

# History of Accelerator

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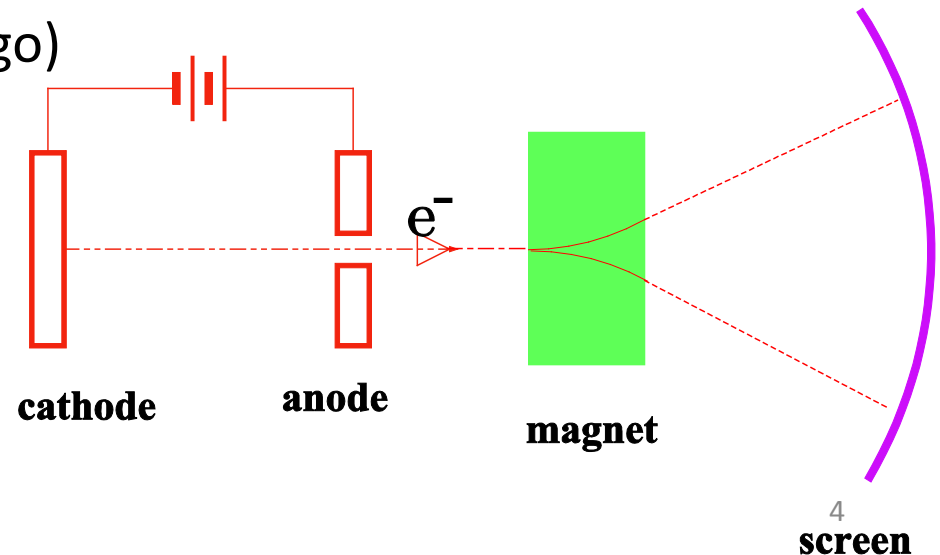
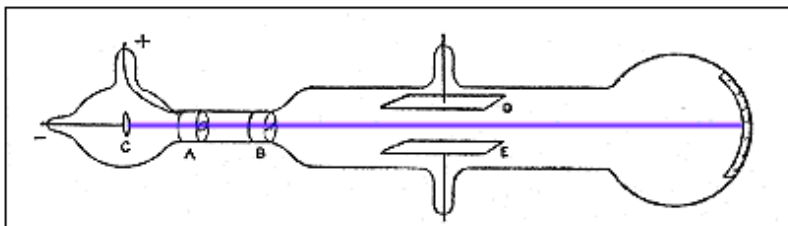
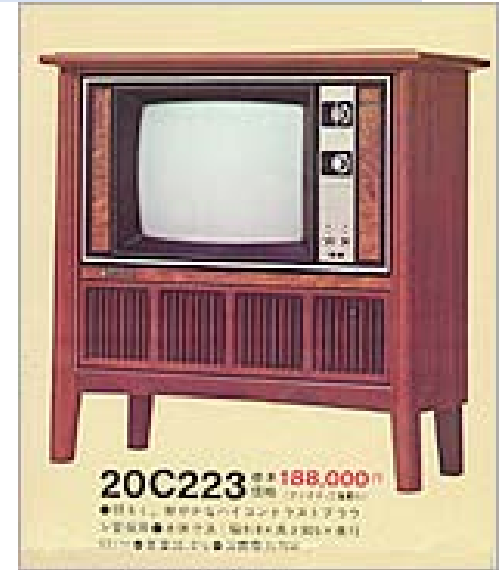
- History of Accelerator
  - DC accelerator
  - Cyclotron
  - Betatron
  - Synchrotron
  - Linear accelerator
  - Collider (next lecture from here)
  - Huge accelerators
- Future Accelerators
  - ILC, CLIC, plasma, etc.
- Try to be very elementary
- Caveats: I treat only accelerators for high energy physics.  
“high energy” = “energy frontier at each time

# What is Accelerator?

- Usually, an accelerator is a device to accelerate charged particles, such as electron and positron, to higher energies by an electro-magnetic field
- Other forces such as gravitation, nuclear force, etc.?
  - Gravitation is too weak
  - Nuclear force is too much “short-range”
- Usually electric field (not magnetic field) is used
  - Magnetic field also possible. Use dB/dt, called betatron
  - In principle, acceleration using magnetic moment is possible (e.g., neutron)

# CRT: Cathode Ray Tube

- The first “accelerator”
- Electric voltage between two metallic plates
- Heat the cathode --- something emitted
- **Proved the existence of electron** in 1897 by J.J. Thomson (Cavendish lab. Cambridge)
- Measured  $e/m$  (charge-mass ratio)
  - Note that  $e$  became known by Millikan’s oil-drop experiment later in 1911
- CRT also led the discovery of X-ray by Roentgen in 1895
- TV monitor (until some years ago)

