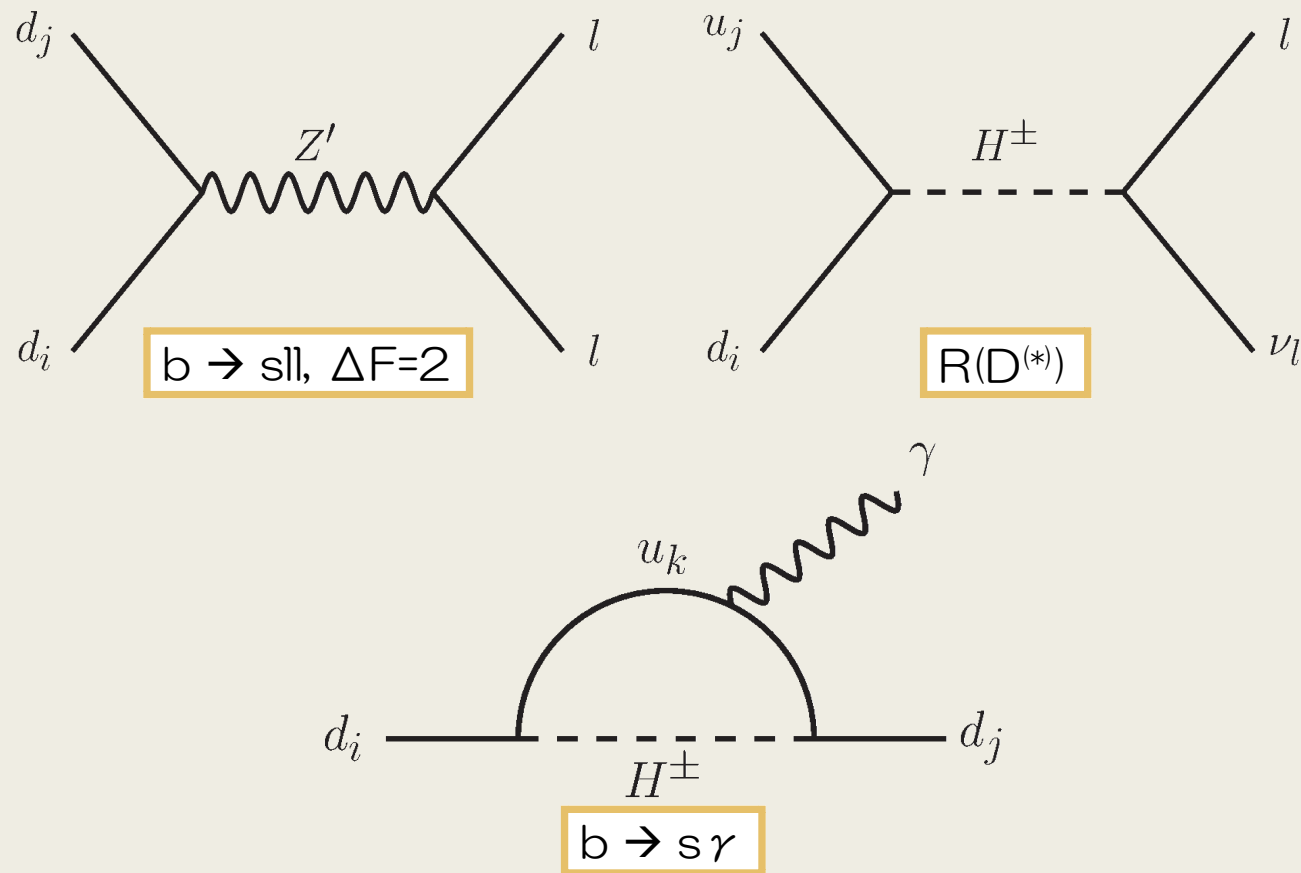
# Flavor Physics Involving $b$

- Flavor-violating processes

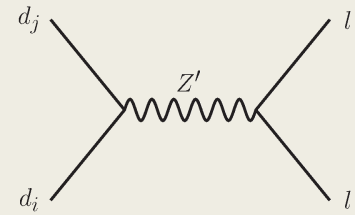


# Flavor Physics Involving $b$

- Flavor-violating processes



# Flavor Physics Involving $b$



## ■ $b \rightarrow sll$

$$\mathcal{H}_{\text{eff}} = -g_{\text{SM}} \left[ C_9^l (\bar{s}_L \gamma_\mu b_L) (\bar{l} \gamma^\mu l) + C_{10}^l (\bar{s}_L \gamma_\mu b_L) (\bar{l} \gamma^\mu \gamma_5 l) + \text{H.c.} \right]$$

$$C_9^e = C_{10}^e = \frac{g'^2}{2g_{\text{SM}} M_{Z'}^2} (g_L^d)_{sb} q_1$$

$$g_{\text{SM}} = \frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \frac{e^2}{16\pi^2}$$

$$C_9^\mu = C_9^\tau = -\frac{g'^2}{2g_{\text{SM}} M_{Z'}^2} (g_L^d)_{sb} (2q_e - q_2)$$

$$C_{10}^\mu = C_{10}^\tau = \frac{g'^2}{2g_{\text{SM}} M_{Z'}^2} (g_L^d)_{sb} q_2$$

exp. bounds

$$-0.29 \text{ } (-0.34) \leq C_9^\mu / C_9^{\text{SM}} \leq -0.013 \text{ } (0.053)$$