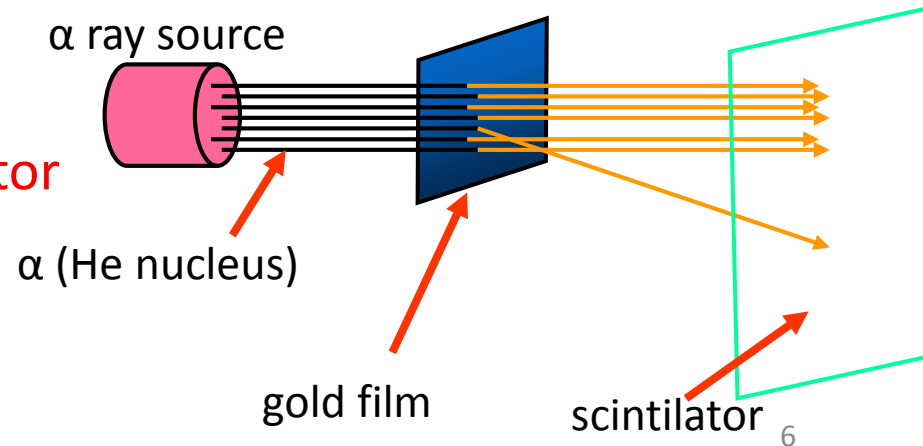
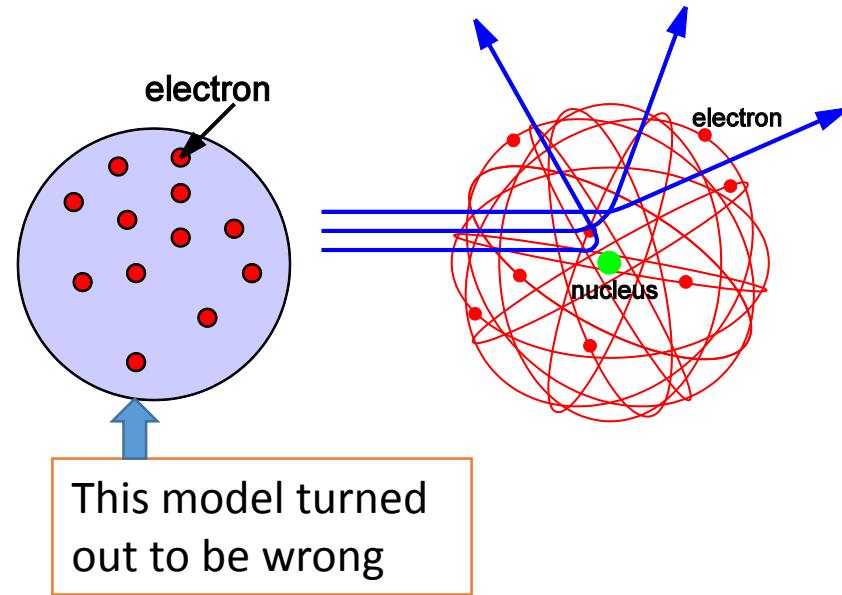


# Units of Energy, Mass, Momentum etc.

- In accelerator physics MKSA is usually used
- However, the energy, mass, etc. of particles the MKSA units, Joule, kg, etc. are seldom used
- For the energy we use  
1eV (electron volt) = the kinetic energy of electron (or positron, proton, etc, particles of charge +e or -e) accelerated by the voltage 1 Volt.
- Then, keV, MeV, GeV, TeV, etc.
- Particle mass is measured in  $\text{eV}/c^2$ 
  - $c$  = velocity of light
  - Electron mass =  $0.511 \text{ MeV}/c^2$
  - Proton mass =  $938 \text{ MeV}/c^2$
- Momentum is in  $\text{eV}/c$

# Experiment by Rutherford

- Earnest Rutherford (Manchester) was the first to see inside an atom (1911)
- “A particle” (alpha particle from radium) was made to collide with the atom
- Turned out there is something extremely small (now called nucleus) at the center, surrounded by electrons
  - To explain the rare events with very large angles (cannot be explained as multiple scattering)
- The particles which were made to collide came **from a natural radioactive element, not from accelerator**
  - A few MeV was necessary ( $\alpha$  from  $^{226}\text{Ra}$   $\sim 5\text{MeV}$ )
  - There was no such accelerator



# Electro-Static Accelerator

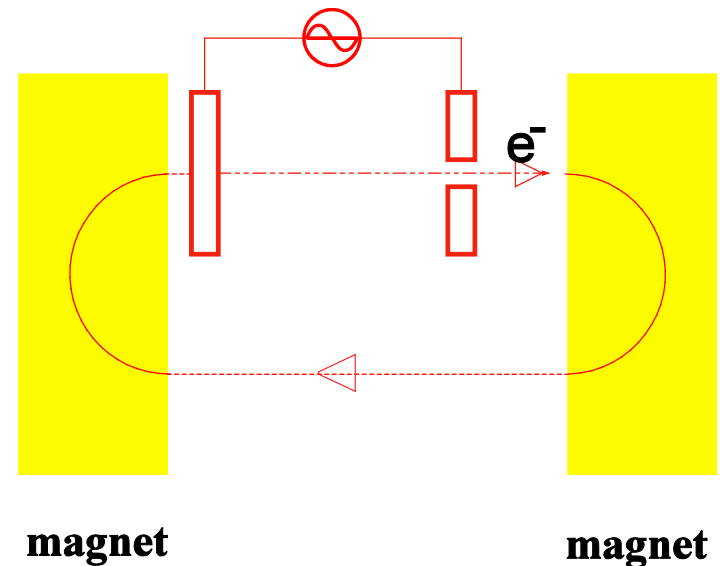
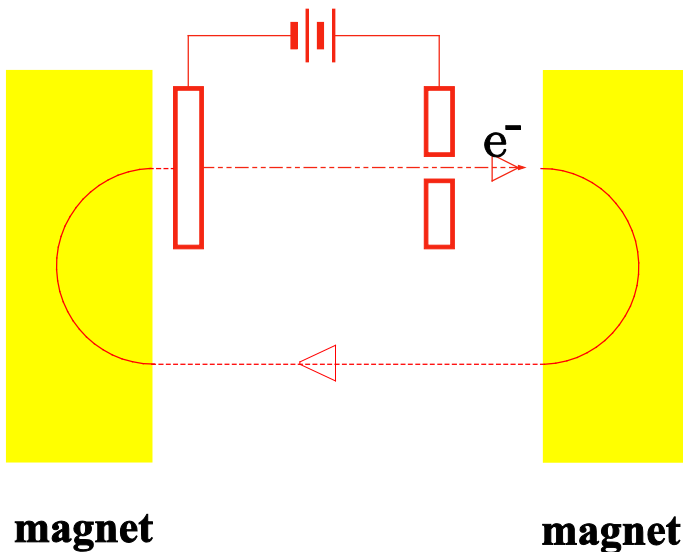
- Cockcroft-Walton
- Collect static electricity
- First nuclear transformation by accelerator
- $H + Li \rightarrow 2 He$
- Cavendish Institute in 1932
  - The same year as the discovery of neutron by Chadwick (also Cavendish) from beryllium irradiated by  $\alpha$ .
- 800keV
- **Limitation by discharge**



KEK 750keV Cockcroft-Walton

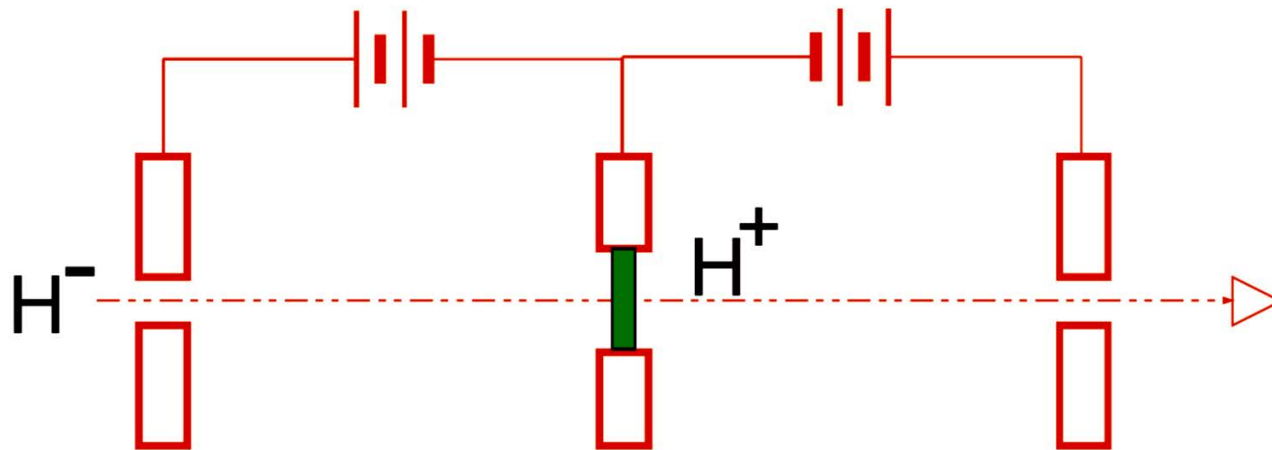
# How to Go to Higher Energies

- Bend the particle after first acceleration by magnetic field
- Accelerate by the same CRT
- Does this work?
- Solution: use alternating voltage
- But **high frequency is needed**





- A clever (but very limited) way is the tandem (2 houses harnessed in series) accelerator

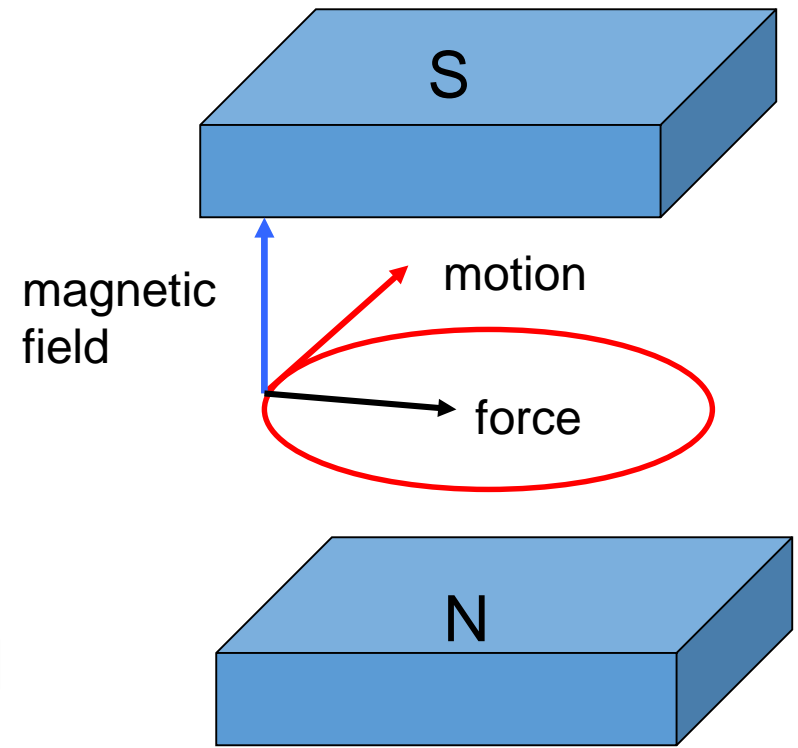


# Motion in Magnetic Field

- A charged particle draws a circle
- $p = e \times B \times \rho$

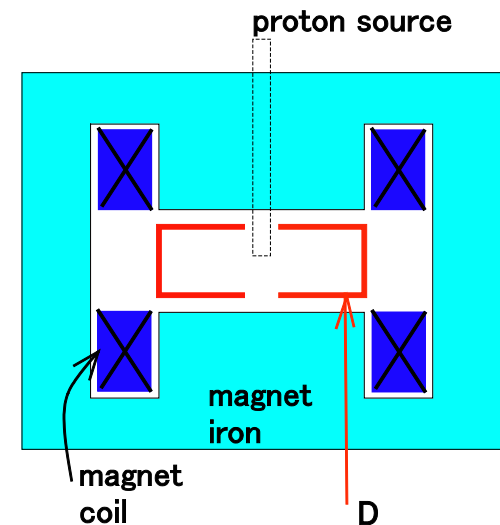
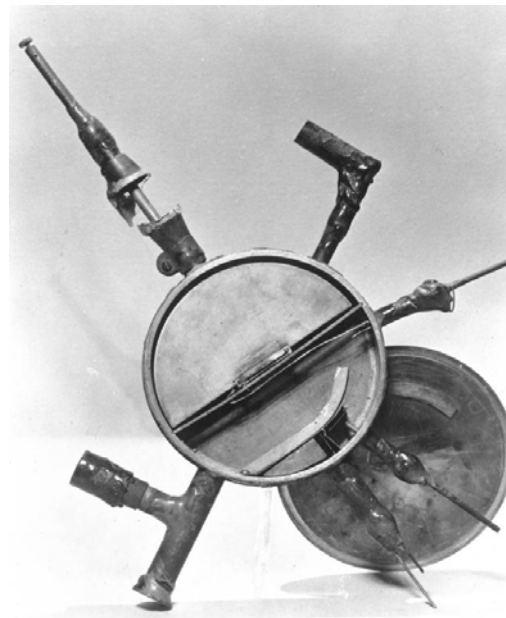
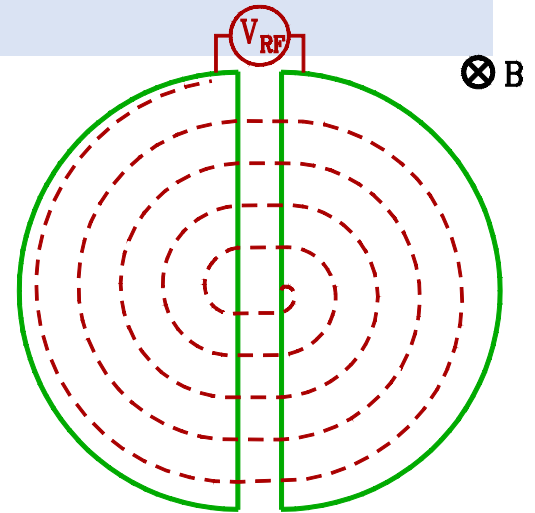
- $p$ : particle momentum
- $e$ : electric charge
- $B$ : magnetic field
- $\rho$ : orbit radius