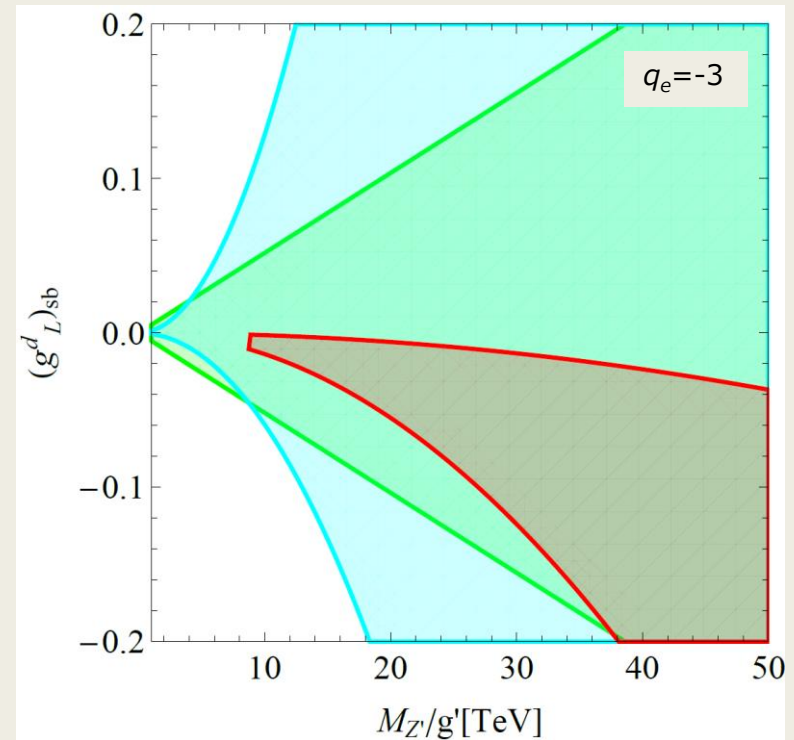
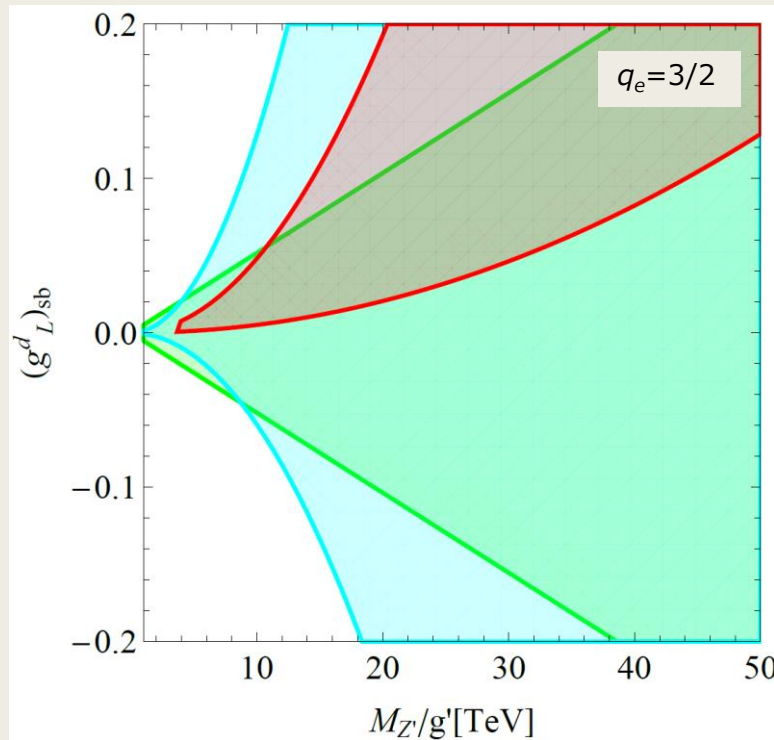
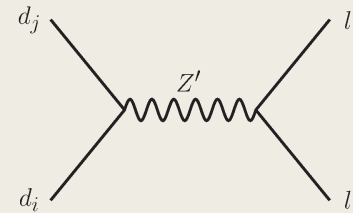
$$-0.19 \text{ } (-0.29) \leq C_{10}^\mu / C_{10}^{\text{SM}} \leq 0.088 \text{ } (0.15)$$

T. Hurth, F. Mahmoudi, and S. Neshatpour, NPB **909**, 737 (2016)

## ■ $\Delta F=2$

$$\mathcal{H}_{\text{eff}}^{\Delta F=2} = C_1^{ij} (\bar{d}_L^i \gamma_\mu d_L^j) (\bar{d}_L^i \gamma_\mu d_L^j), \quad C_1^{ij} = \frac{g'^2}{2M_{Z'}^2} (g_L^d)_{ij} (g_L^d)_{ij}$$

# $b \rightarrow sl$ & $\Delta F=2$ process



Allowed region for red:  $C_9^\mu$ , cyan:  $C_{10}^\mu$ , green:  $B_s$ - $B_s$ bar mixing