$$p \text{ [GeV/c]} = 0.3 \times B \text{ [T]} \times \rho \text{ [m]}$$



# Cyclotron

- Jan. 1931
- Berkeley, California
- Lawrence & Livingston, Phys. Rev. 40, 19, 1932



First cyclotron  
diameter 13cm  
Proton energy 80keV  
Wikipedia says ~25\$

# Cyclotron (2)

- Cyclotron makes use of the fact that the time for one turn is independent of the electron energy
  - $p = eB\rho$
  - $p = mv$
  - $\rightarrow T = \frac{2\pi\rho}{v} = \frac{2\pi m}{eB}$   
 $T = \text{time for one revolution, } m : \text{particle mass, } v : \text{velocity}$
- But,  $p = mv$  is an approximation.  
Exact formula with the special relativity is
$$p = mv / \sqrt{1 - (v/c)^2}$$
- " $T = \text{independent of } p$ " breaks down when  $v$  approaches  $c$ .
- Large difference between electron and proton

# Exercise (1)

Assuming that the first cyclotron had maximum orbit diameter 13cm and reached the maximum proton energy 80keV, compute

- The magnetic field
- Frequency of the voltage

(caution: these may differ a bit from the real one.)

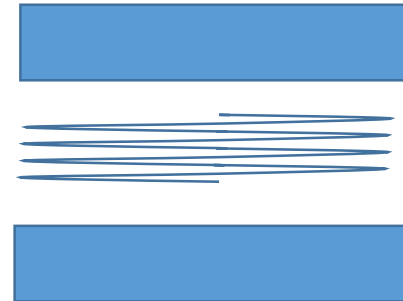
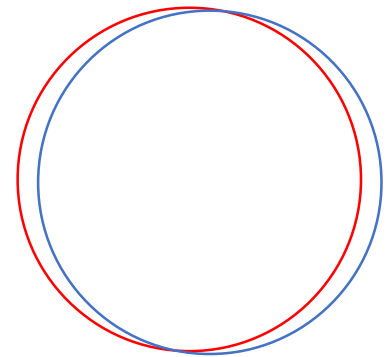
# Betatron

- D. W. Kerst, ~1940
- Induction accelerator (time-dependent magnetic field)

$$\text{rot } E = - \frac{\partial B}{\partial t} \rightarrow E_{\phi} = \frac{1}{2}$$

# Betatron Oscillation

- If a particle velocity has an off-circle motion, the particle draws a circle with a shifted center but does not go far away (horizontal focusing)
- But once a particle gets vertical velocity, then the particles eventually hit the magnet and is lost.
- There must be a force which gives a vertical force to the particle to bend the orbit back to the medium plane.
- Transverse motion is called “Betatron Oscillation”
- Previous figure: The magnet gap is larger outside
  - Stability of betatron oscillation



# (Weak) Focusing

- Simple (vertical) magnetic field makes a circular orbit. Once a particle gets vertical velocity, it will soon hit the magnet and lost

- Use a magnet like →

- $B_y = B_0 \left(1 - \frac{nx}{r_0}\right)$

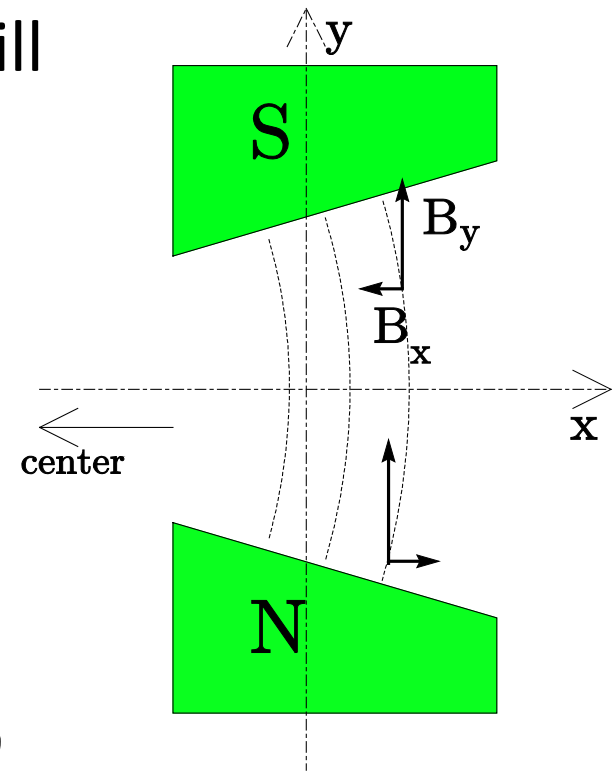
- $B_x = -B_0 \left(\frac{ny}{r_0}\right)$

Note:  $\frac{\partial B_y}{\partial x} = \frac{\partial B_x}{\partial y}$

- Then,

$$x \propto \sin \sqrt{1-n}\theta, \quad y \propto \sin \sqrt{n}\theta$$

- Stable if  $0 < n < 1$ .





# Synchrotron

- Change the magnetic field  $B(t)$  so that the orbit radius does not change as energy increases

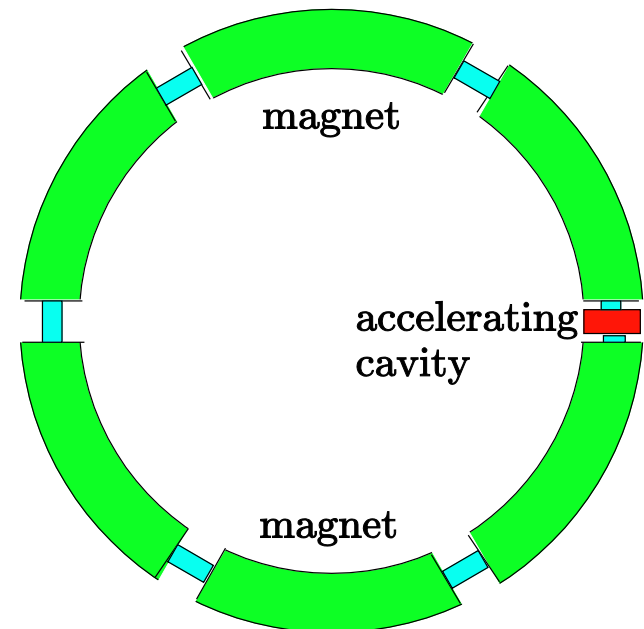
$$p(t) = eB(t)\rho$$

- Then, the magnets need not cover inside the circle. → Much smaller magnets.
- The price to pay: Pulsed operation. No continuous beam.
- Acceleration only a few points in the ring
- High frequency needed
  - RF: radio frequency
  - $c = f_{RF} \times \lambda_{RF}$

- Circumference must be an integer multiple of the RF wave length

$$C = h \times \lambda_{RF}$$

$h$  is called “harmonic number”



# Particle Discovery before the Era of Accelerator

- Neutron 1932 ( $\alpha$  on beryllium)
- Neutrino  $\sim$ 1932 (to explain beta decay)
- positron 1932 (from cosmic ray)
- muon 1937 (cosmic ray)
- $\pi$  meson 1947 (cosmic ray)
  
- Accelerators, improved to high energies, started to discover new particles in 1950's

# GeV-class Synchrotrons

- 1950's
- A few GeV proton synchrotrons
  - Cosmotron (BNL) 3GeV
  - Bevatron (LBL) 6.2GeV
- Many new particles found
  - anti-proton, anti-neutron
  - $\Lambda$ ,  $\Sigma$ ,  $\Xi$ ,  $\Omega$ ,.....
  - Systematic description introducing “Quarks” by Gell-Mann in 1964



Cosmotron

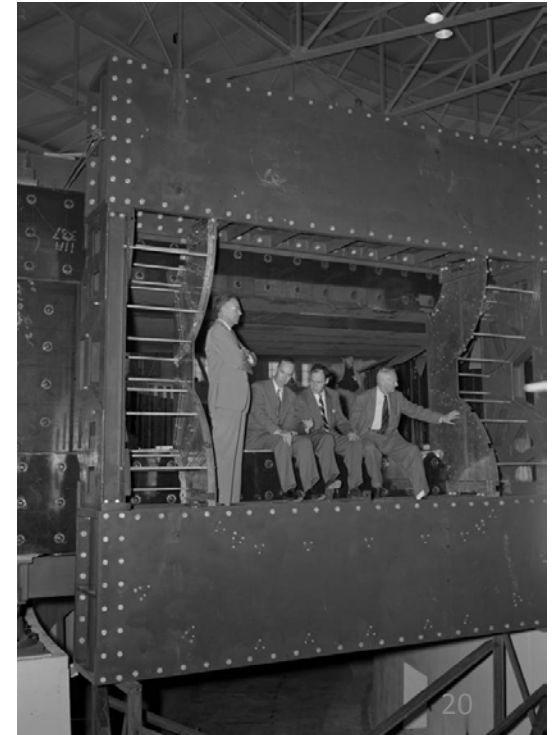
# Bevatron

- Weak-focusing synchrotron
- Lawrence Berkeley Laboratory
- Start operation in 1954
- Bev.. = Billion Electron Volt  
= Giga Electron Volt (GeV)
- Discovered antiproton in 1955



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Yokoya <http://www.lbl.gov/image-gallery/image-library.html>



# Principle of Strong Focusing

- Found by Earnest Courant, et.al.
- E. D. Courant, M.S. Livingston, H. S. Snyder, Phys.Rev. 88 (1952)
- Note that no single magnet can focus simultaneously in x and y.



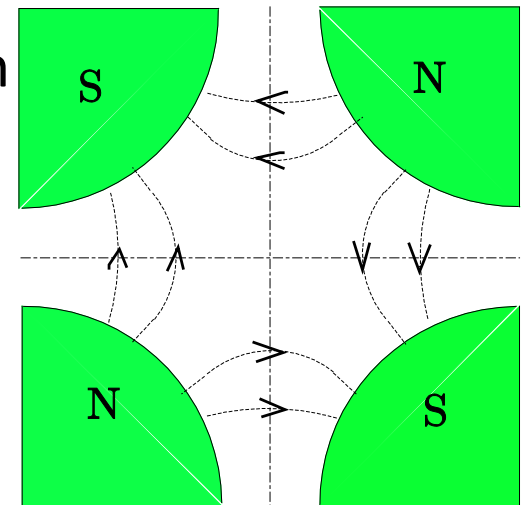
- But arranging  and  alternately, the beam can be focused in x and y
- Two lenses with the focal length  $f_1, f_2$  placed with the distance  $d$  make a lens of focal length