$$-0.29 (-0.34) \leq C_9^\mu / C_9^{\text{SM}} \leq -0.013 (0.053)$$

$$-0.19 (-0.29) \leq C_{10}^\mu / C_{10}^{\text{SM}} \leq 0.088 (0.15)$$

T. Hurth, F. Mahmoudi, and S. Neshatpour, NPB **909**, 737 (2016)

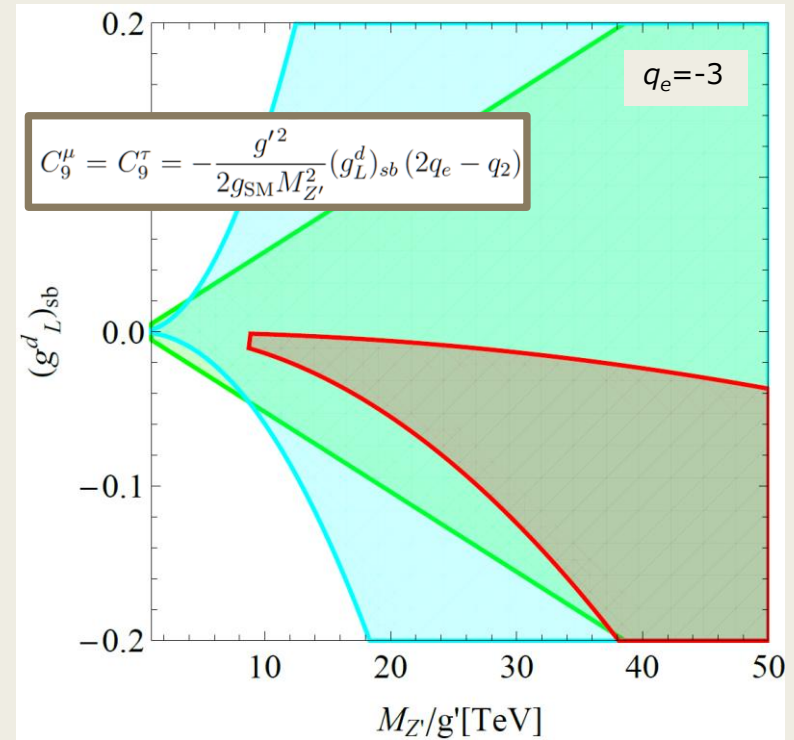
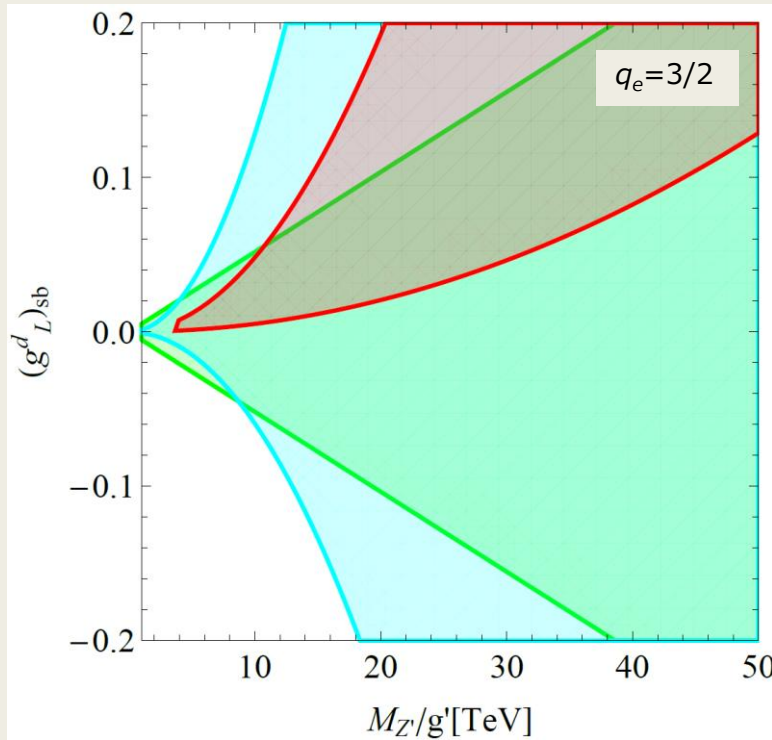
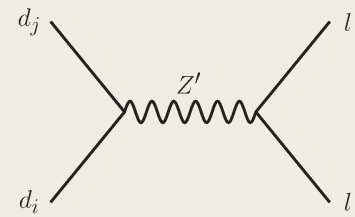
$$\Delta m_s = 17.757 \pm 0.021 \text{ ps}^{-1}$$

S. Aoki *et al.*, EPJC **77**, 112 (2017).

Y. Amhis *et al.* [HFAG], arXiv:1412.7515 [hep-ex].



# $b \rightarrow sl$ & $\Delta F=2$ process



Allowed region for red:  $C_9^\mu$ , cyan:  $C_{10}^\mu$ , green:  $B_s$ - $B_s$ bar mixing