$$\frac{1}{F} = \frac{1}{f_1} + \frac{1}{f_2} - \frac{d}{f_1 f_2}$$

$$\text{If } f_1 = -f_2 = f, \text{ then } F = \frac{d}{f^2}$$

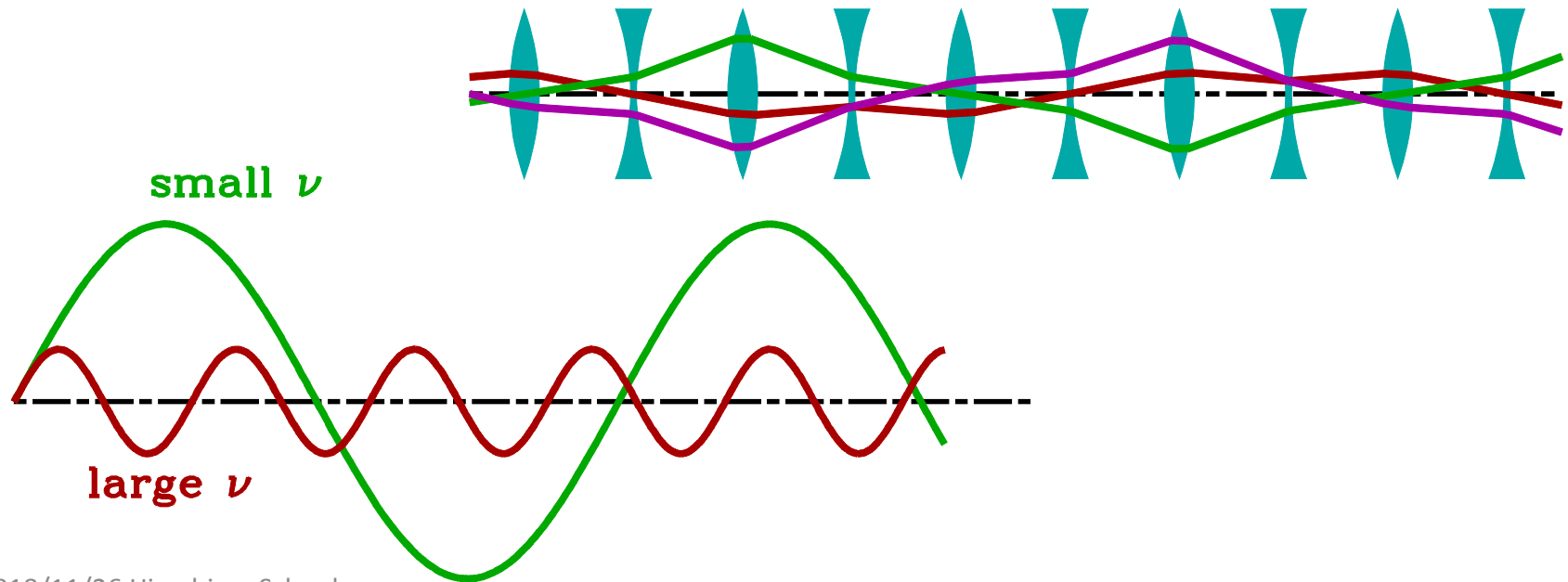
i.e., a focusing lens

- Can also be done by quadrupole magnets



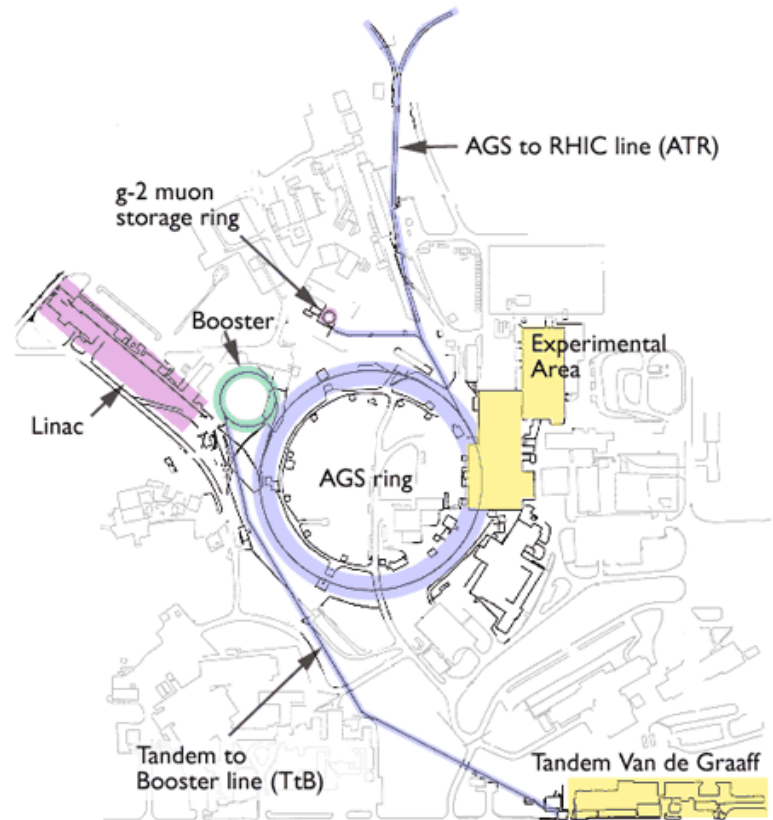
# Principle of Strong Focusing (2)

- With many focusing and defocusing lenses, the orbit oscillates many times during one turn
- The beam size becomes much smaller than weak-focusing  $\rightarrow$  magnet becomes much smaller
- The price to pay was the accuracy of the field

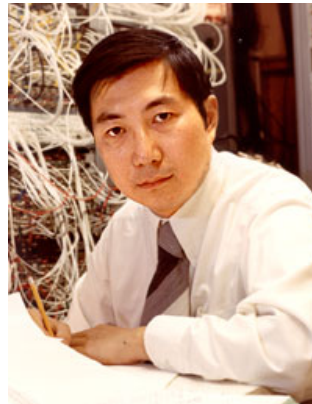


# AGS: Alternating Gradient Synchrotron

- First strong-focusing synchrotron
- Brookhaven Laboratory
- Start operation in 1960,  $\sim 20\text{GeV}$
- Discovery of new particles
  - $J/\psi$
  - $\nu_\mu$



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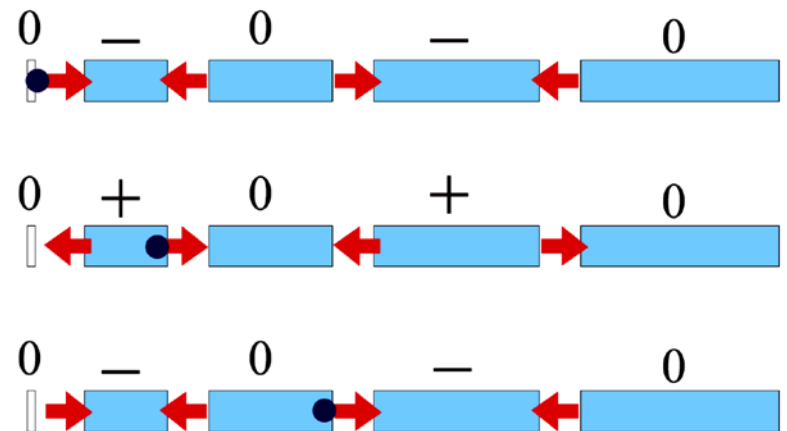
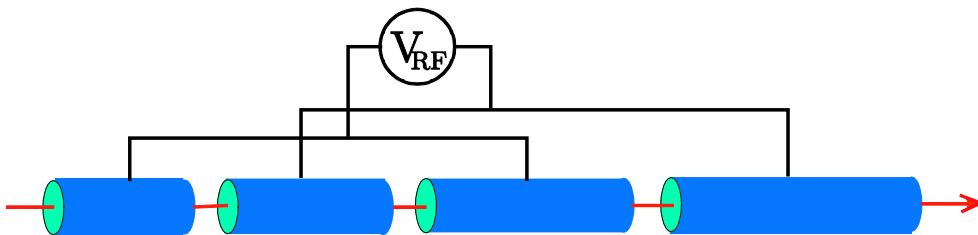


Sam Ting



# Linear Accelerator

- Solve the problem of DC accelerator by another way
- Apply Alternating Voltage on the individual metallic tubes (drift-tube)
- The electric field is zero inside the tubes
- Protons at the left end are accelerated when the voltage on the first tube becomes negative
- If the voltage is flipped by the time the protons reach the exit of the first tube, they are accelerated in the gap between tube 1 and 2



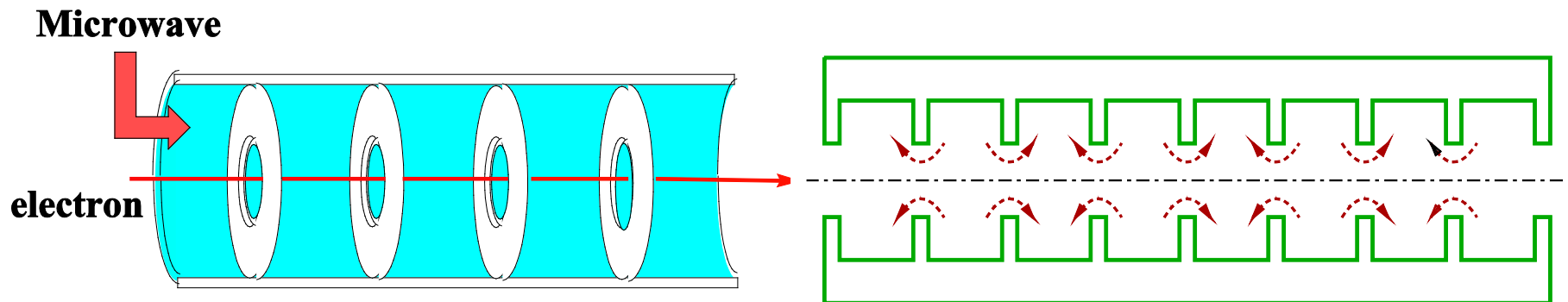


## Exercise (2)

- Assume the particle is proton, the voltage is  $\pm 500\text{kV}$ , the length of the first drift tube is  $5\text{cm}$ , and the gap length is negligible.
- Compute (Use non-relativistic kinematics)
  - the proton velocity in the first tube
  - required frequency
  - the length of the second tube
  - the length of the  $n$ -th tube
- One more question: how long is the tube in the limit of  $n \rightarrow \infty$  (use special relativity)

# Linear Accelerator (2)

- The discovery of the principle is old, but actual development much later
  - Progress of **microwave technology** (radar) during WW-II
- Resonator type accelerator for particles with  $v$  close to  $c$



# Stanford Linear Accelerator

- Electron linear accelerator
- Length 2 miles
- Operation started in 1967
- ~1968 Research of deep inelastic scattering (scattering of electron and target proton, investigate structure of proton)
- This accelerator has later been used for various purposes. It is still now the highest energy linac. SPEAR, PEP-II, SLC, LCLS, LCLSII ....