$$-0.29 (-0.34) \leq C_9^\mu / C_9^{\text{SM}} \leq -0.013 (0.053)$$

$$-0.19 (-0.29) \leq C_{10}^\mu / C_{10}^{\text{SM}} \leq 0.088 (0.15)$$

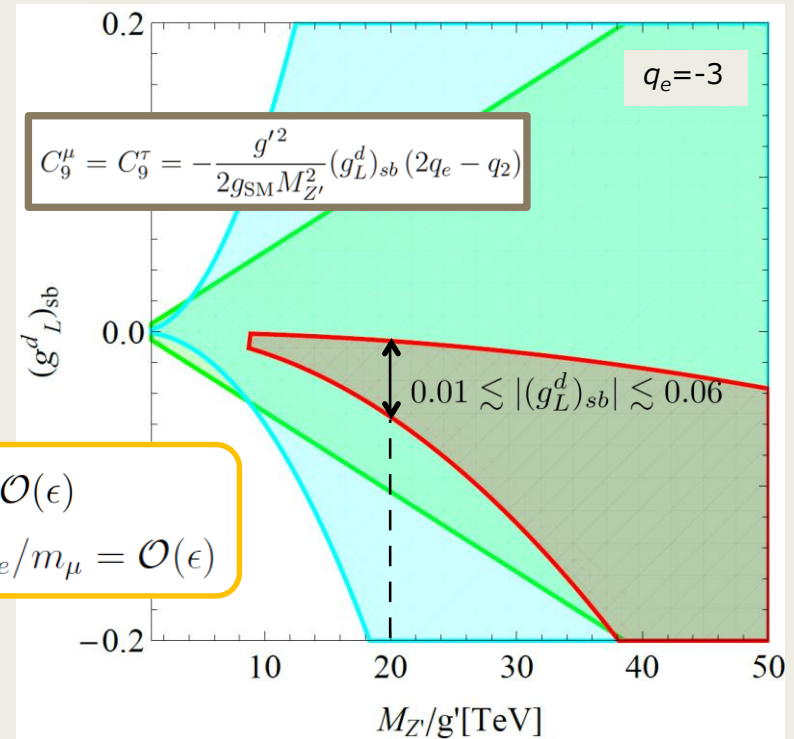
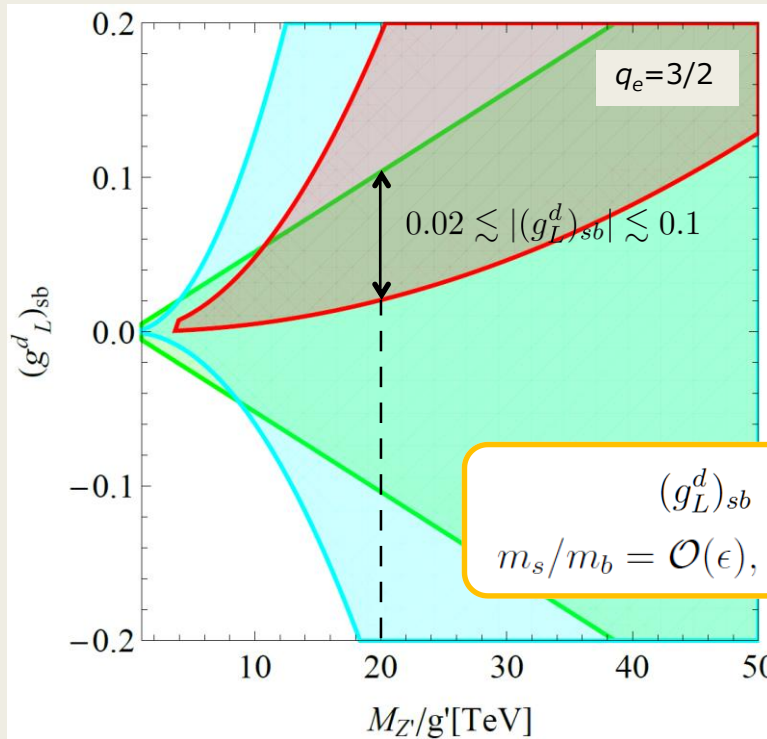
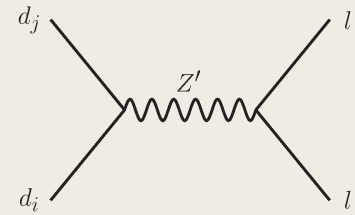
T. Hurth, F. Mahmoudi, and S. Neshatpour, NPB **909**, 737 (2016)

$$\Delta m_s = 17.757 \pm 0.021 \text{ ps}^{-1}$$

S. Aoki *et al.*, EPJC **77**, 112 (2017).

Y. Amhis *et al.* [HFAG], arXiv:1412.7515 [hep-ex].

# $b \rightarrow sl$ & $\Delta F=2$ process



$$(g_L^d)_{sb} = \mathcal{O}(\epsilon)$$

$$m_s/m_b = \mathcal{O}(\epsilon), m_e/m_\mu = \mathcal{O}(\epsilon)$$

Allowed region for red:  $C_9^\mu$ , cyan:  $C_{10}^\mu$ , green:  $B_s$ - $B_s$ bar mixing

$$-0.29 (-0.34) \leq C_9^\mu / C_9^{\text{SM}} \leq -0.013 (0.053)$$

$$-0.19 (-0.29) \leq C_{10}^\mu / C_{10}^{\text{SM}} \leq 0.088 (0.15)$$

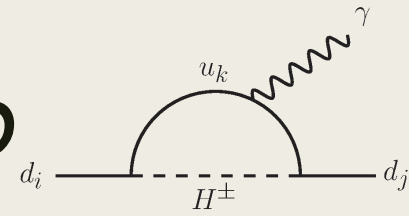
T. Hurth, F. Mahmoudi, and S. Neshatpour, NPB **909**, 737 (2016)

$$\Delta m_s = 17.757 \pm 0.021 \text{ ps}^{-1}$$

S. Aoki *et al.*, EPJC **77**, 112 (2017).

Y. Amhis *et al.* [HFAG], arXiv:1412.7515 [hep-ex].

# Flavor Physics Involving $b$



■  $B \rightarrow X_s \gamma$   $\mathcal{H}_{\text{eff}}^{b \rightarrow s \gamma} = -\frac{4G_F}{\sqrt{2}} V_{ts}^* V_{tb} (C_7 \mathcal{O}_7 + C_8 \mathcal{O}_8)$

$$\mathcal{O}_7 = \frac{e}{16\pi^2} m_b (\bar{s}_L \sigma^{\mu\nu} b_R) F_{\mu\nu}, \quad \mathcal{O}_8 = \frac{g_s}{16\pi^2} m_b (\bar{s}_L t^a \sigma^{\mu\nu} b_R) G_{\mu\nu}^a$$

$$C_7 = \left( \frac{m_j^u m_k^u}{m_t^2} \right) \frac{V_{kb} V_{js}^*}{V_{tb} V_{ts}^*} G_{ki}^* G_{ji} C_7^{(1)}(x_i) + \left( \frac{m_k^u}{m_t} \right) \frac{V_{ib} V_{ks}^*}{V_{tb} V_{ts}^*} G_{ki} \tan \beta C_7^{(2)}(x_i)$$

$$C_8 = \left( \frac{m_j^u m_k^u}{m_t^2} \right) \frac{V_{kb} V_{js}^*}{V_{tb} V_{ts}^*} G_{ki}^* G_{ji} C_8^{(1)}(x_i) + \left( \frac{m_k^u}{m_t} \right) \frac{V_{ib} V_{ks}^*}{V_{tb} V_{ts}^*} G_{ki} \tan \beta C_8^{(2)}(x_i)$$

$$G_{ij} = -\tan \beta \delta_{ij} + \left( \tan \beta + \frac{1}{\tan \beta} \right) (G_R^u)_{ij}$$

$$(G_R^u)_{ij} \equiv (U_R^u)_{i3} (U_R^u)^*_{j3}$$

Loop integrals:

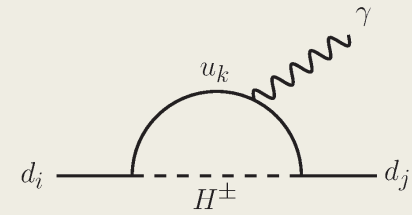
$$C_7^{(1)}(x) = \frac{x}{72} \left\{ \frac{-8x^3 + 3x^2 + 12x - 7 + (18x^2 - 12x) \ln x}{(x-1)^4} \right\},$$

$$C_7^{(2)}(x) = \frac{x}{12} \left\{ \frac{-5x^2 + 8x - 3 + (6x - 4) \ln x}{(x-1)^3} \right\},$$

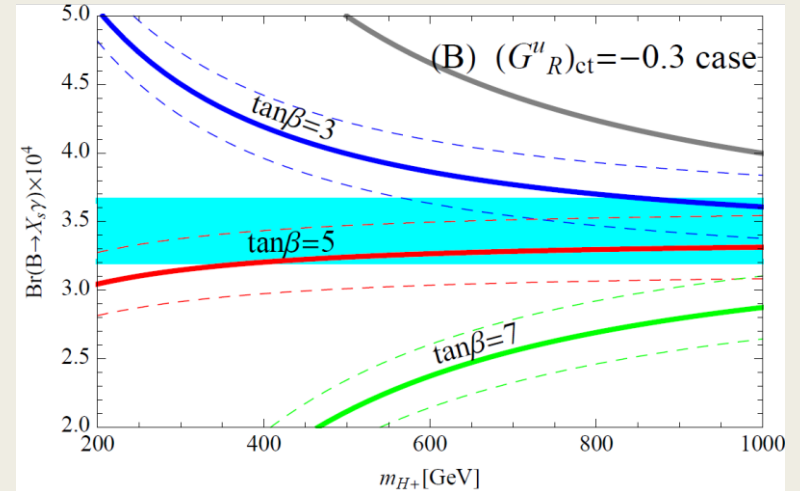
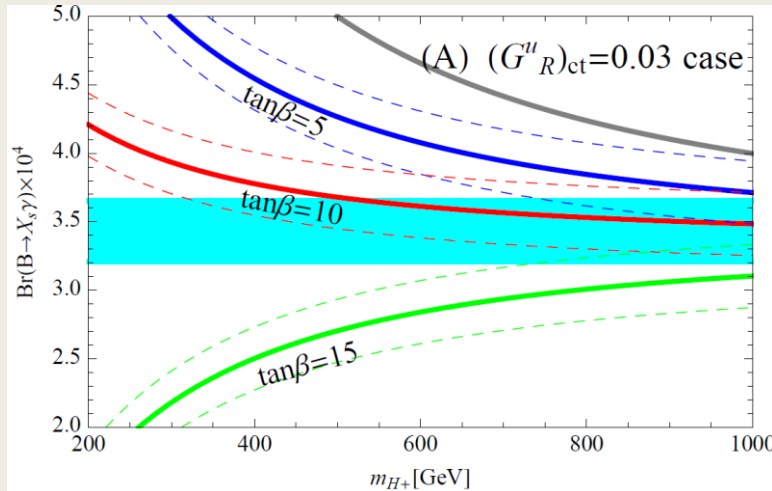
$$C_8^{(1)}(x) = \frac{x}{24} \left\{ \frac{-x^3 + 6x^2 - 3x - 2 - 6x \ln x}{(x-1)^4} \right\},$$

$$C_8^{(2)}(x) = \frac{x}{4} \left\{ \frac{-x^2 + 4x - 3 - 2 \ln x}{(x-1)^3} \right\}.$$

$$B \rightarrow X_s \gamma$$



- (A)  $((G_R^u)_{tt}, (G_R^u)_{tc}, (G_R^u)_{cc}, (G_R^u)_{uu}) = (1 - (G_R^u)_{cc}, 0.03, 10^{-3}, 0)$
- (B)  $((G_R^u)_{tt}, (G_R^u)_{tc}, (G_R^u)_{cc}, (G_R^u)_{uu}) = (1 - (G_R^u)_{cc}, -0.3, 0.1, 0)$



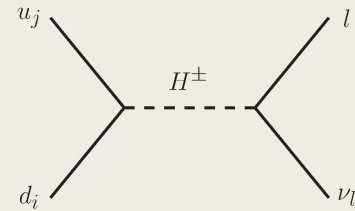
cyan band: experimental results (HFAG, arXiv:1412.7515)

gray line:  $\tan \beta = 50$ ,  $(G_R^u)_{ct} = -10^{-3}$  ( $\rightarrow$  for  $R(D^{(*)})$ )

Note: coupling of charged Higgs

$$(Y_{\pm}^u)_{st} \simeq -\frac{m_t \sqrt{2}}{v} V_{ts}^* G_{tt} - \frac{m_c \sqrt{2}}{v} V_{cs}^* G_{ct}$$