# Stanford Linear Accelerator



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# Synchrotron Radiation

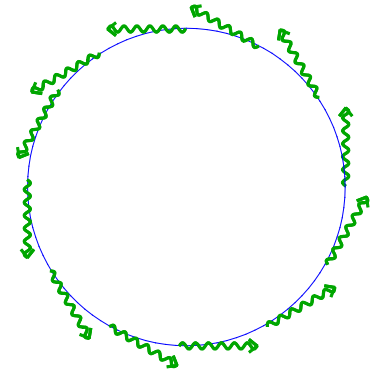
- Charged particles lose energy by synchrotron radiation
- proportional to  $1/m^4$ 
  - Almost negligible from protons but visible in LHC
- Loss per turn (electron)

$$U = 0.088 \frac{E^4 [\text{GeV}]}{\rho [\text{m}]} \quad [\text{MeV}]$$

- Average photon energy

$$E_\gamma = 0.683 \frac{E^3 [\text{GeV}]}{\rho [\text{m}]} \quad [\text{keV}]$$

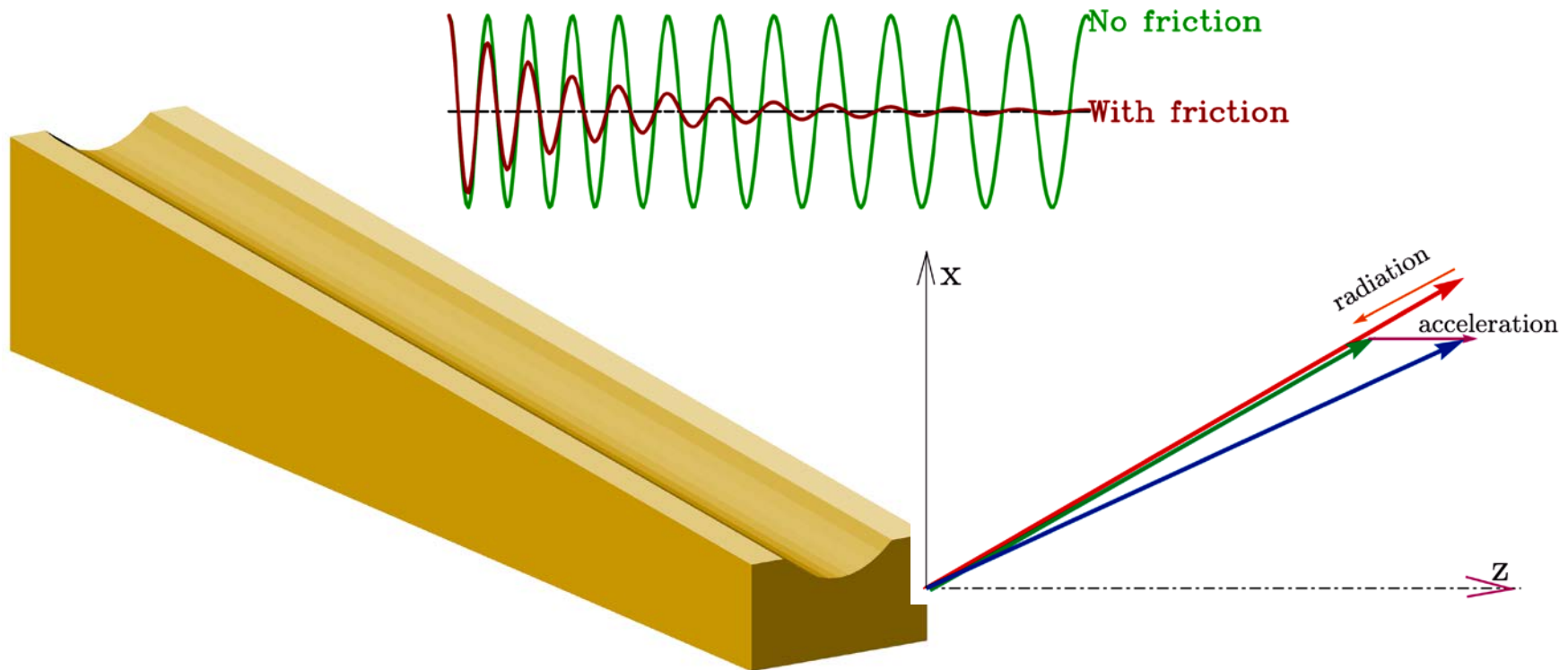
- Not only unwelcomed effects but
  - can be used as light source
  - radiation damping
    - Stabilize beam oscillation
    - Lower the emittance





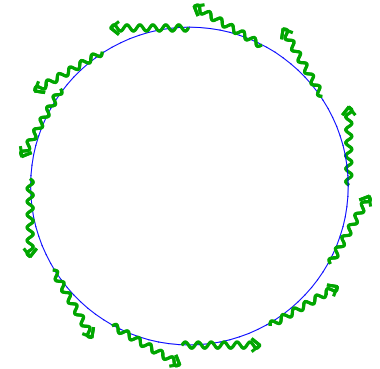
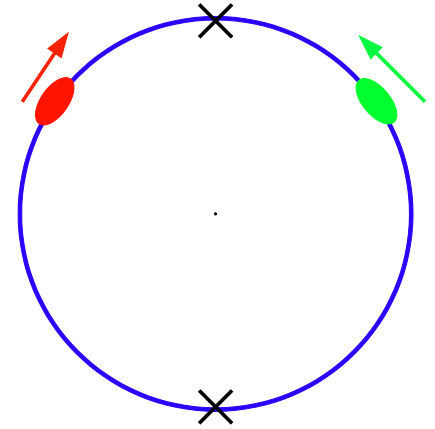
# Radiation Damping

- Synchrotron radiation loss is larger for higher-energy particle  $\rightarrow$  damping of energy spread
- Momentum loss in the direction of motion (like frictional force)  $\rightarrow$  damping of transverse oscillation



# Storage Ring

- Synchrotron can be used to store beams for seconds to days
- Usage
  - Collider
  - Synchrotron light source
  - Beam manipulation
    - Low emittance
    - Buncher/debuncher
    - Stacking
- Principle same as synchrotron but
  - no need of rapid acceleration (even no acceleration)
  - longer beam life required (e.g., better vacuum)
  - insertion structure (colliding region, undulator, etc)



# Radiation Source

- Many accelerators have been built to make use of the synchrotron radiation
- First generation: parasitic use of radiation from bending magnets of colliders
- Second generation: parasitic use of radiation from insertion magnets of colliders
  - Undulators
- Third generation: Radiation in a ring dedicated for light source
- Fourth generation?: FEL, ERL,