# Flavor Physics Involving $b$



■  $R(D) \text{ \& } R(D^*) \quad R(D^{(*)}) = \frac{\text{Br}(B \rightarrow D^{(*)} \tau \nu)}{\text{Br}(B \rightarrow D^{(*)} l \nu)}$

$$\mathcal{H}_{\text{eff}}^{B-\tau} = C_{\text{SM}}^{cb} (\bar{c}_L \gamma_\mu b_L) (\bar{\tau}_L \gamma^\mu \nu_L) + C_R^{cb} (\bar{c}_L b_R) (\bar{\tau}_R \nu_L) + C_L^{cb} (\bar{c}_R b_L) (\bar{\tau}_R \nu_L)$$

$$R(D) = R_{\text{SM}} \left( 1 + 1.5 \text{Re} \left( \frac{C_R^{cb} + C_L^{cb}}{C_{\text{SM}}^{cb}} \right) + \left| \frac{C_R^{cb} + C_L^{cb}}{C_{\text{SM}}^{cb}} \right|^2 \right),$$

$$R(D^*) = R_{\text{SM}}^* \left( 1 + 0.12 \text{Re} \left( \frac{C_R^{cb} - C_L^{cb}}{C_{\text{SM}}^{cb}} \right) + 0.05 \left| \frac{C_R^{cb} - C_L^{cb}}{C_{\text{SM}}^{cb}} \right|^2 \right),$$

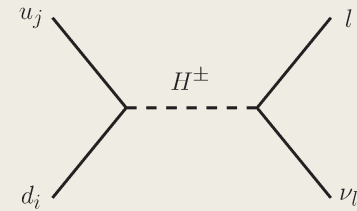
A. Crivellin, et al. PRD **86**, 054014 (2012)

$$C_{\text{SM}}^{cb} = 2V_{cb}/v^2,$$

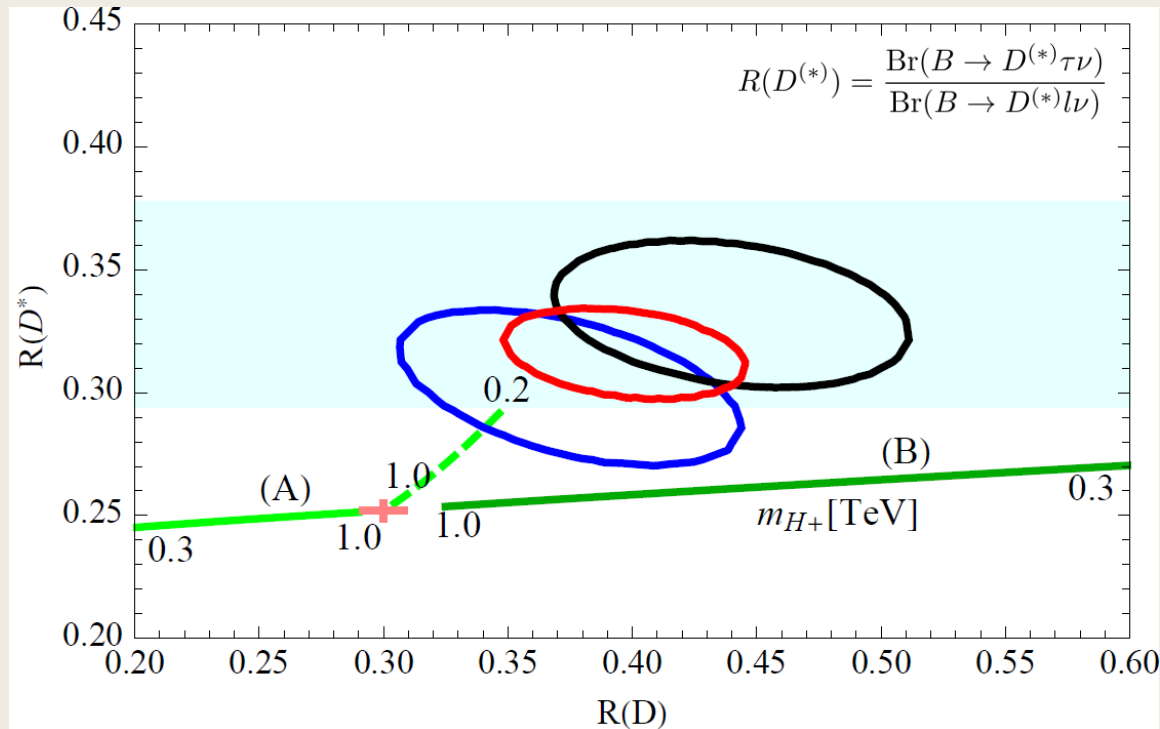
SM & our model coef.:  $\frac{C_L^{cb}}{C_{\text{SM}}^{cb}} = \frac{m_c m_\tau}{m_{H_\pm}^2} \tan^2 \beta - \sum_k \frac{V_{kb}}{V_{cb}} \frac{m_k^u m_\tau (G_R^u)_{kc}^*}{m_{H_\pm}^2 \cos^2 \beta},$

$$\frac{C_R^{cb}}{C_{\text{SM}}^{cb}} = -\frac{m_b m_\tau}{m_{H_\pm}^2} \tan^2 \beta.$$

# R(D) & R(D\*)



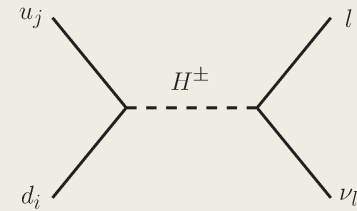
- (A)  $((G_R^u)_{tt}, (G_R^u)_{tc}, (G_R^u)_{cc}, (G_R^u)_{uu}) = (1 - (G_R^u)_{cc}, 0.03, 10^{-3}, 0)$  ( $\tan \beta = 10$ )
- (B)  $((G_R^u)_{tt}, (G_R^u)_{tc}, (G_R^u)_{cc}, (G_R^u)_{uu}) = (1 - (G_R^u)_{cc}, -0.3, 0.1, 0)$  ( $\tan \beta = 5$ )



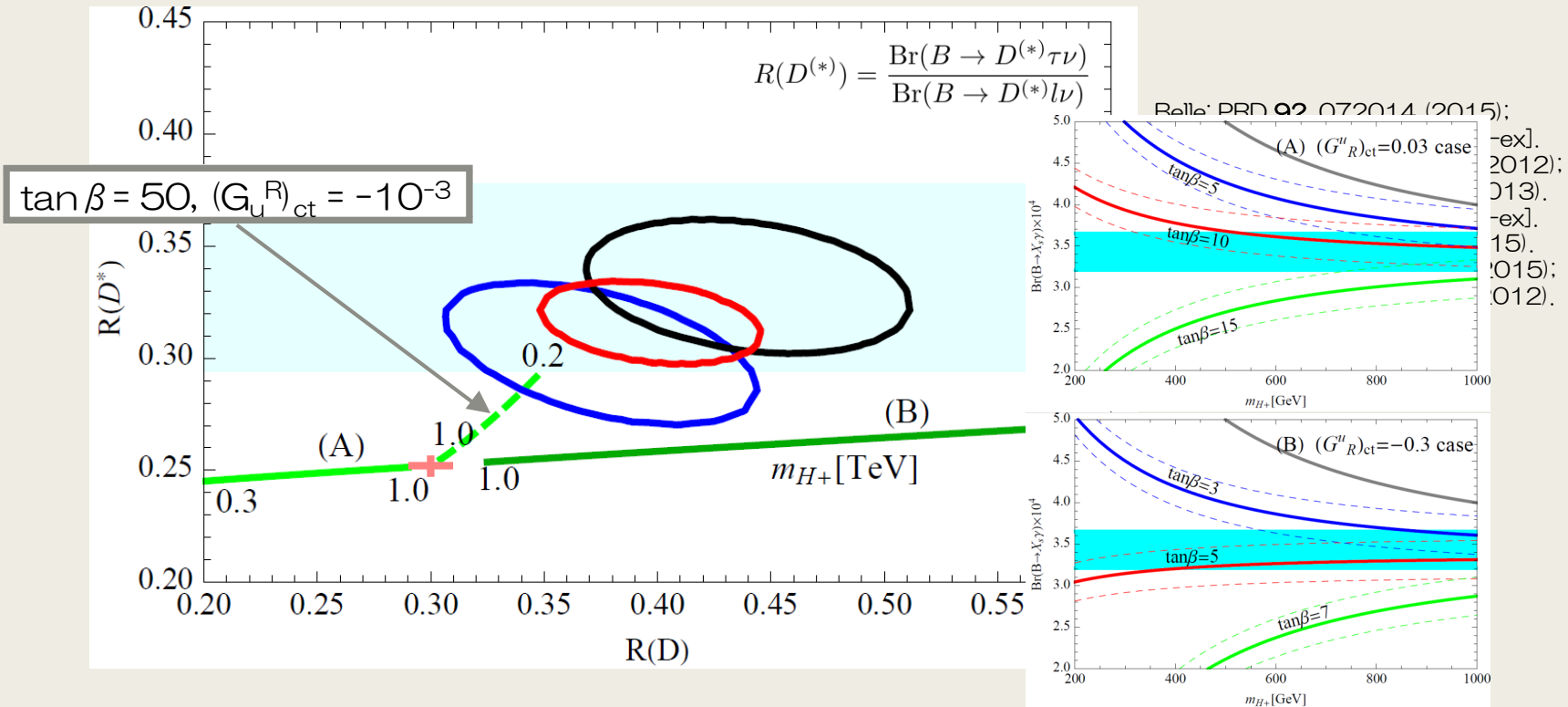
Belle: PRD **92**, 072014 (2015);  
 arXiv:1603.06711 [hep-ex].  
 BABAR: PRL **109**, 101802 (2012);  
 PRD **88**, 072012 (2013).  
 HFAG: arXiv:1412.7515 [hep-ex].  
 LHCb: PRL **115**, 111803 (2015).  
 SM pred.: PRD **92**, 054510 (2015);  
 PRD **85**, 094025 (2012).

Ellipse  $\rightarrow$   $1\sigma$  results for the Belle (blue), *BABAR* (black), HFAG (red)  
 cyan band: LHCb  $1\sigma$  result

# R(D) & R(D\*)



- (A)  $((G_R^u)_{tt}, (G_R^u)_{tc}, (G_R^u)_{cc}, (G_R^u)_{uu}) = (1 - (G_R^u)_{cc}, 0.03, 10^{-3}, 0)$  ( $\tan \beta = 10$ )
- (B)  $((G_R^u)_{tt}, (G_R^u)_{tc}, (G_R^u)_{cc}, (G_R^u)_{uu}) = (1 - (G_R^u)_{cc}, -0.3, 0.1, 0)$  ( $\tan \beta = 5$ )



Ellipse  $\rightarrow$  1  $\sigma$  results for the Bell (blue), BABAR (black), HFAG (red) cyan band: LHCb 1  $\sigma$  result



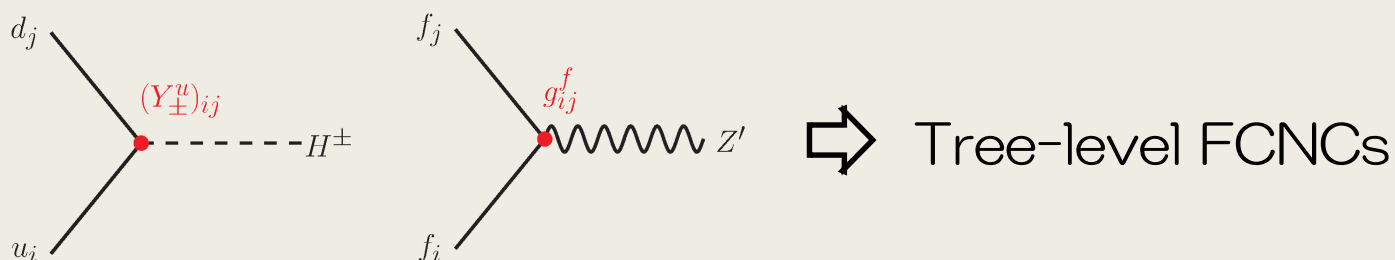
Summary



# Summary

- We consider  $U(1)'$  extended model  
new Higgs doublets  $\rightarrow$  can explain fermion masses

- There are flavor-violating couplings:



- focus on B physics mediated by  $Z'$  and  $H^\pm$ 
  - $b \rightarrow sll$  &  $\Delta F=2$  : can explain simultaneously
  - $B \rightarrow X_s \gamma$  :  $m_{H^\pm} > 500$  (300) GeV,  $\tan \beta = 10$  (5)
  - $R(D)$  &  $R(D^*)$  : hard to explain



Buck up

# Comment

- In this model, (t,c)-element becomes large

$$(G_R^u)_{tc} \sim \mathcal{O}(0.01)$$

if the sensitivity of LHC is improved,  
this model can be tested via  $t \rightarrow ch$  channel

$$\frac{m_t}{v} \tan \beta (G_R^u)_{tc} \{ \sin(\alpha - \beta) h + \cos(\alpha - \beta) H - iA \} \bar{t}_{LCR} + \text{H.c.}$$

Note: if  $\sin(\alpha - \beta) < 0.1$ , our model is safe for the LHC bound

# Extra matters

Fields	Spin	SU(3) <sub>c</sub>	SU(2) <sub>L</sub>	U(1) <sub>Y</sub>	U(1)'
$Q'_R$	1/2	<b>3</b>	<b>2</b>	1/6	1
$Q'_L$	1/2	<b>3</b>	<b>2</b>	1/6	0
$u'_L$	1/2	<b>3</b>	<b>1</b>	2/3	1
$u'_R$	1/2	<b>3</b>	<b>1</b>	2/3	0
$u''_L$	1/2	<b>3</b>	<b>1</b>	2/3	1 + $q_3$
$u''_R$	1/2	<b>3</b>	<b>1</b>	2/3	0
$R'_\mu$	1/2	<b>1</b>	<b>2</b>	-1/2	$q_e$
$L'_\mu$	1/2	<b>1</b>	<b>2</b>	-1/2	0
$R'_\tau$	1/2	<b>1</b>	<b>2</b>	-1/2	$q_e$
$L'_\tau$	1/2	<b>1</b>	<b>2</b>	-1/2	0
$\mu'_L$	1/2	<b>1</b>	<b>1</b>	-1	$q_e - 1$
$\mu'_R$	1/2	<b>1</b>	<b>1</b>	-1	0
$\tau'_L$	1/2	<b>1</b>	<b>1</b>	-1	$q_e - 1$
$\tau'_R$	1/2	<b>1</b>	<b>1</b>	-1	0
$\Phi_l$	0	<b>1</b>	<b>1</b>	0	$q_e$
$\Phi_r$	0	<b>1</b>	<b>1</b>	0	$q_e - 1$

Table 4: The extra chiral fermions for the anomaly-free conditions with  $(q_1, q_2) = (0, 1)$ . The bold entries “**3**” (“**2**”) show the fundamental representation of SU(3) (SU(2)) and “**1**” shows singlet under SU(3) or SU(2).

# Yukawa couplings

## ■ Yukawa couplings (S = h, H, A)

$$\begin{aligned}
 -\mathcal{L}_Y = & (Y_S^u)_{ij} S \overline{u}_L^i u_R^j + (Y_S^d)_{ij} h \overline{d}_L^i d_R^j + (Y_S^e)_{ij} H \overline{e}_L^i e_R^j \\
 & + (Y_{\pm}^u)_{ij} H^- \overline{d}_L^i u_R^j + (Y_{\pm}^d)_{ij} H^+ \overline{u}_L^i d_R^j + (Y_{\pm}^e)_{ij} H^+ \overline{\nu}_L^i e_R^j + \text{H.c.}
 \end{aligned}$$

Up-type

$$(Y_h^u)_{ij} = \frac{m_u^i \sin(\alpha - \beta)}{v} G_{ij} + \frac{m_u^i \cos(\alpha - \beta)}{v} \delta_{ij},$$

$$(Y_H^u)_{ij} = \frac{m_u^i \cos(\alpha - \beta)}{v} G_{ij} - \frac{m_u^i \sin(\alpha - \beta)}{v} \delta_{ij},$$

$$(Y_A^u)_{ij} = -i \frac{m_u^i}{v} G_{ij},$$

$$(Y_{\pm}^u)_{ij} = -\frac{m_u^k \sqrt{2}}{v} V_{ki}^* G_{kj},$$

Down-type

$$(Y_h^d)_{ij} = -\delta_{ij} \frac{m_d^i \cos \alpha}{v \cos \beta},$$

$$(Y_H^d)_{ij} = \delta_{ij} \frac{m_d^i \sin \alpha}{v \cos \beta},$$

$$(Y_A^d)_{ij} = -i \delta_{ij} \frac{m_d^i}{v} \tan \beta,$$

$$(Y_{\pm}^d)_{ij} = -V_{ij} \frac{m_d^j \sqrt{2}}{v} \tan \beta$$

# Flavor Physics Involving $b$

- input parameters from PDG [73]

$\alpha_s(M_Z)$	0.1193(16) [73]	$\lambda$	0.22537(61) [73]
$G_F$	$1.1663787(6) \times 10^{-5} \text{ GeV}^{-2}$ [73]	$A$	$0.814_{-0.024}^{+0.023}$ [73]
$m_b$	$4.18 \pm 0.03 \text{ GeV}$ [73]	$\bar{\rho}$	0.117(21) [73]
$m_t$	$160_{-4}^{+5} \text{ GeV}$ [73]	$\bar{\eta}$	0.353(13) [73]
$m_c$	$1.275 \pm 0.025 \text{ GeV}$ [73]		